

Enhanced binding and cold compression of nuclei due to admixture of antibaryons

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Abstract

We discuss the possibility of producing a new kind of nuclear system by putting a few antibaryons inside ordinary nuclei. The structure of such systems is calculated within the relativistic mean-field model assuming that the nucleon and antinucleon potentials are related by the G-parity transformation. The presence of antinucleons leads to decreasing vector potential and increasing scalar potential for the nucleons. As a result, a strongly bound system of high density is formed. Due to the significant reduction of the available phase space the annihilation probability might be strongly suppressed in such systems.

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1 Introduction

Presently it is widely accepted that the relativistic mean-field (RMF) model [1] gives a good description of nuclear matter and finite nuclei [2]. Within this approach the nucleons are supposed to obey the Dirac equation coupled to mean meson fields. Large scalar and vector potentials, of the order of 300 MeV, are necessary to explain the strong spin-orbit splitting in nuclei. The most debated aspect of this model is related to the negative-energy states of the Dirac equation. In most applications these states are simply ignored (no-sea approximation) or "taken into account" via the non-linear and derivative terms of the scalar potential. On the other hand, explicit consideration of the Dirac sea combined with the G-parity arguments leads to such interesting conjectures as the existence of deeply-bound antinucleon states in nuclei [3] or even spontaneous production of nucleon-antinucleon pairs [4, 5]. These predictions are based on the assumption that the relativistic description of the nucleon within the RMF model is a valid concept (for a discussion see

Refs. [6, 7, 8]). Unfortunately, the experimental information on the antinucleon effective potential in nuclei is obscured by the strong absorption caused by annihilation. As follows from the analysis of Ref. [9], the real part of the antiproton effective potential might be as large as 200–300 MeV, with the uncertainty reaching 100% in the deep interior of the nucleus.

Keeping in mind all possible limitations of the RMF approach, below we consider yet another interesting application of this model. Namely, we study properties of light nuclear systems containing a few real antibaryons. At first sight this may appear ridiculous because of the fast annihilation of antibaryons in the dense baryonic environment. But as our estimates show, due to a significant reduction of the available phase space for annihilation, the life time of such states might be long enough for their observation. In a certain sense, these states are analogous to the famous baryonium states in the $N\bar{N}$ system [10], although their existence has never been unambiguously confirmed.

It should be emphasized that previous discussions of the negative-energy states in nuclei were somewhat academic because their contributions to the source terms for the meson fields were ignored. In contrast, our primary goal here is to study properties of physical systems containing both real baryons and real antibaryons. There could be different theoretical schemes for solving this problem but we find the RMF model most suitable for this study. To our knowledge, up till now a self-consistent calculation of antinucleon states in nuclei has not been performed. Our calculations can be regarded as the first attempt to fill this gap. We consider two nuclear systems, namely ^{16}O and ^8Be , and study the changes in their structure due to the presence of an antiproton.

2 Theoretical framework

Below we use the RMF model which previously has been successfully applied for describing ground-states of nuclei at and away from the β -stability line. For nucleons, the scalar and vector potentials contribute with opposite signs in the central potential, while their sum enters in the spin-orbit potential. Due to G-parity, for antiprotons the vector potential changes sign and therefore both the scalar and the vector mesons generate attractive potentials.

To estimate uncertainties of this approach we use three different parametrizations of the model, namely NL3 [11], NL-Z2 [12] and TM1 [13]. Their parameters are found by fitting binding energies and observables related to formfactors of spherical nuclei from ^{16}O (not included in the TM1 fit) to Lead isotopes. In NL3, properties of symmetric nuclear matter have been included in the fit as well. The TM1 model, implementing a self-interaction of the ω -meson, gives a softer rise of the vector potential with density. This leads to smaller meson fields as compared to the NL3 and NL-Z2 parametrizations. In this paper we assume that the antiproton interactions are fully determined by the G-parity transformation. Following Mao et al. [14], we solve the effective Schrödinger equations for

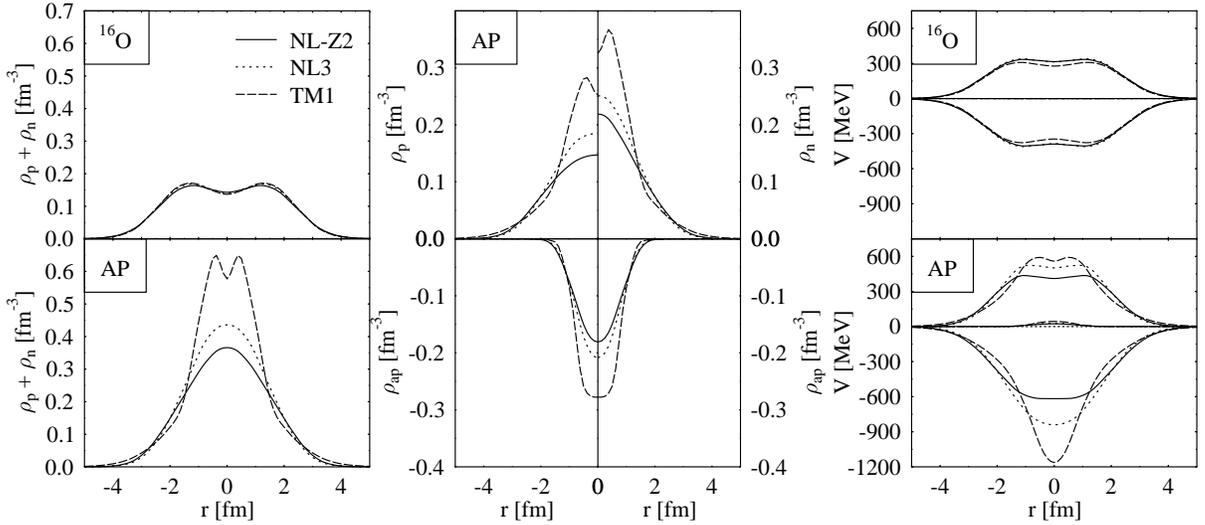


Figure 1: The left panel represents the sum of proton and neutron densities as function of nuclear radius for ^{16}O without (top) and with an antiproton (denoted by AP). The left and right parts of the upper middle panel show separately the proton and neutron densities, the lower part of this panel displays the antiproton density. The right panel shows the scalar (negative) and vector (positive) parts of the nucleon potential. Small contributions shown in the lower row correspond to the isovector (ρ -meson) part.

both the nucleons and the antiprotons. Although we neglect the Dirac sea polarization, we take into account explicitly the contribution of the antibaryon into the scalar and vector densities. For protons and neutrons we include pairing correlations within the BCS model with a δ -force (volume pairing) [15]. Calculations are done within the blocking approximation [16] for the antiproton, and assuming the time-reversal invariance of the nuclear ground-state. The energy of the system is found by using the damped gradient iteration method [17]. The coupled set of equations for nucleons, antinucleons and mesons is solved iteratively and self-consistently. The numerical code employs axial and reflection symmetry, allowing for axially symmetric deformations of the system.

3 Structure of nuclei containing antiprotons

As an example, we consider the nucleus ^{16}O with one antiproton in the lowest bound state. This nucleus is the lightest nucleus for which the mean-field approximation is acceptable, and it is included into the fit of the effective forces NL3 and NL-Z2. The antiproton state is assumed to be in the $s_{1/2}^+$ state. The antiproton contributes with the same sign as nucleons to the scalar density, but with opposite sign to the vector density. This leads to an overall increase of attraction and decrease of repulsion for all nucleons.

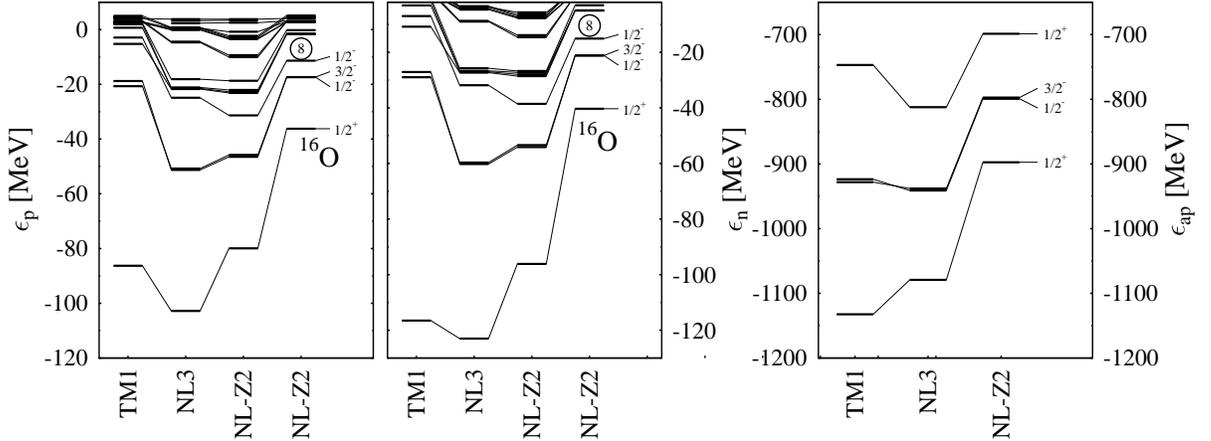


Figure 2: Proton (left), neutron (middle) and antiproton (right) energy levels for the nucleus ^{16}O with one antiproton and without it (rightmost columns in left and middle panel).

The antiproton becomes very deeply bound in the $s_{1/2^+}$ state. To maximize attraction, protons and neutrons move to the center of the nucleus, where the antiproton has its largest occupation probability. This leads to a cold compression of the nucleus to a high density.

Figure 1 shows the densities and potentials for ^{16}O with and without the antiproton. For normal ^{16}O all RMF parametrizations considered produce very similar results. The presence of an antiproton dramatically changes the structure of the nucleus. The sum of proton and neutron densities reaches a maximum value of $(2-4)\rho_0$, where $\rho_0 \simeq 0.15\text{ fm}^{-3}$ is the normal nuclear density, depending on the parametrization. The largest compression is predicted by the TM1 model. This follows from the fact that this parametrization gives the softest equation of state as compared to other forces considered here.

According to our calculations, the difference between proton and neutron densities is quite large, which leads to an increase in symmetry energy. The reason is that protons, though they feel additional Coulomb attraction to the antiproton, repel each other. As a consequence, neutrons are concentrated closer to the center than protons and the symmetry energy increases. As compared to the case without the antiproton, absolute values of vector and scalar potentials increase in the central region of the nucleus. This leads to an enormous drop of the effective baryon mass near the nuclear center, which should strongly suppress local rates of annihilation (see below). The effective mass for TM1 even becomes negative at $r \lesssim 1\text{ fm}$.

Since nucleons feel a deeper potential as compared to the nucleus without the antiproton, their binding energy increases too. This can be seen in Fig. 2. The nucleon binding is largest within the NL3 parametrization. In the TM1 case, the $s_{1/2^+}$ state is also deep,

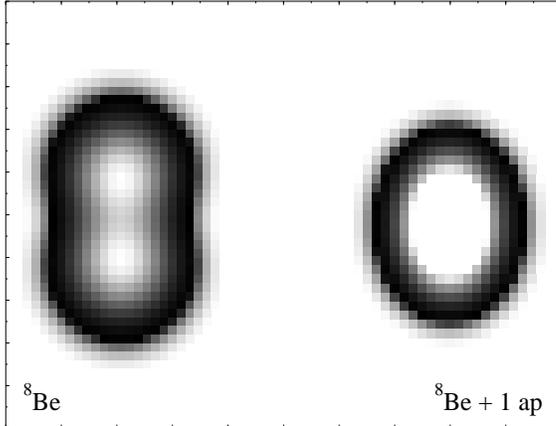


Figure 3: Contour plot of nucleon densities for ${}^8\text{Be}$ without (left) and with (right) antiproton calculated with the parametrization NL3. The maximum density of normal ${}^8\text{Be}$ is 0.20 fm^{-3} , while for nucleus with antiproton it is 0.61 fm^{-3} .

but higher levels are less bound as compared to the NL3 and NL-Z2 calculations. This is a consequence of the smaller spatial extension of the potential in this case. The highest $s_{1/2}^-$ level is even less bound than for the system without an antiproton.

For the antiproton levels, the TM1 parametrization predicts the deepest bound state with binding energy of about 1130 MeV. The NL3 calculation gives nearly the same binding, while in the NL-Z2 case, antiproton states are more shallow and have smaller spacing. It should be noted that the antiprotons are more strongly bound than was obtained in Ref. [14]. This follows from the fact that here we calculate both nucleons and the antinucleon self-consistently allowing the target nucleus to change its shape and structure due to the presence of the antiproton. The total binding energy of the system is predicted to be 828 MeV for NL-Z2, 1051 MeV for NL3, and 1159 MeV for TM1. For comparison, the binding energy of a normal ${}^{16}\text{O}$ nucleus is 127.8, 128.7 and 130.3 MeV in the case of NL-Z2, NL3, and TM1, respectively. Due to this anomalous binding we call these systems Super Bound Nuclei (SBN).

As a second example, we investigate the effect of a single antiproton inserted into the ${}^8\text{Be}$ nucleus. In this calculation only the NL3 parametrization was used (the effect is similar for all three forces). The normal ${}^8\text{Be}$ nucleus is not spherical, exhibiting a clearly visible 2α structure with the deformation $\beta_2 \simeq 1.20$ in the ground-state. Inserting the antiproton gives rise to compression and change of nuclear shape, resulting in a much less elongated nucleus with $\beta_2 \simeq 0.23$. Its maximum density increases by a factor of three from 0.20 fm^{-3} to 0.61 fm^{-3} . The cluster structure of ground state completely vanishes. A similar effect has been predicted in Ref. [18] for the case of the K^- bound state in the ${}^8\text{Be}$ nucleus. In the considered case the binding energy increases from 52.9 MeV (the

experimental value is 56.5 MeV) to about 700 MeV!

4 Life time, formation probability and signatures of SBNs

The crucial question concerning a possible observation of the SBNs is their life time. The only decay channel for such states is the annihilation on surrounding nucleons. The mean life time of an antiproton in nucleonic matter of density ρ_B can be estimated as $\tau = \langle \sigma_A v_{rel} \rho_B \rangle^{-1}$, where angular brackets denote averaging over the wave function of the antiproton and v_{rel} is its relative velocity with respect to nucleons. In vacuum the $N\bar{N}$ annihilation cross section at low v_{rel} can be parametrized as [21] $\sigma_A = C + D/v_{rel}$ with $C=38$ mb and $D=35$ mb. For $\langle \rho_B \rangle \simeq 2\rho_0$ this would lead to a very short life time, $\tau \simeq 0.7$ fm/c (for $v_{rel} \simeq 0.2$). However, one should bear in mind that the annihilation process is very sensitive to the phase space available for decay products. For a bound nucleon and antinucleon the available energy is $Q = 2m_N - B_N - B_{\bar{N}}$, where B_N and $B_{\bar{N}}$ are the corresponding binding energies. As follows from the calculations presented above (see Fig. 2), this energy is strongly reduced compared to $2m_N$, namely, $Q \simeq 600 - 680$ MeV (TM1), 810–880 MeV (NL3) and 990–1050 MeV (NL-Z2) for the lowest antiproton states.

For such low values of Q many important annihilation channels involving two heavy mesons (ρ , ω , η , η' , ...) are simply closed. Other two-body channels such as $\pi\rho$, $\pi\omega$ are considerably suppressed due to the closeness to the threshold. As is well known, the two-pion final states contribute only about 0.4% of the annihilation cross section. Even in vacuum all above mentioned channels contribute to σ_A not more than 15% [22]. Therefore, we expect that only multi-pion final states contribute significantly to antiproton annihilation in the SBN. But these channels are strongly suppressed due to the reduction of the available phase space. Our calculations show that changing Q from 2 GeV to 1 GeV results in suppression factors 5, 40 and 1000 for the annihilation channels with 3, 4 and 5 pions in the final state, respectively. Applying these suppression factors to the experimental branching ratios [23] we come to the conclusion that in the SBNs the annihilation rates can be easily suppressed by factor of 20–30. There could be additional suppression factors of a structural origin which are difficult to estimate at present. This brings the SBN life time to the level of 15–20 fm/c which makes their experimental observation feasible. The corresponding width, $\Gamma \simeq 10$ MeV, is comparable to that of the ω -meson.

Let us discuss now how these exotic nuclear states can be produced in the laboratory. We believe that the most direct way is to use antiproton beams of multi-GeV energy. This high energy is needed to suppress annihilation on the nuclear surface which dominates at low energies. To form a deeply bound state, the fast antiproton must transfer its

energy and momentum to one of the surrounding nucleons. This can be achieved through reactions of the type $\bar{p}p \rightarrow B\bar{B}$ in the nucleus,

$$\bar{p} + (A, Z) \rightarrow B + \bar{B}(A-1, Z') , \quad (1)$$

where $B = n, p, \Lambda, \Sigma$. The fast antibaryon B can be used as a trigger of events where the antibaryon \bar{B} is trapped in the nucleus. Of course, some additional soft pions can be emitted too. One can think even about producing an additional baryon-antibaryon pair and forming a nucleus with two antibaryons in the deeply bound states. In this case two fast nucleons will be knocked out from the nucleus.

Without detailed transport calculations it is difficult to find the formation probability, W , of final nuclei with trapped antinucleons in these reactions. A rough estimate can be obtained by assuming that antiproton stopping is achieved in a single inelastic collision somewhere in the nuclear interior i.e. taking the penetration length of the order of the nuclear radius R . From the Poisson distribution in the number of collisions the probability of such an event is

$$w_1 = \frac{R}{\lambda_{\text{in}}} \exp\left(-\frac{R}{\lambda}\right), \quad (2)$$

where $\lambda_{\text{in}}^{-1} = \sigma_{\text{in}}\rho_0$ and $\lambda^{-1} = (\sigma_{\text{in}} + \sigma_A)\rho_0$ (here σ_{in} and σ_A are the inelastic and annihilation parts of the $\bar{p}N$ cross section). The exponential factor in Eq. (2) includes the probability to avoid annihilation. For initial antiproton momenta $p_{\text{lab}} \simeq 10$ GeV we use $\sigma_{\text{in}} \simeq 25$ mb, $\sigma_A \simeq 15$ mb [23] and get $\lambda \simeq 1.6$ fm which is comparable with the radii of light nuclei. For an oxygen target, using $R \simeq 3$ fm leads to $w_1 \simeq 0.17$.

In fact we need relatively small final antiproton momenta to overlap significantly with the momentum distribution of a bound state, namely, $\Delta p \sim \pi/R_{\bar{p}}$, where $R_{\bar{p}} \simeq 1.5$ fm is characteristic size of antiproton spatial distribution (see Fig. 1). The probability of such a momentum loss can be estimated by the method of Refs. [24, 25] which was previously used for calculating proton spectra in high-energy pA collisions. At relativistic bombarding energies the differential cross sections of the $\bar{p}p \rightarrow \bar{p}X$ and $pp \rightarrow pX$ reactions are similar. The inelastic parts of these cross sections drop rapidly with transverse momentum, but they are practically flat as a function of longitudinal momentum of secondary particles. Thus, the probability of final antiproton momentum to fall in the interval Δp is simply $\Delta p/p_{\text{lab}}$. For $p_{\text{lab}} = 10$ GeV and $\Delta p = 0.4$ GeV this gives 0.04. Assuming the geometrical fraction of central events $\sim 20\%$ we get the final estimate $W \simeq 0.17 \times 0.04 \times 0.2 \simeq 1.4 \cdot 10^{-3}$. Even with extra factors ~ 0.1 which may come from the detailed calculations this is well within the modern experimental possibilities.

Finally, we mention a few possible signatures of SBNs which can be used for their experimental detection. First of all, we remind the reader that according to the Dirac picture, any real antibaryon should be interpreted as a hole in the otherwise filled Dirac sea. Therefore, the nucleons from the positive-energy states of the Fermi sea can make direct transitions to the vacant negative-energy states of the Dirac sea. These super-transitions will be accompanied by the emission of a single pion or kaon depending on

the nature of the trapped antibaryon. The energy of such a super-transition is fixed by the discrete levels of the initial and final baryons and according to our calculations should be of about 1 GeV. This 1-pion or 1-kaon annihilation is a unique feature of finite nuclear systems. In vacuum such transitions are forbidden by the energy-momentum conservation. Therefore, the observation of a line in the pion or kaon spectrum at energies between 1 and 2 GeV would be a clear signal of the deep antibaryon states in nuclei. One can also look for narrow photon lines with energies in the range from 40 to 200 MeV corresponding to the transitions of nucleons and antibaryons between their respective levels. It is interesting to note that these signals will survive even if due to the lack of time the nucleus does not fully rearrange to a new structure. Another strong signal may come from the response of the nuclear remnant to the annihilation of the antibaryon in the deeply bound state. Since the remnant nucleus will initially be in a highly compressed state, it will expand and eventually break up into fragments. Therefore, the annihilation process will lead to rather cold multifragmentation with large collective flow of fragments. Both proposed signatures require rather ordinary measurements, which should be easy to perform with standard detectors.

5 Discussion and conclusions

Our main goal with this paper was to demonstrate that energetic antiproton beams can be used to study new interesting phenomena in nuclear physics. We discuss the possible existence of a completely new kind of strongly interacting systems where both the nucleons and the antinucleons coexist within the same volume and where annihilation is suppressed due to the reduction of the available phase space. Such systems are characterized by large binding energy and high nucleon density. Certainly, antinucleons can be replaced by antihyperons or even by antiquarks. We have presented the first self-consistent calculation of a finite nuclear system containing one antiproton in a deeply bound state. For this study we have used several versions of the RMF model which give excellent description of ordinary nuclei. The presence of an antiproton in a light nucleus like ^8Be or ^{16}O changes drastically the whole structure of the nucleus leading to a much more dense and bound state. Even stronger effects are expected in the ^4He nucleus. It is clear however that these structural changes can occur only if the life time of the antibaryons in the nuclear interior is long enough.

One should bear in mind that originally the RMF model was formulated within the Hartree and no-sea approximations. Implementing the Dirac sea may require serious revision of the model and inclusion of additional terms. Hartree calculations including the Dirac sea [14] and Hartree-Fock calculations [1, 19] including exchange terms lead to smaller nucleon potentials in normal nuclei. Shallower potentials will produce smaller attraction for antinucleons, but the qualitative effect that the presence of antiprotons reduces repulsion and enhances attraction for nucleons will remain valid. We expect that

the additional binding and compression of the nucleus will appear even for an antinucleon potential as low as 200 MeV.

Since nucleon densities in the considered systems could reach $(2 - 3) \rho_0$, it becomes questionable if the RMF model with nucleonic degrees of freedom is applicable at all. Coupling constants of RMF models, obtained by the fitting procedure, are predominantly constrained by observables at saturation density. On the other hand, the nuclear systems studied here are sensitive to the equation of state far above the saturation density. At such high densities nucleons might have to be substituted by quark degrees of freedom or modified by an admixture of them. Recently, we have used an extended version of the Nambu–Jona-Lasinio model to study bulk properties of systems composed of quarks and antiquarks [20]. It has been found that deeply bound states also appear in this model, but the corresponding binding energies are considerably smaller by about a factor of 3.

In summary, on the basis of the RMF model we have studied the structure of nuclear systems containing a few real antibaryons. We have demonstrated that the antibaryons act as strong attractors for the nucleons leading to enhanced binding and compression of the recipient nucleus. As our estimates show the life times of antibaryons in the nuclear environment could be significantly enhanced due to the reduction of the phase space available for annihilation. Narrow peaks in the pion or kaon spectra at the energy around 1 GeV are proposed as the most clear signature of deeply-bound antibaryon states in nuclei.

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