Beam Energy Dependence of Dielectron Production in Au+Au Collisions from STAR at RHIC

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> von Patrick Huck aus Stuttgart

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Dekan: Prof. Dr. Rene Reifarth

Gutachter: Prof. Dr. Nu Xu und Prof. Dr. Joachim Stroth

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Abstract

At sufficiently high temperatures and baryon densities, nuclear matter is expected to undergo a transition into the Quark-Gluon-Plasma (QGP) consisting of deconfined quarks and gluons and accompanied by chiral symmetry restoration. Signals of these two fundamental characteristics of Quantum-Chromo-Dynamics (QCD) can be studied in ultra-relativistic heavy-ion collisions producing a relatively large volume of high energy and nucleon densities as existent in the early universe. Dileptons are unique bulk-penetrating sources for this purpose since they penetrate through the surrounding medium with negligible interaction and are created throughout the entire evolution of the initially created fireball. A multitude of experiments at SIS18, SPS and RHIC have taken on the challenging task to measure these rare probes in a heavy-ion environment. NA60's results from high-quality dimuon measurements have identified the broadened ρ spectral function as favorable scenario to explain the low-mass dilepton excess, and partonic sources as dominant at intermediate dilepton masses.

Enabled by the addition of a TOF detector system in 2010, the first phase of the Beam Energy Scan (BES-I) at RHIC allows STAR to conduct an unprecedented energy-dependent study of dielectron production within a homogeneous experimental environment, and hence close the wide gap in the QCD phase diagram between SPS and top RHIC energies. This thesis concentrates on the understanding of the LMR enhancement regarding its M_{ee}, p_T and energy dependence. It studies dielectron production in Au+Au collisions at beam energies of 19.6, 27, 39, and 62.4 GeV with sufficient statistics. In conjunction with the published STAR results at top RHIC energy, this thesis presents results on the first comprehensive energy-dependent study of dielectron production.

This includes M_{ee} - and p_T -spectra for the four beam energies measured in 0-80% minimumbias Au+Au collisions with high statistics up to 3.5 GeV/ c^2 and 2.2 GeV/c, respectively. Their comparison with cocktail simulations of hadronic sources reveals a sizeable and steadily increasing excess yield in the LMR at all beam energies. The scenario of broadened in-medium ρ spectral functions proves to not only serve well as dominating underlying source but also to be *universal* in nature since it quantitatively and qualitatively explains the LMR enhancements measured over the wide range from SPS to top RHIC energies. It shows that most of the enhancement is governed by interactions of the ρ meson with thermal resonance excitations in the late(r)-stage hot and dense hadronic phase. This conclusion is supported by the energy-dependent measurement of integrated LMR excess yields and enhancement factors. The former do not exhibit a strong dependence on beam energy as expected from the approximately constant total baryon density above 20 GeV, and the latter show agreement with model calculations over the wide RHIC energy regime makes a strong case for LMR enhancements on the order of a factor 2 - 3.

The extent of the results presented here enables a more solid discussion of its relation to chiral symmetry restoration from a theoretical point of view. High-statistics measurements at BES-II hold the promise to confirm these conclusions along with the LMR enhancment's relation to total baryon density with decreasing beam energy.

Zusammenfassung

Die vorliegende Doktorarbeit besteht aus einem Hauptteil (Part I) im Themengebiet der hochenergetischen Kernphysik und einem Nebenteil (Part II) über Entwicklung und Beitrag von neuen Software Modulen zur Kollaboration und der Öffentlichkeit. Der Hauptteil behandelt das Thema der Energieabhängigkeit von Dielektronen-Produktion in ultra-relativistischen Schwerionen-Kollisionen mithilfe des STAR Detektors (Solenoidal Tracker at RHIC) am Brookhaven National Laboratory in Upton, NY. Im Nebenteil werden zum Einen sieben C++ und Python Bibliotheken für Datenanalyse und Dokumentation vorgestellt. Zum Anderen wird in diesem Teil der Übergang der gesamten 15-jährigen Geschichte des STAR Softwarepakets in ein modernes System der Versionskontrolle beschrieben. Beide Teile sind im Folgenden ausführlich zusammengefasst.

Messung der energieabhängigen Dielektronen-Produktion mit STAR

Der Phasenzustand von Kernmaterie ändert sich mit zunehmender Temperatur und Baryonendichte (Section 1.1). Die Theorie der Quanten-Chromo-Dynamik (QCD) hat sich sehr erfolgreich darin erwiesen [1], die Eigenschaften dieser Phasen vorherzusagen und zu bestätigen. Im QCD Vakuum sind Quarks und Gluonen darauf beschränkt als Bestandteile von farb-neutralen Hadronen vorzukommen. Außerdem ist die globale chirale Symmetrie des QCD Langrangian im Vakuum spontan gebrochen [2]. Mit diesen beiden Charakteristiken ist die QCD in der Lage, die grundlegenden Eigenschaften des experimentellen Hadronenspektrums zu beschreiben [3].

Bei ausreichend hohen Temperaturen und Baryonendichten durchläuft Kernmaterie den Phasenübergang ins Quark-Gluon-Plasma (QGP), in dem freie Quarks und Gluonen die Freiheitsgrade bestimmen (*Deconfinement*) und chirale Symmetrie wiederhergestellt ist [4]. Diese fundamentalen Eigenschaften der QCD Materie können in ultra-relativistischen Schwerionen-Kollisionen untersucht werden [5, 6]. In den Kernstößen wird ein verhältnismäßig großes Volumen mit hohen Energie- und Nukleonendichten produziert, die vergleichbar zu den Bedingungen im frühen Universum sind (Section 1.2). Während der darauffolgenden Ausdehnung und Abkühlung durchschreitet die heiße und dichte Materie mehrere QCD Phasen, bevor sie in die beobachtbaren Teilchen des QCD Vakuums hadronisiert und ausfriert [7].

Messungen des elliptischen Flusses von Mesonen und Baryonen, zum Beispiel, geben Aufschlüsse sowohl über die Zeitskala der Thermalisierung des Mediums als auch über den Grad der kollektiven Expansion [8, 9]. Es ist allerdings wichtig, (eindeutige) Signale für die beiden fundamentalen QCD Charakteristiken des Deconfinements und der Chiralen Symmetrie Restauration zu beobachten und umfassend zu messen: Wenn Quark-Antiquark ($q\bar{q}$) Paare in einem thermisch ausgeglichenen deconfined QCD Medium annihilieren, sollte man thermische elektromagnetische Strahlung direkt vom QGP beobachten können; Änderungen der Spektralfunktion von Vektormesonen im Medium könnten Vorläufereffekte eines Verschwindens der QCD Vakuumstruktur sein [10, 11]. Die Diskussion des letzteren Zusammenhangs (Section 1.3) legt dar, dass eine koordinierte Anstrengung von theoretischer und experimenteller

Seite notwendig ist, um die Schlussfolgerungen aus den Dielektronenmessungen der ρ -Spektralfunktion bezüglich (teilweiser) Chiraler Symmetrie Restauration zu stärken.

In diesem Bezug sind Dileptonen ein einzigartiges Werkzeug. Sie durchdringen das umgebende Medium mit vernachlässigbarer Wechselwirkung und entstammen der gesamten Evolution des Systems (Figure 1.6). Die Verteilungen von invarianter Masse (M_{ee}) und Transversalimpuls (p_T) widerspiegeln ihre zeitlich geordnete Emission und sind daher empfindlich auf die Evolutionsdynamik des Systems. Insbesondere die *Low-Mass-* (LMR) und *Intermediate-Mass-*Regionen der Dielektronenspektren versprechen jeweils Zugang zur in-Medium modifizierten ρ -Spektralfunktion und zur effektiven QGP Temperatur. Für die Extraktion der QGP Temperatur muss allerdings der Beitrag eines möglicherweise Medium-modifizierten Charm Kontinuums bekannt sein [12].

Eine Vielzahl von Experimenten an SIS18 (Schwerionen-Synchrotron), SPS (Super Proton Synchrotron), und RHIC (Relativistic Heavy Ion Collider) haben die schwere Aufgabe auf sich genommen, diese seltenen Proben in einer Schwerionen-Umgebung zu messen (Section 1.3.1). CERES beobachtete als erstes Experiment einen beträchtlichen und unerklärten LMR Produktionsüberschuss im Vergleich zu einem Cocktail aus erwarteten hadronischen Quellen [13]. Die NA60 Resultate von hoch-qualitativen Dimuonen-Messungen haben die verbreiterte ρ -Spektralfunktion als bevorzugtes Szenario für den LMR Überschuss und einen partonischen Ursprung für die dominanten Quellen im IMR identifiziert [14]. PHENIX folgte mit Dielektronen-Messungen bei höchsten RHIC Energien, die eine bedeutende Verstärkung des LMR Signals und gute Übereinstimmung der IMR Produktion mit einem Charm Kontinuum von $N_{\rm bin}$ -skalierten p+p Kollisionen aufweisen [15].

Im Gegensatz zu den NA60 Ergebnissen, konnte die Größe der LMR Signalverstärkung nicht durch existierende Modellrechnungen erklärt werden - selbst mit Ausnutzung des gesamten verfügbaren Parameterraums. Messungen der Dielektronen-Produktion bei identischen Energien mit STAR am RHIC führten zu einer moderateren Verstärkung, die im Einklang ist mit den NA60 Resultaten und mit Modellrechnungen basierend auf in-Medium verbreiterten ρ -Spektralfunktionen [16]. Es sei an dieser Stelle angemerkt, dass HADES für niedrige Temperaturen und hohe Baryonendichten das *DLS Rätsel* mit einem LMR Verstärkungsfaktor von \sim 2-3 bestätigt hat [17, 18].

Diese Vorgeschichte schafft die Voraussetzungen für die umfassende Untersuchung der Dielektronenproduktion in dieser Doktorarbeit. Ermöglicht durch die Hinzufügung des Time-Of-Flight (TOF) Detektors im Jahre 2010 liefert STAR ausgezeichnete Teilchenidentifikation, niedriges Materialbudget, volle azimuthale Akzeptanz bei mittleren Rapiditäten, und breite p_T-Abdeckung [19]. Insbesondere mit der ersten Phase des *Beam Energy Scans* (BES-I) [20] bietet STAR die noch nie da gewesene Gelegenheit, eine energie-abhängige Untersuchung der Dielektronenproduktion innerhalb eines homogenen experimentellen Umfelds durchzuführen und damit die große Lücke im QCD Phasendiagram zwischen SPS und höchsten RHIC Energien zu schliessen (Section 1.4).

Die vorliegende Arbeit konzentriert sich auf die Analyse von Au+Au Kollisionen bei Strahlenergien von 19.6, 27, 39, und 62.4 GeV, die während BES-I mit ausreichender Statistik für eine solche Untersuchung aufgenommen wurden (Section 2.1). In Verbindung mit den veröffentlichten STAR Ergebnissen bei höchsten RHIC Energien stellt dies den ersten umfassenden und energie-abhängigen Datensatz bereit. Angesichts des beträchtlichen Aufwands wird dieser Datensatz der wohl einzig verfügbare bei diesen Energien in naher Zukunft bleiben.¹

 $^{^{1}}$ STAR wird weiterhin Daten mit hoher Statistik bei $\sqrt{s_{NN}}$ < 20 GeV während BES-II aufnehmen.

Zu Beginn der Analyse werden geeignete Auswahlkriterien angewandt, um den Datensatz auf hoch-qualitative Kollisionsereignisse (*Events*) und Teilchenspuren zu reduzieren (Section 2.2). Die zusätzliche Rekonstruktion der Eventebene (Section 2.2.2) ist Voraussetzung für die statistische Generierung von Untergrund-Paarverteilungen. Elektronen und Positronen werden durch Kombination von Impuls, Geschwindigkeit, und Energieverlust gemessen im TOF Detektor und der Time-Projection-Chamber (TPC) sauber identifiziert (Section 2.3). Dielektronen (e⁺/e⁻ Paare) werden aus der resultierenden Auswahl von Elektronen und Positronen kinetisch rekonstruiert und Untergrund-Beiträge statistisch abgezogen (Section 2.4), indem von *Same*- und *Mixed-Event* Methoden auf p_T-integrierte und -differentierte Weise Gebrauch gemacht wird.

Für den Vergleich zu theoretischen Rechnungen und zwischen Energien müssen die rohen M_{ee}- und p_T-Verteilungen der Dielektronen korrigiert werden (Chapter 3), um Verluste durch Detektor-Ineffizienzen und Auswahlkriterien zu beheben. Zu diesem Zweck werden simulierte Teilchenspuren in reale Events eingebettet (*Embedding*) und mit denselben Mitteln wie für die experimentelle Eventrekonstruktion durch den Detektor verfolgt (Section 3.1). Die Abschätzung von systematischen Unsicherheiten erfordert den Vergleich von simulierten zu sauberen experimentellen Verteilungen basierend auf geeigneter Teilchenauswahl. Die Berechnung von Gesamt-Effizienzen der Spurrekonstruktion und -verfolgung folgt dem Vorgehen der experimentellen Datenanalyse und benutzt die dedizierte Teilchenauswahl von Embedding und Experiment (Section 3.2). Die Spureffizienzen werden schließlich mithilfe einer einfachen Zwei-Körper Monte-Carlo Simulation in Paareffizienzen übertragen (Section 3.3).

Die Physik-Interpretation der experimentellen Ergebnisse in dieser Arbeit (Chapter 5) basiert auf (i) der Simulation hadronischer Zerfallskanäle, die bekanntermaßen zur Dielektronenproduktion in elementaren Kollisionen beitragen, und (ii) effektive Modellrechnungen, die die in-Medium Effekte beschreiben. Ersteres stellt den sogenannten hadronischen Cocktail dar, dessen Quellen und charakteristischen Massenregionen in der Einleitung im Zusammenhang mit p+p Kollisionen vorgestellt und mit früheren Dielektronen-Messungen in Schwerionen-Kollisionen verglichen werden (Section 1.3). Die Einzelheiten der Cocktail Simulationen, wie sie für die energie-abhängige Dielektronen-Produktion in Au+Au Kollisionen bei BES-I Energien verwendet werden, sind ausführlich beschrieben (Section 4.1). In der Einleitung (Section 1.3) wird auch der gemessene LMR Produktionüberschuss über dem Cocktail und dessen mögliche Verbindung zu Chiraler Symmetrie Restaurierung mittels Hadronic Many-Body Theory (HMBT) behandelt. Im Simulationskapitel (Section 4.2) werden einige veranschauliche Einzelheiten und die Ergebnisse dieser Berechnungen für BES-I Energien diskutiert.

Für die genannten vier Strahlenergien, legt diese Dissertation M_{ee} - and p_T -Spektren vor (Chapter 5), gemessen in 0-80% *minimum-bias* Au+Au Kollisionen mit hoher Statistik bis zu jeweils 3.5 GeV/ c^2 und 2.2 GeV/c. Deren Vergleich zu Cocktail Simulationen aus hadronischen Quellen deckt einen beträchtigen und stetig zunehmenden LMR Überschuss bei allen Energien auf. Dieser kann weder durch Vakuum ρ/ω -Spektralfunktionen, die durch die Feuerball-Expansion propagiert wurden, noch durch die entsprechenden bloßen Ausfrierungsbeiträge beschrieben werden. Modellrechnungen mit einer in-Medium verbreiterten ρ -Spektralfunktion auf Grundlage von HMBT erreichen stattdessen gute Übereinstimmung sowohl über den gesamten Energiebereich als auch in der Form der M_{ee} - und p_T - Verteilungen. Dieser Beitrag dominiert im LMR über die $q\bar{q}$ Beiträge vom QGP und dient daher im Allgemeinen gut als zugrunde liegende Ursache des gemessen Überschusses im gesamten RHIC Energiebereich. Die Beobachtung bedeutet auch, dass der Großteil der Signalverstärkung durch Wechselwirkungen des ρ -Mesons mit thermischen Resonanzanregungen in der spät(er)en heißen und dichten hadronischen Phase geregelt wird.

Die Energie-Abhängigkeit sowohl der M_{ee} -integrierten und auf invariante Pionen-Produktion normierten LMR Überschüsse als auch der LMR Signalverstärkung unterstützen diese Schlussfolgerung. Im Einklang mit der etwa konstanten totalen Baryonendichte überhalb von 20 GeV weisen die absoluten Überschüsse keine starke Abhängigkeit von der Strahlenergie auf. Die Verstärkungsfaktoren des LMR Signals stimmen mit CERES Messungen bei SPS Energien trotz unterschiedlicher Akzeptanzen überein - die STAR Daten sind jedoch von höherer Qualität. Die von STAR gemessene Beständigkeit des LMR Überschusses und dessen Übereinstimmung mit Modellrechnungen über den breiten RHIC Energiebereich liefern überzeugende Argumente für Verstärkungsfaktoren eher im Bereich 2 - 3 als 5 oder mehr.

Die Energie-Abhängigkeit der integrierten LMR Überschüsse ermöglicht eine interessante Prognose für die zweite Phase des *Beam Energy Scans* (BES-II). Im Energiebereich unterhalb von 20 GeV weisen sowohl Messungen der totalen Baryonendichten als auch ρ -Meson-basierte PHSD Rechnungen auf eine ungefähre Verdopplung des LMR Überschusses hin [21, 22]. Messungen während BES-II mit hoher Statistik sollten ausreichend Genauigkeit bieten, um diese Vorhersagen zu testen und unser Verständnis der LMR Signalverstärkung sowie dessen zugrunde liegende Ursache weiter zu kräftigen [23]. Außer gesteigerter Statistik wird BES-II mit der beabsichtigten iTPC Aufrüstung feinere Spurverfolgung und verbesserte Fähigkeiten zur Dimuonen-Messung liefern.

In der gegenwärtigen Untersuchung sind verlässliche Rückschlüsse auf QGP Strahlung im IMR leider beschränkt durch a) die vorhandene Statistik, b) die Unsicherheiten in den $c\bar{c}$ Wirkungsquerschnitten in Nukleon-Nukleon Kollisionen, und c) die möglichen Medium-Modifikationen des Charm Kontinuums durch Entkorrelation der e^+/e^- Zerfallsprodukte. Mithilfe der kürzlich abgeschlossenen Aufrüstungen der HFT (Heavy Flavor Tracker) und MTD (Muon Telescope Detector) Detektor-Teilsysteme werden es BES-II Messungen aber ermöglichen, das Charm Kontinuum und damit indirekt QGP Strahlung zu untersuchen. Dies ist insbesondere wichtig für den LMR, da der $c\bar{c}$ Beitrag zum Gesamt-Cocktail im 0.4 - 0.7 GeV/ c^2 Massenbereich von etwa 20% bei 19.6 GeV auf etwa 60% bei 200 GeV steigt.

Zusammenfassend stellen die STAR Messungen während BES-I hoch-qualitative Datensätze zur Verfügung, die wesentlich für das Verständnis der LMR Signalverstärkung bezüglich ihrer M_{ee^-} , p_T^- und Energie-Abhängigkeit sind. Die Untersuchung der zugehörigen Zentralitätsabhängigkeit in der nahen Zukunft würde die extrahierbaren Ergebnisse vervollständigen und könnte neue Informationen über die Energie-Abhängigkeit der Feuerball-Lebensdauer preisgeben. Das Szenario der in-Medium verbreiterten ρ -Spektralfunktionen erklärt quantitativ und qualitativ die gemessene LMR Signalverstärkung über den breiten Bereich von SPS bis zu höchsten RHIC Energien. Diese Erklärung erweist sich daher nicht nur dazu in der Lage als dominante zugrunde liegende Ursache zu dienen sondern auch als *universell* in ihrem Wesen.

Der Umfang der dargelegten Ergebnisse erlaubt eine solidere Diskussion im Hinblick auf deren Beziehung zu Chiraler Symmetrie Restauration vom theoretischen Standpunkt aus. Messungen mit hoher Statistik während BES-II verprechen, diese Folgerungen sowie die Relation von LMR Signalverstärkung zu totaler Baryonendichte mit abnehmender Strahlenergie zu bestätigen.

X

Software Projekte für STAR und Open-Source

Die C++ Softwareklasse StV0TofCorrection (Section 7.1) implementiert Funktionen, um die Flugzeit von Teilchen aus V_0 (Off-Vertex) Zerfällen zu korrigieren. Der zugrunde liegende Algorithmus basiert auf der berichtigten Rekonstruktion der Mutterteilchen. Die Anwendung auf Λ - und Ω -Zerfälle legt dessen Fähigkeit dar, zusätzlich Untergrund von anderen Zerfällen zu verwerfen. Außerdem erlaubt die Klasse dem Benutzer, einen Standardfilter auf die korrigierten Teilchenmassen anzulegen und damit das Signal-zu-Untergrund Verhätnis zu verbessern. Der Quellcode dieser Arbeit ist seit Januar 2011 Teil des StBTofUtil [24] Moduls in der offiziellen STAR Code Repositorie. Die neueste Revision der Implementation ist von Dezember 2013. Ein interner Report wurde der STAR Kollaboration zugänglich gemacht [25, 26] 2 .

Die C++ Softwareklasse StBadRdosDb (Section 7.2) wurde im Rahmen dieser Arbeit entwickelt, um im Laufe einer Analyse bequem Informationen über die Anzahl der fehlenden Auslese-Boards der TPC zu erfragen. Die Daten der 2010 und 2011 Strahlzeiten werden in zeitliche Perioden (run ranges) mit gleicher Anzahl fehlender Boards unterteilt und in einem passenden Datenbankformat gespeichert. StBadRdosDb kann dann benutzt werden, um die zugehörige Periode für einen spezifischen Run zu erhalten. Dies ist insbesondere hilfreich für Analysen, die sich auf stabile Detektorbedingungen während der Strahlzeit verlassen und daher empfindlich auf run-range-abhängige Effizienzkorrekturen sind. StBadRdosDb wurde der gesamten STAR Kollaboration bekannt gemacht [27] und ebenfalls in der STAR CVS Repositorie zur Verfügung gestellt [28].

Die C++ Softwareklasse StRunIdEventsDb (Section 7.3) wurde entwickelt, um die Handhabung von Run-abhängigen Untersuchungen über mehrere Strahlenergien (Part I) zu erleichtern. Für alle BES-I Energien der Jahre 2010 und 2011 stellt die Implementation eine Abbildung von einer spezifischen Run Identifikationsnummer zum zugehörigen Listenindex bereit. Für eine Kombination von Run und Trigger kann desweiteren die Anzahl an Events für alle Energien abgefragt werden.

Ein weiteres Kapitel im zweiten Teil dieser Dissertation (Chapter 8) beschäftigt sich mit der Ausführung des Übergangs der zentralen STAR Code Repositorie von CVS zu git. Es wird vorgeführt, wie die gesamte Geschichte aller STAR Module mithilfe von cvs2git konvertiert werden kann. Außerdem wird gerrit als neues Review-System für zukünftige Code-Änderungen und als Gateway für alle Interaktionen mit der zentralen Repositorie eingeführt. Dies bezieht die Bereitstellung der notwendigen Skripten und Anweisungen sowie die Demonstration eines Einsatzes des Review-System auf einem entfernten Server mit ein. Als Ersatz für cvsweb zum Browsen der neuen Repositorien wird cgit vorgeschlagen.

Die Größe und projektinternen Bibliotheksabhängigkeiten machen die Organisation von Software entwickelt für Physik-Analysen (Part I) mühsam [29]. Oft werden die ROOT-basierten shared libraries von länglichen Makros anstatt von kompilierten Programmen aus aufgerufen, obwohl es die Qualität des Softwareprojekts erheblich verbessern würde. Das C++ Programm ckon (Section 9.1) wurde daher entwickelt, um den Arbeitsablauf der Kompilation und Ausführung von ROOT Analysen zu automatisieren. Mit den Befehlen ckon setup && ckon erlaubt ckon dem Benutzer, den Erstellungsprozess eines gesamten Softwareprojekts automatisiert zu durchlaufen, aber gleichzeitig über dessen Ordner-Layout zu entscheiden. Der Benutzer ist nicht nur vom Makefile-Schreiben befreit sondern kann auch auf einfache Weise fremden Code oder Dritt-Bibliotheken sowie eigene Hilfs- und Datenbankklassen mithilfe einer YAML Konfigurationsdatei einbauen.

² Dieser Teil der Dissertation wurde vom DAAD durch ein Auslandsstipendium unterstützt.

Das graphische Darstellungswerkzeug *ccsgp* (Section 9.2) wurde entwickelt, um Veröffentlichungs-fertige wissenschaftliche Abbildungen mit Gnuplot und Python zu produzieren. Die Repositorie *wp-pdf* (Section 9.3) umfasst eine Ansammlung an Anweisungen und Software, um —basierend auf denselben AsciiDoc Dateien — simultan eine Website und einen gedruckten Report für den STAR-internen Review-Prozess zu generieren. Das Kommandozeilen-Program *rmrg* (Section 9.4) erweitert ROOTs hadd Programm [30] mit fehlenden Features und besserer Kontrolle, um ROOT Bäume oder Histogramme zusammenzufügen.

Part I

Physics: Energy-Dependence of Dielectron Production in STAR

Chapter 1

Introduction

«We should investigate [novel] phenomena by distributing high energy or high nucleon density over a relatively large volume.»

— T.D. Lee (1974 [5])

1.1 The Phases of QCD

The Standard Model of particle physics [2] comprises a collection of quantum field theories describing the electromagnetic, weak, and strong interactions of subatomic particles with relative strengths at the size of a nucleon according to their coupling constants:

$$\alpha_{\rm s} \sim 1$$
, $\alpha_{\rm em} \sim 1/137$, and $\alpha_{\rm w} \sim 10^{-6}$.

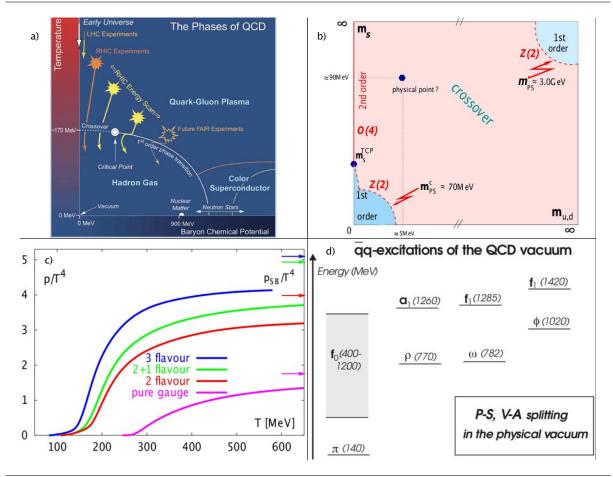
Quantum-Chromo-Dynamics (QCD) [31-35] has emerged [1] as the underlying theory of strong interactions describing the fundamental properties of quarks and their color-exchanging interactions via gluons. Even though QCD has been a very successful theory to predict and guide experimental observations (e.g. α_s [36], jets [37]), some fundamental questions remain unresolved: For instance, the nuclear constituents of ordinary matter are known but it is yet to be understood how they arrange themselves into the composite structures observed in nature. The running coupling constant α_s of QCD separates the low-energy regime (low momentum transfers Q, large distances) from the high-energy regime in which α_s is small enough for QCD to be treated perturbatively, i.e. by Taylor expansion in orders of α_s [38]. This expansion is applicable down to $Q \sim 1$ GeV/c or above distances of about 0.2 fm which is still about an order of magnitude smaller than the nucleon radius. Hence, the solution of the QCD equations and therefore the behavior of the nuclear force on energy scales relevant for the description of stable atomic nuclei remain unsettled.

Significant progress in this non-perturbative regime has most successfully been made within the computational framework of *Lattice QCD* as major mathematical constraints ¹ can be avoided at zero net baryon densities and finite temperatures [39, 40]. However, on scales relevant to the internals of the nucleons, i.e. for the study of *quark matter* phases with quarks and gluons as degrees of freedom, perturbative QCD suggests the existence of asymptotically free (deconfined) quarks and gluons allowing them to escape their *confinement* into color-neutral hadrons [38]. Hence, under high temperatures and energy densities, the equations of QCD predict that nuclear matter undergoes a phase transition into the so-called Quark-Gluon-Plasma (QGP) [4] — a "soup" in which quarks and gluons constitute the relevant degrees of freedom.

¹ in form of the numerical sign problem impeding importance sampling.

In 2005, theorists and experimentalists [41] claimed the discovery of a strongly coupled QGP (sQGP) sourced in a so-called Color Glass Condensate (CGC) which was critically discussed at the time by the experiments at the Relativistic Heavy-Ion Collider (RHIC, [42]) emphasizing the need for additional measurements of various other variables [43-46]. It turns out that this sQGP behaves much like a *perfect fluid* with a viscosity near the quantum limit [47] and unlike a weakly interacting plasma as would intuitively be suggested by the small α_s in the perturbative regime of QCD. In recent years, the study of the properties of this dense nuclear matter has been the main focus of the *High Energy Nuclear Physics* community [48-50].

Figure 1.1 (Details see text) a) Diagram highlighting the current conception on the possible phases of QCD versus temperature and baryon chemical potential. b) Columbia phase diagram from Lattice QCD as function of up/down ($m_{\rm u,d}$) and strange ($m_{\rm s}$) quark masses [39]. The lower left and upper right regions depict the first-order chiral and deconfinement transitions, respectively. The calculations reveal the point of the transition corresponding to physical quark masses to be located in the large crossover regime. c) Temperature dependence of QCD pressure for different degrees of freedom released during the transition from hadron gas to QGP [51]. Arrows indicate the respective Stefan-Boltzmann limit valid for vanishing coupling, i.e. for $T\rightarrow\infty$. d) Measured quark-antiquark excitation spectrum showing the splitting of pseudoscalar-scalar (P-S) and vector-axialvector (V-A) chiral partners in the QCD vacuum [3]. Note that, Section 1.3 later refers to the ρ -a₁ partners as particularly interesting for the study of chiral symmetry breaking.



The QCD phase diagram shown in Figure 1.1a represents the current conception how strongly interacting nuclear matter evolves into other phases when varying the thermodynamical environment, namely temperature T and baryon-chemical potential μ_B which is linked to net baryon density. Reaching a better understanding of the QCD phase diagram has direct implications on the role of nuclear matter in the cosmos. The part of the phase diagram at low temperatures and high baryon densities, on the one hand, is closely related to the dense nuclear matter at the core of neutron stars [52]. Due to the tiny ratio of baryon to photon number of about 10^{-9} ($\propto \mu_B/T$) [2], the part at high temperatures and low densities, on the other hand, corresponds to the thermodynamical path that the expanding and cooling early universe took microseconds after the big bang.

At moderate temperatures and baryon densities, nuclear matter exists in form of a Hadron Gas [53] as dictated by the confining long-range nature of QCD. Around temperatures of about 170 MeV, Lattice QCD predicts the liberation of the confined quarks to the QGP [54] resulting in a notable rise in pressure with increasing temperature due to the release of many additional degrees of freedom (see Figure 1.1c). The calculation for 2+1 flavors using light up/down quarks and a heavy strange quark corresponds to the most realistic case for the equation of state [51]. The calculations in Figure 1.1b at zero net baryon density [39] also identify the transition to be of rapid analytical crossover type given the location of the physical quark masses in the broad range of possible $m_{u,d}$ and m_s configurations in the so-called Columbia phase diagram [55].

Even though Taylor expansion in μ_B allows Lattice QCD to be extended into the small nonzero $\mu_{\rm B}$ regime, effective models like Nambu-Jona-Lasinio [56, 57] need to be employed instead to cover predictions beyond $\mu_B \sim T$. However, such models also need to incorporate the second fundamental QGP characteristics after deconfinement, namely chiral symmetry breaking (χ SB). Chiral symmetry is evident in the zero quark mass limit of the QCD Lagrangian in form of a re-organization of the QCD vacuum in left and right handed contributions with respect to the orientation of spin versus parity. It is spontaneously broken by the QCD vacuum exhibiting a non-zero quark-antiquark condensate $(\langle \bar{q}q \rangle)$ [58], and hence expected to be restored at high temperatures [59]. Spontaneous χ SB explains the basic features of the experimental hadron spectrum [3], i.e. the manifestation of eight (nearly) massless Goldstone bosons (π , K, η) as well as non-degenerated opposite parity isospin multiplets as observed in Figure 1.1d. The effective models used at $\mu_B > T$ suggest this chiral transition to be of first order for realistic light quark masses [60, 61]. Together with the Lattice QCD predictions at zero μ_B , it results in the appearance of a critical point between the crossover and first-order regions. The latter might end in another critical point at low temperatures due to an unclear border between superfluid nuclear matter and superconducting quark matter [62].

The occurrence of the deconfinement and chiral transitions can intuitively be understood using the MIT bag model [63, 51] which treats hadrons as objects confining the valence quarks within a finite size of vanishing $\langle \bar{q}q \rangle$: At high temperatures, the individual bags merge into a single large bag allowing quarks and gluons to move freely (see percolation models for QCD [64]). Also, the hadronic bag is larger than the constituent quark bag defined by current quarks covered in a cloud of virtual quarks and gluons. This has lead to the speculation of distinct deconfinement and chiral phase transitions with $T_d \leq T_{\gamma}$ [65, 66].

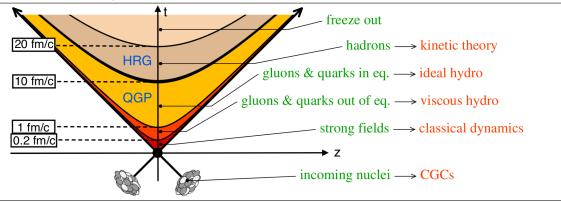
The preceding discussion only outlines the most prominent features of the rich QCD phase diagram bearing relevance to the contents and objective of this thesis (Section 1.4). The publications [62] and [67] including the references therein review the phase diagram in dense QCD and at high baryon densities giving rise to additional partially conjectured phase structures like *quarkyonic matter*, for instance, which shares properties from baryonic and quark matter phases.

1.2 Ultra-relativistic Heavy-Ion Collisions

The quote at the beginning of Chapter 1 [68], recalls T.D. Lee's suggestion to try restoring the broken symmetries of the physical vacuum temporarily by studying extended environments of high energy or nucleon densities. It was subsequently demonstrated [5, 6] that the latter could be achieved via relativistic heavy-ion collisions which are still to date the only means to recreate nuclear matter in the laboratory as it existed during the early universe. The phase diagram in Figure 1.1a also depicts μ_B -T-regions currently reachable by experiments at the Large Hadron Collider (LHC), in RHIC's top energy and Beam Energy Scan (BES) programs as well as at the future Facility for Antiproton and Ion Research (FAIR) — to name a selected few. The initial phase of the BES program in the years 2010/11 (BES-I) serves the purpose of scanning the phase diagram of QCD, first and foremost, for evidence of the critical point and the first order phase transition. To locate these characteristics of nuclear matter, the considerable capabilities of the Solenoidal Tracker at RHIC (STAR) allow for a multitude of observables like particle production, collective flow, fluctuations, cumulants, jets and others to be measured and studied in BES-I [20]. Consistently combining the resulting various signatures over a wide range of beam energies makes the BES program a powerful tool to explore the \sqrt{s-dependence} as well as possible "turn on/off" effects of partonic media.

Figure 1.1a also indicates the according evolution trajectories such a medium takes through the QCD phase diagram while expanding and cooling. To provide the reader with better insights regarding the evolution of a heavy-ion collision, the space-time picture of the subsequential stages are depicted in Figure 1.2 and schematically discussed in the following [69] in terms of the invariant *proper time* $\tau = \sqrt{t^2 - z^2}$.

Figure 1.2 Stages of a heavy-ion collision versus time t and collision axis z [69]. The invariant *proper time* τ is constant along the solid hyperbolic curves and approximate values corresponding to the various transitions are given in the boxes on the left. The annotations on the right denote some of the stages' features and theoretical treatments. See text for more details.



Before the collision (τ < 0), the incoming nuclei travel at ultra-relativistic speeds and time dilation causes them to appear as pancake-like objects to an observer in the center-of-mass frame. The nuclear constituents within these thin disks are forced by the Lorentz contraction on very small distances at which (color-carrying) gluons have taken over as the dominating content of hadrons [70]. The gluons can then self-generate very high gluon densities via gluon-splitting (condensate) which inversely corresponds to very high transverse momenta making the incoming nuclei effectively behave like gluonic walls. Such a solid-type behavior on short as opposed to liquid-type on long time scales coined the term for this other new form of nuclear matter: *color glass condensate* (CGC) [71]. The stochastic source of these self-generating high-density gluon fields is hence of basically static nature which allows the parton distributions to be replaced by an ensemble of coherent classical fields for the CGC's theoretical treatment [72].

The initial scattering at $\tau = 0$ is followed by so-called *hard* processes with momentum trans-

fers of typically Q > 10 GeV/c at LHC energies resulting in the characteristic di-jet events [73, 74], for instance. Around $\tau \sim 0.2$ fm/c, the transverse momentum scale becomes *semi-hard* with $Q \sim 1$ GeV/c and the gluons composed in the CGC are liberated generating most of the final-state multiplicity via fragmentation and hadronization of these initial-state gluons. The liberated partons form the non-equilibrium state of partonic matter called *Glasma* until it thermalizes into the QGP at $\tau \sim 1$ fm/c [75]. Naively speaking, thermalization occurs when scattering times characterized by small interaction lengths are small compared to expansion times. Such a quick approach to thermalization at about 1 fm/c requires coherent and strong self-interaction of the liberated partons to compete the medium expansion [76]. However, redistribution of energy in spite of being rapidly driven apart only works to a certain degree since the QGP keeps on expanding and cooling. The result is a space-time dependent temperature profile which only allows for local thermal equilibrium to be reached during expansion. The development of thermal equilibrium distinguishes the respective theoretical treatment of Glasma and QGP via viscous and ideal hydrodynamics [77] which describe the medium's expansion and flow, thus referring to the fluid's long-range behavior.

At $\tau \sim 10$ fm/c, hadronization traps quarks and gluons inside color-less hadrons corresponding to the previously discussed phase transition into a Hadron Resonance Gas (HRG). The continuously expanding and cooling HRG subsequently undergoes two conceptually different so-called *freeze-out* transitions [7]: (i) a chemical freeze-out stopping inelastic processes that change hadronic species into each other and hence freezing hadronic abundances, and (ii) a thermal freeze-out at which all momentum-changing interactions, i.e. also all elastic collisions, cease. The cross section of the abundance-changing inelastic hadron-hadron reactions is (usually much) smaller than the total cross-section which drives all momentum-changing and hence thermally equilibrating reactions. This makes it increasingly harder for inelastic reactions to keep up with the continuously decreasing density. They hence become unlikely earlier during the medium expansion than elastic reactions, and thus cause the chemical freeze-out to occur at higher temperatures than the thermal freeze-out [78]. The latter happens at $au\sim 20$ fm/c when the HRG cannot keep the local thermal equilibrium intact anymore. Freely streaming particles are then allowed to escape to the detector measuring momentum distributions that are expected to be the same as the thermal distribution in the very late-stage expansion [79]. Note that, for RHIC (7.7 - 200 GeV) and SPS (160 - 200 AGeV) energy regimes, the chemical freeze-out temperature is close to the critical temperature of the deconfinement transition. At energies covered at the Alternating Gradient Synchrotron (AGS, < 11 AGeV), however, the chemical and thermal freeze-out temperatures approach each other and finally coincide at energies measured at the Heavy-Ion Synchrotron (SIS18, < 2 AGeV) [80].

An important concept in the evolution of heavy-ion collisions is the aforementioned development of a collective motion called flow [81]. In the simplified case of a (strictly) central collision, the interaction zone is circular when viewed along the incident beam directions. The constituents rescattering in the expanding nuclear liquid move outward collectively in a radially isotropic manner typically referred to as $radial\ flow$ [82]. The according radial expansion velocity β can be extracted from the paramaterization of the Blast-Wave model to final-state hadron p_T spectra [83] which are a result of inherently isotropic thermal emission at temperature T and radial flow. The latter is reflected in the definition of the initial effective temperature of the medium [84, 85]:

$$T_{
m eff} pprox T \sqrt{rac{1+eta}{1-eta}}.$$

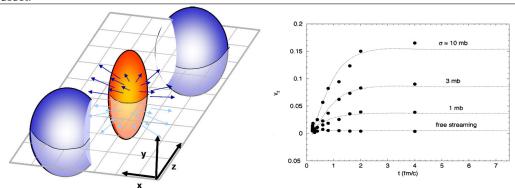
The initial overlap zone of two non-centrally colliding nuclei, illustrated in Figure 1.3 (left) [86], is usually of elliptic shape which results in a higher pressure gradient along the shorter direction than along the longer direction. Rescattering thus causes the constituents of the liquid to collectively flow faster in the shorter direction effectively converting the initial spatial

into a momentum anisotropy. The azimuthal anisotropy in flow velocity also reveals the self-quenching nature of this so-called *elliptic flow* as it drives the matter toward a spherical shape. Elliptic flow is characterized by the second Fourier coefficient v_2 in azimuthal multiplicity distributions of final state hadrons [8, 9]:

$$\frac{1}{N}\frac{\mathrm{d}N}{\mathrm{d}\phi} = v_0 + 2v_1\cos\phi + 2v_2\cos(2\phi) + \cdots$$

The chronological build-up of elliptic flow during the expansion is shown in Figure 1.3 (right) using the v_2 measure. The full magnitude of the elliptic flow only develops late(r) in the evolution with the specific timing depending on the effective parton scattering cross sections. Hence, particles created early in the evolution and embedded in this anisotropically expanding medium experience no significant flow, yet. The early saturation of elliptic flow well before the hadronization transition is also indicative of the thermalization to happen on the quark rather than the hadronic level [87].

Figure 1.3 (left) Illustration of the development of flow in a non-central heavy-ion collision caused by the asymmetric spatial shape of the collisional overlap zone. (right) Time-dependence of elliptic flow v_2 for different partonic scattering cross sections [87]. See text for discussion.



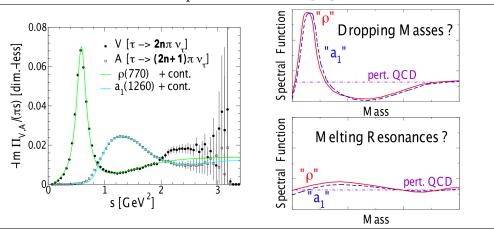
In summary, Figure 1.2 reiterates the similarity of the space-time picture of a heavy-ion collision to Big Bang cosmology and the related discussion identifies a few fundamental questions that need particular attention in the context of heavy-ion collisions — especially if one wants to prove the creation of a QGP [88, 45]. First, whether thermal equilibrium is reached through sufficient rescattering during the initial stage of the collision. Measurements of elliptic flow at RHIC reveal a magnitude of collective expansion that indicates thermalization time scales of less than 1-2 fm/c and hence, justify the characterization of the medium using bulk thermodynamic variables [89]. Second, whether a distinctive footprint for individual partons can be identified. Number-of-constituent (NCQ) scaling holding up for mesons and baryons suggests a collectively expanding partonic source [90, 91]. Third, signals of the two fundamental QCD characteristics, chiral symmetry restoration and deconfinement, need to be comprehensively studied. For the latter characteristic, detection of direct thermal electromagnetic radiation as expected from $q\bar{q}$ annihilation in a thermally equilibrated deconfined QCD medium, would provide one of the desired *smoking guns*. Another would be to unequivocally measure the disappearance of the vacuum consequences of spontaneous χSB in the QCD medium (see Figure 1.1d and Section 1.1).

As will be discussed in the remainder of this introductory chapter, both signatures might be accessible via *dileptons* which are regarded as *golden probes* of the early stages due to their bulk-penetrating electromagnetic nature. To cover the various aspects of these striking final-state ingredients of a heavy-ion collision, Section 1.3 further motivates the study of dilepton production including a recapitulation of its experimental and theoretical status. Section 1.4 concludes the introduction with a brief overview of the thesis and its objective.

1.3 Dileptons as Bulk-Penetrating Electromagnetic Probes

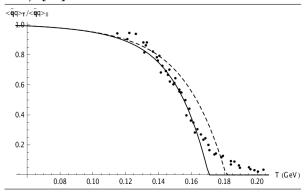
The precise measurement of the ρ - and a_1 -mesons' spectral functions in hadronic τ decays at the Large Electron-Positron collider (LEP) [92] is shown in Figure 1.4 (left), underlying the vector-axialvector (V-A) splitting of about 500 MeV in Figure 1.1d. It exhibits a clear separation of the respective pole masses as expected from spontaneous χ SB in the QCD vacuum. In a simplified picture, two scenarios can be distinguished for the degeneration of the chiral partners in a quark matter environment (Figure 1.4 right, [88]): (i) the a_1 pole mass drops to the ρ mass and/or they approach each other, hence keeping the resonant strucure intact, or (ii) the resonances "melt" down to approach the according production rates from perturbative QCD. The clarifying study of the fate of chiral symmetry and its manner of possible restoration in dense states of nuclear matter, thus requires experimental access to the so-called *in-medium* spectral functions of the chiral partners.

Figure 1.4 (left) Measurement of the chiral partners ρ - and a_1 -meson in hadronic decays at LEP. (right) Simplified scenarios of dropping pole masses or melting resonances for the degeneration of the chiral partners in an environment of hot and dense nuclear matter. Above an invariant mass of about 1.5 GeV/c² ($\sqrt{s} = M_{ee}$) called the *duality threshold*, the production rates are expected to resemble the ones from perturbative QCD. [88]



However, the relation of medium-modifications of vector meson spectral functions to chiral symmetry restoration (χ SR) is not straight-forward. Spectral functions need to be connected, on the one hand, to the order parameter of the chiral transition, namely (a reduction in) the $q\bar{q}$ condensate, and, on the other hand, to the measured dilepton yields emanating from the entire fireball evolution. This paragraph follows the arguments in [10] (Section 2.7.1) and [11] in an effort to make the connection that allows dilepton production measured in heavy-ion collisions to be interpreted with respect to χ SR.

Figure 1.5 Temperature dependence of the chiral quark condensate from Lattice QCD calculations (solid circles) compared to the condensate-diminishing effect of thermal excitations in the HRG (dashed line). A high-order temperature-dependent correction improves the agreement above 140 MeV (solid line). [11]



Qualitatively, the relation can be retraced through the discussion of the model-independent (T, μ_B)-dependence of the chiral condensate in a pion or nucleon gas at low μ_B and T [93-95]:

$$\frac{\langle \bar{q}q \rangle (T, \mu_B)}{\langle \bar{q}q \rangle_0} = 1 - \sum_h \frac{\rho_h^s \Sigma_h}{f_\pi^2 m_\pi^2}$$

with f_{π} the pion decay constant, ρ_h^s the (scalar) density and $\Sigma_h = m_q \langle h | \bar{q}q | h \rangle$ the sigma commutator of hadron h. In the non-relativistic limit, Σ_h/m_q denotes the scalar quark density in the hadron. The expression illustrates that χ SR is an additive effect since every hadron contributes a certain decrease to the quark condensate according to its Σ_h , with ρ_h^s being produced through thermally excited hadrons [95]. The expression has been generalized for a hadron resonance gas in leading order of den-

sity, also taking care of hadronic interactions in a manner consistent with chiral symmetry. In other words, thermal resonance excitations in the hadron gas give rise to the so-called "vacuum cleaner" effect since the resonances' quark content "sweeps up" the chiral condensate of the vacuum [11]. Together with Figure 1.5, this shows that presence of hadrons alone already results in the reduction of the chiral quark condensate consistent with ab-initio Lattice QCD calculations. The connection to spectral functions becomes clear when studying the mechanisms of the effective hadronic model in Section 4.2 and [96] that are required to comply with the results of the dilepton measurements introduced in Section 1.3.1 and especially with the results of this thesis (Chapter 5). In short, the components that underlie the preferred scenario of a broadening of the ρ -meson's spectral function, are (i) the modified coupling of its pion cloud to the medium $(\rho \pi \pi)$, and (ii) its direct interactions with the mesons and baryons in the heat bath exciting further resonances (ρ MB). Hence, thermal resonance excitations driving the reduction of the chiral condensate are actually one of the processes causing the ρ -broadening (in addition to chiral mixing through the pion cloud). This close relation of (partial) χ SR and ρ spectral function is further strengthened by the fact that the $\rho\pi\pi$ and ρ MB medium effects find their counterparts in the Σ_h term since it decomposes into short- and long-distance contributions from the hadron's quark core and pion cloud, respectively [97].

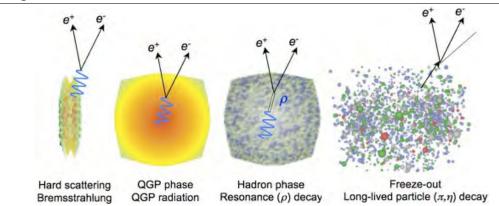
Taking the direct approach and measuring the a_1 meson in the medium is experimentally difficult due to its low production rates and broad width. Instead, a coordinated procedure has to be followed to quantitatively connect the chiral quark condensate to measured dilepton yields through the ρ meson's spectral function [10]: On the theoretical side, the vector and axial-vector spectral functions are calculated within a chirally invariant model carefully constrained by basic symmetry principles using effective vertices in agreement with available data. Using Weinberg sum rules, temperature-dependent pion decay constants and quark condensates can be deduced and compared for consistency with Lattice QCD results. The spectral functions are propagated through a realistic model for the fireball expansion taking into account measured hadronic observables (e.g. v₂). On the experimental side, this enables the detailed comparison to data with respect to centrality-, $\sqrt{s_{\rm NN}}$ -, mass- and p_T-dependence. Besides centrality, this thesis covers these pivotal ingredients and hence tightens the connection for dilepton data to be interpreted in terms of χ SR. Since spectral functions are difficult to obtain in Lattice QCD in the near future, this approach is the only way to enable another leap forward in dilepton physics.

Vector mesons are generally a good choice for the *in-medium* spectroscopy of a quickly expanding and cooling fireball. As indicated by the life times listed below, short-lived resonances such as the ρ -, ω - and ϕ -mesons decay on time scales very similar to the evolution of a heavy-ion collision (cf. Figure 1.2). The long-lived pseudo-scalar π - and η -mesons, on the other hand, decay long after freeze-out and hence, are not suitable for the study of the early-stage QCD medium.

ρ	Δ	ω	φ	η	π^0
1.3 fm/c	1.7 fm/c	23 fm/c	46 fm/c	151 pm/c	26 nm/c

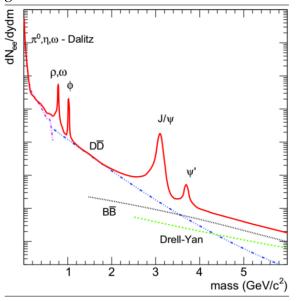
Due to the matching quantum numbers $J^{PC}=1^{--}$, Vector Meson Dominance [98] also allows vector mesons to couple to virtual photons which in turn directly decay into *dielectrons* (e^+e^- pairs) and *dimuons* ($\mu^+\mu^-$ pairs) collectively called *dileptons*. The electromagnetic nature of their interactions causes interaction lengths λ_{mfp} much larger than the fireball life time rendering final-state interactions negligible. Hence, *dileptons* can serve as pristine probes allowing for direct and undistorted access to the properties of *in-medium* spectral functions which makes them the most promising candidates to conduct these studies. Note that, even though Δ -baryons exhibit life times comparable to the ρ -meson, such in-medium information would be lost in the respective hadronic decay channels $\Delta \to \pi N$ and $\rho \to \pi \pi$. The decay products suffer rescattering in the fireball which basically restricts their sensitivity to the break-up stages of the collision.

Figure 1.6 Sources of dielectron production during the subsequential stages of a heavy-ion collision. Dielectrons can be referred to as *bulk-penetrating* probes since they penetrate through the surrounding medium without noticeable interaction and also emanate from the earliest (bulk) stages.



As visually depicted in Figure 1.6, dielectrons also emanate from the initial hard scattering via Bremsstrahlung and from the QGP phase via electromagnetic (thermal) radiation in addition to the decays during hadron gas and freeze-out phases. Being thus created throughout the entire evolution of the hot dense medium, dielectrons can be considered *bulk-penetrating* probes and provide dynamic as well as direct information about their original heavy-ion collision stage encoded in their invariant mass (Mee) and transverse momentum (p_T). At this point, it is illustrative to discuss the prevalent features of a simulated dielectron invariant mass spectrum in p+p collisions as shown in Figure 1.7 and compare to the expected sources of dielectron production in heavy-ion collisions. There are multiple categories of electromagnetic radiation and *background* sources at play contributing to different invariant mass regions of the "physical" spectrum. It can generally be concluded that in heavy-ion collisions, earlier creation times correspond to higher temperatures and thus to higher dielectron invariant masses and vice versa.

Figure 1.7 Simulated dielectron invariant mass spectrum in p+p collisions at 200 GeV [12]. Details on the simulation at BES energies in STAR can be found in Section 4.1.



The High-Mass Region (HMR, $M_{ee} > 3$ GeV/ c^2) is primarily occupied by yields from the prompt production during the primordial nucleon-nucleon collision. Drell-Yan annihilation of quark and antiquark of two passing hadrons dominates over thermal emission in this region. Hidden heavy flavor vector mesons (J/ ψ , ψ') appear on top of this continuum that also has contributions from semi-leptonic weak decays of B-mesons and Λ_b -baryons originating from back-to-back $b\bar{b}$ pairs and hence, resulting in correlated dileptons.

The Intermediate-Mass Region (IMR, 1.1 < $M_{\rm ee}$ < $3~{\rm GeV/c^2}$) also exhibits a continuous yield of correlated e^+e^- pairs from semi-leptonic decays of charmed mesons competing in a heavyion environment with thermal radiation via $q\bar{q}$ annihilation from the QGP. With contributions from possibly medium-modified correlated charmed decays known, an initial effective temperature of the fireball can be deduced

in this region from the slope of dielectron m_T spectra given sufficient statistics. Due to the scarcity of electromagnetic probes, the latter impedes such a measurement even at SPS or lowest RHIC energies where the $c\bar{c}$ cross sections fall off steeply.

In the Low-Mass Region (LMR, M_{ee} < 1.1 GeV/ c^2), dielectron production is dominated by the decay products from final-state hadronic sources culminating in a *cocktail* of light pseudoscalar and vector mesons $(\pi, \eta, \eta', \rho, \omega, \phi)$. Electromagnetic *radiation* due to (multiple) reinteractions in the hot and dense HRG populates this region and could provide information about in-medium modifications of the vector mesons' spectral function properties. Modifications of the dielectron rates and their integration over the fireball evolution as well as consequences on the invariant mass spectrum are addressed in the context of this thesis within an effective multi-body hadronic theory in Section 4.2.

1.3.1 Measurements of Dilepton Production

The challenging measurement of dilepton production has been an active field of research in experimental high energy nuclear physics through multiple generations of detectors at colliders and fixed-target machines since the 1990's. The reader is referred to the main part of the thesis for details on the general analysis and simulation techniques employed to arrive at the spectra presented in the following. Here, we concentrate on the results of selected influential measurements and their current interpretations and conclusions leading up to the important contributions of this thesis to the progress of dielectron physics.

The CERES and NA45 collaborations [13, 99-101] first reported an unexplained LMR excess yield in S+Au collisions while achieving excellent agreement of cocktail simulations and data in p+N collisions (Figure 1.8a). However, follow-up comparisons of measured LMR invariant mass spectra with calculated dropping-mass and broadening spectral functions of the ρ -meson in Pb+Au collisions, did not allow for the distinction of the two scenarios. The emergence of high-quality dimuon measurements in In+In collisions by the NA60 collaboration [14] significantly accelerated the progress by clearly favoring the broadened spectral function scenario for the modifications of the ρ -meson driven by (multiple) baryonic interactions in the hot hadronic phase (Figure 1.8b). The tail above the ρ -mass can be described by 4π -mixing, cor-

related charm and QGP contributions [102]. Also particularly interesting are the conclusions that can be drawn from NA60's measurement of the effective temperature T_{eff} and its mass dependence in Figure 1.8c. The steady rise up to $M_{\mu\mu}$ of about 1 GeV/c² is consistent with the radial flow expected from the hadronic emission source $\pi\pi \to \rho \to \mu\mu$. The sudden drop and hence absence of significant flow above 1 GeV/c², however, suggests the partonic emmission via $q\bar{q} \to \mu\mu$ as dominant source. Accumulation of further evidence as discussed in [14], is even consistent with the interpretation of the excess dimuons as thermal radiation. This not only triggered renewed attention to dilepton physics by the theory community, but also independent and dedicated high-accuracy measurements of the dielectron decay channels at top RHIC energy — first by PHENIX and recently complemented by STAR.

Figure 1.8 a) CERES/NA45 dielectron measurements in p+N and N+N collisions reporting a LMR enhancement for the first time but failing to distinguish possible vector meson in-medium scenarios [13, 99-101]. b,c) NA60 dimuon measurement establishing ρ in-medium broadening and identifying partonic sources as dominant in IMR [14].

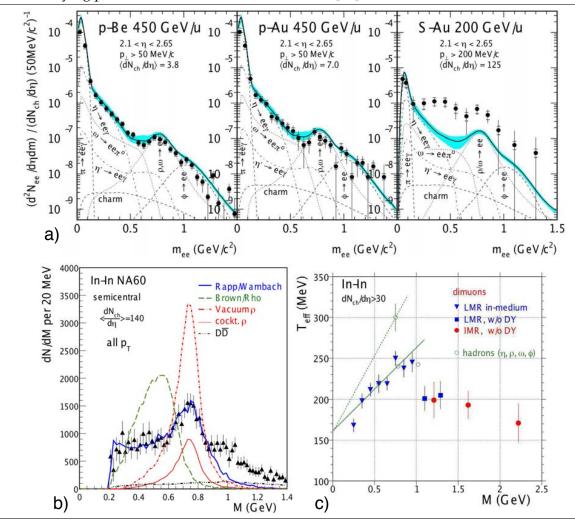
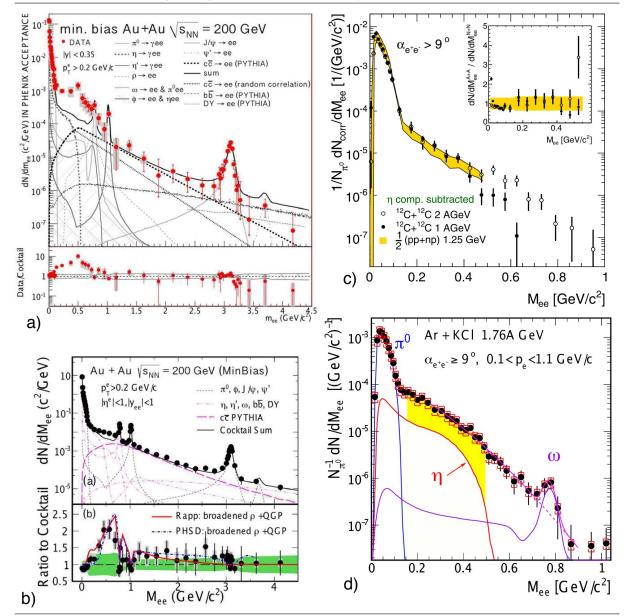


Figure 1.9 a) PHENIX dielectron measurement at top RHIC energy exhibiting significant and yet insufficiently explained LMR excess [15]. b) STAR dielectron measurements at top RHIC energy exhibiting reasonable agreement with broadened ρ calculations for the LMR excess, also in its p_T and N_{part} dependence. c) HADES measurement in C+C collisions described by superposition of elementary reactions [103]. d) HADES measurement in Ar+KCl collisions at 1.76 AGeV also showing unexplained enhancement by a factor 2.5-3 [104].



The PHENIX detector system has measured invariant mass and transverse momentum spectra in d+Au collisions and seen very good agreement of the data with next-to-leading order perturbative QCD calculations over the entire accessible phase space [105]. Hence, any enhancement seen in the heavy-ion collisions is not due to cold nuclear matter effects. More importantly, PHENIX has also published dielectron invariant mass spectra in Au+Au collisions [15] exhibiting a significant LMR enhancement of more than a factor of 5 over an expected cocktail of hadronic sources (Figure 1.9a). None of the scenarios for in-medium spectral functions of the vector mesons could satisfactorily explain the magnitude of the enhancement, even by exhausting the full parameter space allowed. Same is true for PHSD calculations in which neither the incorporated hadronic nor partonic sources were able to account for the enhancement observed by PHENIX. It is interesting to note, that the latest dielectron measurements by PHENIX

using the novel Hadron-Blind Detector (HBD) show a more moderate enhancement factor of 2-3 for the 20-40% centrality bin [106]. It remains to be seen whether the large enhancement of the original measurement bears up in the future since the most central bin of the HBD measurement, to which most of the enhancement has been attributed, has not been shown to date.

As detailed in Section 1.4, STAR has in recent years entered the landscape of dielectron measurements enabled by major upgrades to this large acceptance mid-rapidity (multi-purpose) detector. Figure 1.9b shows STAR's main results of the very recently completed analysis of dielectron production in Au+Au collisions at top RHIC energy [16]. The statistical quality of the measurement allowed STAR to observe an enhancement factor of about 1.8 in the mass region $0.30-0.76 \text{ GeV/}c^2$ which is significantly lower than reported by PHENIX. Neither comparisons of cocktail simulations nor of production yields within PHENIX acceptance revealed any explanation for the discrepancy in the magnitude of the LMR excess. A detailed comparison of the LMR invariant mass shapes shows that the data disfavors a pure vacuum- ρ spectral function for the excess but is in reasonable agreement with broadened ρ and QGP contributions calculated within hadronic multi-body as well as PHSD models. This conclusion further supports the NA60 findings in size and shape. When split in ρ -, ω - and ϕ -like mass regions, the data over cocktail ratios in the latter two can be reproduced by the cocktail calculations as opposed to the ratio in the ρ -like region which is reasonably well described by the aforementioned models and weakly dependent on the number of participants (N_{part} , centrality) and transverse momentum. A power-law fit to the N_{part}-scaled ho-like dielectron excess results in an exponent of 0.54 ± 0.18 possibly indicating sensitivity to QCD medium dynamics like the lifetime of the HRG phase (see [107]).

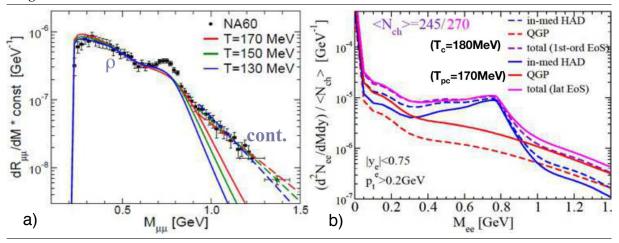
For completeness, we also need to discuss measurements of dielectron production in the energy range of normal to moderate temperatures and baryon densities. One of the early measurements in 1.04 AGeV Ca+Ca collisions by the DiLepton Spectrometer (DLS) at the BE-VALAC [108] compares dielectron invariant mass distributions to freeze-out decays as well as in-medium modified ω - and ρ -mesons. While reasonably described by at SPS energies [102], neither the dropping mass nor the broadened in-medium spectral function scenario can account for the considerable excess yield in the low mass region [109, 110] which led to the so-called "DLS-puzzle". The second-generation High Acceptance Di-Electron Spectrometer (HADES) was subsequently built in an effort to systematically study this excess with high precision in the SIS18 energy regime. Taking into account the different acceptances, HADES was able to confirm the DLS measurements in its invariant mass and transverse momentum dependence for 1 and 2 AGeV C+C collisions [17, 18]. The HADES findings further show that such light collision systems can in first order be described as an isospin-averaged (incoherent) superposition of elementary N+N processes (Figure 1.9c). However, in the heavier collision system of Ar+KCl at 1.76 AGeV the η -subtracted invariant mass spectrum exceeds this N+N reference by a factor of about 2.5 to 3 between 0.15 and 0.5 GeV/c^2 (Figure 1.9d). The excitation function covered by the DLS and HADES experiments indicates that the excess closer resembles the scaling of pion rather than η production. Hence, the interpretation of dielectron production in the regime of 1-2 AGeV bombarding energies requires a better theoretical understanding of the relevant N^* resonances and their ρ -meson coupling.

1.3.2 Underlying source of Dilepton Enhancement

The final part of this section is dedicated to the empirical discussion of a few theoretical, partly data-driven observations that collectively support the interpretation of the experimental results as thermally emitted dileptons [111]. The purpose is not to provide a complete and resilient overview but rather briefly describe the interplay of a few theoretical points which pinpoint the observed dilepton emission to temperatures around the chiral transition. It provides an

instructive exercise since the main conclusion of this thesis plays an integral part in the argumentation.

Figure 1.10 Theoretical observations supporting the interpretation of the measured LMR excess as emanating from a thermal emission source around the chiral transition temperature T_{pc}^{χ} [111]. a) Indication of dimuon continuum radiation from $T \sim 150$ MeV. b) First-order and Lattice QCD equation-of-states lead to identical dilepton yields in the 150 MeV temperature range.



Due to its unique connection to theory, dilepton invariant mass spectra directly reflect the thermal emission rate (see Section 4.2.1). The slopes of the dashed lines in the continuum region of the NA60 dimuon measurements in Figure 1.10a reveal an emission temperature of about 150 MeV or at least between 130 and 170 MeV. This temperature range happens to correspond to the temperature of the chiral transition T_{pc}^{χ} . Figure 1.10b studies in-medium hadronic and QGP contributions for an equation of state (EoS) with a first-order phase transition at $T_c \sim 180$ MeV with respect to a Lattice EoS with T_{pc} at 170 MeV. The lower T_{pc} is balanced by enhanced QGP and depleted hadronic contributions resulting in almost identical low-mass yields and corroborating a predominant emission source around T_{pc}. Also, an effective excess temperature of 220 MeV as well as rather large flow expansion velocities (β ~0.3) both extracted from direct photon spectra measured by PHENIX, suggest a "later" emission at T \sim 220 MeV / 1.35 $\sim 160 \text{ MeV} \sim T_{pc}$. Theoretically, one observes that the in-medium ρ -meson rates smoothly "melt" into the according rates from QGP continuum radiation. Experimentally, the NA60 data has quantitatively confirmed the broadened ρ spectral function scenario as explanation for the low-mass excess yields. Since, as previously discussed, the hadronic in-medium spectral functions are related to the $q\bar{q}$ condensate, the development of a pion cloud and excitation of baryonic as well as mesonic resonances as mechanisms underlying this " ρ -melting", are possibly precursor to the dynamic restoration of chiral symmetry. The preceding theoretical and experimental observations, as a whole, allow the authors of [111] to speculate about a three-fold degeneracy of contributions from in-medium HRG, perturbative QCD and Lattice QCD convening at the chiral phase transition temperature.

It is crucial, however, to study the dilepton LMR enhancements for various regions of the QCD phase diagram and establish the degree of universality of in-medium vector meson modifications as underlying source. In anticipation of the results, this thesis reports on the extensive energy-dependent measurements during STAR's BES-I which indeed indicate the universal character of this scenario (see Chapter 5). Hence, the study of emission temperature and in-medium scenarios results in the important observation that spectral slopes, yields and flow of low-mass dileptons at SPS and RHIC point toward a *universal* underlying source with average emission temperatures of about 150 MeV coinciding with T_{pc}^{χ} .

However, there are caveats that need to be kept in mind. It is important to also identify conditions in a heavy-ion environment under which these medium effects turn off. While peripheral collisions are challenging in this regard since the dense hadronic phase still persists, high(er) p_T data like the NA60 dimuon measurements or elementary projectiles on cold nuclei like γ +A \rightarrow eeX by CLAS are promising candidates [112]. Last but not least, a thorough theoretical framework needs to relate the measured ρ spectral functions to its chiral partner a_1 to convincingly address the long-standing question of chiral symmetry restoration. Progress in this direction has recently been made in [113].

1.4 Thesis Objective and Overview

As later outlined in Section 4.2, the most distinct features of electromagnetic radiation from the hot hadronic phase are unfortunately hidden by the according hadronic freeze-out decays. However, model calculations still predict about 50% reduction in the ρ/ω region and more importantly, about a factor of two enhancement at 0.5 GeV/c² when comparing a broadened to a vacuum-like spectral function for the dielectron spectrum from direct decays of ρ , ω and ϕ over the fireball evolution [114, 88]. The ω/ϕ resonances appear to be less susceptible to the different scenarios. The preceding introduction has argued that theory can connect these modifications to chiral symmetry restoration with sufficient experimental data at its disposal. However, the accuracy required to test the respective differences from various scenarios in the (ρ) spectral function, is experimentally very challenging.

The completion of the Barrel Time-of-Flight detector (TOF) in 2010 has allowed STAR to play an important role in the study of dielectron production [16, 115, 116] with excellent particle identification, low material budget, full azimuthal acceptance at mid-rapidity, and a wide momentum coverage [19, 117, 118]. STAR is thus one of the most versatile mid-rapidity detectors currently available to the High Energy Nuclear Physics community. For instance, TOF efficiently rejects slow hadrons and provides pure electron identification together with the energy loss measured in STAR's Time-Projection-Chamber (TPC), which makes the two detectors the primary subsystems employed in dielectron analyses at STAR. In particular, combined with the first phase of the Beam Energy Scan Program (BES-I, [20]), STAR presents the unprecedented opportunity to map out a significant portion of the QCD phase diagram within a homogeneous experimental environment.

The objective of this thesis in the main Part I is to present STAR's novel and successful endeavor extending the dielectron measurements from top RHIC energies down to the SPS energy regime. The results of this thesis therefore not only close a wide gap in the QCD phase diagram, but also provide the first comprehensive dataset of dielectron measurements with respect to energy dependence and experimental environment. In the particular context of the dielectron analyses presented in this thesis, STAR aims to look for energy-dependent changes in the in-medium spectral function modifications and QGP radiation, possibly identifying the underlying universal nature of the respective dielectron emission source(s). Only by varying beam energy and accessing different regions of the phase diagram, we can objectively verify conclusions reached for energies at which a QGP is or is not expected to form. This fundamentally distinguishes the efforts in this thesis from dielectron measurements previously undertaken. The discussion in Section 1.3 in particular, has identified such measurements as crucial experimental input to explore the connection between measured dilepton yields and chiral symmetry restoration.

The thesis is outlined as follows. Chapter 2 starts out by briefly introducing the concepts of RHIC as well as important aspects of the STAR detector setup relevant to dielectron analyses.

It continues with the key elements of the experimental raw data analyses ranging from event and track selection including particle identification to pair reconstruction and background subtraction. Chapter 3 presents the procedure employed to derive and apply corrections due to detector inefficiencies. Chapter 5 discusses the obtained results including new and energy-dependent invariant mass spectra as well as p_T spectra in comparison to the simulations and model calculations of Chapter 4. In the end, Chapter 6 summarizes the main results of the thesis and gives an outlook on the role of dielectron measurements in the current STAR upgrades, the future second phase of the Beam Energy Scan program (BES-II), and CERN's LHC. Preliminary versions of the results in Chapter 5 have been presented at various major conferences in recent years, and published in the respective proceedings [119]. Papers based on the results of this thesis are in preparation to be published in the journals *Physical Review Letters* and *Physical Review C*.

Additional parts on software (Part II) and hardware (Chapter 11) projects developed within the framework of this thesis contain a multitude of contributions to the STAR ² and Open-Source community as well as the inital development of a Xe-Excimer Lamp designed to enable pad-by-pad efficiency corrections for the RICH detector of the HADES experiment.

² a selection will possibly be published as STAR notes in the future

Chapter 2

Data Acquisition and Analysis

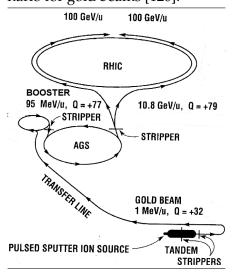
This chapter discusses the complex but integral part of gathering and analyzing the (raw) data required to perform an energy-dependent measurement of dielectron production at the Relativistic Heavy Ion Collider (RHIC). Section 2.1 briefly presents relevant aspects of experimental setup and data acquisition by means of the Solenoidal Tracker at RHIC (STAR). In Section 2.2, the datasets used in this thesis are introduced and suitable selection criteria are discussed to reduce the data to high-quality collision events and particle tracks. The separate reconstruction and analysis of the event plane described in Section 2.2.2 is a prerequisite for the statistical generation of background pair distributions. The procedure to cleanly identify electrons and positrons using STAR's detector subsystems Time-Of-Flight (TOF) and Time Projection Chamber (TPC) is discussed in Section 2.3 along with the resulting sample purities. Dielectrons (e⁺/e⁻ pairs) are reconstructed and background contributions substracted statistically in Section 2.4 by employing same and mixed event techniques in p_T-integrated and -differential manner. Note that corrections to account for efficiency losses in the detector and to be applied on the raw spectra are derived in Chapter 3.

2.1 Experiment: RHIC and STAR

It is beyond the scope of this thesis to give a complete introduction to neither the functionality of heavyion accelerators nor the technology used to build the detectors around the collision zone. Since excellent reviews about RHIC and STAR already exist [121], this section gives overviews merely outlining the general concepts of the two and concentrates on some additional details relevant to dielectron analyses. Where appropriate the reader is referred to references containing in-depth information.

The scenario to feed Au ions into RHIC using an injector chain of accelerator rings is sketched out in Figure 2.1 [120]. The Tandem Van de Graaff as well as the Booster and the Alternating Gradient (AGS) synchrotrons are pre-existing hadron accelerators at the Brookhaven National Laboratory (BNL) [122] that provide three different stages of increasing beam energy after each of which the Au ions are partially stripped of their electrons to adjust their charge to the according next-stage ring diameters and

Figure 2.1 RHIC acceleration scenario for gold beams [120].

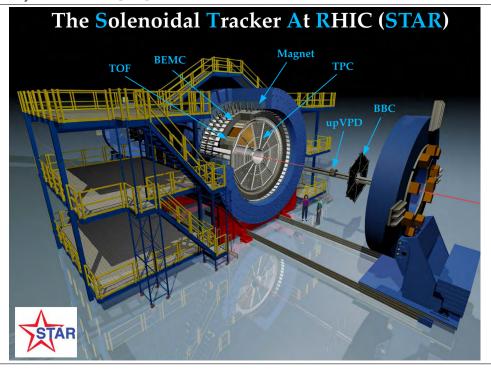


intended energies. The Tandem [123] uses its characteristic two-stage acceleration mode including mid-way electron stripping to boost Au^- ions from the sputter ion source [124] to an energy of 1 MeV/u. A charge state of +32 is subsequently selected by bending magnets for the deliv-

ery via the Heavy Ion Transfer Line [125] to the Booster Synchrotron [126, 127] in which the Au ions are accelerated to 95 MeV/u. Au⁺⁷⁷ ions exit the Booster for the final step of acceleration in the AGS [128] to an energy of 10.8 GeV/u before bunch-wise injection into RHIC as Au⁺⁷⁹ via the AGS-to-RHIC transfer line [129]. RHIC consists of a pair of superconducting rings with 3.8 km circumference capable of accelerating and storing two counter-circulating gold beams with energies up to 100 GeV/u each [130]. The rings intersect at four points along the circumference allowing for a complementary set of detectors [131] to conduct experiments using relativistic heavy ion collisions. Each experiment operates a pair of Zero-Degree Calorimeters (ZDCs) [132, 133] as a common detector subsystem on either side of and close to the respective interaction zones. The ZDCs detect neutron multiplicities from the collisions and enable the accelerator staff to monitor luminosity and locate collision vertices ("steering"). For more details on RHIC, the reader may want to use [134] as an entry point.

The data for the energy-dependent analysis of dielectron production presented here has been obtained by means of the STAR detector [135, 136]. The STAR detector serves the study of a very broad physics program ranging from high-density QCD, over the proton's spin structure to ultra-peripheral collisions via electromagnetic interactions of passing ions. Such a program requires a suite of multi-purpose and complementary detector subsystems. Figure 2.2 shows a graphical rendering of the STAR detector with its subsystems Endcap [137] & Barrel [138] Electromagnetic Calorimeters (EEMC & BEMC), Beam-Beam Counter [139] (BBC), upgraded pseudo Vertex Position Detector [140, 141] (upVPD), and Magnet [142]. Also depicted are TPC and TOF, the combination of which is particularly important for the study of dielectrons and discussed to some detail in Section 2.1.1 followed by STAR's Data Acquisition (DAQ) and Trigger systems in Section 2.1.2.

Figure 2.2 Graphical rendering of the STAR detector system with subsystems reflecting the status in the years 2010/11 [143]. Details and references see text.



2.1.1 TPC and TOF

The cylindrical Time Projection Chamber (TPC) [144] constitutes the very heart of the STAR detector system measuring 4 m in diameter as well as length, and stretching from 50 to 200 cm in radial distance from the beam axis. Stable and unstable particles emanate from the collision

zone located approximately in the center of the TPC and traverse through the covered volume filled with P10 gas (10% methane, 90% argon). Along their path, the particles ionize the P10 gas leaving behind a track of released secondary electrons. A thin conductive membrane at the center of the TPC, the concentric field-cage cylinders, and the end caps define a uniform electric field of \sim 135 V/cm which induces a drift of the electrons along its field lines toward the readout caps at both ends of the chamber. P10 gas is a well-established choice for this purpose since it exhibits fast drift velocities at comparably low electric fields. The charge of the drifting electrons, registered when they reach the TPC's readout plane, allows for the measurement of a track segment's x/y and z coordinates through its projection into two dimensions and the elapsed drift time, respectively.

The TPC is furthermore installed inside a large solenoidal, room-temperature magnet providing a uniform field of up to 0.5 T along the z-direction (beam axis). In addition to the spatial reconstruction, the charged particle's momentum can hence be derived from the track's curvature in the magnetic field enabling high-resolution 3D-imaging of the heavy-ion collision. Electric field uniformity is critical in this context to achieve a track reconstruction precision of less than 1 mm with electron drift paths of up to 2.1 m. A relative momentum resolution of $\delta p/p = 0.02$ is achieved which improves with the number of hits induced by a track's secondary electrons in the TPC's readout end caps and with decreasing particle momentum. Particularly noteworthy is the TPC's resulting large acceptance of close to 4π in azimuth and $|\eta| < 1$ in pseudo-rapidity for charged particle tracking and the full range of multiplicities.

The reconstructed momentum does not suffice to determine the particle species. However, in every ionizing collision with the atoms along its path through the gas, the particle releases energy from $\mathcal{O}(10 \text{ eV})$ frequently up to $\mathcal{O}(100 \text{ eV})$ rarely. The momentum dependence of this energy loss dE/dx per length dx of the ionization cluster is specific to the particle species (c.f. Bethe formula [145]) and its measurement hence allows for a very capable particle identification below the relativistic rise (see Section 2.3). The deposition of collisional energy in the ionization clusters along the track is a stochastic process which impedes the accurate measurement of an average dE/dx since the according track segments are too short to neglect the resulting fluctuations. Instead, dE/dx distributions can satisfactorily be parameterized by varying the most probable energy loss with the length of the ionization cluster [146, 147]. With an energy loss resolution of 8%, pions and kaons can be identified cleanly up to a transverse momentum of 0.7 GeV/c and protons up to 1 GeV/c. The challenge in achieving the target dE/dx resolution lies in TPC calibration and understanding of signal as well as gain variations during TPC readout.

The TPC readout system [148] is based on Multi-Wire Proportional Chambers (MWPC) with readout anode planes partitioned into ~140k pads in total. The high electric fields at the MWPC's anode wires cause an avalanche of liberated electrons initiated by an ionizing collision of the drifting electrons which amplifies the electronic signal by about three orders of magnitude. The positive ions left behind by the avalanche electrons induce a temporary image charge on the pad plane distributed over multiple neighboring pads. The resulting charge distribution is accurate enough to determine the original track segment's x/y-position within 20% of the pad width. The readout systems on either side of the TPC are composed of 12 sectors using different pad geometries for inner and outer subsectors due to the varying track density. The inner subsectors use small pad sizes arranged in widely spaced rows as opposed to the outer subsectors with larger but densely packed pads. This setup allows for good two-track separation and optimized dE/dx resolution using a moderate number of pads at small and large radii, respectively. A future upgrade of the inner TPC sectors [23] will cover the small radii with densely packed pads, too. The electronic readout of the TPC pad planes consists of small Front-End Electronics (FEE) cards responsible for amplification, shaping and analog-todigital conversion of the avalanche signal. Each readout board (RDO) controls 36 FEE cards, provides power and sends the processed signals to the DAQ system. See Section 7.2 for details on so-called "bad" RDOs missing during the time when the data sets used in this thesis were taken.

Finding and reconstructing particle tracks from the ionization clusters recorded on adjacent pads of the TPC readout plane (so-called tracking via pattern recognition), is an integral ingredient of raw data processing to enable event classification and successful physics analyses. The fast tracking algorithm [149] employed in STAR utilizes the fact that the solenoidal magnetic field forces the particles on helical trajectories. In the plane perpendicular to the field (e.g. TPC readout plane), the helical paths are projected into circles. These circular paths transform into straight lines when applying a conformal mapping from cartesian coordinates to the (s,z)-plane with s the trajectory length. This procedure simplifies the design of a fast algorithm by linking closest space points into track segments and extending them with the unused space point closest to a straight line fit. The algorithm proceeds inward due to the smaller track densities (less ambiguity) on outer layers of the TPC and accepts or rejects track candidates based on the χ^2 -quality of the fit. The initialization of this nose-following method requires a space point on the track to be known which in the general, unbiased case of global tracks, simply is the first point associated with the track. For so-called *primary* tracks that match well with the interaction point, however, the primary vertex is included in the fit to effectively constrain the track's origin to the event vertex. After a full track is found it can be parameterized anew using a helix model in three-dimensional space. The reconstruction of secondary and tertiary vertices for K_0 , Λ , Ξ and Ω decays, for instance, can then be achieved by calculating the Distance-of-Closest-Approach (DCA) of two global helices via a numerical minimization algorithm (c.f. Section 3.1). A difficulty requiring special attention in this context, is the reconstruction of the particle's momentum vector. For its physical determination the according track needs to be correctly assigned to the particle's true vertex of origin. However, in addition to the main interaction and secondary vertices, the latter can also be a spurious interaction vertex caused by event pile-up or merely a scattering center. The assignment of a track to a particular vertex is an integral part of STAR's event reconstruction chain (see Section 2.2) [150].

The level-3 trigger explained in Section 2.1.2 performs the above tracking procedure in each of the TPC sectors separately and in real-time. Tracks that cross sector boundaries will hence be split. This phenomenon also increasingly occurs the further away the two incoming nuclei collide from the TPC's central membrane. A track crossing the membrane will have two parts of its ionization electrons drifting toward opposite sides of the TPC readout system (end caps). To remove such split tracks in the data analysis, the selection criteria in Table 2.1 (Section 2.2) require more than half the possible number of ionization clusters (i.e. electronic *hits* in the pad plane) to be used in the reconstruction of a track.

The particle identification (PID) abilities of the TPC are limited to hadrons with momenta up to the relativistic rise above which the particle separation power ceases due the merging energy loss bands. Extracting the maximum physics information contained in hadron spectra, for instance, hence makes it imperative to extend the measurable hadron momentum range up to 2-3 GeV/c. This has been achieved in STAR by the installation of an additional detector subsystem in 2010 that allows for the measurement of a particle's velocity β and its characteristic momentum dependence. The barrel Time-Of-Flight (TOF) detector [151] is based on the Multigap Resistive Plate Chamber (MRPC) technology and covers a pseudo-rapidity range of $|\eta|$ < 1. Within the acceptance of the TOF detector, the β selection on average doubles the fraction of kaons and protons identified successfully with a separation up to momenta of \sim 1.7 and \sim 3.0 GeV/c, respectively.

The basic quantity underlying the β measurement is the time interval Δt elapsed between the initial nuclear collision and registration of a particle in a TOF tray at a certain (r, η, ϕ) spatial position. Each signal in the TOF's trays can be associated with a track reconstructed in the TPC by extrapolation (*TOF matching*) which additionally provides the track's momentum p and path length s. The interval Δt hence suffices to identify the particle species through its mass m via

$$\beta = s/c\Delta t$$
 and $m^2 = p^2(1/\beta^2 - 1)$.

Particle identification via β consequently requires the measurement of a global *start time* and many particle-specific *stop times* in each event. The separate detector subsystem upVPD [152, 141] mounted close to the beam pipe at $z=\pm 5$ m is used to obtain the start time. It is, however, unfeasible to distribute the start time from the upVPD to each TOF tray taking the stop time and to install bulky electronics for the digitization of each TOF tray logic signal with respect to the start time. Instead, the upVPD and TOF tray signals can be digitized in the same electronics versus a common clock synchronized within 10-20 ps which does not change the relative timing information required to determine β . All successful TOF detector systems share this approach.

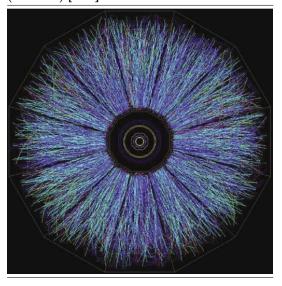
The combination of information from TOF and TPC dE/dx does not only improve STAR's hadron PID capabilities but also allows it to cleanly identify electrons over a wide momentum range and with large acceptance coverage for the first time (see Section 2.3). Physics-wise, it enables STAR to effectively reconstruct and study the properties of resonances that are sensitive to the dense medium in which they are created. Section 1.3 has extensively discussed dielectrons as promising probes for these resonances which is why the installation of TOF has been crucial in opening up an entirely new realm of physics analyses to STAR (c.f. Section 1.4).

2.1.2 Trigger and DAQ

In the year 2000, RHIC collided Au ions with a bunch crossing rate of about 10 MHz which natively separates STAR's detector system into two classes. The fast subdetectors, on the one hand, can keep up with the beam crossing rate and measure global event properties like the charged particle multiplicity at mid-rapidity (Central Trigger Barrel, CTB), the neutron multiplicity at forward/backward-rapidities (ZDCs), and energy localization for electrons/photons (BEMC). The slow subdetectors (primarily the TPC), on the other hand, require additional time to conduct a track-based analysis for a more sophisticated event selection resulting in a data rate of about 100 Hz. STAR hence implements a multi-level trigger system [153] using the fast detectors to reduce the data rate by about 5 orders of magnitude.

Its first stage consists of three trigger levels called *Level-0*, -1, and -2 based on the signal from the fast detectors. These levels are fully pipelined since the fast detectors do not need to process multiple events at the same time. Within about 1.5 μ s

Figure 2.3 TPC end view of a single Au+Au event with particle tracks reconstructed in real-time ("online") during the second stage of the STAR trigger system (Level-3) [136].



after each bunch crossing, Level-0 processes the measured global multiplicities and energies and signals the slow detectors to initiate their cycle of amplification, digitization and acquisition (ADA). During the Level-1 trigger phase of about $100~\mu s$, characteristics in the particle distributions are used to identify background from beam-gas collisions and abort the ADA cycle during the 40 ms required for the readout of the TPC. Signal digitization on its FEE takes about 10 ms and is the reason for the above limit of 100 Hz on the TPC's readout rate. About 5 ms elapse after the collision until the raw data in a fine pixel array is analyzed on the Level-2 trigger CPU farm to decide whether to abort the event during the TPC digitization phase and before transmission to the DAQ. The pixel array is well-suited to isolate jets or to refine particle topologies which constrain the event selection to specific interaction mechanisms. A minimal

constraint on the latter is achieved by selecting events with at least one neutron measured coincidentally in each of the ZDCs. This corresponds to 95% of the geometrical cross-section and defines the *minimum bias trigger* (MinBias).

The Level-2 trigger phase only provides a prototype event to be fed into the second stage of STAR's trigger system. This so-called *Level-3* trigger [154] is responsible to reach a final decision whether or not to store the full event information. For this purpose, it analyzes all available data within 200 ms after the collision via a complete online event reconstruction in a dedicated CPU farm. Single particle properties like momentum and energy loss can subsequently be used to select J/ψ and anti-nuclei candidates as well as back-to-back tracks in ultra-peripheral collisions, for instance. An online display for the visual inspection of individual events in real time is included in the Level-3 trigger [155]. Figure 2.3 shows a screenshot of the online display with the detected tracks emerging from a representative Au+Au collision and demonstrates that the TPC is capable of reconstructing >1000 tracks per pseudo-rapidity unit.

The STAR Data Acquisition System (DAQ) [156] receives data from the many detector subsystems at input rates up to 100 Hz (c.f. Level-3 data rate), reduces it to 20-50 MB/s via zero suppression (\sim 2 events/s for central collisions), and sends built events via Gigabit Ethernet to the RHIC Computing Facility (RCF) [157] where they are stored to tape using HPSS [158]. The duration of the Level-3 trigger phase limits the processing time available for the DAQ and hence requires a fully integrated farm of \sim 50 CPUs [159] to parallelize the tracking. The DAQ also needs to handle many events at the same time and in different stages of completion since the decision from the Level-3 trigger to build an event arrives long after the event has been received. The data stored on tape in a unified format provides the basis for STAR's offline event reconstruction chain. The latter is introduced in Section 2.2 and the resulting compact data files analyzed through-out the remainder of this chapter.

2.2 Datasets and Event/Track Selection

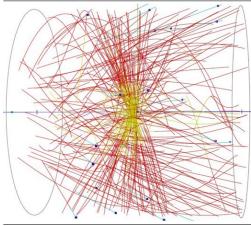
The zero-suppression performed in the STAR DAQ system [156] only does a minimum to reduce the size of the recorded raw data by discarding signals that fall within the expected electronic noise. The task of further data reduction becomes the duty and responsibility of the STAR event reconstruction chain [150, 160, 161]. This broad first stage of STAR data analysis combines raw digitized detector data into detector hits (e.g. TPC cluster finder), integrates all detector components during tracking to obtain physical particle properties (e.g. calibration and TOF matching), and performs various post-tracking procedures such as vertex and possibly secondary/tertiary vertex (V₀) finding. Each of these specific data reduction tasks is implemented in a dedicated software module as part of the so-called Big Full Chain (BFC, see StarClassLibrary documentation in [162]). As a result, the BFC produces the more compact Data Summary Tapes (DSTs) containing the "real data" in form of a list of events with associated particles and their physical properties (see StEvent and StTrack documentation in [162]). While being taken during the running experiment, the raw data is run through parts of the reconstruction chain to control and monitor its quality "online". In addition to the DST production phase, the original raw detector data is needed offline only for detector calibration purposes. Once calibration is completed the final set of DST files is produced along with so-called *micro-DST* files (MuDSTs) and both committed to long-term archival storage at RCF. MuDSTs [163] further reduce stored event sizes from 2-3 MB to 200-300 KB and obey a standardized file format organized in ROOT [164] branches suitable for physics analyses across all STAR working groups. Note that global and primary tracks matching the event vertex are stored twice in the dual list of tracks in the MuDST files. These derived data sets are redistributed to STAR member institutions across the globe to be readily available for analysis by collaborators.

The second stage of the STAR data analysis concentrates on the study of the reconstructed

collisions with respect to a specific physics phenomenon. It builds on the MuDST files which already provide reconstructed tracks from the best primary vertex matched to the according TOF hits. Using all global tracks and established basic event- and track-wise selection criteria, so-called *PicoDSTs* are produced to further reduce the data needed for a common STAR physics analysis [165]. Table 2.1 summarizes the main properties of the four datasets relevant to this thesis along with the event and track selection criteria used in the production of derived ROOT trees containing electron and positron candidates (also see Section 2.3). The data taken in the years 2010/11 hold excellent premises for a successful study of dielectron production. STAR's unique and versatile capabilities come combined during these runs with particularly low material budget (due to the retired Silicon Vertex Tracker) and high statistics both of which are favorable for the difficult extraction of physics via the rare electromagnetic probes. Of the energies recorded during this first phase of the RHIC Beam Energy Scan (BES-I), $\sqrt{s_{NN}}$ = 19.6, 27, 39 and 62.4 GeV have been selected as very promising for the statistics-hungry analysis of dielectron production.

Most of the criteria used in Table 2.1 for data reduction are considered established in STAR and ensure a minimum quality that defines a "good" event or track, for instance. Their notation and meaning are briefly explained in the according footnotes. Two less common choices for the criteria should be noted, though: i) The VPD cut used at 200 GeV [16] is not employed at BES energies due to the VPD's significantly reduced efficiency. ii) An event like in Figure 2.4 triggered by a beam-pipe collision with a simultaneous Au+Au event in the center of the TPC, is not rejected by the selection of the 0-80% most central events. Unlike other beam-pipe events it also exhibits a (reference) multiplicity appropriate for a Au+Au collision but most of the primary tracks are not matched with TOF due to the wrong timing information (c.f. Section 2.1.1). Hence, an additional requirement of a min-

Figure 2.4 Au+Au event with good primary vertex but triggered by a beampipe event just outside the TPC [166].



imum number of TOF-matched primary tracks is used to remove such events [166]. Table 2.1 also contains a detailed list of number of events per analysis stage as well as the final number of events with which to normalize the efficiency-corrected dielectron spectra (Chapter 5). Further details in Section 2.2.1 accompany the analysis stages involving the concept of reference multiplicity (RefMult) and refined run-by-run event quality assurance (RunQA). Section 2.2.2 explains the procedure to obtain uniform distributions of the event plane angle used for event classification in Section 2.4.

Table 2.1: Properties of the datasets analyzed in this thesis (PicoDST level) and the criteria used for event/track selection. Also included is the reduction in number of events with each analysis cut (in order of application). The footnotes give brief explanations of the selection criteria/stages.

$\sqrt{s_{ m NN}}$ (GeV)	19.6	27	39	62.4
Year	2011	2011	2010	2010
Days	112 - 122	172 - 179	99 - 112	80 - 82, 84 - 98
# Runs	483	382	615	735
# Files	9757	13896	24922	25569
# Events (M)	48.7024	95.4347	170.859	120.528
Size (TB)	1.1	1.9	3.8	4.9
	E	Event Selection	'	'
MinBias Trigger ¹	3400 01/11/21	360001	280001	2700 01/11/21
Event Vertex ²	$V_r < 2 \text{ cm } \&$	V_z < 70 cm	$V_r < 2 \text{ cm } \&$	$V_z < 40 \text{ cm}$
Min. Ref. Mult. ³	(6	5	7
Others	#GlobTracks < 3	3000 ⁴ & #TofMatc	hedPrims \geq 2 5 &	$\#TracksEP > 0^6$
	Prim	ary Track Selectio	n	
Momentum		$p_T > 0.2 \& p$	< 10 GeV/c	
Track Quality		& nHitsFit/nHits		
TOF Matching	TofN	$MatchFlag>0\ ^{10}$ &	: TofYLocal < 1.8 c	rm ¹¹
Others		$ \eta $ < 1 & glD	CA < 1 cm ¹²	
	Number of Events	(in Millions) by	Analysis Stage	
STAR RunQA ¹³	48.1469	91.2154	164.116	109.177
Minimum Bias	46.4914	90.4904	164.116	84.2632
#GlobTracks	46.4909	90.4904	164.116	84.2618
Event Vertex	37.0639	71.3360	133.213	70.7260
#TofMatchedPrims	36.1075	70.8353	132.195	68.2627
Refined RunQA 14	33.6811	67.2199	131.324	62.6191
Min. Ref. Mult.	30.8784	61.7139	118.704	56.7663
#TracksEP	30.8783	61.7137	118.691	56.7082
Final (weighted) ¹⁵	32.2307	63.6828	122.390	59.4631

¹ STAR-internal IDs to select minimum bias trigger events.

² fiducial event vertex volume to remove beam on beam-pipe events.

³ minimum reference multiplicity to select the 0-80% most central events (see Section 2.2.1).

⁴ total number of global tracks in an event.

⁵ number of primary tracks matched to TOF hit(s) in an event.

⁶ number of global tracks in an event used for its event plane reconstruction (see Section 2.2.2).

⁷ number of TPC dE/dx cluster hits used for particle helix fit.

⁸ remove split tracks (see Section 2.1.1).

⁹ total number of TPC dE/dx cluster hits in an event.

 $^{^{10}}$ flag determining whether a track is matched to TOF hit(s): 0 - no match, 1/2 - one-to-one/multiple.

¹¹ constrain distance btw. TPC track extrapolation endpoint and TOF pad center to remove false TOF matches.

¹² distance-of-closest-approach of global track to event vertex.

¹³ collaboration-wide list for bad run rejection via StRefMultCorr (see Section 2.2.1).

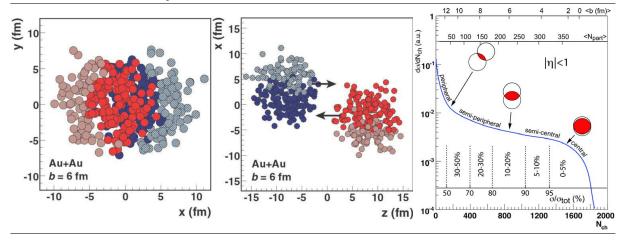
¹⁴ additional run rejection specific to this physics analysis (see Section 2.2.1).

¹⁵ corrected for trigger inefficiencies (see Section 2.2.1).

2.2.1 Reference Multiplicity and Quality Assurance

In heavy-ion collisions, the impact parameter of the two incoming nuclei cannot be observed directly due to the femtoscopic length scales at play. However, related geometric parameters such as the number of participating nucleons (N_{part}) or the number of binary nucleon-nucleon collisions (N_{coll}) are typically needed to classify the centrality of an event during a physics analysis. For instance, in Section 2.4 an event's centrality class is used to group it with other similar events for the generation of background distributions using the event mixing technique, and in Section 4.1 N_{coll} constitutes the factor required to scale simulations of charm continuum distributions from p+p to Au+Au collisions (quoted in Table 4.2). This predicament is commonly addressed nowadays using Glauber Monte Carlo simulations [167] which provide a theoretical mechanism to estimate the necessary quantities from experimental data by modeling the multiple scattering of the traversing nucleons inside the colliding nuclei. As illustrated in Figure 2.5 (left and middle), the latter are assembled in-silico using suitable nuclear density distributions and brought to collision with an impact parameter b chosen randomly according to $d\sigma/db = 2\pi b$. The collision subsequently proceeds via a sequence of independent (inelastic) binary nucleon-nucleon collisions with the participants traveling along straight lines inbetween collisions. In very simple terms, a nucleon-nucleon collision occurs when the criterion $d^2 \leq \sigma_{
m inel}^{
m NN}/\pi$ is satisfied for their radial distance d (black disk, $\sigma_{
m inel}^{
m NN}$: total inelastic nucleon-nucleon cross-section).

Figure 2.5 Glauber Monte Carlo event viewed in transverse plane (left) and along the beam axis (middle). Nucleons are depicted with diameter d according to the black disk collision criterion (see text). Darker disks represent participating nucleons. (right) Cartoon depicting the experimentally measurable charged particle multiplicity (N_{ch}) distribution along with mean impact parameter and N_{part} calculated from Glauber simulations for the centrality classes. [167]



One of the advantages of Glauber Monte Carlo models is their capability to simulate experimental final-stage observables like the charged particle multiplicity N_{ch} . The cartoon in Figure 2.5 (right), for instance, connects the N_{ch} distribution $d\sigma/dN_{ch}$ to the fundamental geometry-related parameters b and N_{part} . The $d\sigma/dN_{ch}$ distribution is thus a good experimental measure to indirectly determine a set of centrality classes ranging from central to peripheral collisions by calculating fractions of the total reaction cross section (σ/σ_{tot}). The N_{ch} multiplicities then serve as a reference for the centrality of a collision which is why a single measured N_{ch} is commonly referred to as *reference multiplicity* (RefMult) of an event. In Table 2.1, a minimum reference multiplicity has been used to select the 0-80% most central events, i.e. events with impact parameters approximately up to 80% of the maximum radial distance between the incoming nuclei ($\langle N_{part} \rangle > 0$).

Figure 2.6 shows the (raw) reference multiplicity distributions of charged particle tracks

reconstructed by STAR within $|\eta|$ < 0.5 at BES-I energies [168]. All experimental distributions are accurately described by Glauber Monte Carlo simulations over the full N_{ch} range except for some of the most peripheral events suffering trigger inefficiencies. The effect is corrected by using the N_{ch}-dependent ratio of simulation over data as a weighting factor on event- but also track-wise observables (Section 2.4). The final number of events listed in Table 2.1, for instance, is obtained by calculating the according weighted sums of events. Note that the correction is as large as 30% for the peripheral centrality bin whereas negligible in more central collisions. The z-vertex dependence of other sources of inefficiencies due to changes in the trigger configuration throughout the run are also included in the correctional weighting factors.

Figure 2.6 Raw multiplicity distributions measured in STAR at $|\eta|$ < 0.5 for BES-I energies (black points). The data is compared to a Glauber Monte Carlo simulation (red solid line) and three different centrality classes are indicated (grey shaded regions). [168]

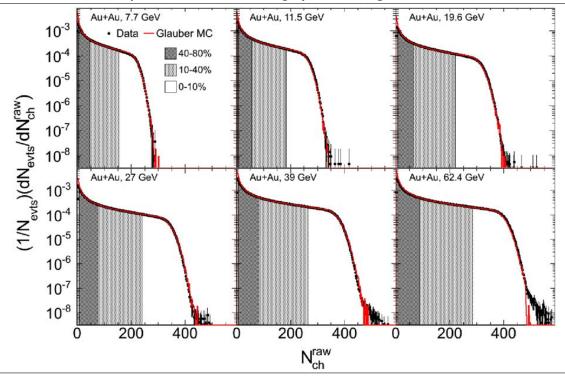
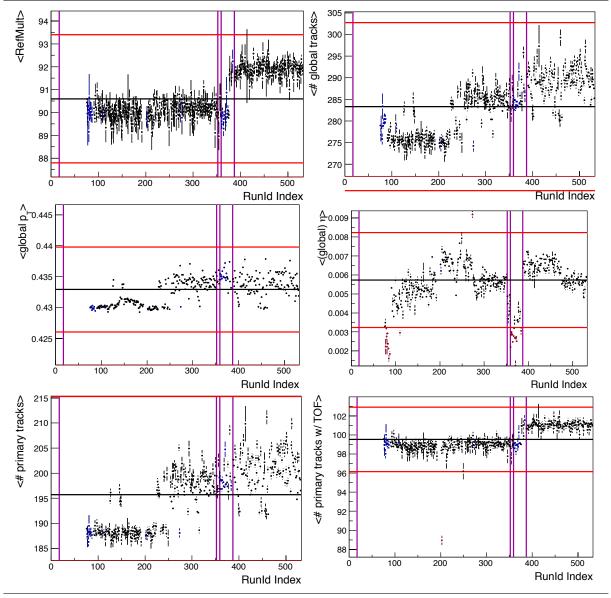


Table 2.2: Reference multiplicities at BES-I energies used in this dielectron analysis to define the centrality classes [169]. An event belongs to a certain centrality class (in %) if its reference multiplicity is larger than the value listed but smaller than the one for the next more central class.

$\sqrt{s_{ m NN}}$	70-80	60-70	50-60	40-50	30-40	20-30	10-20	5-10	0-5
19.6	6	12	23	40	66	102	152	220	263
27	6	13	26	45	74	114	168	241	288
39	7	15	28	50	81	125	185	265	316
62.4	7	16	30	54	88	135	199	285	339

The preceding procedure culminated in the development of a STAR software module called StRefMultCorr [169, 170] which not only provides the centrality classes listed in Table 2.2 but also includes basic quality assurance (QA) to reject bad runs based on their average RefMult. The according list can be found in Table A.1 and is refined for this dielectron analysis as follows.

Figure 2.7 Set of event-wise observables used for run-by-run quality assurance (Run QA) at 19.6 GeV, representatively. Figures for the Run QA at all BES-I energies used here are appended in Section A.3. Solid black points denote the experimental data for the observable averaged over the events within a run whereas black horizontal lines reflect the observable's average over the entire beam time. The runs are identified using the index obtained via the dedicated library StRunIdEventsDb in Section 7.3. Vertical magenta lines indicate run ranges with the same number of missing RDOs (see Section 2.1.1 and the library StBadRdosDb in Section 7.2). Horizontal red lines result from the Grubbs test for outliers [171] and separate accepted runs (black) from rejected (red) runs. Blue points depict runs that have been rejected based on one of the other observables.



A so-called *run* compiles a set of events taken during a time with steady detector conditions and, depending on the beam energy, lasts for about 30-60 minutes with a few million events. The choice to split the data acquisition into chunks called *runs* is rather arbitrary but simplifies time-dependent studies like the quality assurance in Figure 2.7. For the latter, the event-by-event observables reference multiplicity (RefMult), number of global/primary tracks with and without TOF match, global momentum and pseudo-rapidity are averaged over the events contained in the run with an index specific to the corresponding RunID (see Section 7.3). To obtain a refined list of "bad" runs in addition to the one provided by StRefMultCorr, outliers from

the general trend of these observables across all runs are detected using the Grubbs test [171]. In its two-sided form, this test continuously recalculates the statistic $G = \max |Y_i - \bar{Y}|/\sigma$ for the observable Y, its sample mean \bar{Y} and standard deviation σ . Using this statistic, the iterative algorithm [172] intrinsically starts testing for outliers with the data point currently farthest away from the sample mean when properly weighted with its statistical uncertainty. This data point is marked as outlier at a significance level α and removed from the sample before the next iteration if the statistic satisfies

$$G > \frac{N-1}{\sqrt{N}} \sqrt{\frac{t^2}{N-2+t^2}}$$

with N the sample size and t the quantile of the Student's t-distribution for probability $\alpha/2N$ and N-2 degrees of freedom. The iteration is aborted and no further RunIDs rejected once no outliers are found anymore according to the above criterion. Note that normal distribution of the data technically is a requirement for the validity of the Grubbs test. For the observables used for the Run QA in Figure 2.7 and Section A.3, this requirement could be satisfied by partitioning the data into suitable run ranges (e.g. the ones provided by StBadRdosDb in Section 7.2) and applying the algorithm on the subsets separately. However, this would have complicated the analysis unnecessarily since the simplified implementation chosen in [172] with $\alpha=0.95$ has proven to be effective enough in rejecting the worst outliers and can also be applied across all energies without modifications. The resulting refined list of rejected runs is also included in Table A.1.

2.2.2 Event Plane Reconstruction

The event plane method [9, 173] is a concept integral to many physics analyses trying to measure elliptic flow v_2 in a heavy-ion collision (see Section 1.2). In such analyses, an identified particle's v_2 signal can be extracted from a fit to its yield distribution in the form of

$$dN/d(\phi - \Psi_2) \propto 1 + 2v_2 \cos(2(\phi - \Psi_2))$$

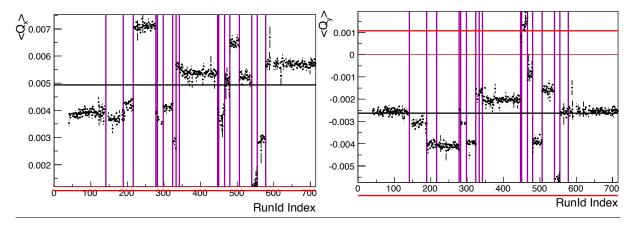
as function of its azimuthal angle ϕ with respect to the second harmonic event plane angle Ψ_2 [168]. The measurement of dielectron elliptic flow [174] is beyond the scope of this thesis and the v_2 signal extraction requiring corrections for self-correlations and calculation of event plane resolutions, for instance, thus not part of this analysis. However, an event's Ψ_2 and hence the full reconstruction of the event plane are still needed to later allow for the correct statistical subtraction of background from combinatorial e^+e^- pairs. The latter is an important step to obtain the dielectron spectra from physical sources. The study of event mixing in Section 2.4 further reveals that event classification taking the event plane angle into account is imperative for the correct background shape.

The reconstruction of the event plane relies on the particles' observed azimuthal angles and hence the event's anisotropic flow itself to arrive at a reasonable estimate for the more fundamental plane defined by the participating nucleons. Direct experimental access to the participant plane is not possible but an estimate for it is important since theoretical models commonly use it to describe flow measurements. The initial elliptical overlap zone containing the participant nucleons (see Figure 1.3) is oriented isotropically in space due to the stochastic nature of a nucleus-nucleus collision. The reaction plane defined by the incoming nuclei is hence distributed uniformly regarding its azimuthal angle with respect to the beam axis. This uniformity in the initial reaction consequently demands a flat distribution of the event plane angle $\Psi_2 = 0.5 \tan^{-1}{(Q_y/Q_x)}$ with $\vec{Q} = (Q_x, Q_y)$ the event flow vector in the laboratory determined by the measured azimuthal angles ϕ_i of the reconstructed particles in an event:

$$\vec{Q}_{\text{raw}} = \frac{1}{N} \sum_{i=0}^{N} \begin{pmatrix} w_i \cos(2\phi_i) \\ w_i \sin(2\phi_i) \end{pmatrix} \text{ with } w_i = \begin{cases} p_T & \text{if } p_T \le 2 \, GeV/c \\ 2 & \text{if } p_T > 2 \, GeV/c. \end{cases}$$

where N denotes the number of tracks with global DCA < 1 cm, $|\eta|$ < 1 (full TPC), and global momenta of 0.15 - 5 GeV/c. In the optimal case, the weights w_i in the above raw event flow vector are chosen such that they reflect the elliptic flow v_2 which is often linearly dependent on the particle's transverse momentum p_T up to about 2 GeV/c.

Figure 2.8 RunID-dependence of the raw event flow vector at 39 GeV averaged over all events within an experimental run. Color coding and run indexing are identical to Figure 2.7. Note however, that horizontal red lines do not bear any meaning here since the event flow vector is not used as an observable for Run QA. Figures for all BES-I energies are appended in Section A.3.



As a representative for all BES-I energies (see Section A.3), Figure 2.8 depicts the run-byrun averaged raw event flow vectors at $\sqrt{s_{\rm NN}}$ = 39 GeV. The averages clearly correlate with the number of missing RDOs for the different run ranges indicated by the magenta vertical lines (see Section 7.2). Within each run range, the average Q-vectors are approximately constant when taking statistical uncertainties into account. These observations are in agreement with expectations since such inefficiencies in the detector response immediately destroy isotropy and induce a preferential direction on the average Q-vector. Detector imperfections, in general, hence introduce acceptance correlations on the Ψ_2 distribution. This necessitates the application of analysis methods to correct for the resulting effects and flatten the Ψ_2 distribution. The intuitive procedure called *Phi-Weighting* is to weight each contributing particle with the inverse of an azimuthal angle distribution averaged over a sufficiently large number of events. But strong variations in acceptance or entirely missing sectors are difficult to compensate using Phi-Weighting. Alternatively, an average raw event flow vector $\langle \hat{Q}_{\text{raw}} \rangle$ can be derived from a large enough selection of events and subtracted from Q_{raw} on an event-by-event basis to obtain the recentered event flow vector $\vec{Q}_{rc} = \vec{Q}_{raw} - \langle \vec{Q}_{raw} \rangle$ [9, 173]. This Recentering method is not only more practical to implement but also guarantees a zero $\langle \vec{Q}_{\rm rc} \rangle$. The corrected event plane angle $\Psi_{2,rc}$ is subsequently recalculated using the recentered Q-vector Q_{rc} .

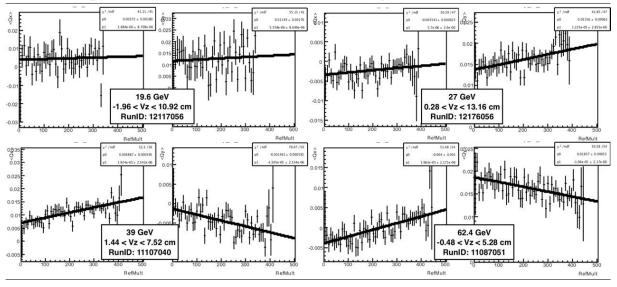
The event samples used for the purpose of obtaining an average raw event flow vector should be small enough to register changes in detector response and beam performance during the experiment but also large enough to ensure statistically significant averages. In this analysis [175, 176], the datasets at each energy are therefore divided into 10 z-vertex (V_z) intervals and raw Q-vector averages are calculated for each run separately. Samples with less than four events for a specific V_z bin and RunID are ignored in the subsequent analysis steps. Instead of using equi-distant intervals, the V_z distributions for each energy are parameterized using the functional forms listed in Table 2.3 and partitioned such that each bin contains the approximately equal number of events. The resulting V_z intervals are appended in Table 2.3 and also used for event classification during event mixing in Section 2.4. Exemplatory $\langle \vec{Q}_{\text{raw}} \rangle$ coordinates for all BES-I energies are shown in Figure 2.9 as a function of reference multiplicity. The dependence is parameterized with a straight line to smoothen the statistical fluctuations

and the resulting fit parameters are used to obtain event-by-event \vec{Q}_{rc} vectors according to the event's V_z , RunID, and RefMult.

Table 2.3: Parameterization of V	V_z distributions for binni	ng with equal number of events.

$\sqrt{s_{ m NN}}$	Form						1	l)	С	
19.6		$a - bV_z - cV_z^2$ 6631.45			1.45	7.6	321	0.372	181		
27		a	$1 - b v_z - c$	v_z^-		482	40.6	8.16	5007	2.56	18
39		/	(1 + 1/17 +	12)		1.671	47e-3	8.058	54e-4	-2.007	757
62.4		a/	$(1+b(V_z+$	$-c)^{-})$		1.770	48e-3	1.042	52e-3	1.366	577
·	V_z intervals (in cm)										
19.6	-70	-54.88	-40.88	-27.72	-14.84	- 1.96	10.92	24.36	38.64	54.32	70
27	-70	-54.04	-39.48	-25.76	-12.6	0.28	13.16	26.32	40.04	54.88	70
39	-40	-27.84	-18.72	-11.2	-4.64	1.44	7.52	13.92	21.12	29.76	40
62.4	-40 -28 -19.36 -12.32 -6.24					- 0.48	5.28	11.52	18.88	28.16	40

Figure 2.9 Typical reference multiplicity dependencies of average raw event flow vector coordinates $Q_{x,y}$ at all BES-I energies for specific V_z intervals and RunIDs. Also shown are linear fits and their parameters which are used for the recentering correction of the raw Q-vector.



Finally, any residual correlations remaining in the recentered Ψ_2 distribution can be forced flat on average via the *Shift Correction* method [9, 173]: The $\Psi_{2,rc}$ distribution averaged over the events in each combination of V_z interval and RunID is fit with a second order Fourier expansion

$$dN/d\Psi_{2,rc} \propto 1 + 2(p_1\cos(2\Psi_{2,rc}) + p_2\cos(4\Psi_{2,rc}) + p_3\sin(2\Psi_{2,rc}) + p_4\sin(4\Psi_{2,rc}))$$

from which the fully corrected event plane angle $\Psi_{2,corr} = \Psi_{2,rc} + \Psi_{2,shift}$ can be obtained using

$$\Psi_{2,\text{shift}} = -p_3 \cos(2\Psi_{2,\text{rc}}) + p_1 \sin(2\Psi_{2,\text{rc}}) + 0.5 \left(-p_4 \cos(4\Psi_{2,\text{rc}}) + p_2 \sin(4\Psi_{2,\text{rc}})\right).$$

Figure 2.10 depicts typical second order Fourier expansion parameterizations of the $\Psi_{2,rc}$ distributions at all BES-I energies. Figure 2.11 compares the according raw event plane angle distributions to the recentered and shift-corrected ones proving the successful flattening of the

averaged Ψ_2 distributions. The latter can hence be split into several Ψ_2 intervals and the corrections used on the raw event plane angles in Section 2.4 to categorize similar events in the event mixing technique.

Figure 2.10 Typical second order Fourier expansion parameterizations of the $\Psi_{2,rc}$ (PsiRc) distributions at all BES-I energies for the same V_z intervals and RunIDs as in Figure 2.9.

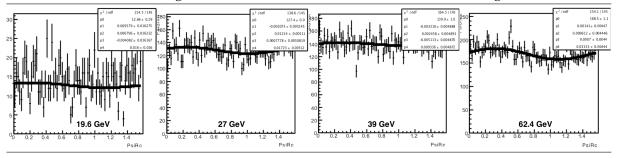
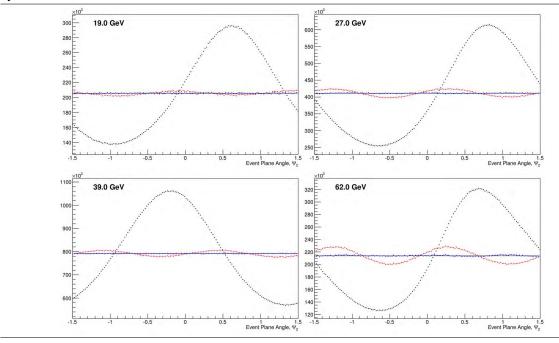


Figure 2.11 Comparison of raw (black), recentered (red), and shift-corrected (blue) Ψ_2 distributions at all BES-I energies. The black solid line represents a constant fit to guide the reader's eye.



2.3 Single-Electron/Positron Samples

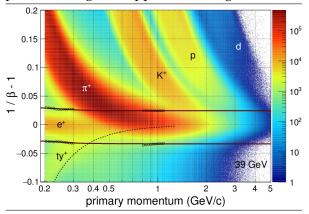
So far, suitable event and track selection criteria (Table 2.1) have been applied on the BES-I datasets derived from the according STAR DSTs [175]. This first raw data analysis step has also included run-by-run quality assurance (Figure 2.7) and event plane reconstruction to provide improved event classification in Section 2.4 via a uniformly distributed event plane angle Ψ_2 (Figure 2.11). Next, the resulting *good* tracks in an accepted event need to be reduced to the particle species of interest in the particular data analysis. In the context of this thesis and its intended physics results (Chapter 5), the suppression of hadrons facilitated through the usage of the TOF detector is of crucial importance for the identification of electrons and positrons. Section 2.3.1 describes the procedure with which clean electron and positron samples are obtained in combination with the particles' specific energy loss in the TPC. Section 2.3.2 studies

the samples in detail revealing their high degree of purity which makes them ideally suited for the study of dielectron production. Note that this section only includes selected figures at a single energy and particle charge in order to support the text whereas the complete set can be found in Section A.4.

2.3.1 Electron/Positron Identification via TOF and TPC

In dependence of primary momentum and representatively for $\sqrt{s_{\rm NN}}$ = 39 GeV, Figure 2.12 shows the distribution of the inverse velocity for positive particles measured with respect to the expected positron velocity of about 1. In this representation the positrons appear as an approximately constant band around zero which allows for the determination of simplified criteria to select the region containing a certain fraction of all reconstructed positrons.

Figure 2.12 Measured inverse velocity $1/\beta$ for positive particles as a function of primary momentum at $\sqrt{s_{NN}} = 39$ GeV. Superposed are the velocity limits used to select positrons (solid lines) derived from the band's 3σ windows below 320 MeV/c and from the according distribution using pions as reference at higher momenta (open black circles). The expected correlation for the tachyonic artefacts (ty⁺, dashed line) is depicted as well. Details see text. All remaining combinations of beam energy and particle charge are appended in Figure A.9.

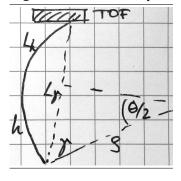


A clear separation of the positrons from slow hadrons up to momenta of about 320 MeV/c is observed beyond which the positrons' band starts merging with the one from the abundant pions. Together with a separate pion sample at 1 GeV/c, this region is hence used in the following as part of the procedure to determine a 3σ selection criterion which efficiently rejects the dominant contamination from pions, kaons, protons and deuterons. When applied on the inverse velocity distribution, this criterion prepares a set of track candidates from which the final positron sample can subsequently be extracted via the TPC energy loss (see Figure 2.14).

Also note the additional band of tracks that appear to be reconstructed in Figure 2.12 with $\beta > 1$. This non-physical band of seemingly faster-than-light ("tachyonic") particles is observed even though electrons/positrons must reach the TOF detector before all other detectable particles. Photons, however, can convert into electron/positron pairs in the outer TPC field cage or inside the TOF detec-

tor itself causing the according TOF hit to have a photon timing. Due to the occupancy in the detector these TOF hits are accidentally matched to hadron tracks in the TPC resulting in an artefact of apparently tachyonic particles.

Figure 2.13 TOF Tachyon



The momentum dependence of this detector peculiarity can be derived through simple geometrical considerations outlined briefly in the following and depicted in Figure 2.12 as a dashed line to guide the reader's eye. For the definition of the variables see Figure 2.13. The paths of a photon γ with length L_{γ} and a hadron h with length L_h meet in the same TOF hit with a timing corresponding to L_h . With the photon time-of-flight $t_{\gamma} = L_{\gamma}/c$, the tachyonic velocity amounts to $\beta_{ty} = L_h/ct_{\gamma} = L_h/L_{\gamma}$ where L_h is related to L_{γ} via $L_h = \rho \theta = 2\rho \arcsin(L_{\gamma}/2\rho)$ with ρ the radius of the helix's projected circle and θ the according central angle of the circular segment. Embedded in a magnetic field B, the track's transverse momentum is $p_T = 0.3B\rho$ resulting in $\beta_{ty} = \arcsin(p_T^*)/p_T^*$ with $p_T^* = 0.3BL_{\gamma}/2p_T$.

The functional form of the 3σ TOF selection criterion is derived programmatically [177] through a series of analysis steps based on the momentum-dependent inverse velocity distribution. First, one-dimensional $1/\beta$ distributions are obtained from the projection in momentum intervals small enough to approximate a gaussian distribution for the pions. Second, the $1/\beta$ interval with the most entries is identified as the pion peak in the respective momentum bin and the distribution parameterized with a gaussian in the peak's vicinity. Third, the resulting gaussian is subtracted from the experimental $1/\beta$ distribution to remove contributions from the pion tail to the positron band. Fourth, the slopes of the entire remaining distribution are determined bin-by-bin through linear interpolation using five points at a time. Fifth, a sign change in the slopes and exception of the tachyonic artefact then reveals the positron peak, the position of which is used to determine the range limits of its gaussian parameterization. The calculation of the two 3σ endpoints for the latter results in the positions of the solid open circles below 320 MeV/c in Figure 2.12. For the determination of the positron band's gaussian widths around 1 GeV/c the $1/\beta$ - $1/\beta_{\pi}$ representation is used assuming particle species independence in the TOF measurement. Here $1/\beta_{\pi}$ denotes the inverse velocity expected for a particle with pion mass at the respective primary momentum. The two regions are combined using a χ^2 minimization of the momentum-dependent selection functional

$$\frac{1}{\beta(p)} - 1 = A \cdot \left(\frac{\pi}{2} - \arctan\left(B \cdot (p - C)\right)\right) + \begin{cases} D, & \text{upper limit} \\ d, & \text{lower limit} \end{cases}$$

to the data points of the experimental 3σ windows. This allows for a constant 3σ selection around the positron distribution across all momenta. Table 2.4 compiles the parameters resulting from the above fit of the TOF selection functional. The preceding arguments, conclusions and procedure to extract positrons via TOF with a probability of $99.73\%^{16}$ are also valid and hence employed for other particles and energies as apparent from Figure A.9.

Table 2.4: Parameters of electron/positron TOF selection functional.

	A	В	С	D	d
19.6 GeV	2.322e-3	16.2	0.2458	2.459e-2	-3.426e-2
27 GeV	3.078e-3	17.04	0.2383	1.693e-2	-2.627e-2
39 GeV	2.0785e-3	18.3	0.2478	2.429e-2	-3.361e-2
62.4 GeV	2.158e-3	12.56	0.2265	1.739e-2	-4.174e-2

To conclude the identification of electrons and positrons, a momentum-dependent selection criterion to be subsequently applied on the energy loss measured in the TPC is developed in the following. For better handling of dE/dx selection windows, the energy loss is transformed into

$$n\sigma_{\rm el} \propto \ln \left(\frac{dE}{dx} \bigg|_{\rm meas} / \frac{dE}{dx} \bigg|_{\rm el} \right)$$

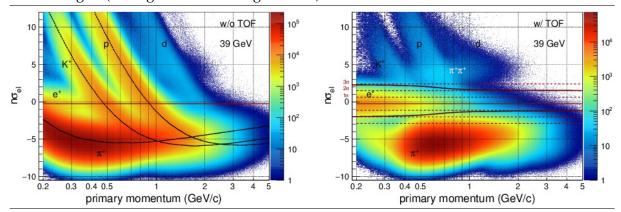
describing the logarithmic deviation of the measured from the expected dE/dx of electrons/positrons in units of the dE/dx distribution's width 17 . By means of this representation, STAR's new particle identification (PID) capabilities are illustrated in Figure 2.14 by comparing the momentum dependence of $n\sigma_{el}$ distributions for positive particles at $\sqrt{s_{NN}}$ = 39 GeV with and without using the TOF selection functional of Figure 2.12. Without employing TOF to reduce hadron contamination, the positron band is effectively buried underneath the substantial overlaps of pion, kaon, and proton energy losses below 1.5 GeV/c. Combining TOF and TPC for particle identification purposes, however, now also allows STAR to cleanly identify electrons

 17 due to TPC mis-calibration at 27 GeV, a $n\sigma_{el}$ correction factor of 1.9 is taken into account in Figure A.10.

¹⁶ at the time of this writing, systematic uncertainties on the TOF selection have not been taken into account, yet.

and positrons down to momenta as low as $0.2~{\rm GeV/c}$. The combined PID continues to work well up to the high momenta at which the magnetic calorimeters provide good energy resolution for e^+/e^- identification. Unlike elementary collisions (see Figure 47 in [151]), the well separated pions and positrons/electrons are not the only bands visible in the $n\sigma_{\rm el}$ distributions. Due to the high occupancy in heavy-ion collisions, hadrons in the tachyon band above about 280 MeV/c survive the TOF selection in Figure 2.12 and cause residual contamination from kaons and protons as well as so-called *merged* pions in Figure 2.14 (right). The latter is caused by close-by pion pairs, the tracks of which are not resolved in the TPC and thus result in approximately double the energy loss with a momentum dependence resembling single pions.

Figure 2.14 Distributions of TPC energy loss relative to the expected positron dE/dx for positive particles at $\sqrt{s_{NN}} = 39$ GeV in dependence of primary momentum and in units of the dE/dx width. The two versions shown are $n\sigma_{el}$ distributions without (left) and with (right) a TOF requirement selecting the positron $1/\beta$ band (see Figure 2.12). Horizontal red solid lines correspond to the positrons' momentum-integrated (global) gaussian mean μ_{gl} (Table 3.3) derived from the separate positron sample of Section 3.1. Dashed horizontal lines denote $1/2/3\sigma$ -windows based on the σ_{opt} widths in Table 3.3. Also depicted are the adjusted Bichsel functions of Section 2.3.2 (black lines in left figure) and the TPC selection functional (red solid lines in right figure). The procedure to select e^+/e^- via their TPC energy loss is very similar for all BES-I energies (see Figure A.10 and Figure A.11).



Horizontal solid and dashed lines in Figure 2.14 indicate gaussian mean as well as 1σ , 2σ and 3σ windows. Mean and width are based on the separate analysis of pure e^+/e^- samples from photon conversions and Dalitz decays in Section 3.1 and Table 3.3. The windows are used as guidelines for the definition of the momentum-dependent criterion on the TPC energy loss to select electrons and positrons. Similar to the TOF selection functional, the resulting TPC dE/dx selection functional basically consist of a common bare part plus an offset for the lower and upper limits, respectively:

$$n\sigma_{\rm el}(p) = \pm \frac{A}{\pi} \arctan(5p-3) + \begin{cases} D, & \text{lower limit} \\ d+A/2, & \text{upper limit} \end{cases}$$

with A=0.9 and the values of the parameters D and d listed in Table 2.5. The upper limit at every BES-I energy is tuned to select about 3σ of the electrons/positrons at very low momenta followed by a smooth transition down to about 2σ across the region in which the residual kaons and proton traverse the e^+/e^- band. However, the multiples of dE/dx width for the lower limit are chosen to transition from 2 down to 1 due to the significant potential of pion contamination into the $n\sigma_{\rm el}<0$ tail of the e^+/e^- distributions. The figures containing $n\sigma_{\rm el}$ distributions and the resulting TPC selection functions are included for all BES-I energies in Figure A.10 and Figure A.11.

Figure 2.15 Run-by-run averaged single electron (black open circles) and positron (blue open circles) yields per event in dependence of RunId index (Section 7.3) for all BES-I energies. Also depicted are number of e⁻ (green dashed line) and e⁺ (red dashed line) averaged over the entire run. Vertical magenta lines indicate run ranges with the same number of missing RDOs (Section 7.2).

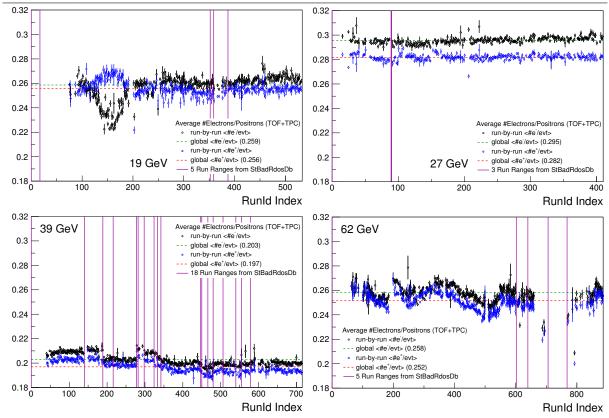


Table 2.5: Parameters of electron/positron TPC dE/dx selection functional.

	19.6/39 GeV	27 GeV	62.4 GeV		19.6/39 GeV	27 GeV	62.4 GeV
D	-1.65	-1	-1.3	d	1.5	0.5	1.7

The electron and positron samples resulting from the combined TOF/TPC PID are characterized in Figure 2.15 at all energies by means of their respective run-by-run dependent average number per event. Some of the observed structures at 39 GeV, for instance, can be linked to the different phases of data taking using the same set of missing RDOs as indicated by vertical magenta lines. Others, however, e.g. at 19.6 GeV, are related to other possible acceptance effects of the detector. The number of electrons and positrons averaged over the entire beam time ranges from 0.2 at 39 GeV, and 0.26 at 19.6/62.4 GeV, up to 0.29 at 27 GeV. Not only does 27 GeV deliver the highest average number of electrons/positrons per event but it also appears to be the most stable beam time in terms of changing detector conditions. Figure A.12 in the appendix shows the number of events for a given combination of electrons and positrons reiterating that the bulk of the events (91-96%) does not contain any electrons/positrons at all, only one of each or at most a single unlike-sign pair. Further, more detailed studies of samples quality follow in Section 2.3.2.

2.3.2 Sample Purities

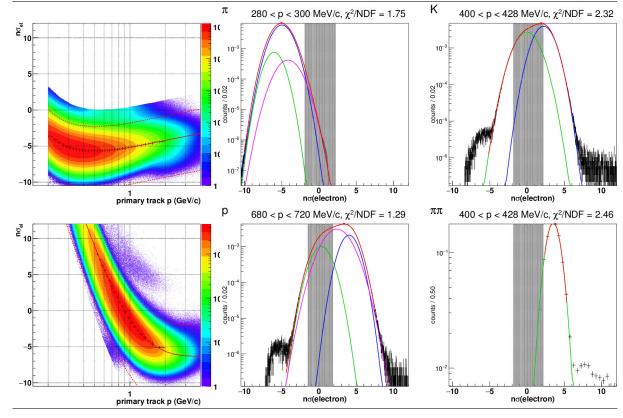
The study of hadron contamination levels in the electron/positron samples generated in Section 2.3.1 is especially important for the analysis of dielectron production if a detailed understanding of the sample qualities in terms of purity is to be obtained. Due to scarcity of these electromagnetic probes, however, the accurate momentum-dependent determination of single hadron contributions to the electron/positron samples is challenging and complex. A generic functional form that works well across beam energies and momentum ranges needs to be derived to parameterize the $n\sigma_{el}$ distributions in Figure 2.14 resulting from the application of electron/positron TOF selection criteria (see Figure 2.12). It is immediately evident, though, that the multitude of possible contaminations by pions, kaons, protons, and merged pions causes a high number of floating parameters for the χ^2 minimization of $n\sigma_{el}$ parameterizations. A fully automated procedure to successfully perform such multi-particle fits hence necessitates a preceding analysis of pure hadron samples in the $n\sigma_{el}$ -vs-momentum space that provides a good handle on their respective functional shapes and allows for most of the parameters to be either fixed or constrained within reasonable limits. As a result, an elaborate twoprong approach consisting of (i) multi-gaussian fits to pure hadron $n\sigma_{el}$ distributions, and (ii) simultaneous multi-particle fits to $n\sigma_{el}$ distributions of electron/positron candidates has been developed. It is presented in detail in the remainder of this subsection which concludes with momentum-dependent purities calculated at all BES energies. The purities serve as a basis for the important estimate of systematic uncertainties on dielectron invariant mass spectra caused by hadron contaminations (see Section 2.4).

Analysis of pure hadron distributions. The same functional form and parameters as for the electron/positron selection via TOF (see Table 2.4 and accompanying text) are used for the generation of pure $\pi/K/p$ samples. Merely the selection window is reduced to 1σ around the $1/\beta$ - $1/\beta_{POI}$ band (β_{POI} = velocity of the particle of interest) using the offset parameters d and D at the respective energy. As discussed in Section 2.3.1, a qualitatively sufficient sample of merged pions ($\pi\pi$) appears as part of the pure pion sample at about twice the single pion energy loss. In Figure 2.16, the resulting $n\sigma_{el}$ distributions of the pure hadron samples are subsequently analyzed in dependence of particle momentum. Before starting their iterative parameterization via *multi-gaussian* fits, the initial values for the first gaussian means and a suitable $n\sigma_{el}$ parameterization range are determined by studying the momentum dependence of the most probable energy loss using Bichsel functions [146, 147] (Figure 2.16 left column). The peak of the projected $n\sigma_{el}$ distribution in each momentum bin is taken as the most probable energy loss (solid crosses) and its momentum dependence parameterized (solid red line) via

$$n\sigma_{\rm el}^{\rm POI} = a \ln \left[\ dE/dx (m_{\rm POI}) \ / \ dE/dx (m_{\rm e}) \ \right] + b$$

with a the proportionality factor and dE/dx the Bichsel function depending on e^+/e^- mass m_e and hadron mass m_{POI} . The shift parameter b is used to set the upper and lower range limits (dashed red lines). For merged pions, a and m_{POI} are fixed to the final parameters of the pion fit with the offset initiated to $b = a \ln 2$. Table 2.6 lists the initial and final parameters of all $n\sigma_{el}$ functions.

Figure 2.16 (left column) Momentum-dependent $n\sigma_{el}$ distributions for pure pion (top) and proton (bottom) samples obtained through the according 1σ TOF selection on $1/\beta$ - $1/\beta_{POI}$. The peak positions in each momentum bin (black crosses) are parameterized with Bichsel energy loss functions [146, 147] (red solid line) which in turn are offset to obtain reasonable parameter limits for the *multi-gaussian* fits. (right two columns) Representative selection of *multi-gaussian* fits to $n\sigma_{el}$ distributions of pure π , K, p, and merged- π ($\pi\pi$) samples for different momentum ranges at $\sqrt{s_{NN}} = 39$ GeV. The pure hadron samples are parameterized using a sum of multiple gaussians (green, blue, magenta) to describe the overall shape (red) sufficiently well (note the indicated reduced χ^2). The grey dotted areas denote the TPC selection window defining the electrons/positrons samples at the corresponding momentum (c.f. Figure 2.14 right). The full momentum-dependent set of *multi-gaussian* fits for all hadrons at all BES energies is appended in Section A.5.



\sqrt{s}	NN	19.6 GeV	27 GeV	39 GeV	62.4 GeV
	a	$12.5 \rightarrow 12.5051$	$6.579 \rightarrow 6.199$	$12.5 \rightarrow 12.2$	$12.5 \rightarrow 12.421$
π	m	$0.13957 \rightarrow 0.1235$	$0.13957 \rightarrow 0.12298$	$\begin{array}{c} 0.13957 \rightarrow \\ 0.12346 \end{array}$	$0.13957 \rightarrow 0.12379$
	b	0 ightarrow -0.4446	0 ightarrow -0.22654	$0 \rightarrow$ -0.38356	$0 \rightarrow$ -0.10062
	а	$12.5 \rightarrow 13.1061$	$6.579 \rightarrow 6.5254$	$12.5 \rightarrow 12.3772$	$12.5 \rightarrow 12.7731$
K	m	$0.49368 \rightarrow \\ 0.45557$	$0.49368 \rightarrow \\ 0.45243$	0.49368 o 0.4542	0.49368 o 0.45213
	b	0 ightarrow -0.307	0 ightarrow -0.1462	0 ightarrow -0.4072	0 ightarrow -0.0601
	а	$12.5 \rightarrow 11.7627$	$6.579 \rightarrow 5.8754$	$12.5 \rightarrow 11.299$	$12.5 \rightarrow 11.2449$
p	m	$0.93827 \to \\ 0.93989$	$\begin{array}{c} 0.93827 \rightarrow \\ 0.93538 \end{array}$	$0.93827 \to \\ 0.92899$	$0.93827 \to 0.94254$
	b	0 ightarrow -1.2483	0 ightarrow -0.6287	$0 \rightarrow$ -1.1916	$0 \rightarrow$ -1.0686
	а	12.5051	6.199	12.2	12.421
$\pi\pi$	m	0.1235	0.12298	0.12346	0.12379
	b	$8.66784 \rightarrow \\ 9.05812$	$4.29681 \rightarrow \\ 4.51977$	$8.45682 \rightarrow \\ 8.82378$	$8.60922 \rightarrow 9.11032$

Table 2.6: Initial and final fit parameters of $n\sigma_{el}$ functions. Arrows denote the change in value.

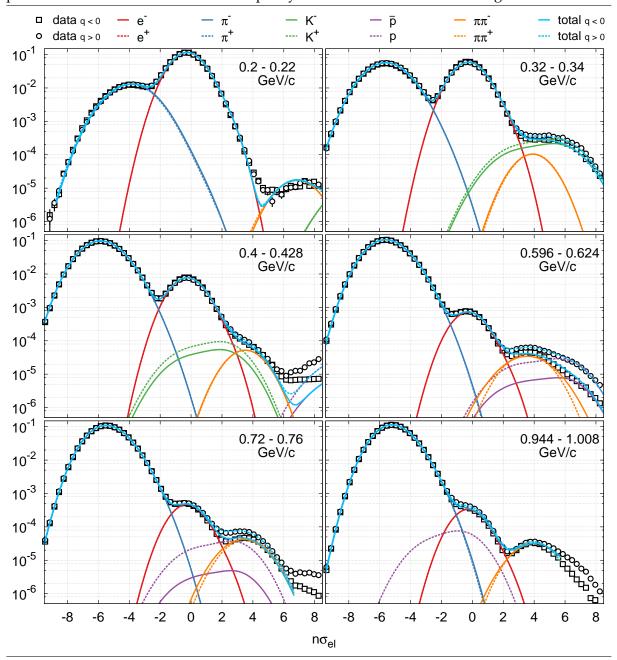
By extrapolation, this initialization phase not only allows access to reliable estimates of the most probable energy loss as well as reasonable fit ranges across the entire momentum range. It also ensures sanitized starting parameters for the following iteration procedure to accurately describe the momentum dependence of hadron $n\sigma_{el}$ distributions (Figure 2.16 right two columns).

A particle's energy loss measured in the TPC is distributed normal around its most probably energy loss which results in a gaussian function as valid description of the rather momentumindependent $n\sigma_{POI}$ distributions with normalized widths of ~ 1 . However, in the representation of a hadron's energy loss in the $n\sigma_{el}$ -vs-p plane, i.e. with respect to the energy loss expected from electrons/positrons, its momentum dependence becomes non-constant as illustrated for the protons in Figure 2.16 (lower left). Especially in the regions where $n\sigma_{el}$ falls off steeply with increasing momentum, several gaussians start contributing to the overall shape unless momentum intervals are kept unmanagably small. The multiple overlapping gaussians with approximately equal widths are slightly shifted towards each other and contribute with different yields to the measured $n\sigma_{el}$ distribution of the hadrons in the respective momentum bin. Iteratively increasing the number of gaussians used to fit the pure hadron samples' $n\sigma_{el}$ distributions until satisfactory agreement is achieved, thus makes for an intuitive approach to solve this issue and cope with finite momentum bin widths. The underlying algorithm reiterates a χ^2 minimization of an increasing sum of gaussians until either the reduced χ^2 is less than 3.5 (or alternatively, the minimum χ^2/NDF is reached), or the number of gaussians used exceeds 6. The right two columns of Figure 2.16 depict representative examples of this procedure's end results for the π , K, p and $\pi\pi$'s n $\sigma_{\rm el}$ distributions at selected momenta. The full list of these multi-gaussian parameterizations at all BES energies are attached in Section A.5 demonstrating the excellent level of control over the distributions' shapes which is an essential requirement for the success of the following simultaneous *multi-particle* fits.

Analysis of electron/positron candidate distributions. The momentum dependence of the experimental $n\sigma_{el}$ distributions for electron/positron candidates resulting from the 3σ TOF selection in Figure 2.12 is now parameterized using the functional representation of the hadron $n\sigma_{el}$ distributions extracted in the previous paragraph. Figure 2.17 depicts a selection of distributions in momentum ranges that illustrate how the π , K, p, and $\pi\pi$ bands are traversing and overlapping the electron/positron band. Each of the graphs shows the total parameterization

of the full experimental $n\sigma_{el}$ distribution along with the respective single contributions, all of which are the outcome of the minimization procedure discussed in the following.

Figure 2.17 Selected momentum ranges for *multi-particle* fits to the experimental $n\sigma_{el}$ distributions for electron (open squares) and positron (open circles) candidates at $\sqrt{s_{NN}} = 39$ GeV obtained after application of the 3σ TOF selection criterion from Figure 2.12. Residual contaminations caused by positive and negative hadrons as well as the resulting total parameterizations are depicted in solid and dashed lines, respectively. The selected momentum bins up to 1 GeV/c show the dominant overlap regions of π , K, and p bands with the electrons/positrons at $n\sigma_{el}\sim0$, and cover 99% of the available total electron/positron statistics (c.f. Figure 2.18). The full momentum-dependent set of *multi-particle* fits at all BES energies including the final values for the floating parameters is appended in Section A.5. The single particle parameterizations provide the basis for the calculation of purity and contamination levels in Figure 2.18.



The full momentum-dependent parameterization of electron/positron candidate $n\sigma_{el}$ distributions involves a large number of parameters to be optimized. The extraction of accurate

shapes and positions for the according contaminating hadron distributions through the analysis of pure hadron samples allows for a considerable reduction of the floating parameter space. The parameters of the resulting *multi-gaussian* functions can be kept fixed and symmetric with respect to particle charge. This leaves (at most) the $4 \cdot 2 = 8$ yields for the hadron contaminations as floating parameters plus the yields as well as gaussian means and widths for electrons and positrons. The latter can confidently be fixed to the charge-averaged mean $\mu_{\rm gl}$ and width $\sigma_{\rm opt}$ (Table 3.3) deduced from the experimental electron/positron samples of photon conversion and Dalitz decays in Section 3.1. However, a closer look at the lowest momentum range 0.2 - 0.22 GeV/c, in which hadron contaminations are small, reveals that a secondary gaussian is required to satisfactorily describe the high-end tail of the electron/positron band. In an initialization fit, this gaussian is tuned to the tail in the lowest momentum bin and subsequently used in identical form throughout all higher momenta. To utilitize the symmetries between electron and positron candidate distributions and further reduce the parameter space by linking most of the 10 remaining floating yields, a simultaneous parameterization of the electron and positron candidate $n\sigma_{el}$ distributions has been implemented using the ROOT extension library Roofit [178]. This allows for the e^+/e^- , π^+/π^- , and $\pi\pi^+/\pi\pi^-$ yields to be forced the same while K^+/K^- and especially p/\bar{p} yields are allowed to vary separately. A successful fit minimization further requires sensible initial values for the yields of the single contributions to be set in each momentum bin. Reasonable estimates for the current momentum bin are achieved by extrapolating the optimized yields of the previous four momentum ranges via a power law (ax^b), and imposing 20-70% parameter limits based on the resulting central value (see last page of Section A.5). The $n\sigma_{el}$ range used for the simultaneous fit corresponds to the lowest and highest limits given by the underlying hadron $n\sigma_{el}$ parameterization ranges. Since kaons are skipped between 0.48 - 1.2 GeV/c, (anti-)protons below 0.4 and above 1.2 GeV/c, and antiprotons above 0.8 GeV/c where their respective contributions are negligible, most momentum bins only require five floating parameters for a successful description of the electron/positron candidate $n\sigma_{el}$ distributions. As demonstrated in Figure 2.17 and Section A.5, the above procedure works very well across the entire momentum range and most importantly across all energies without modifications. The only minor adjustment happens at small momenta below 0.6 and 0.3 GeV/c where correctional shifts for π and $\pi\pi$, respectively, are required in form of two additional floating parameters shifting the full multi-gaussian functions. The functional representation of the electron/positron candidate $n\sigma_{el}$ distributions now allows for purity and contamination levels to be calculated for the electron and positron samples based on the TPC selection window applied in each momentum bin (see Figure 2.14 right).

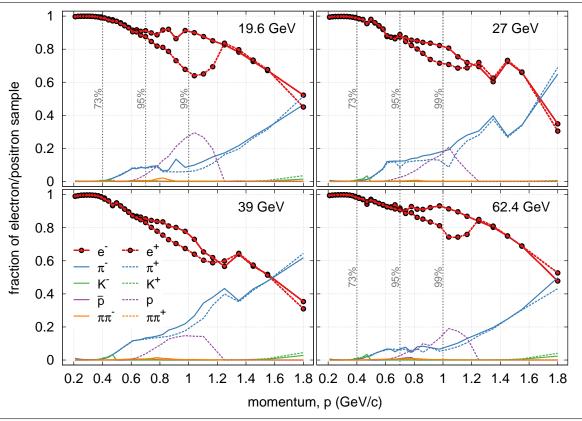
Electron/positron sample purities and contamination levels. For the purpose of quantifying sample qualities, the ultimate goal of this section is to derive purities and contamination levels of the electron/positron samples resulting from the application of TOF and TPC selection criteria. Figure 2.18 gives an overview of their momentum dependence at all BES energies exhibiting characteristic patterns common to all energies. For 73% of the full electron/positron sample or up to 0.4 GeV/c, excellent purities very close to 1 are achieved which drive the - for electrons and positrons exceptional - total sample purities of \sim 97-98.5% listed in Table 2.7. At higher and with increasing momentum the pion tail and the traversing proton band begin to dominate the contamination of the electron/positron samples causing a continuous reduction in purity down to about 40% at 2 GeV/c. Anti-protons are produced in heavy-ion collisions with significantly smaller cross sections than protons, the effect of which is observed at 0.7 - 1.2 GeV/c through an estimated purity decrease of 10-15% for the positron samples. It affects, however, only 5% of the total electron/positron statistics with momenta above 0.7 GeV/c. Contaminations by kaons at 0.4 - 0.5 GeV/c and by merged pions predominantly at 0.7 - 0.8 GeV/c are barely visible and on the sub-0.5% level. During the pair reconstruction procedure in Section 2.4, these impurities (as deviations from 100% pure electron/positron samples) are

considered part of the systematic uncertainties on the respective invariant mass spectra ¹⁸. As a final note on the side: The momentum dependence of upper and lower TPC selection limits has been varied to optimize the window for best sample significance. It turns out that only a minor improvement of the sample significances could be achieved by updating the current TPC selection functional with parameter values resulting from a fit to the result of the significance tuning.

Table 2.7: Total purities of electron and positron samples for all BES energies (in %).

$\sqrt{s_{NN} \text{ (GeV)}}$	19.6	27	39	62.4	√s _{NN} (GeV)	19.6	27	39	62.4
e ⁻	98.5	97.8	97.0	98.2	e^+	98.1	97.8	96.8	98.1

Figure 2.18 Momentum dependence of purity (red) and hadron contamination (π : blue, K: green, p: purple, merged- π : orange) levels of electron/positron samples identified via the TOF & TPC selection criteria discussed in Section 2.3.1 at all BES energies. The dominating contributions to the electron/positron samples by the pion tail and the band-traversing proton are clearly visible. To guide the reader's eye, vertical grey dotted lines are depicted at momenta of 0.4, 0.7, and 1 GeV/c respectively corresponding to \sim 73%, 95%, and 99% of the available electron/positron statistics. The relation of purity to these sample fractions results in the high total purities listed in Table 2.7.



 $^{^{18}}$ the propagation of impurity levels to systematic uncertainties on M_{ee} spectra is in progress.

2.4 Pair Reconstruction

The single electrons and positrons identified with high purities in Section 2.3 on an event-byevent basis constitute a list of particles originating from various, a priori unknown sources. Combining the four-momenta of all electrons and positrons in an event to form dielectrons with invariant masses M_{ee} and transverse momenta p_T results in the so-called unlike-sign (opposite charge) foreground spectra. These contain the actual dielectron signal plus background contributions from purely combinatorial or correlated sources. The former consist of e^+e^- pairs formed from disparate decays and the latter of cross pairs caused by the combination of $e^+e^$ pairs within the same π^0 Dalitz or 2γ decay (c.f. Figure 2.24 left). To identify the signal emanating from the interesting physical sources (see Table 4.1) by disentangling it from the background, two well-established and complementary statistical techniques are employed: i) the like-sign same-event method which reproduces both combinatorial and correlated background but is statistically limited at higher M_{ee}, and ii) the mixed-event method which exclusively provides the combinatorial background but instead with effectively unlimited statistical accuracy. Since the ρ/ω region of STAR dielectron spectra typically exhibits signal-to-background ratios of only 1/100 - 1/250 at BES-I energies, accurate background subtraction is crucial to enable the successful reconstruction of the dielectron signal and its comparison to the cocktail simulations and model calculations of Chapter 4.

In Section 2.4.1 [176], the prerequisite p_T -dependent dielectron M_{ee} -distributions are prepared for all like- and unlike-sign charge combinations of electrons and positrons from within the same event and from different events via *event-mixing*. Quality assurance of the mixed events is presented and pair-based selection criteria applied on all distributions to reject photon conversions. Section 2.4.2 [179] explains the statistical techniques in detail and performs the background subtraction. At the end of this chapter, raw dielectron M_{ee} - and p_T -distributions are readily available for the application of Chapter 3's efficiency corrections which ultimately enables the spectra's physics interpretation in Chapter 5.

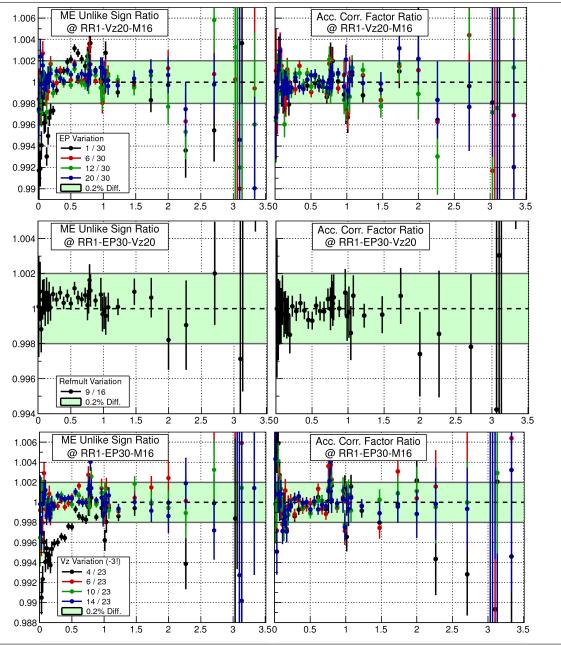
2.4.1 Generation of Pair Distributions

The reconstruction of all e^+e^- pairs for an event in a so-called *same-event analysis* and the subsequent generation of unlike-sign foreground distributions by means of the particles' Lorentz vectors is a straight-forward task in combinatorics. Special attention only has to be paid in the case of like-sign combinations to avoid double counting of pairs (i.e. start secondary iteration at j=i+1). In the *like-sign same-event* background subtraction method discussed in Section 2.4.2, the two resulting like-sign background distributions are averaged and corrected for the acceptance difference between like- and unlike-sign pairs which is obtained from mixed-event distributions.

The mixed-event technique enables the population of unlike- and like-sign background distributions with pairs from uncorrelated sources by combining electrons and positrons from two different events within the same event class. Here, an event class is defined by an event's primary z-vertex V_z (Table 2.3), its reference multiplicity RefMult (Table 2.2), and its event plane angle Ψ_2 (Figure 2.11). The space of event classes is discretized into 10, 9, and 10 bins for the V_z -, RefMult-, and Ψ_2 -dimension, respectively. This ensures the quick aggregation of a sufficient amount of similar events from which to generate high-statistics unlike- and like-sign distributions while avoiding changes in shapes due to a too coarse binning. The particular configuration choice is supported by the study of different event class discretization levels in Figure 2.19. The ratios of unlike-sign distributions and acceptance correction factors - both characteristic for the mixed-event technique (see Section 2.4.2) - with respect to the respective fine-grained discretization reveal that coarser binnings for Ψ_2 and V_z affect the underlying distributions' shapes at least up to $M_{ee} \sim 1~{\rm GeV/c^2}$. With finer binning the shape effects quickly diminish making the above configuration choice sufficiently accurate within 0.2%. These ob-

servations motivate the use of Ψ_2 as additional dimension in the event class definition which entails the separate reconstruction of the event plane and the event-by-event correction of event flow vectors in Section 2.2.2.

Figure 2.19 M_{ee} -dependent ratios of mixed-event unlike-sign distributions (left column) and acceptance correction factors (right column) for varying configurations of event buffers (top to bottom) at $\sqrt{s_{NN}}=39$ GeV. For each dimension of an event class (Ψ_2 , RefMult, and V_z), different discretization levels (black, red, green, and blue points) are compared to a reasonably fine-grained level to identify potential shape changes induced by event-mixing. The green band indicates 0.2% deviations supporting the choice of $10~\Psi_2$, $10~V_z$, and 9~RefMult bins as sensible event buffer configuration.



On a technical level, the following strategy is pursued to obtain like- and unlike-sign mixedevent distributions. During the (same-)event loop, the current event is appended to an inmemory *event buffer* of size 20 pertaining to the respective event class. When an event buffer at full capacity is encountered, the (same-)event loop is put on halt and the *event-mixing* started using the list of events in the buffer. For each combination of two unequal events A and B in the buffer, the respective particle lists are iterated such that every e^- (e^+) in A is partnered (i) with every e^- (e^+) in B to form like-sign pairs in which case no double counting occurs since the particle lists originate from different events, and (ii) with every e^+ (e^-) in B to form unlike-sign pairs. Once completed, the event buffer is cleared and the (same-)event loop resumed until the next full event buffer is found and the procedure repeated.

An alternative strategy would be to trigger event-mixing during the (same-)event loop every time an event is attributed to the specific buffer. When a full event buffer is encountered, one event is selected randomly and removed to make space for the incoming event. This method would result in more statistics for the same buffer size but the two strategies are not expected to cause significant discrepancies in the mixed-event distributions.

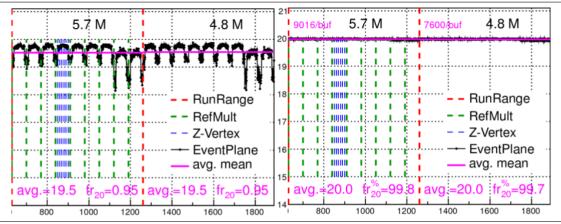
Note that events without any electrons or positrons are also included in the buffers and subsequently the even-mixing. If such empty events were skipped, most event buffers would preferably be filled with more central events which possibly changes the shape of the like- and unlike-sign distributions. Instead of accounting for this effect by applying correction factors on the more peripheral events, the loss in produced statistics is recovered by using an increased buffer size.

For the event buffer configuration chosen here, event-mixing requires that a total of $9\cdot 10\cdot 10\cdot 20=18,000$ events are simultaneously kept in memory. To keep the memory footprint to a minimum, a dedicated event class is used containing only minimal event and track information. Furthermore, storing events for re-usage during event-mixing requires an explicit copy as opposed to a same-event analysis in which the same allocated memory (via TClonesArray) can be used repeatedly for event storage. A custom copy constructor has hence been implemented as part of the dedicated event class which omits the event header and only clones the track arrays of non-zero length when transfering the current event to the event buffer's reusable STL container.

In Section 2.4.2, the resulting mixed-event spectra are normalized to the corresponding same-event distributions and used in the mass region where combinatorial contributions account for the uncorrelated background. Particularly the intermediate mass region of the dielectron spectrum (IMR) requires the large statistics provided by event-mixing to contain the statistical errors to the ones dictated by the unlike-sign foreground.

Finally, an important question to pose is whether all event buffers are sufficiently filled up to their intended size before performing event-mixing. In Figure 2.20, an insufficient configuration for the setup of event buffers and for the partitioning of the full statistics (left) is compared to the optimal case (right). In the scenario on the left, the available event statistics has been processed in parallel by dividing it into smaller sub-samples and attributed to event buffers based on equal-length segments in V_z . This approach evidently causes event-mixing based on "truncated" event buffers observed in the reduced buffer utilization, both overall as 95% of buffers are actually full when event-mixing starts, as well as at both ends of the V_z selection window. These issues are resolved in the scenario on the right, by partitioning the V_z distribution into intervals with approximately equal number of events (see Table 2.3) and by processing the full event statistics sequentially.

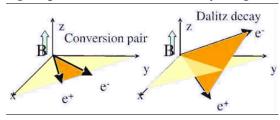
Figure 2.20 Average sizes/utilization of event buffers defined by reference multiplicity (Table 2.2), primary z-vertex (V_z , Table 2.3), and event plane angle ($\Psi_{2,corr}$, Figure 2.11) used during event-mixing. Two setup configurations are compared for the same two RunID ranges (RunRange, Section 7.2): Partitioning of the available statistics and equi-distant V_z binning (left) lead to only partially filled event buffers (horizontal magenta lines) as opposed to purely sequential processing and equi-event-number V_z binning (right). See text for more details.



Based on the like- and unlike-sign pairs extracted from the above same- and mixed-event analyses, six p_T -dependent fore- and background pair invariant mass distributions are generated in M_{ee} and p_T intervals of 1 MeV/ c^2 and 10 MeV/c, respectively. However, before the according histograms can be used as basis for the statistical background subtraction and extraction of raw dielectron signal spectra in Section 2.4.2, a few pair-based selections and corrections need to be applied. First, only pairs with rapidities |y| < 1 are considered. Second, the event class dependent weighting factors which correct the raw reference multiplicity distributions (see Figure 2.6 and accompanying text) for trigger inefficiencies and configuration changes, are applied on a pair-by-pair basis.

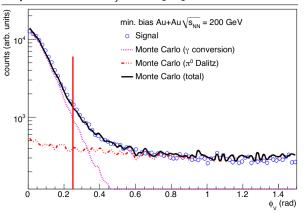
Last, pairs emanating from photon conversions are rejected by reducing the selection for $\rm M_{ee} < 0.2~\rm GeV/c^2$ to pairs with a large enough so-called $\phi_{\rm V}$ angle. Figure 2.21 highlights the different orientations of the e^+e^- decay planes with respect to the magnetic field for background conversion pairs and signal pairs from π^0 Dalitz decays. The bulk of the photons radiating outward from the primary vertex hit the radially symmetric detector material close to the beam axis approximately orthogonally. The created conversion pairs have no intrinsic opening angle causing the

Figure 2.21 Orientation of the dielectron decay plane in a B-field for background pairs from photon conversions (left) and signal pairs from π^0 Dalitz decays (right).



involved electrons and positrons to only be deflected within the azimuthal plane by the magnetic field. Electrons and positrons from π^0 Dalitz decays, however, exhibit a non-zero initial opening angle and hence do not show such a preferred orientation of their decay plane. These distinguishing in- and out-of-plane orientations lie at the heart of the mathematical definition of the ϕ_V angle found in [15]. The study of simulated versus experimental ϕ_V distributions in Figure 2.22 further strengthens the use of ϕ_V as a potential means to separate photon conversions from physical sources.

Figure 2.22 Demonstration of ϕ_V 's capabilities of γ conversion rejection [15]. Details see text.



The sum of the Monte Carlo simulations for photon conversions and π^0 Dalitz decays describes the measured ϕ_V distribution very well. As expected from a proper definition of ϕ_V reflecting the differences in the respective decay plane orientations, the π^0 Dalitz distribution is mostly uniform whereas the γ conversion distribution peaks at zero when consistently ordering the charges of the pair for the ϕ_V calculation. Based on the simulations, PHENIX chose to reject all pairs with $\phi_V < 0.25$ (vertical red line) in Figure 2.22 [15]. In contrast, for the dielectron analyses at top RHIC energy [16], an $M_{\rm ee}$ -dependent ϕ_V selection

criterion has been employed to efficiently reject photon conversions while still maintaining as much signal from the physical sources as possible:

$$\phi_V(M_{\rm ee}) > 0.84326 \exp(-49.4819 M_{\rm ee}) - 0.996609 M_{\rm ee} + 0.19801.$$

In Figure 2.23 (left), the above functional form is obtained from a sample of e^+e^- pairs produced via a photon embedding run through the full STAR reconstruction chain (c.f. Section 3.1). Applying the ϕ_V selection criterion on all like- and unlike-sign pairs in same- and mixed-event analyses rejects more than 98% of photon conversions.

Figure 2.23 Rejection of e⁺e⁻ pairs from photon conversions via ϕ_V at $\sqrt{s_{NN}}=200$ GeV [16]. (left) M_{ee}-dependence of ϕ_V along with the imposed selection functional (black line) based on a photon embedding driven through the full STAR reconstruction chain. (right) Raw dielectron invariant mass signal spectrum up to the ω peak with (red line) and without (black points) conversion rejection. The distribution of the rejected conversion pairs exhibits features characteristic for the radial positions of inner STAR detector material (grey histogram and inlet).

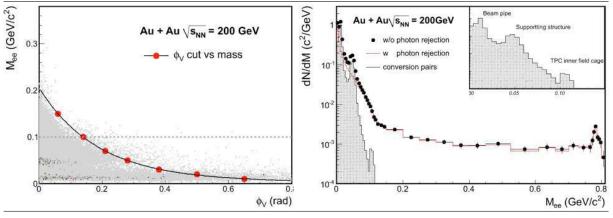


Figure 2.23 (right) depicts the (raw) background-subtracted dielectron invariant mass spectrum at $\sqrt{s_{\rm NN}}$ = 200 GeV from STAR [16] with and without the above $\phi_{\rm V}$ selection applied. Peaklike structures caused by STAR's beam pipe, SVT support cones and inner TPC field cage can be clearly identified in the distribution of the rejected pairs. Their successive appearance with increasing invariant mass is rooted in the tracking algorithm's assumption (and definition) that primary tracks originate from the collision vertex. This introduces an artificial opening angle in the reconstruction of pairs from off-vertex converting photons which increases with the radial distance of the pair's point of origin. For reasons of consistency and simplicity, the analyses of dielectron production at BES energies presented in this thesis, use the same functional form for

the ϕ_V selection as derived at 200 GeV. Significant variations in the ϕ_V selection's photon conversion rejection power are not expected due to its inherent geometric nature. Still, individual ϕ_V selection criteria for the BES energies as well as a study of its possible dependence on the V_z selection are in preparation.

2.4.2 Extraction of raw Signal Spectra

In the following, the background distributions obtained from the same- and mixed-event analyses in Section 2.4.1 are combined, scaled and corrected to construct unlike-sign distributions suitable for subtraction from the foreground. As argued in [15], since electrons and positrons are always created pair-wise in heavy-ion collisions, the unlike-sign background can in general be constructed as the geometric mean of the same- or mixed-event like-sign background distributions regardless of single-particle efficiencies or acceptances: $\langle BG_{+-} \rangle = 2\sqrt{\langle BG_{++} \rangle \langle BG_{--} \rangle}$. The resulting background-subtracted invariant mass (M_{ee}) and transverse momentum (p_T) spectra then contain the dielectron signal steming from physical sources only (c.f. Chapter 4). For the remainder of this section, the subscripts +-, ++, and -- refer to unlike-sign, positive like-sign, and negative like-sign distributions, respectively, whereas SE and ME (ME^N) denote bin contents of the respective same- and (normalized) mixed-event histograms.

Mixed-Event Normalization. As a consequence of the above argument, the unlike-sign mixed-event distributions have to be normalized by scaling their integrated yield ($\sum_{PS} ME_{+-}$, PS: M_{ee} - p_T -space) to the according yield obtained from the geometric mean of the positive and negative like-sign same-event distributions. However, the latter two also contain correlated e^+e^+/e^-e^- pairs which are not accounted for in distributions produced via event-mixing. Hence, the proper yield to use for the normalization factor A_{\pm} is reproduced by the geometric mean of the normalized positive and negative like-sign *mixed-event* distributions:

$$A_{\pm} = 2\sqrt{\left(\sum_{\mathrm{PS}} \mathrm{ME}_{--}^{N}\right)\left(\sum_{\mathrm{PS}} \mathrm{ME}_{++}^{N}\right)} / \sum_{\mathrm{PS}} \mathrm{ME}_{+-}$$

where $ME_{++(--,+-)}^{N} = A_{+(-,\pm)} \cdot ME_{++(--,+-)}$. For the separate calculation of the required positive (A_{+}) and negative (A_{-}) like-sign normalization factors,

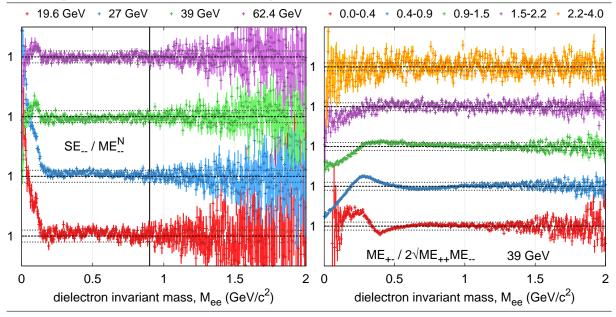
$$A_{+(-)} = \sum_{NR} SE_{++(--)} / \sum_{NR} ME_{++(--)}$$

an adequate normalization region NR is chosen as $M_{\rm ee} > 0.9~{\rm GeV/c^2}$ in Figure 2.24 (left) by comparing same- and mixed-event like-sign spectra and identifying an invariant mass region in which their respective shapes agree well within statistical errors. Table 2.8 lists the normalization factors for all BES energies including their statistical and systematic uncertainties. An estimate for the systematic uncertainties is determined by recalculating the normalization factors with $M_{ee} = 1.3 \text{ GeV/c}^2$ as the lower limit of the normalization region and subtracting the result from the values at $M_{ee} = 0.9 \text{ GeV}/c^2$. Both, statistical and systematic uncertainties on the normalization factors are separately propagated to the final efficiency-corrected spectra presented in Chapter 5. The total relative uncertainties on A_{\pm} are also quoted in Table 2.8 which can contribute substantially to the final spectra uncertainties in invariant mass regions with the lowest signal-to-background ratios. In the BES dielectron analyses, these can be as low $\sim \! 1/200$ requiring relative errors on the mixed-event normalizations of less than 0.5% to avoid 100% uncertainties on the data points in the final spectra. All BES energies analyzed here achieve an uncertainty level of about 0.5% or less. Finally note that calculating normalization factors for the mixed-event distributions in each p_T interval individually would only introduce larger statistical errors and hence complicate the identification of adequate normalization regions.

Table 2.8: Normalization factors calculated at all BES energies for positive/negative like- and unlike-sign mixed-event distributions relative to their same-event counterparts (see text). The numbers given in parenthesis are statistical and systematic uncertainties on the last digits, respectively. Also listed are the total relative errors on A_{\pm} which folded with the signal-to-background ratio directly give the uncertainty on the signal spectra caused by mixed-event normalization.

	19.6 GeV	27 GeV	39 GeV	62.4 GeV
A_{-}	0.026629(29)(266)	0.026533(18)(139)	0.026780(18)(56)	0.026714(20)(142)
A_{+}	0.026635(28)(23)	0.026549(18)(136)	0.026859(18)(253)	0.026737(20)(10)
A_\pm	0.026668(21)(134)	0.026554(13)(97)	0.026816(13)(129)	0.026726(14)(71)
$\Delta\!A_{\pm}^{ m tot}$	0.51%	0.37%	0.48%	0.27%

Figure 2.24 (left) Identification of mixed-event normalization range $M_{ee} > 0.9 \text{ GeV/c}^2$ (vertical line) using the negative like-sign SE/ME^N ratios. (right) p_T -dependence of acceptance correction factor at $\sqrt{s_{NN}} = 39 \text{ GeV}$. Dotted lines denote a $\pm 2\%$ envelope. All graphs for the like-sign ratios and acceptance factors are collected in Figure A.13.



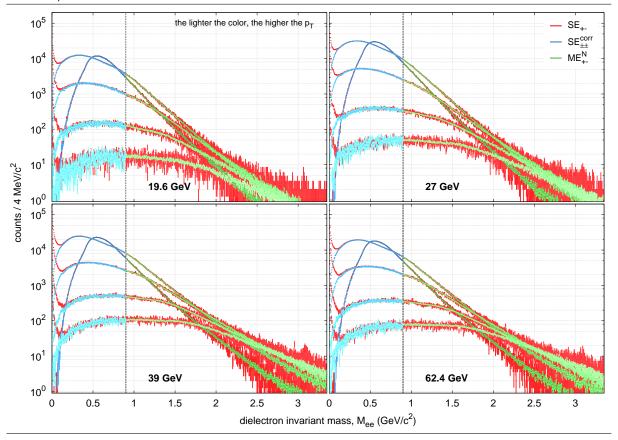
Same-Event Acceptance Correction. Below the normalization region identified in Figure 2.24 (left), correlated pairs play a role in the shape of the same-event like- and unlike-sign distributions. Therefore, the same-event like-sign distribution $SE_{\pm\pm} = 2\sqrt{SE_{++}SE_{--}}$ needs to be subtracted from the foreground instead of the normalized unlike-sign mixed-event distribution ME_{+-}^N to correctly extract the dielectron signal. The like-sign pairs generating the $SE_{\pm\pm}$ distribution, however, are exposed to different acceptance losses than the unlike-sign pairs of the foreground. The effect can be accounted for by bin-wise applying the acceptance correction factor f_{acc} deduced from the according mixed-event distributions on the $SE_{\pm\pm}$ distribution:

$$SE_{\pm\pm}^{corr} = SE_{\pm\pm} \cdot f_{acc} = SE_{\pm\pm} \cdot ME_{+-} / 2\sqrt{ME_{++}ME_{--}}.$$

To avoid subtraction artefacts due to limited statistics at high invariant masses, the arithmetic instead of the geometric mean is used in the calculation of $SE_{\pm\pm}^{corr}$ for invariant mass bins with zero bin content in any of the involved like-sign same-event or mixed-event distributions. The acceptance correction factors (Figure 2.24 right) are applied and $SE_{\pm\pm}^{corr}$ calculated using the p_T

intervals 0.-0.4, 0.4-0.9, 0.9-1.5, 1.5-2.2, and 2.2-4 GeV/c which coincide with the p_T edges employed in the determination of pair efficiencies (c.f. Figure 3.12). The lowest transverse momentum bin requires special attention since it is significantly impacted by STAR's acceptance hole for single track transverse momenta below 0.2 GeV/c. For the current version of the efficiency-corrected dielectron p_T -spectra in Figure 5.6, the data point for the lowest p_T interval is thus omitted but yet shown for completeness as part of the raw data presented in this section.

Figure 2.25 p_T-dependent invariant mass distributions at all BES energies used to generate dielectron signal spectra via subtraction: the unlike-sign foreground (red) as well as the two backgrounds of acceptance-corrected like-sign same-event (blue) and normalized unlike-sign mixed-event (green). The lighter the respective colors, the higher the pair transverse momentum corresponding to the p_T intervals 0.-0.4, 0.4-0.9, 0.9-1.5, 1.5-2.2, and 2.2-4 GeV/c. The vertical dashed lines indicate the transition from same- to mixed-event background subtraction at 0.9 GeV/ c^2 .



Background Subtraction and Dielectron Signal. Figure 2.25 shows all resulting invariant mass distributions for the unlike-sign foreground along with the corresponding background which are used to generate dielectron signal spectra $\mathscr S$ in the different p_T intervals separately:

$$\mathcal{S} = \begin{cases} \text{SE}_{+-} - \text{SE}_{\pm\pm}^{\text{corr}} & \text{if } M_{ee} \le 0.9 \,\text{GeV}/c^2 \\ \text{SE}_{+-} - \text{ME}_{+-}^{\text{N}} & \text{if } M_{ee} > 0.9 \,\text{GeV}/c^2 \end{cases}$$

The subtraction is based on the original distributions' 4 MeV/c^2 invariant mass binning. In this representation, the raw dielectron signal also contains negative entries due to statistical fluctuations in fore- and background. A better representation of the signal spectra thus needs to be found in form of a variable (invariant mass dependent) binning which widens the bin widths enough to reduce statistical errors but still catches the important resonance as well as continuum features of the distributions. In Figure 2.26, the invariant mass spectra from the

 p_T -integrated analyses at all BES energies, i.e. constructed based on p_T -integrated background generation and subtraction, are used to establish a variable binning suited to the available statistics at each individual energy. For this purpose, an automated rebinning algorithm is employed with the following strategy.

- Start with the bin at the upper invariant mass limit.
- Sum up bin contents until a positive number of entries is aggregated, and
- the relative statistical error is smaller than a given mass-range-dependent limit, and
- (optionally) a minimum, also mass-range-dependent bin width is reached.
- When all criteria are satisfied, define the covered invariant mass range as bin for the rebinned distribution, reset the bin entries counter, and reiterate.

This strategy makes the prolonged trial-and-error approach of manually finding a suitable variable binning obsolete. It is replaced by an algorithm-based approach which is easily controllable via a small set of parameters, i.e. a handful of statistical error limits per beam energy. Such a reproducible and dynamic environment for the rebinning of dielectron signal spectra is especially important when analyzing dielectron production at multiple beam energies. The optimized bin definitions of Figure 2.26 are subsequently applied to the signal spectra obtained via the above subtraction method from the p_T -differential analyses in Figure 2.25.

These p_T -dependent rebinned invariant mass spectra form the basis for all physics results discussed in Chapter 5: The pair efficiencies of Figure 3.12 are applied in dependence of M_{ee} and p_T on the differential spectra which are subsequently summed up to arrive at the efficiency-corrected and p_T -integrated dielectron invariant mass spectra shown in Figure 5.1 and Figure 5.2. As can be seen in Figure 2.27, the statistics in the signal spectra yields pronounced resonance peaks for ω , ϕ , and J/Ψ but is not sufficient for fully differential M_{ee} - and p_T -dependent analyses. The invariant mass distributions in the different p_T intervals are hence separately integrated over the characteristic mass regions to obtain the efficiency-corrected dielectron p_T -spectra depicted in Figure 5.6.

Figure 2.26 Rebinning of raw signal spectra from p_T -integrated analyses at all BES energies. Only the mass region where actual rebinning takes place is shown ($M_{ee} > 0.1~\text{GeV/c}^2$). All distributions are divided by the measured number of minimum bias events listed in Table 2.1. Grey and black error bars denote statistical errors and bin widths for signal distributions with equi-width and variable binning, respectively. Systematic uncertainties on the rebinned signal caused by the uncertainty in mixed-event normalization (Table 2.8) are also included (red error bars). Note that the lower half of each energy contains the negative entries on a reversed logarithmic scale which are part of the background-subtracted raw signal distribution and hence have to be taken into account during the automated rebinning procedure. The vertical dashed line indicates the invariant mass of 0.9 GeV/ c^2 at which same-event- is replaced by mixed-event-based background subtraction.

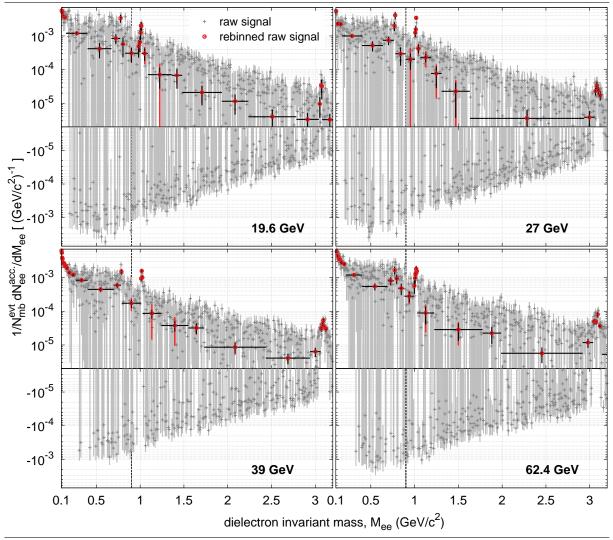
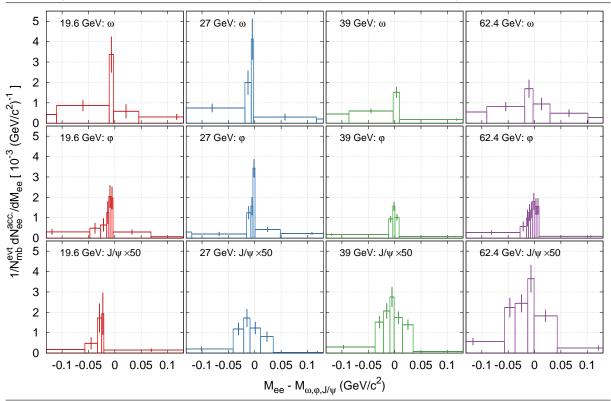


Figure 2.27 Total raw dielectron invariant mass spectra for all BES energies after p_T -differential rebinning and summation concentrating on the ω , ϕ , and J/ψ mass regions on a linear scale.



Chapter 3

Efficiency Correction

For the comparison to theoretical calculations and amongst energies (Chapter 5) the raw dielectron invariant mass and p_T distributions resulting from the data analysis in Chapter 2 have to be corrected for losses caused by detector inefficiencies and by analysis selection cuts (c.f. Table 2.1). For this purpose, simulated tracks are embedded into real events and tracked through the detector using the same tools as for real data event reconstruction (Section 3.1). The estimation of systematic uncertainties requires the comparison of simulated to clean experimental distributions of suitable particle samples as also described in Section 3.1. Section 3.2 follows the analysis procedure of Chapter 2 to calculate total single track efficiencies using the particle samples from embedding and experiment. Finally in Section 3.3, the single track efficiencies are propagated into pair efficiencies using a simple two-body Monte-Carlo simulation.

3.1 Particle Samples

The procedure employed in Section 3.2 to obtain total single track efficiencies is mostly based on electron and positron samples generated through the *embedding* technique. 5% of the collision's multiplicity is included within a measured Au+Au event as simulated tracks with known kinematics and of known type. The percentage of embedded tracks is chosen such that the additional multiplicity does not change the real event's centrality class. Generation of events with the appropriate simulated multiplicity is achieved by means of the software package GSTAR [180] which extends GEANT [181, 182] with STAR-specific geometry definitions of detailed detector material information. It also provides a plugin-like framework for the development of external software modules to read event generator output and define signals (hits) induced by particles traversing the sensitive detector elements. In the case of the TPC, for instance, GSTAR produces electron clusters along the charged particle tracks provided by GEANT's event generator. The clusters are used by the dedicated tss plugin library to realistically simulate their transport and diffusion in the drift field to the TPC's wire plane followed by electron avalanche, spread over read-out pads, and pixel-by-pixel digitization to ADC counts [183]. The resulting output of this TPC response simulation is subsequently propagated through the TPC cluster/hit finder of STAR's standard event reconstruction software [160] which also includes, amongst others, track and vertex reconstruction, and provides the usual data summary files (DSTs) for further physics analysis. See Section 2.2 for details on this first analysis stage of event reconstruction from raw detector data. As a result, the embedding procedure allows for the determination of single track efficiencies by calculating the fraction of simulated tracks still available at different stages of the dielectron analysis chain (Chapter 2).

Embedding has been established as a request based STAR-wide procedure with dedicated teams incorporated in the organizational structure [184]. Table 3.1 hence summarizes general information on the charge-separated embedding requests needed to access the simulation results for the minimum-bias dielectron analyses at BES-I energies and analyzed in Section 3.2.

All single-electron embedding requests have the uniform simulation of rapidity $y \in (-1.2, 1.2)$ and azimuthal angle $\varphi \in (0, 2\pi)$ in common. All of them use a subset of events ensured to cover the entire beam time.

Table 3.1: STAR e⁺/e⁻ embedding requests for dielectron analyses at BES-I energies [184] with *MC* and *Matched* the total number of tracks simulated and reconstructed, respectively. FSET denotes a STAR-internal suffix for the set of simulation output files used for analysis in Section 3.2.

$\sqrt{s_{ m NN}}$	Events	MC	Matched	FSETs	Id(s)	$ V_z ^{\max}$	p_T	STAR
(GeV)	(10^3)	(10^6)	(10^6)	F3E1S	(20)	(cm)	(GeV/c)	Library
19.6	217	1.43	0.80	200-204	121203/4	70	0.2-5	P11id
27	228	1.59	0.94	200-204	123601/2	50	0.2-4	P11id
39	141	1.03	0.60	200-201	113301	50	<2	SL10d
62.4	103	0.82	0.45	200-202	12401	50	<2	SL10k

To ascertain the quality of simulated particle samples in general, track quality and global distance-of-closest-approach (DCA) distributions, for instance, are compared for tracks from embedding and from experiment (Section 3.2.1). Hence, sufficiently pure e^+/e^- and π^+/π^- samples need to be generated from measured quantities provided by the TPC alone since TOF hits not only impose a certain track quality but also restrict the sample to tracks originating from and using helixes re-fitted to the primary vertex. Both would distort the according distributions rendering them unsuitable for the use in quality assurance (QA). In STAR and unlike pions, however, the satisfactory identification of rarely produced leptons requires the measurement of their time-of-flights to achieve a small level of hadronic contamination in the particle sample (see Section 2.3). This fundamentally distinguishes the embedding QA of electron and positron tracks from the rather standard one of hadrons. Suitable high-statistics experimental samples for pions, on the one hand, can simply be obtained by requiring minimal track qualities of nHitsFit > 14 and nHitsFit/nHitsPoss > 0.52 for primary tracks with $|n\sigma_{\pi}| < 0.2$. Minimal track quality and the track's energy loss in the TPC alone, on the other hand, only allows for the selection of e^+/e^- candidates via $|n\sigma_{e}| < 2$.

One way to obtain clean experimental e^+/e^- samples is by combining the unlike-sign candidates into dielectrons and employing pair-based cuts to reduce them to the ones originating from Dalitz decays or photon conversions. The procedure for the electron (positron) sample starts by requiring the electron (positron) to be associated with a primary track which is then paired with all global positron (electron) candidates. The physical helices (StPhysicalHel ixD) of both partner tracks are constructed with the respective global momenta and used in a minimization algorithm (StHelix::pathLengths()) to determine the pair's DCA (dcaee). The secondary decay vertex is defined midway between the partner helices' closest points of approach. After rejecting pair combinations with $dca_{ee} > 1$ cm (Figure 3.1 upper left) the partners' 4-momenta are calculated at the secondary decay vertex based on the global helices to obtain the correct "global-global" dielectron invariant mass Mgg. Dielectrons from physical sources (Dalitz decay or photon conversion in this context) appear as a peak structure at very low invariant masses and are separated from pairs of purely combinatorial origin via $M_{gg} < 4$ MeV/c^2 (Figure 3.1 lower left). The perpendicular decay length L_{xy} denotes the distance of secondary to primary vertex in the x-y-plane and can subsequently be used to identify dielectrons mostly from photon conversion in the detector material (3.8 < L_{xv} < 6.1 cm) and mostly from Dalitz decays (L_{xy} < 2 cm), see Figure 3.1 upper right. An improved selection of electrons and positrons attributed to either Dalitz decays or photon conversions can be achieved using the "primary-global" dielectron invariant mass M_{pg} . As indicated by the overall M_{pg} distribution in Figure 3.1 (lower right) most of the dielectrons originating from Dalitz decays exhibit invariant masses M_{pg} < 2.9 MeV/ c^2 whereas most of the dielectrons caused by photon conversion appear in $3.0 < M_{pg} < 7.0 \, \text{MeV/c}^2$. This appreciable separation is due to the invariant mass shift induced on primary tracks that in fact emanate from off-event-vertex decays like photon conversion. The M_{pg} 's distinction power, however, is less than optimal to justify a further decrease in statistics for the already challengingly small final particle sample. Electrons and positrons from both sources are hence combined into the respective final samples used in Section 3.2. As soon as a primary positron (electron) in the e^+e^- (e^-e^+) candidate combinations survives the preceding selection criteria for photon conversion or Dalitz decay it is attributed to the final experimental positron (electron) sample.

Figure 3.2 shows the electron sample's distribution of TPC $n\sigma_e$ versus its primary momentum. It illustrates the procedure's power to reduce the candidates sample contaminated by pions, kaons and protons to the final (almost) pure e^+/e^- sample.

Figure 3.1 Overview of the strategy employed to generate pure electron/positron samples from experimental data at 19.6 GeV chosen as representative for all BES-I energies. Grey areas denote the part of the respective spectrum selected to generate the distribution for the next criterion in the procedure (directions: top-bottom \rightarrow left-right). The last panel also includes separate contributions based on the selection intervals for Dalitz decays and photon conversions in the perpendicular decay length distribution. See text for details on the selection criteria and associated variable names.

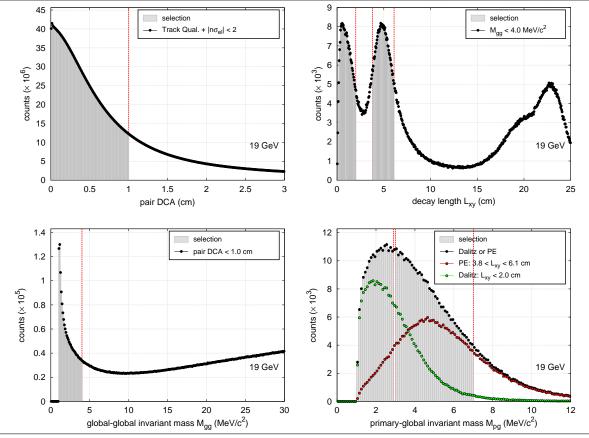
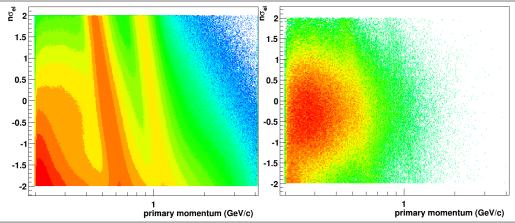


Figure 3.2 TPC energy loss distribution versus primary momentum for the electron/positron candidates (left) and the final sample (right). In the candidates sample, the leptons' distribution around zero is hidden beneath hadron contaminations by pions, kaons and protons (narrow bands in increasing momentum). Note that the latter (almost) vanish in the final particle sample.



In addition to their importance in the QA of embedding samples, the final experimental e^+/e^- samples are used to derive the dominant systematic uncertainties by comparison of simulated and measured track quality as well as global DCA distributions. Since a slow simulator for the newly installed TOF detector as plugin to GSTAR has not been available during the time frame of this thesis, the final experimental e^+/e^- samples also serve to calculate TOF matching efficiencies. Moreover, due to its abundant statistics, the pion samples play a crucial role in the determination of TOF matching efficiencies (Section 3.2.2).

3.2 Single-Track Efficiencies

In the following subsections, the particle samples produced in Section 3.1 are used to determine detector- and analysis-related efficiencies step by step and separately in particle charges. In general, the calculations follow the raw data analysis procedure of Chapter 2 and the according selection criteria listed in Table 2.1. The experimental as well as simulated particle samples are first reduced to tracks abiding the criteria for event vertex and minimum reference multiplicity at the respective energy. For the embedding samples, however, special attention has to be paid to the removal of electrons and positrons (i) emanating from photon conversions in the detector material (Parent Geant Id=0), and (ii) sharing a minimum number of common TPC hits between simulated and associated reconstructed tracks (NCommonHit>=10). Separate histograms for the latter two are subsequently filled and divided at each step of the analysis chain starting at an appropriate initial binning in transverse momentum p_T , pseudo-rapidity η , and azimuthal angle ϕ . The total single track efficiencies $\varepsilon_{\text{total}}^{\text{track}}$ (Equation 3.1) can then be obtained through the product of contributions due to detector inefficiencies (ε_{det}), minimum track quality requirements ($\varepsilon_{\text{qual}}$), cuts on the global DCA ($\varepsilon_{\text{glDCA}}$), and track matching to hits in the TOF detector ($\varepsilon_{\text{match}}^{\text{TOF}}$), as well as TOF ($\varepsilon_{\text{select}}^{\text{TOF}}$) and TPC ($\varepsilon_{\text{select}}^{\text{TPC}}$) selection. The dependencies on p_T , η , ϕ , and momentum p indicate the kinematic variables used to determine and propagate the efficiencies for each of the contributions. Note that the TOF selection efficiency has been tuned versus particle momentum in Section 2.3 to a constant value of 3σ . Also shown in Equation 3.1 are the forms and dependencies of the systematic uncertainties $\Delta \varepsilon_{\rm syst}$ for the dominating contributions that are taken into account in the determination of total systematic uncertainties on the single track efficiencies. Losses and systematic uncertainties due to detector inefficiencies as well as track quality and global DCA cuts are covered in Section 3.2.1, whereas the ones due to TOF Matching and TPC Selection are addressed in Section 3.2.2 and Section 3.2.3, respectively. Section 3.2.4 summarizes the resulting total single track efficiencies for electrons and positrons including the propagated systematic uncertainties. The full set of efficiencies and uncertainties are tabularized in Section A.8. For reasons of clarity and conciseness, most of the figures in the following subsections use electrons at $\sqrt{s_{\rm NN}}$ = 39 GeV as representative examples for all energies and particles with supporting figures included in Section A.9.

Equation 3.1 Calculation of total single track efficiencies and according systematic uncertainties.

$$\varepsilon_{\text{total}}^{\text{track}}(p_T, \eta, \varphi) = \varepsilon_{\text{det}}(p_T, \eta, \varphi) \times \underbrace{\varepsilon_{\text{qual}}(p_T, \eta, \varphi) \times \varepsilon_{\text{glDCA}}(p_T)}_{\Delta \varepsilon_{\text{syst}}/\varepsilon(p_T)} \times \underbrace{\varepsilon_{\text{match}}^{\text{TOF}}(p_T, \eta, \varphi)}_{\Delta \varepsilon_{\text{syst}}(\eta, \varphi)} \times \underbrace{\varepsilon_{\text{select}}^{\text{TOF}}}_{=0.9973} \times \underbrace{\varepsilon_{\text{select}}^{\text{TPC}}(p_T)}_{\Delta \varepsilon_{\text{syst}}(p_T)}$$

3.2.1 Detector, Track Quality and Global DCA

As explained in Section 3.1, the embedding procedure already emulates the simulation of the detector's response such that the detector efficiency $\varepsilon_{\rm det}$ within STAR acceptance can be calculated as the ratio of the number of reconstructed over the number of simulated tracks in a chosen $p_T/\eta/\phi$ interval (bin). The fractions $\varepsilon_{\rm fit}$ and $\varepsilon_{\rm dedx}$ of tracks that satisfy the minimum track quality requirements in Table 2.1 for nHitsFit and nHitsdEdx, respectively, are then based on the selection of simulated tracks remaining after losses due to the detector response. The resulting p_T dependencies of detector and track quality efficiencies are depicted in Figure 3.3 for electrons in an examplatory η/ϕ window at $\sqrt{s_{\rm NN}}$ = 39 GeV. The ϕ -interval $\Delta\phi$ = 15° is chosen according to the detector's sector-wise segmentation and compared to $\Delta \phi = 5^{\circ}$. The p_T -dependency's shape varies considerably with the narrower azimuthal binning but at the same time suffers enlarged statistical errors. Similar behavior can be observed when comparing different choices of η -intervals albeit to much lesser extent. The two effects compete when aiming for a better handle on the efficiencies' differential shapes, on the one hand, as opposed to avoiding sizeable statistical fluctuations dictated by the limitations of the embedding sample, on the other hand. The related variations, however, should not be propagated as part of the systematic uncertainties. Instead, one needs to arrive at a conscious decision on a binning in p_T , η , and ϕ capable of reproducing the predominant features of the efficiencies' integrated p_T -, η , and ϕ dependencies.

Figure 3.3 e^- efficiency comparisons at $\sqrt{s_{\rm NN}}=39$ GeV for detector response and minimum track quality requirements in $0<\eta<0.25$ and $45^\circ<\phi<60^\circ$ for $\Delta\phi=15^\circ$ (lines & points) versus 5° (lines only). Solid lines show the p_T -dependence for $\Delta p_T=0.2$ GeV/c and dashed lines the p_T -integrated efficiencies for the respective $\Delta\phi$. All combined efficiencies for $\Delta\phi=15^\circ$ are listed in Table A.2.

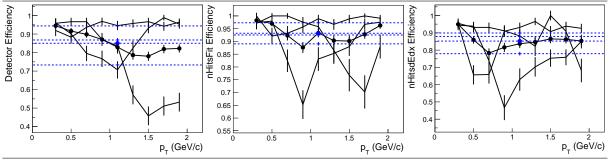
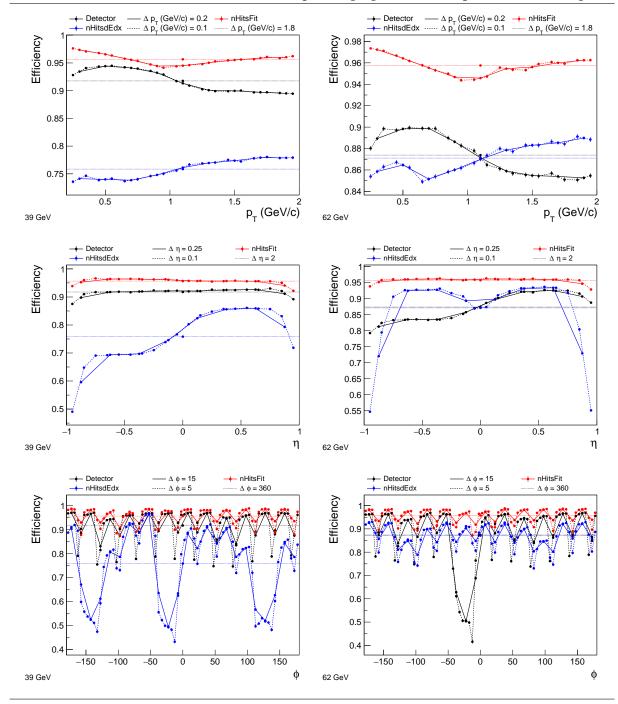


Figure 3.4 Overview of calculated electron efficiencies at $\sqrt{s_{\rm NN}} = 39$ GeV (left column) and 62.4 GeV (right column) separately for detector response (black) as well as minimum track quality requirements for nHitsFit (red) and nHitsdEdx (blue) by means of their respective p_T -, η -, and ϕ -dependencies (top to bottom). For each of the kinematic variables and analysis steps, the dependencies are compared to the fully integrated values (dotted, Table 3.2) and to two different suitable choices in binning (dashed/solid lines): $\Delta p_T = 0.1/0.2$ GeV/c, $\Delta \eta = 0.1/0.25$, and $\Delta \phi = 5/15^\circ$. See Section A.9 for the corresponding figures of other particles and energies.



For this purpose, two reasonable interval choices for the kinematic variables p_T , η , and ϕ are compared in Figure 3.4 for the according dependencies of detector and track quality efficiencies at $\sqrt{s_{\rm NN}}$ = 39 & 62.4 GeV. In comparison to their narrower counterparts, it turns out that the wider choices of Δp_T = 0.2 GeV/c, $\Delta \eta$ = 0.25, and $\Delta \phi$ = 15° still sufficiently account not only for the efficiencies' comparably smooth dependence on p_T but also for their more prominent

features in η and ϕ . This includes the differences in positive and negative pseudo-rapidities and, in particular, the azimuthal structures reflecting the lower efficiencies at sector borders and the overall reduced efficiencies in the less performing sectors. Figure 3.4 also serves the purpose of giving an overview comparison across energies allowing for a better understanding of the detector's performance during the respective beam times and possibly revealing issues characteristic to a specific energy. For instance, the number of missing or mal-functioning TPC read-out boards (bad RDOs) varies considerably during a run and especially over the time period in which the BES-I data has been taken (\sim two years). The reduced efficiencies for some of the sectors visible in the ϕ -dependencies (c.f. additional figures in Section A.9) can be correlated with the number of bad RDOs in different RunID ranges of an energy run. For details, the reader is referred to the specially developed STAR software module StBadRdosDb in Section 7.2 providing the required databases (Section B.2) and interface utilities. The higher number of bad RDOs during the runs in 2010 as compared to 2011 also explains the lower fully integrated efficiencies for 39 and 62.4 GeV versus 19.6 and 27 GeV in Table 3.2.

Table 3.2: Integrated detector (ε_{det}), nHitsFit (ε_{fit}), and nHitsdEdx (ε_{dedx}) efficiencies.

19.6 GeV		27 GeV		39 GeV		62.4 GeV					
$arepsilon_{ m det}$	$arepsilon_{ m fit}$ 95%	$arepsilon_{ m dedx}$ 91%	$arepsilon_{ m det}$ 92%	$arepsilon_{ m fit}$	$arepsilon_{ m dedx}$ 91%	$arepsilon_{ m det}$ 92%	$arepsilon_{ m fit}$ 96%	$arepsilon_{ m dedx}$	$arepsilon_{ m det}$	$arepsilon_{ m fit}$ 96%	$arepsilon_{ m dedx}$ 87%

A *side note* on the statistical error bars used in Figure 3.3 and later in Figure 3.7: Since $\hat{\epsilon} = k/n$ intuitively provides a good estimator for the (unknown) true efficiency, calculations of the latter boil down to the division of two histogram bin contents k and n in the same $p_T/\eta/\phi$ -interval with k (out of n) the number of tracks passing the selection criterion. It proves more difficult, however, to assign the correct statistical uncertainties on the calculated efficiencies. As discussed in [185], using poisson or binomial distributions to derive the mean efficiency $\bar{\epsilon}$ and its variance σ_{ϵ}^2 either falsely assumes non-correlated k and n or results in unphysical zero values for the border cases k=0 or k=n. The correct probability density function derived in [185], on the other hand, not only exhibits a most probable value of $\hat{\epsilon}$ but also dismisses the ill-behaving variances in favor of

$$\sigma_{\varepsilon} = \sqrt{\frac{(k+1)(k+2)}{(n+2)(n+3)} - \left(\frac{k+1}{n+2}\right)^2}$$

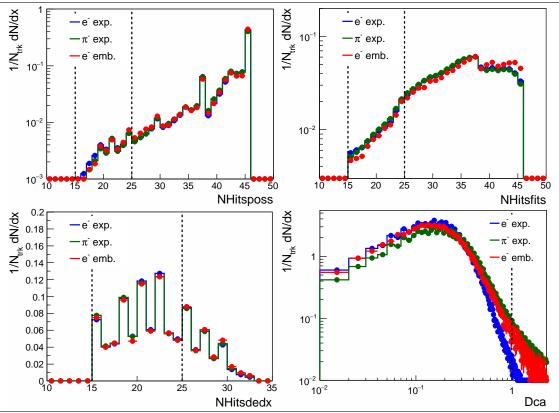
which yields physical non-zero values in the extreme cases for *k*.

For reasons of quality assurance, Figure 3.5 compares track quality and global DCA distributions produced via embedding to distributions obtained from the experimental particle samples. All distributions generally show good agreement between the simulated and measured data creating confidence in the quality of the embedding samples. The level of agreement in the <code>nHitsdEdx</code> distributions, in particular, is worth highlighting since it only recently emerged from a STAR-internal effort to improve the simulation of a particle's energy loss in the TPC during the embedding procedure. As a consequence, <code>nHitsdEdx</code> efficiencies can now confidently be derived from simulated distributions instead of, as previously, relying on the experimental ones.

In the case of global DCA, the according embedding distributions in Figure 3.5 also serve to derive p_T -dependent efficiencies for the restriction of the particle samples to tracks with global DCAs (glDCA) of less than 1 cm. The electrons and positrons from physical sources sought after in this thesis emanate from the primary vertex which is why the data analysis (Chapter 2) and the detector efficiencies (Figure 3.3 and Table A.2) are based on primary instead of global tracks. However, only tracks with glDCA < 3 cm are tagged as primary and associated with

the global partner. Given the glDCA distribution's shape, the bulk of the tracks appears within the glDCA < 1 cm criterion resulting in $\varepsilon_{\text{glDCA}}$ close to 1.

Figure 3.5 Comparison of track quality (nHitsPoss, nHitsFit, nHitsdEdx) and global DCA distributions for electrons from embedding (red) as well as electrons (blue) and π^- (green) from experimental data at $\sqrt{s_{NN}} = 39$ GeV for $0.5 < p_T < 0.8$ GeV/c. Vertical dashed lines denote selection criteria used in the determination of relative systematic uncertainties on the combined track quality and global DCA efficiencies (see text following this figure).



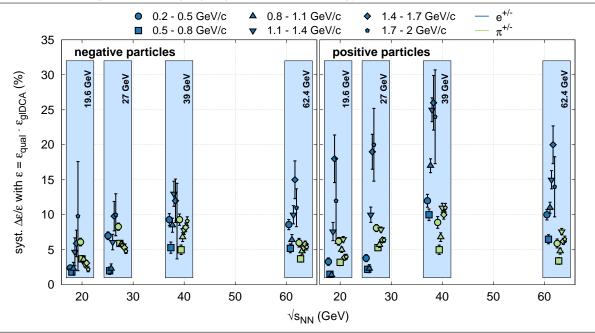
Relative systematic uncertainties on the combined track quality and global DCA efficiencies can be estimated by quantifying how well each of the embedding distributions reproduces the efficiencies calculated from the according experimental distribution. Note that, for reasons of simplification during the raw data analysis, the latter have been produced using the same minimum track quality requirements as chosen in the data analysis (see Table 2.1) which also conincide with the lowest values recommended by STAR to define a good track. Hence, for the determination of systematic uncertainties on track quality efficiencies, an alternate minimum requirement of nHitsPoss/Fit/dEdx > 24 is employed (c.f. vertical lines in Figure 3.5). For each of the distributions, the respective selection criteria are then used to calculate the relative efficiencies difference

$$\Delta oldsymbol{arepsilon}_{ ext{syst}}^{ ext{rel}} = rac{|oldsymbol{arepsilon}_{ ext{exp}} - oldsymbol{arepsilon}_{ ext{emb}}|}{oldsymbol{arepsilon}_{ ext{emb}}}$$

with $\varepsilon_{\rm exp}$ and $\varepsilon_{\rm emb}$ the efficiencies deduced from the experimental and embedding distributions, respectively. The resulting $\Delta\varepsilon_{\rm syst}^{\rm rel}$ for each of the track quality and global DCA distributions are propagated quadratically to obtain the total relative uncertainties compiled in Figure 3.6. For all particles and at all energies, the p_T -interval 0.5 - 0.8 GeV/c exhibits the smallest uncertainties and hence best overall agreement in the underlying distributions. At the energies 19.6 and 27 GeV, the uncertainties for electrons and positrons in this momentum bin are about 2% and well below the ones derived from the comparison to pion distributions. At 39 and 62.4 GeV, however, these uncertainties range around 5% roughly in agreement with the pions except

for a 10% uncertainty for positrons at 39 GeV. The trend of higher systematic uncertainties at 39 and 62.4 GeV with respect to 19.6 and 27 GeV is possibly caused by mis-matching nHitsdEdx distributions due to the larger number of (RunID ranges with) bad RDOs (Section 7.2 and Section B.2), especially at 39 GeV. For most energies and particles, one observes systematically larger uncertainties in the lowest and the higher p_T -intervals which can probably be attributed, respectively, to the residual pion and kaon/proton contaminations in the experimental samples (Figure 3.2). The combined relative systematic uncertainties on track quality and global DCA efficiencies are propagated in Section 3.2.4 along with the systematic uncertainties of TOF matching (Section 3.2.2) and TPC selection (Section 3.2.3) efficiencies.

Figure 3.6 $\sqrt{s_{NN}}$ and p_T -dependence of total relative systematic uncertainties on track quality and global DCA efficiencies obtained through the comparison of electrons/positrons from embedding to electrons/positrons (blue symbols) and pions (green symbols) from experimental data, c.f. Figure 3.5. The p_T -dependence is based on intervals Δp_T of 0.3 GeV/c between 0.2 - 2 GeV/c. The data points are slightly shifted against each other for better visibility and blue boxes frame the points belonging together at each energy.

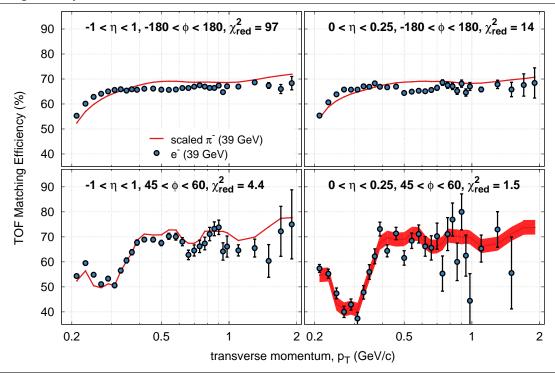


3.2.2 TOF Matching

The measurement of a particle's velocity β via the TOF detector in addition to its momentum and energy loss in the TPC is crucial for the successful identification of rare electrons and positrons (Section 2.3). Tracks measured in the TPC are therefore matched to TOF detector hits during the first phase of the event reconstruction analysis chain (Section 2.2). The according matching efficiencies are determined by the selection criteria $\beta > 0$ and |yLocal| < 1.8 cm (Table 2.1), and based on the sample of tracks remaining after detector response, track quality requirements and global DCA cuts (c.f. Equation 3.1). Two major issues complicate the derivation of TOF matching efficiencies: (i) a slow simulator of the TOF's response for the use in GSTAR has not been available as of this writing, and (ii) the experimental electron and positron samples generated in Section 3.1 do not provide sufficient statistics to calculate efficiencies in a narrow enough $p_T/\eta/\phi$ binning without being dominated by statistical errors. Dependence on $p_T/\eta/\phi$ during the determination of efficiencies, however, is imperative since the differential efficiency shapes vary significantly for different kinematic regions. A possible solution is to properly scale the TOF matching efficiencies derived from pion samples to the ones from

electrons/positrons given that their shape is satisfactorily reproduced. Figure 3.7 explores this solution by comparing p_T -dependent electron to π^- TOF matching efficiences for the different scenarios from η/ϕ -integrated to η/ϕ -differential. For each scenario of η/ϕ -interval choices the pion efficiencies (red lines) are independently scaled to the respective electron efficiencies (blue symbols) using their p_T -averaged ratio as scaling factor.

Figure 3.7 p_T -dependent comparison of TOF matching efficiencies for electrons (blue symbols) and scaled π^- (red lines) at $\sqrt{s_{\rm NN}}=39$ GeV using combinations of the interval choices $\Delta\eta=2$ & 0.25, and $\Delta\phi=15^\circ$ & 360°. The reduced χ^2 is a measure for the goodness-of-fit between electrons and pions. The band around the pion efficiencies in the fully differential scenario indicates p_T -averaged systematic uncertainties. Details see text. All TOF matching efficiencies finally utilized in the efficiency correction are listed in Table A.3 and Table A.4 for $\eta<0$ and $\eta>0$, respectively.

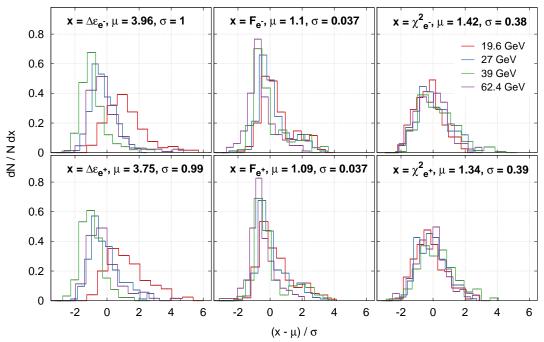


The level of agreement between p_T -dependent electron and pion efficiencies can be quantified using the reduced χ^2 as a measure for the "goodness-of-fit". As for its usual parameterization via χ^2 minimization, a value around one indicates a good description of the data (electron efficiencies) by the model (scaled pion efficiencies) taking into account the statistical errors on the data. The reduced χ^2 values calculated for the different scenarios in Figure 3.7 support the visual impression that electron efficiencies can only be reproduced well by the pion efficiencies in the fully differential case ($\Delta \eta = 0.25$, $\Delta \phi = 15^{\circ}$) and not when integrating over one or both of the kinematic variables η and ϕ . The reproducibility in shape also allows for the p_T -averaged absolute deviation of electron from scaled pion efficiencies to be taken as estimate for the systematic uncertainty in the respective η/ϕ -interval (red band in Figure 3.7).

To further scrutinize the validity of the procedure, Figure 3.8 shows normalized distributions of the factors F involved in the scaling of pion efficiencies as well as of the reduced χ^2 goodness-of-fit parameters and the resulting systematic uncertainties on the TOF matching efficiencies. For better comparison and clarity, all distributions are shifted and scaled by the energy-averaged gaussian means and widths to exhibit $\mu=0$ and $\sigma=1$, respectively. The original mean and widths are quoted in the labels. The first important observation is that 95% of all reduced χ^2 values for electrons and positrons at all energies lie between 0.5 and 2.1 with a mean of about

1.4 and no significant differences amongst energies or particles (right column). This strongly supports the previous conclusion that the pion efficiencies' shapes agree well with the ones of electrons and positrons. Since, moreover, also 95% of the scaling factors are in the range 1.01 - 1.17 with a mean of about 1.1 (middle column), the scaled pion efficiencies can confidently be used as a replacement for the statistically challenged electrons/positrons. The left column in Figure 3.8 reveals overall mean systematic uncertainties of about 5% at 19.6 GeV and about 3% at the other energies.

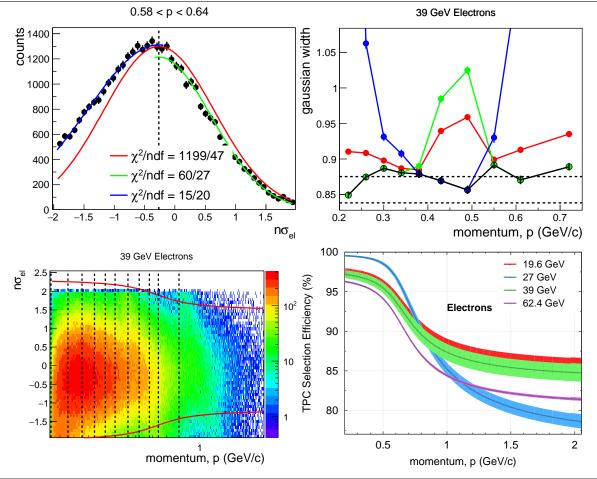
Figure 3.8 Distributions of systematic uncertainties $\Delta \varepsilon$ on TOF matching efficiencies (left column), scaling factors F for pion efficiencies (middle column) and reduced χ^2 (right column) for electrons (top panel) and positrons (bottom panel) at all energies determined in η - and ϕ -intervals of 0.25 and 15°, respectively. Details see text. The data underlying the distributions is listed in Table A.5.



3.2.3 TPC Selection

Since the TPC's response and related efficiency losses are already accounted for in Section 3.2.1 (ε_{det}), the final step remaining in the calculation of total single track efficiencies (c.f. Equation 3.1) is the determination of TPC selection efficiencies for the momentum-dependent particle identification employed in Section 2.3 via the specific energy loss in the TPC. The respective selection cuts are implemented in a continuous functional form which is why the according efficiences can be derived solely from the assumedly constant gaussian mean and width of the underlying $n\sigma_{el}$ distribution. Figure 3.9 gives an overview of the procedure described in the following.

Figure 3.9 Procedure for the determination of TPC selection efficiencies for the experimental electron sample at $\sqrt{s_{NN}}$ = 39 GeV if not noted otherwise. (upper left) $n\sigma_{el}$ distribution for one of the momentum intervals parameterized via three gaussians with fixed mean (vertical dashed line) over the full range (red) and the two tails (blue, green). (upper right) The resulting gaussian widths versus momentum with the smallest highlighted in open black circles. The upper dashed line denotes the according momentum-averaged width whereas the lower indicates the global width of the momentum-integrated $n\sigma_{el}$ distribution. (lower left) $n\sigma_{el}$ versus momentum with red lines framing the selection used to identify electrons (see Section 2.3). Vertical dashed lines indicate the momentum intervals used to generate momentum-dependent $n\sigma_{el}$ distributions. (lower right) Resulting continuous TPC selection efficiencies at all energies including systematic uncertainties. The full list of efficiencies and systematic uncertainties can be found in Table A.6.



The experimental electron/positron samples of Section 3.1 can be used to calculate global gaussian means μ_{gl} and widths σ_{gl} of the respective momentum-integrated $n\sigma_{el}$ distributions. However, an accurate gaussian width determination in this manner is impeded by hadron contaminations in either tail of the $n\sigma_{el}$ distributions at different momenta. Hence, each projection of the $n\sigma_{el}$ distributions in the momentum range 0.2 - 0.8 GeV/c (Figure 3.9 lower left) is first parameterized with three gaussians independently over the full range and the two tails (Figure 3.9 upper left). The fit functions are initialized with μ_{gl} and σ_{gl} where the mean is kept fixed and the width is limited to 10. The widths resulting from the χ^2 minimization are studied versus the momentum and the smallest is selected as the *most probable* width of the distribution (Figure 3.9 upper right). This choice suggests itself since the contamination bands of pion, kaon and proton run through the constant electron band ($\langle n\sigma_{el} \rangle \sim 0$) and hence effectively broaden the width preferably on one side of the $n\sigma_{el}$ distribution. Since the $n\sigma_{el}$ distribution's width is

expected to be approximately constant in momentum (\sim 1), an optimized width $\sigma_{\rm opt}$ is obtained by averaging over momentum. Its systematic uncertainty $\Delta\sigma_{\rm opt}$ is estimated by the larger of three times its standard deviation and $|\sigma_{\rm gl}-\sigma_{\rm opt}|$. Table 3.3 lists the global means as well as the optimized gaussian widths and their uncertainties.

Table 3.3: Global gaussian means μ_{gl} and optimized (momentum-averaged) gaussian widths σ_{opt} with systematic uncertainties $\Delta\sigma_{opt}$ of experimental electron/positron $n\sigma_{el}$ distributions.

	$\sqrt{s_{ m NN}}$	19.6 GeV	27 GeV	39 GeV	62.4 GeV
e ⁻	$\mu_{ m gl}$	-0.249	-0.136	-0.264	-0.0609
e ⁻	$\sigma_{ m opt}\pm\!$	$0.869 {\pm} 0.043$	$0.836 {\pm} 0.023$	0.876 ± 0.037	$0.861 {\pm} 0.006$
e^+	$\mu_{ m gl}$	-0.235	-0.129	-0.257	-0.0662
e^+	$\sigma_{ m opt}\pm\Delta\sigma_{ m opt}$	$0.869 {\pm} 0.012$	$0.842{\pm}0.006$	$0.881{\pm}0.020$	$0.866{\pm}0.006$

The continuous momentum-dependent TPC selection efficiencies $\varepsilon_{\rm select}^{\rm TPC}(p)$ in Figure 3.9 (lower right) can subsequently be calculated analytically from the integral over a normalized gaussian with mean $\mu = \mu_{\rm gl}$ and width $\sigma = \sigma_{\rm opt}$:

$$\varepsilon_{\text{select}}^{\text{TPC}}(p) = \left[\int_{x_0^p}^{\mu} + \int_{\mu}^{x_1^p}\right] \frac{e^{-t^2}}{\sigma\sqrt{2\pi}} dx = \left[-\int_{t_0^p}^{0} + \int_{0}^{t_1^p}\right] \frac{e^{-t^2}}{\sigma\sqrt{2\pi}} \sigma \sqrt{2} dt = \frac{1}{2} \sum_{i=0}^{1} \operatorname{erf}(t_i^p) \quad \text{with } t = \frac{|x - \mu|}{\sigma\sqrt{2}}$$

where $\operatorname{erf}(t_i^p)$ the error function evaluated at the integration limits $t_{0,1}^p$. For a given momentum p, the lower and upper limits $x_{0,1}^p$ (and indirectly $t_{0,1}^p$) are obtained from the functions $n\sigma_{\operatorname{el}}(p)$ in Section 2.3 which are used for the identification of electrons/positrons through their energy loss in the TPC. The systematic uncertainties $\Delta\sigma = \Delta\sigma_{\operatorname{opt}}$ are propagated quadratically to $\varepsilon_{\operatorname{select}}^{\operatorname{TPC}}$ via

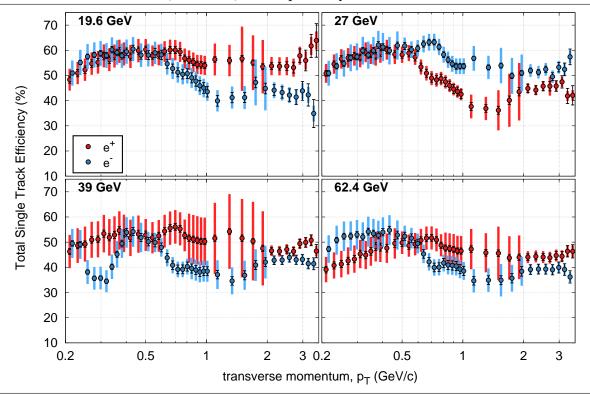
$$\Delta \varepsilon_{\text{select}}^{\text{TPC}}(p) = \sqrt{\sum_{i=0}^{1} \left(\Delta t_{i}^{p} \frac{\partial \text{erf}(t_{i}^{p})}{2 \partial t_{i}^{p}} \right)^{2}} = \sqrt{\sum_{i=0}^{1} \left(\frac{t_{i}^{p} \Delta \sigma}{\sigma \sqrt{\pi}} \exp\left[- \left(t_{i}^{p} \right)^{2} \right] \right)^{2}}.$$

3.2.4 Total Efficiencies and Uncertainties

Concluding this section, the efficiencies derived in the preceding subsections are combined according to Equation 3.1 for electrons and positrons separately using $\Delta \eta = 0.25$, $\Delta \phi = 15^{\circ}$, and the variable p_T binning defined by the TOF matching efficiencies (c.f. Figure 3.7). To account for the different p_T -intervals used in the determination of efficiencies for detector response, track quality requirements ($\Delta p_T = 0.2 \text{ GeV/c}$) and global DCA cuts ($\Delta p_T = 0.3 \text{ GeV/c}$), efficiencies and associated uncertainties are interpolated linearly between bin centers. The propagation of efficiencies beyond the maximum p_T simulated in embedding is achieved by assuming constant values and uncertainties evaluated at 2 GeV/c. In the extreme cases of zero efficiency in which standard propagation of squared relative errors is not applicable, the Monte Carlo technique is employed to generate a random sample of combined efficiencies based on sampling the single uncertainties. Mean and especially width of the sample can then be calculated manually which allows for the conservation of well-defined and physical non-zero statistical and systematic uncertainties. For the application of TPC selection efficiencies and uncertainties (c.f. Figure 3.9), the center p_T and η given by the binning for TOF matching efficiencies are mapped to the momentum $p = p_T \cosh(\eta)$. In the case of relative systematic uncertainties on track quality and global DCA efficiencies (Figure 3.6), a conservative estimate is used for the six p_T bins by propagating the maximum uncertainty allowed by the statistical errors. As an example, Figure 3.10 shows the resulting total single track efficiencies in a single η/ϕ -interval for electrons and positrons at all energies including their statistical and systematic uncertainties. It is worth noticing that statistical errors stay significantly smaller than the systematic uncertainties for

almost the entire p_T range covered - especially at the low momenta where most of the dielectron production emanates from. The efficiencies range between 40-60% and exhibit appreciable differences in shape for electrons and positrons which in hindsight motivate the consistently separated treatment of their respective efficiencies.

Figure 3.10 Total Single Track Efficiencies including statistical and systematic uncertainties in the representative interval of $0 < \eta < 0.25$ and $45^{\circ} < \phi < 60^{\circ}$ at all energies with electrons (blue) and positrons (red) separately. For reasons of improved visibility, electrons are shifted upwards by 3% relative to positrons. Table A.3 and Table A.4 list the full set of single track efficiencies and their uncertainties for $\eta < 0$ and $\eta > 0$, respectively.



3.3 Pair Efficiencies

The calculation of dielectron (pair) efficiencies is the primary purpose of this chapter. In the following, they are derived from the total electron and positron single track efficiencies of Section 3.2.4 via a Monte Carlo simulation of two-body decays. The pair efficiencies need to be determined in dependence of dielectron invariant mass M_{ee} and transverse momentum p_T such that they can be applied as an inverse weight on the raw spectra of Section 2.4 and compared directly to cocktail simulations and model calculations in Chapter 5.

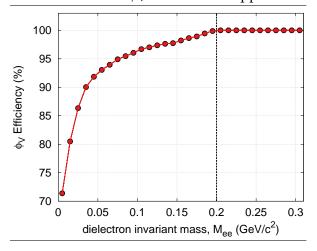
The general idea of the simulation is to (*i*) randomly generate the dielectrons' M_{ee} , p_T , pseudo-rapidity η and azimuthal angle ϕ , (*ii*) decay them according to two-body kinematics, (*iii*) apply STAR acceptance and single track efficiencies on the two daughters as well as pair-based cuts on the parent, and finally (*iv*) rebin, normalize and divide appropriate histograms to obtain the pair efficiencies. As input to this procedure, each dielectron's M_{ee} , p_T and ϕ are hence sampled uniformly in the ranges $2m_e$ - $3.5~\text{GeV/c}^2$, 0 - 4~GeV/c and 0 - 2π , respectively. The pair's rapidity y is also sampled randomly in [-1, 1] and transformed into η via

$$\eta = \sinh^{-1}\left(\frac{m_T}{p_T}\sinh(y)\right) \quad \text{with} \quad m_T = \sqrt{M_{ee}^2 + p_T^2}.$$

At low invariant masses and transverse momenta, STAR's acceptance misses dielectrons exhibiting transverse masses $m_T < 0.4 \text{ GeV/c}^2$. For the lowest p_T -interval 0 - 0.4 GeV/c, this acceptance hole results in quickly falling but still non-zero residual efficiencies at $M_{ee} < 0.4 \text{ GeV/c}^2$. Using a uniform input approach, it is hence very challenging to gather sufficient statistics in this invariant mass range. To alleviate the situation, sets of kinematic variables for 10 additional dielectrons are sampled for each dielectron simulated in the full ranges using identical strategy but separate random generators. Together with a suitable choice of a variable invariant mass binning, significantly fewer iterations are consequently required to sufficiently reduce the statistical errors, i.e. to a level negligible with respect to the systematic uncertainties and to the statistical errors on the raw data.

The subsequent two-body decay of the parent dielectron follows the kinematics for direct vector meson decays discussed in Section 4.1 by calculating the decay daughters' kinematic variables in the dielectron's center of mass frame and then boosting both into the lab frame. To calculate the pair efficiencies for the current dielectron, the total single track efficiencies for each decay leg are obtained for the respective η/ϕ -interval and interpolated linearly in p_T along with the according statistical and systematic uncertainties. The statistical errors of the efficiencies are used to randomly vary the single track efficiencies via gaussian sampling. The resulting efficiencies are multiplied into pair efficiencies and the according systematic uncertainties are propagated either through standard or

Figure 3.11 ϕ_{V} efficiency [16]. The vertical dashed line denotes the maximum invariant mass at which the ϕ_{V} cut has been applied.

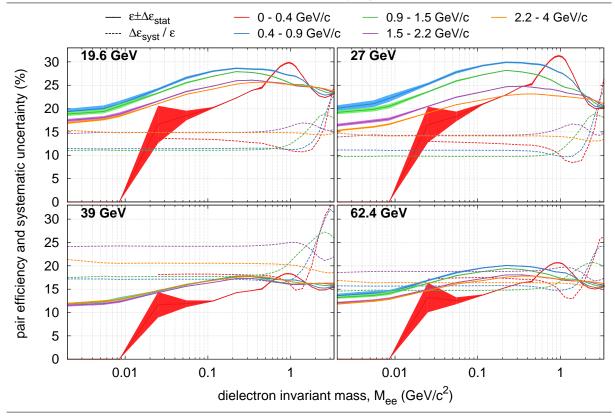


through Monte Carlo propagation to also cover the extreme cases. The last step before filling "output" histograms using the pair efficiencies as weight 1 , is the application of ϕ_V cut efficiencies on the dielectron parent. In Section 2.4 photon conversion is efficiently rejected using a M_{ee} -dependent selection cut which has been tuned at top RHIC energy [16] to deliver good π^0 -Dalitz selection efficiency at optimal photon conversion rejection efficiency. Determining the consequential reduction in pair detection efficiency in this manner, can be achieved through the use of π^0 -Dalitz and photon conversion samples simulated via the embedding technique. The resulting M_{ee} -dependent ϕ_V cut efficiencies are depicted in Figure 3.11 and also interpolated linearly to obtain an efficiency value at arbitrary invariant mass.

Figure 3.12 compiles invariant mass and transverse momentum dependent pair efficiencies for all energies including the respective relative systematic uncertainties. The former peak at roughly 30% for 19.6 & 27 GeV and at about 20% for 39 & 62.4 GeV. At M_{ee} < 1 GeV/ c^2 , the latter range between \sim 10-15% for 19.6 & 27 GeV, and between \sim 15-20% at 39 & 62.4 GeV. As expected, the statistical errors are much smaller than the systematic uncertainties except for the last bin next to STAR's acceptance hole in the lowest p_T -interval. The rather appreciable changes in shape with transverse momentum above $M_{ee} \sim 0.5 \, \text{GeV/}c^2$ signify the importance of a two-dimensional efficiency correction. Also note that the p_T -intervals chosen here purposely coincide with the ones in Figure 5.6.

¹ allows for the automatic averaging of efficiencies incl. stat./syst. uncertainties over the simulated sample.

Figure 3.12 Pair efficiencies (solid lines) and relative systematic uncertainties (dashed lines) for five p_T -intervals at all BES-I energies. The invariant mass range depicted is the full range covered in the simulation. Note that the bands around the efficiency results indicate statistical error bars of the Monte Carlo simulation. The underlying data is listed in Table A.7.



Chapter 4

Simulations and Models

The physics interpretation of the experimental results in Chapter 5 is based on (*i*) the simulation of hadronic decay channels known to contribute to dielectron production in elementary collisions, and (*ii*) effective model calculations that describe the respective in-medium effects. The former constitutes the so-called *hadronic cocktail* whose sources and characteristic mass regions have already been introduced in the context of simulated p+p collisions in Section 1.3 along with its according comparison to previous dielectron measurements in heavy-ion collisions. Section 4.1 describes the details of the cocktail simulations that are employed in this thesis for the energy-dependent dielectron production in Au+Au collisions at BES-I energies. Section 1.3 also highlights the excess yields measured over the cocktail in the Low-Mass-Region (LMR) of the invariant mass spectra as well as its possible connection to chiral symmetry restoration through calculations based on Hadronic Many-Body Theory (HMBT). Section 4.2 discusses some of the illustrating details and shows the results of these calculations for the BES-I energies studied in this thesis.

4.1 Cocktail Simulation

Table 4.1 lists the e^+/e^- decay channels contributing to the total cocktails of this thesis and denotes two conceptionally different categories of dielectron sources: i) direct or Dalitz decay channels of the freeze-out pseudo-scalar/vector mesons in the mass range of interest, or ii) semi-leptonic decays of charmed higher-mass resonances. A Monte Carlo (MC) simulation is employed for the meson decays by sampling correctly parameterized transverse momentum distributions, using appropriate two- and three-body kinematics, and accounting for the detector's momentum resolution. The continuum arising in the Intermediate-Mass-Range (IMR) from the charmed resonances decays, on the other hand, is simulated in p+p collisions using PYTHIA and scaled to Au+Au at the respective energy. At the end of this section, the results of the simulations for all BES-I energies are summarized in preparation for their comparison to the experimental results.

Table 4.1: Decay channels from pseudo-scalar/vector mesons (PSM/VM) and charmed resonances (CR) included in the cocktail simulations for BES-I. Note that the freeze-out ρ -meson is simulated here along with other contributions to allow for comparisons but is not included in the total cocktail (see Chapter 5). Baryonic resonances are not considered for reasons given in Section 1.3.

Dalitz PSM/VM	$\pi,\eta,\eta' ightarrow e^+e^-\gamma$	$\omega ightarrow e^+ e^- \pi^0$	$\phi ightarrow e^+ e^- \eta$
Direct PSM/VM	$\omega,\phi,J/\psi$	e^+e^-	$(ho ightarrow e^+e^-)$
Semi-Leptonic CR		$D^0, D^{\pm}, D_s, \Lambda_c \rightarrow e^{+/-}X$	

As a reference point for the following discussion, all parameters required as input to the simulations are listed in Table 4.2. Many of the details explained in the remainder of this section can be comprehended to greater depth by following along in the simulation code published at [186].

Table 4.2: Input parameters for cocktail simulations. See footnotes and text for details.

Particle Properties									
		do-scalar me	sons		vector i	mesons			
particle	π^0	η	η'	ρ	ω	ϕ	J/ψ		
m_h^{-1}	0.1349766	0.547853	0.95778	0.77526	0.78265	1.019455	3.096916		
Γ^{2}	7.725e-9	1.3e-6	0.199e-3	0.1478	8.49e-3	4.26e-3	9.29e-5		
$ m N_{FS}$ 3		2		-	1		-		
Λ^{-2} 4	1.756	1.95	1.84	-	2.24	3.23	-		
Γ_0^{2} 5	Ċ)	0.02	(j	0.01	0		
BR _{ee} ⁶		-	•	4.72e-5	7.28e-5	2.954e-4	5.94e-2		
$\mathrm{BR_{da}}^{7}$	1.174e-2	6.9e-3	9.0e-4	-	7.7e-4	1.15e-4	-		
M/π^{8}	1	0.085	0.0078	0.06	0.069	0.018	6.2e-6		
	_		Momentun						
Resolı	ition ⁹		Double	le-Tailed Crystal Ball Function ¹⁰					
a	b	\bar{x}	$oldsymbol{\sigma}_0$	n_0	$ \alpha_0 $	n_1	$lpha_1$		
6e-3	8.3e-3	-0.001	0.01	1.29	-1.75	2.92	1.84		
				1	ı				
	Tsallis-Bl	ast-Wave Pa	arameters	Pion					
	40		1)	3/2 11	Charm Continuum				
	$(\beta_{\mathrm{S}} =$	= 1.5β for n	= 1)	Yields		NN			
$\sqrt{s_{NN}}$	T (GeV)	β	q	dN_{π}/dy	$\sigma_{c\bar{c}}^{ m NN}$ (μ b)	$\sigma_{ m mb}^{ m NN} \ ({ m mb})$	$N_{ m coll}$		
19.6 GeV	0.1189	0.3582	1.0272	51.9	6.1±3.9	32	231.75		
27 GeV	0.1222	0.3927	1.014	55.8	19.7±12.6	33	238.7		
39 GeV	0.1229	0.3841	1.02322	58.6	57±36	34	243.16		
62.4 GeV	0.1168	0.3457	1.049	61.7 [187]	160±100	36	252.9		
				D^\pm	D^0	D	. A		
Branching	Ratios of C	Charmed Re	esonances	0.1607	0.0649	D_s 0.065	Λ_c 0.045		
				0.1007	0.0049	0.003	0.043		

 $^{^{1}}$ (hadron) mass of pseudo-scalar/vector meson (in GeV/ c^{2}).

² resonance (or decay) width in Breit-Wigner distribution (in GeV).

 $^{^{3}}$ number of final states in QED part of Kroll-Wada formula.

⁴ parameter in form factor parameterization of Kroll-Wada formula (in GeV⁻²).

 $^{^{5}}$ additional parameter in form factor parameterization of Kroll-Wada formula (in GeV²).

⁶ branching ratio for direct decay.

⁷ branching ratio for Dalitz decay.

⁸ meson-to-pion ratios of invariant yields.

 $^{^{9}}$ parameters for $\ensuremath{p_{T}}$ dependence of momentum resolution.

¹⁰ left-to-right: mean and width of gaussian core, and two parameters defining each of the non-gaussian tails.

¹¹ temperature T, expansion velocity β , and exponent q.

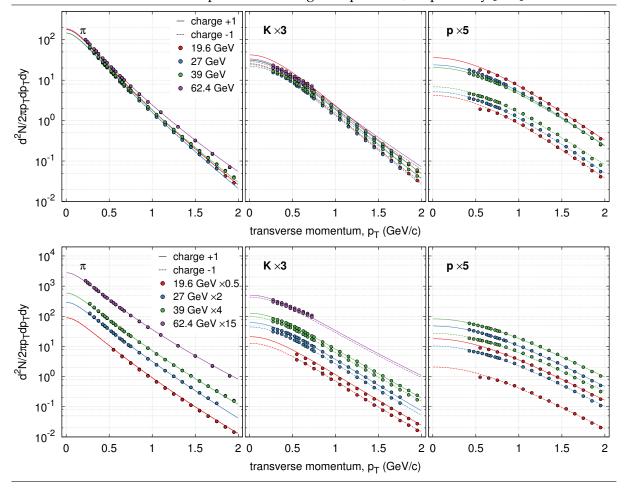
4.1.1 Pseudo-Scalar/Vector Meson Sampling and Decays

One of the important ingredients in the simulation of the cocktails is the input distributions chosen for the pseudo-scalar/vector mesons in Table 4.1. The distributions are used to decay the mesons according to the kinematics of their direct and Dalitz channels. This step is needed to apply momentum smearing on the daughter particles and reject those outside the STAR acceptance, i.e. with transverse momenta $p_T < 0.2 \text{ GeV/c}$ and pseudo-rapidity $|\eta| > 1$. The mesons' rapidity and azimuthal distributions are sampled uniformly in $y \in (-1,1)$ and $\phi \in (0,2\pi)$, respectively. Their p_T distributions (i.e. $dN/m_T dm_T$) are obtained from simultaneous Tsallis-Blast-Wave parameterizations [83] to pion, kaon and proton p_T spectra measured at BES-I energies [187-189] (Figure 4.1) using the meson mass m_h to calculate the respective transverse mass $m_T^2 = p_T^2 + m_h^2$:

$$\frac{\mathrm{d}N}{m_{\mathrm{T}}\,\mathrm{d}m_{\mathrm{T}}} = \mathscr{F} \cdot m_{\mathrm{T}} \int_{-6}^{+6} \cosh(y)\,\mathrm{d}y \int_{-\pi}^{+\pi} \mathrm{d}\phi \int_{0}^{1} r\,\mathrm{d}r \left(1 + \frac{q-1}{T} \left\{ m_{\mathrm{T}} \cosh(y) \cosh(\rho) - p_{\mathrm{T}} \sinh(\rho) \cos(\phi) \right\} \right)^{-1/(q-1)}$$

with the proportionality factors \mathscr{F} (Table 4.3), temperature T, and $\rho = \tanh^{-1}(\beta_S r)$ where β_S the radial surface expansion velocity of the fireball.

Figure 4.1 Simultaneous Tsallis-Blast-Wave parameterizations of $\pi/K/p$ p_T-spectra at BES-I energies. In the lower panel the energies are shifted against each other for better visibility. Solid and dashed lines denote positive and negative particles, respectively [190].



$\sqrt{s_{\rm NN}}$ (GeV)	π^+/π^-	K ⁺	K-	р	
19.6	488.7/498.1	448.9	271.7	4970	577.2
27	404.3	365.1	261.2	4580	994.1
39	391.7	319.1	246.4	2720	909.4
62.4	496.3	295.9	254.9	-	-

Table 4.3: Tsallis-Blast-Wave proportionality factors \mathscr{F} (in GeV⁻²).

For the simple direct two-body decays, the resonance's invariant mass (M_{ee}) shape is sampled based on the Breit-Wigner probability distribution [191]:

$$\frac{dN}{dM_{ee}} = \frac{1}{2\pi} \frac{\Gamma}{(M_{ee} - m_h)^2 + \Gamma^2/4}.$$

The daughters' momenta p in the pseudo-scalar/vector meson's center-of-mass system are then given by $p = \sqrt{M_{ee}^2/4 - m_e^2}$ with m_e the electron mass which allows for the derivation of the kinematic variables of e^- (p_T , η , ϕ) and e^+ (p_T , $-\eta$, $\phi+\pi$). In such back-to-back decays, polar angle θ and azimuthal angle ϕ are distributed uniformly in $(0, \pi)$ and $(0, 2\pi)$, respectively. Given the longitudinal momenta $p_z = p\cos\theta$, the required p_T and η are determined by

$$p_T = \sqrt{p^2 - p_z^2}$$
 and $\eta = 0.5 \ln \left(\frac{p + p_z}{p - p_z} \right)$.

The resulting e^+/e^- Lorentz vectors are finally boosted into the lab frame using the PSM/VM's velocity. For the Dalitz decay channels, the Kroll-Wada formula [192] is used to sample the correct dielectron invariant mass shape within the allowed range of $2m_e$ to m_h - m_d with m_d the daughter hadron's or photon's (=0) rest mass:

$$dN/dM_{ee} = 2M_{ee} \cdot FF^2(M_{ee}) \cdot QED(M_{ee}) \cdot PS(M_{ee})$$

where the QED part, the form factors (FF, [145, 193-195]) and the phase space (PS) are given by

$$\begin{split} \text{QED}(M_{ee}) &= N_{\text{FS}} \frac{\alpha}{3\pi} \frac{1}{M_{ee}^2} \sqrt{1 - \frac{4m_e^2}{M_{ee}^2}} \left(1 + \frac{2m_e^2}{M_{ee}^2}\right) \quad (N_{\text{FS}}: \text{ number of final states}), \\ \text{FF} &= \begin{cases} \left(1 + M_{ee}^2/\Lambda^2\right)^2 & \text{for } \pi^0 \\ \left[(1 - (M_{\text{ee}}/\Lambda)^2)^2 + (\Gamma_0/\Lambda)^2\right]^{-1} & \text{for } \eta/\eta'/\omega/\phi, \end{cases} \\ \text{PS} &= \begin{cases} \left(1 - (M_{ee}/m_h)^2\right)^3 & \text{for } \pi^0/\eta/\eta' \\ \left(\left(1 + M_{ee}^2/\left(m_h^2 - m_d^2\right)\right)^2 - 4m_h^2 M_{ee}^2/\left(m_h^2 - m_d^2\right)^2\right)^{3/2} & \text{for } \omega/\phi. \end{cases} \end{split}$$

The dielectron invariant mass sampled from the Kroll-Wada distribution is first used to simulate the intermediate virtual photon's back-to-back decay into electron and positron in its center-of-mass system via the two-body dielectron kinematics described above. The underlying two-body kinematics can also be employed to obtain the Lorentz vectors of decay hadron/photon and lepton pair (virtual photon) assuming uniformly distributed helicity angles. The required daughter hadron momentum p can be calculated in the parent pseudo-scalar/vector meson's center-of-mass system via $p^2 = E_d^2 - m_d^2$ with $E_d = \left(m_h^2 + m_d^2 - M_{ee}^2\right)/2m_h$. The electron's and positron's Lorentz vectors are boosted first into the lepton pair's rest frame and subsequently into the parent pseudo-scalar/vector meson's lab frame with the latter also for the daughter decay hadron/photon. In the combined case of allowed Dalitz and direct decay modes, the simulation randomly switches between the two kinematics according to the ratio of Dalitz (BR_{da}) and direct (BR_{ee}) branching ratios.

4.1.2 Momentum Smearing and Yield Scaling

The final step in the simulation of the pseudo-scalar/vector mesons is the smearing of their decay daughter's momenta, reminiscent of the reconstruction procedure in the experimental data analysis. Momentum smearing can be achieved by adding a gaussian-like distributed momentum shift $\Delta p_T^{\rm md}$ to the simulated p_T as derived in the following. For the BES-I energies, similar momentum resolution as achieved at $\sqrt{s_{NN}}=200$ GeV is assumed which allows to utilize the same parameterizations tuned to match the measured J/ ψ signal [16]. $\Delta p_T^{\rm rnd}$ needs to be sampled according to the decay leptons' (relative) momentum resolution $\delta p_T \equiv \sigma(p_T)/p_T$ defined by the p_T dependent one standard deviation $\sigma(p_T)$ (width) of gaussian fits to distributions of the relative momentum shift $\Delta p_T^{\rm rel}$. This shift caused by the tracking in the TPC with respect to the true particle momentum can be derived via

$$\Delta p_T^{\mathrm{rel}} = \left(p_T^{\mathrm{rec}} - p_T^{\mathrm{MC}} \right) / p_T^{\mathrm{MC}}$$

with $p_T^{\rm MC}$ the Monte Carlo simulated (true) momentum and $p_T^{\rm rec}$ the according momentum reconstructed in the STAR-specific embedding procedure (see Chapter 3). Statistics gathered in the latter does not allow for reliable fits of the $\Delta p_T^{\rm rel}$ distribution's tails on a bin-by-bin basis in transverse momentum. However, the influence of the tails on the width of the distribution is negligible which is why the p_T dependency of the momentum resolution can be parameterized using

$$\sigma(p_T) = \sqrt{a^2 p_T^2 + b^2}$$

and separated from the tail-including randomization of $\Delta p_T^{\rm rel}$. The $\Delta p_T^{\rm rel}$ distributions of each transverse momentum bin i are scaled such that the respective gaussian widths σ_i equal σ_0 , i.e.

$$\Delta p_{T,i}^{\text{rel}} = \Delta p_{T,i}^{\text{rel}} \cdot \sigma_0 / \sigma_i$$
.

They are subsequently added up to form a universal (p_T independent) distribution dN/dx parameterized by means of a double-tailed Crystal Ball function [196-198] ($x \equiv \Delta p_T^{\rm rel}$ and $y \equiv (x - \bar{x})/\sigma_0$):

$$\frac{dN}{dx} \propto \begin{cases} t_0(x) & \text{if } y < \alpha_0 \\ \exp(-y^2/2) & \text{if } \alpha_0 \le y \le \alpha_1 \\ t_1(x) & \text{if } y > \alpha_1 \end{cases}$$

with

$$t_i(x) = \left\lceil \frac{n_i}{|\alpha_i|} \middle/ \left(\frac{n_i}{|\alpha_i|} - |\alpha_i| + \operatorname{sgn}(\alpha_i) \cdot y \right) \right\rceil^{n_i} \exp\left(-\frac{\alpha_i^2}{2} \right)$$

denoting the two tails of the $\Delta p_T^{\rm rel}$ distribution. In summary, it follows for the smeared daughter momenta $p_T^{\rm sm}$, including the proper scaling of the daughter's functional momentum shape back to the correct width at the specific momentum,

$$p_T^{\rm sm} = p_T + \Delta p_T^{\rm rnd} = p_T \left(1 + \Delta p_T^{\rm rel,rnd} \right) = p_T \left(1 + \Delta p_{T,\rm CB}^{\rm rel,rnd} \cdot \sigma(p_T) / \sigma_0 \right)$$

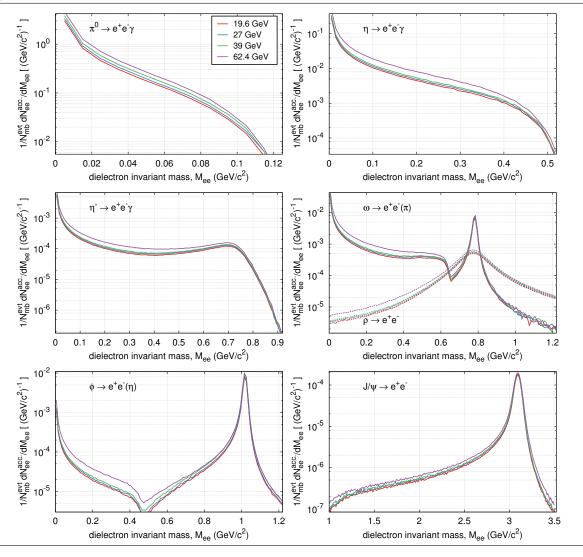
with $\Delta p_{T,\mathrm{CB}}^{\mathrm{rel,rnd}}$ sampled randomly from the above Crystal Ball function.

Finally, the resulting Lorentz vectors for the decay particles are used to generate dielectron invariant mass and p_T spectra at mid-rapidity ($|y_{ee}| \sim |y_{\rm PSM/VM}| < 1$) within STAR acceptance. The acceptance difference between vector mesons and their daughter dielectrons caused by the difference in rapidities for Dalitz decays results in an 8% overall correction [190] and is included in the scaling factors listed in Table 5.1.

So far, the pseudo-scalar/vector meson's invariant mass spectra obtained from the Monte Carlo simulations only provide the correct shape but still need to be scaled to the desired invariant yields before being compiled into the hadronic cocktail. The previous Tsallis-Blast-Wave

fits also provide the total invariant pion yields in STAR (dN_{π}/dy) which are used in conjunction with meson-to-pion (M/ π) ratios from SPS to extract the invariant yields of all other pseudo-scalar/vector mesons. The expected number of dielectrons per event emanating from the decay(s) of a specific pseudo-scalar/vector meson (PSM/VM) within STAR acceptance is calculated from the according number of simulated dielectrons and folded with the total branching ratio for the PSM/VM's direct and Dalitz decays, times the number of PSM/VMs per event:

Figure 4.2 Simulated invariant mass spectra for all pseudo-scalar/vector meson decay channels considered for the cocktail at BES-I energies. Though not included in the total cocktail, the ρ contribution is depicted, too, since it is used for comparisons in Chapter 5. Note that simulated p_T spectra for six characteristic mass regions have also been generated and are displayed in Figure 5.6.



Estimates of systematic uncertainties on the resulting invariant mass spectra shown in Figure 4.2 are primarily due the pseudo-scalar/vector meson yields dN/dy and difficult to obtain at BES-I energies since finalized measurements in heavy-ion collisions by STAR and/or PHENIX are only available at top RHIC energy. The publication of STAR's BES-I data available in preliminary status and used for the pion yields in Table 4.2 is underway at the time of this writing.

Hence, the simulations in this thesis are empirically assigned a lump-sum uncertainty of 30% on the yields. In the BES-I regime, only the rather old measurements from elementary collisions at the Intersecting Storage Rings are also available at all energies in addition to a few from Fermilab. Section A.7 compiles all the data including references and parameterizes the p_T spectra via Levy functions. In the future, this could be used to get a better handle on the simulation-related systematic uncertainties of meson yields using number of participant scaling from p+p to Au+Au collisions.

4.1.3 Charm Continuum

The cocktail simulations also include contributions from correlated semi-leptonic decays of charmed resonances (see Table 4.1). The constituents of a $c\bar{c}$ -pair generated in the initial collision hadronize into D-mesons and Λ_c -baryons by combining with lighter u-, d- or s-quarks. About 16% of the hadrons subsequently undergo semi-leptonic weak decays showing up as a continuum of e^+e^- pairs in the intermediate mass range. The dedicated Monte Carlo event generator PYTHIA (v6.416 [199]) is used through ROOT's interface class TPythia6 to simulate the charm production in center-of-mass minimum-bias p+p collisions. The resulting distributions are subsequently scaled to Au+Au collisions using the average number of binary collisions N_{coll} measured by STAR at the respective beam energy.

The PYTHIA simulation is initialized in its default minimum-bias mode (MSEL=1) with a predefined subset of hard-scattering processes in hadron-hadron collisions, i.e. QCD high-p_T processes as well as low-p_T production. Two main settings are tuned in Figure 4.3 (left) to match STAR's measured charmed meson spectrum in p+p collisions [200] (also see PYTHIA manual [199]): (i) the current default value of 2 GeV/c for the gaussian width of the primordial k_T distribution inside a hadron is much larger than explainable by purely non-perturbative terms, hence reset to PARP (91) = 1.0, and (ii) the default $Q^2=4$ scale of the hard 2-2 scattering processes is tuned to high-p_T Tevatron studies [201] but heavy-flavor production [202, 203] suggests PARP (67) = 1.0. In addition, the non-electron Individual Decay Channels (IDC) 684-735, 755-807, 818/824-850 and 1097-1165 are switched off for the contributing charmed resonances D^+ , D^0 , D_s and Λ_c , respectively. The mesons η_c , J/ψ and χ_{2c} are disabled, i.e. IDC=857-862 switched off, since they do not contribute to the charm continuum in the dielectron invariant mass spectrum. PYTHIA automatically recalculates the effective branching ratios for the open decay channels and adjusts the generated cross section according to the decays simulated. During the simulation run, the hadronization of the quarks generated in the initial collision is modeled via the Lund string fragmentation model [204]: The force's color lines are concentrated in narrow tubes between the quark pairs using appropriate string tension. The quarks oscillate periodically along the direction of this color string until it eventually breaks and the pair fragments into new quark-antiquark pairs. For each generated p+p event, the simulation identifies strings that result from the fragmentation of each of the original c- and \bar{c} -quarks, checks for the existence of their decay products, and counts the associated number of $c\bar{c}$ -pairs

In the analysis of the simulation results, dielectron invariant mass and p_T spectra of the charm continuum are generated within STAR acceptance. Since the PYTHIA settings used here exclusively simulate the semi-leptonic decay channels of the charmed resonances, each of the decay dielectrons needs to be weighted with the product of the two branching ratios reponsible for $c, \bar{c} \rightarrow e^{\pm}$ when filling the according histograms (denoted below by the \otimes symbol). The number of dielectrons within STAR acceptance emanating from charmed resonance decays and expected in a single minimum-bias p+p event is then obtained by scaling the distributions from the relative $c\bar{c}$ cross section in simulation to the one measured in minimum-bias nucleon-

nucleon collisions using the factor

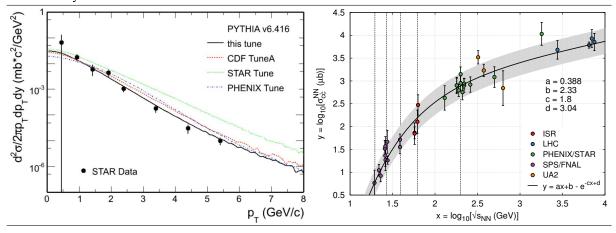
$$\frac{\sigma_{c\bar{c}}^{\rm NN}/\sigma_{\rm mb}^{\rm NN}}{\sigma_{c\bar{c}}^{\rm sim}/\sigma_{\rm mb}^{\rm sim}} = \frac{N_{\rm evt}^{\rm sim}}{N_{c\bar{c}}^{\rm sim}} \cdot \frac{\sigma_{c\bar{c}}^{\rm NN}}{\sigma_{\rm mb}^{\rm NN}}$$

which in summary gives

$$\frac{dN_{ee}^{\rm acc}}{N_{\rm evt}dM_{ee}}\bigg|_{c\bar{c}}^{\rm exp} \quad = \quad \left[\frac{1}{N_{\rm evt}}\left(\frac{dN_{ee}^{\rm acc}}{dM_{ee}}\otimes {\rm BR}_{\bar{c}\to e^+}^2\right)\right]_{c\bar{c}}^{\rm sim} \quad \cdot \quad \frac{N_{\rm evt}^{\rm sim}}{N_{c\bar{c}}^{\rm sim}} \quad \cdot \quad \frac{\sigma_{c\bar{c}}^{\rm NN}}{\sigma_{\rm mb}^{\rm NN}} \quad \cdot \quad N_{\rm coll}.$$

Since to date, many of the according measurements are not available or show sizeable spreads at BES-I energies, a data-driven approach is chosen to determine estimates for the experimental $c\bar{c}$ cross sections $\sigma_{c\bar{c}}^{\rm NN}$. In Figure 4.3 (right) the double-log representation of its measured energy dependence is parameterized via $y \sim x \ominus \exp(-x)$ in the range from SPS up to LHC energies. 1.5-times the (average) standard deviation of the data points from the parameterization is taken as the associated systematic uncertainty at each energy to cover most of the variation in the data.

Figure 4.3 (left) Parameter tuning for the initialization of the PYTHIA simulation via STAR's measured D^0 spectrum in p+p collisions at $\sqrt{s_{NN}} = 200$ GeV [200] in comparison to other or preceding choices. (right) Parameterization of the charm cross section in elementary collisions using data from a variety of experiments and energies. Vertical dashed lines denote BES-I and top RHIC energies. The grey band depicts 1.5x the standard deviation chosen as systematic uncertainty.



4.1.4 Summary of Simulation Results

In conclusion of this section, the panel in Figure 4.4 compiles the total simulated dielectron invariant mass spectra for the BES-I energies including a band for its systematic uncertainties. All the single hadronic contributions to the cocktail are shown as well, with the charm continuum highlighted in blue. Note that the freeze-out ρ is in fact depicted as dashed lines but not included in the total cocktail since the contributions due to in-medium modified spectral functions are derived from model calculations in Section 4.2 and compared to the measured spectra in Chapter 5.

Propagation of the systematic uncertainties in the pseudo-scalar/vector mesons' mid-rapidity yields and the charm cross sections results in total uncertainties of about 20-60% (Figure 4.5 left) on the total cocktail simulation (Figure 4.5 right).

Figure 4.4 Compilation of the cocktail simulations at all BES-I energies as expected from hadronic sources. The red band denotes the total systematic uncertainty on the cocktail. The freeze-out ρ contribution is depicted in dashed lines since it is not part of the cocktail here and instead compared to model calculations and data in Chapter 5.

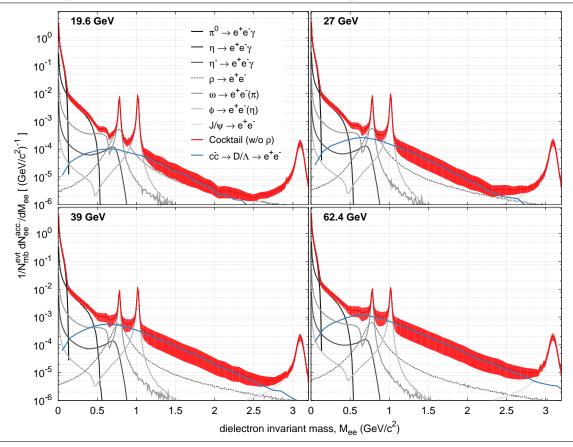
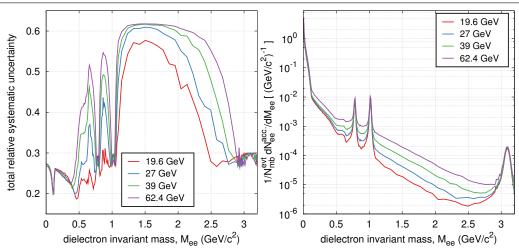


Figure 4.5 Simulated invariant mass and energy dependence of the cocktail's total relative uncertainty (left) and total invariant dielectron yields (right). The former is dominated by uncertainties in the mesons' mid-rapidity yields and the charm cross sections in elementary collisions.



4.2 In-Medium Modifications

The cocktail simulations of Section 4.1 do not include any contributions from the medium, particularly not those from in-medium effects on low-mass vector mesons discussed and connected to chiral symmetry restoration in Chapter 1. In support of the related discussion and the interpretation of the thesis results in Chapter 5, this section is dedicated to a brief introduction of the most prevalent aspects of the Hadronic Many-Body Theory (HMBT) employed in this thesis to predict the effects of in-medium modifications. The theory addresses in-medium spectral functions and fireball evolution, both necessary to arrive at the integrated dielectron emission rates measured experimentally via invariant mass spectra. Many and more of the details selected in the following recapitulation can primarily be found in [114] but also in [3, 205, 88]. The conclusion of this section presents the latest model calculations performed by Rapp [206]. In Chapter 5, they are compared to the efficiency-corrected experimental data obtained in Chapter 2 and Chapter 3.

4.2.1 Dilepton Production Rates

The time-reverse process to dielectron production (in the vacuum) is e^+e^- annihilation into a myriad of hadrons depending on the center-of-mass energy $\sqrt{s} = M_{ee}$. The QCD effects can be separated from the basic QED-only processes by taking the ratio $R(\sqrt{s})$ of the total e^+e^- cross section $\sigma(e^+e^- \to \text{hadrons})$ to the according $\sigma(e^+e^- \to \mu^+\mu^-) = 4\pi\alpha_s^2(s)/3s$ with the running coupling constant for the strong force $\alpha_s^{-1}(s) = \beta_0 \ln(s/\Lambda^2)$ where $\beta_0 = (11 - 2n_f/3)/4\pi$, $\Lambda = 217$ MeV the QCD scale, and n_f the number of quark flavors [207].

Figure 4.6 World data on hadronic annihilation cross section in e^+e^- collisions for ratio to QED-only processes. Data from [208]. Details see text.

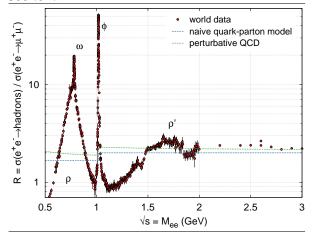


Figure 4.6 shows the available world data for $R(\sqrt{s})$ below 3 GeV where the light u-, d- and s-quarks determine the hadronic production dynamics since the collision energy is not sufficient to produce the bound $c\bar{c}$ state J/ψ , yet. The data is compared to a naive quark-parton model (blue dashed line) in which the ratio is predicted by purely electro-weak considerations to

$$R_{\text{EW}}(\sqrt{s}) = 3\sum_{q} e_q^2 = \begin{cases} 5/3 & q \in [u, d], \sqrt{s} < m_{\phi} \\ 2 & q \in [u, d, s], \sqrt{s} \ge m_{\phi} \end{cases}$$

with e_q the electric charge of quark q and m_ϕ the ϕ -meson rest mass. Also depicted in green dashed lines is the ratio

$$R(\sqrt{s}) = R_{\text{EW}}(\sqrt{s}) \left(1 + \delta_{\text{QCD}}(\sqrt{s})\right)$$

including corrections $\delta_{\rm QCD}$ to $R_{\rm EW}$ due to the QCD effects which can be calculated perturbatively up to α_s^4 via [207, 209]

$$\delta_{\text{QCD}}(\sqrt{s}) = \sum_{n=1}^{4} c_n \left(\frac{\alpha_s(s)}{\pi}\right)^n + \mathcal{O}\left(\frac{\Lambda^4}{s^2}\right) \text{ with } c_1 = 1, \begin{cases} c_2 = 1.76, c_3 = -9.14, c_4 = -121 & \text{for } n_f = 2\\ c_2 = 1.64, c_3 = -10.3, c_4 = -107 & \text{for } n_f = 3. \end{cases}$$

Above about $M_{\rm dual} = 1.5$ - 2 GeV, the measured e^+e^- annihiliation cross section approaches and is satisfactorily accounted for by the calculated perturbative QCD rate and thus negligibly impacted by hadronization. $M_{\rm dual}$ hence constitutes a *duality threshold* below which the resonance structures can accurately be described by the light vector mesons ρ , ω and ϕ through Vector

Meson Dominance (VMD, [98]). This allows for the decomposition of the imaginary part of the vacuum electro-magnetic current-current correlator into

$$\operatorname{Im}\Pi_{\mathrm{em}}^{\mathrm{vac}} = egin{cases} \sum_{V} m_{V}^{4}/g_{V}^{2} & \cdot & \operatorname{Im}D_{V} & ext{if } M_{ee} \leq M_{\mathrm{dual}}, V =
ho, \omega, \phi \\ -M_{ee}^{2}/12\pi & \cdot & R(\sqrt{s} = M_{ee}) & ext{if } M_{ee} > M_{\mathrm{dual}} \end{cases}$$

with the imaginary part of the vector meson propagator $\text{Im}D_V$ denoting its spectral function. $\text{Im}\Pi_{\text{em}}$ provides the general framework for the study of thermal dilepton emission [210, 211] since the according dilepton production rate can directly be obtained via

$$\frac{\mathrm{d}R_{ee}}{\mathrm{d}^4q} = -\frac{\alpha_{\mathrm{em}}^2}{\pi^3 M_{ee}^2} f^B \,\mathrm{Im}\Pi_{\mathrm{em}}$$

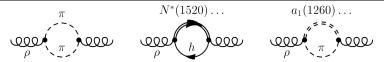
with f^B the thermal Bose distribution function.

When embedding low-mass vector mesons in an environment of hot hadronic matter the extension of $\operatorname{Im}\Pi_{\operatorname{em}}$ to finite temperature and baryo-chemical potentials is achieved by calculating approximations of the respective spectral functions - assuming that VMD still holds in the medium. In HMBT, standard many-body techniques are employed to incorporate medium effects on a microscopic level in the ρ -meson propagator D_{ρ} through self-energy corrections Σ due to π -cloud polarization and resonant interaction with surrounding mesons M and baryons B:

$$D_{\rho}(M_{ee}; \mu_B, T) = \left[M_{ee}^2 - m_{\rho}^2 - \Sigma_{\rho\pi\pi} - \Sigma_{\rho B} - \Sigma_{\rho M}\right]^{-1}$$

with $M = \pi, K, \rho, \ldots$ and $B = N, \Lambda, \Delta, \ldots$ from the heat bath. The calculation of processes involved in the Σ corrections is represented by the Feynman diagrams in Figure 4.7, for instance, which are allowed to subsequently occur multiple times and in different combinations.

Figure 4.7 Feynman diagrams for self-energy corrections in the ρ -meson propagator.



The resulting LMR medium effects for the ρ -meson turn out to cause the most prominent contribution to the calculated invariant mass spectra (Figure 4.10) while being well accessible in experiment (Chapter 5). In comparison, the changes in the spectral functions of ω - and ϕ -meson are mostly hidden beneath the according freeze-out decays. For details on the self-energy corrections of ω - and ϕ -mesons, the reader is referred to the literature [114] since the remainder of this section will concentrate on the discussion of LMR in-medium effects caused by the ρ -meson.

Figure 4.8 (left) shows the resulting temperature dependence for the ρ -meson spectral function. A rather strong broadening is observed towards the phase boundary at $T \sim 180$ MeV (with a small mass shift). Since the ρ -meson is its own antiparticle with respect to the strong force, an appreciable additional broadening arises around the phase boundary temperature from its equal interaction with baryons and antibaryons (Figure 4.8 right). In contrary, note that the ϕ -meson is mostly agnostic to these in-medium effects presumably due to the OZI-rule which explains the absence of baryonic resonances with ϕ N decay channels by the strong suppression of antistrange quark annihilation needed to supply the excitation energy.

M [GeV]

M [GeV]

-10 — vacuum

-8 — T=120M eV ,ρ_{eff}=0.02ρ₀

-10 — vacuum

-7 =150M eV ,ρ_{eff}=0.12ρ₀

-10 — vacuum

-8 — νacuum

-9 — νacuum

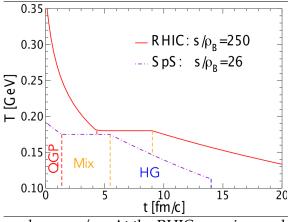
-9

Figure 4.8 T- (left) and μ_B -dependence (right) of ρ -meson spectral function [114]. The effective baryon densities $\rho_{\rm eff}$ correspond to μ_B of 91, 40 and 27 MeV from top to bottom, respectively.

Above the duality threshold, the free electro-magnetic correlator can be evaluated using the lowest-order thermal $q\bar{q}$ annihilation rate. For the QGP phase, this constitutes a lower limit of the true emission rates since theoretical predictions for in-medium corrections are challenging. Recent progress to calculate QGP dilepton rates non-perturbatively has been achieved using thermal Lattice QCD (IQCD, [212]) which is used in Section 2.2 of [116] to construct an extension of the QGP rates to finite 3-momentum. When compared to the according HMBT calculations close to the transition temperature, the "melting" of the ρ -meson's vacuum resonance structure in the medium suggests a smooth transition into the structureless IQCD shape with partonic degrees of freedom. Since leading-order temperature effects alone already reduce the duality threshold towards the ϕ , the QGP rate is extrapolated into the hadronic phase and employed down to $M_{\rm ee} \sim 1.1~{\rm GeV/c^2}$.

4.2.2 Fireball Evolution

Figure 4.9 Fireball temperature profile at SPS and RHIC conditions exhibiting QGP, Mix(ed) and Hadron Gas phase [114].



For the calculation of dielectron invariant mass spectra and their comparison to experimental results, the production rates need to be integrated over the space-time evolution of a heavy-ion collision. A simplified fireball expansion model with time-dependent cylindrical volume $V_{FC}(t)$ is employed in [206] using parameters that reflect measured expansion/flow velocities and particle spectra as most important features of the full hydrodynamic simulation. Figure 4.9 shows the time-dependent temperature profile of the fireball expansion which is needed for the derivation of the dilepton production rates. Throughout the entire evolution the system's trajectory in (T,μ_B) is determined by isentropic expansion, i.e. constant entropy

per baryon s/ρ_B . At the RHIC energies used in this thesis, chemical freeze-out can be assumed to coincide with the critical temperature for the chiral/deconfinement transition and is hence fixed at $T_c \sim 170$ MeV. The hadronic phase's entropy below T_c develops toward thermal (kinetic) freeze-out according to the standard HRG equation of state (EoS), whereas above T_c , the QGP phase's entropy is governed by a lQCD EoS starting at its formation time. Note that [116] also contains a discussion of this thesis's results in a preliminary version compared to model calculations using a quasi-particle EoS and $T_c = 180$ MeV. However, as already discussed in

Section 1.3.2, the total yield stays approximately the same due to the duality of emission rates around T_c which enhances the QGP but equally reduces the hadronic yield. During the mixed phase at constant T_c , the hadronic matter fraction can be inferred from entropy balance since the entire system is in the QGP phase if its total volumetric entropy density $S_{\rm tot}/V_{\rm FC}(t)$ is larger than $s_{\rm QGP}(T_c)$. Table 4.4 quotes the charged particles rapidity densities $dN_{\rm ch}/dy$ which are the remaining necessary input parameters for the model calculations at BES-I energies. Also listed are the initial temperatures T_0 for a chemically equilibrated QGP resulting from the fireball expansion parameters.

Table 4.4: QGP temperature T_0 and charged particles dN_{ch}/dy for HMBT at BES-I energies [206].

$\sqrt{s_{\rm NN}}$ (GeV)	19.6	27	39	62.4	$\sqrt{s_{\mathrm{NN}}}$ (GeV)	19.6	27	39	62.4
T_0 (MeV)	224	230	237	283	$dN_{\rm ch}/dy$	135	140	145	185

4.2.3 Summary of Model Calculation Results

The e^+e^- pair yields have been computed for the use in this thesis [206] uniformly in rapidity $y \in (-1,1)$ employing STAR acceptance cuts for the individual leptons and neglecting momentum smearing to account for the detector's mass resolution. Figure 4.10 summarizes the results of the model calculations described in this section by studying their energy dependence (left) and discussing the consequences on the dielectron invariant mass spectra using $\sqrt{s_{\rm NN}} = 27~{\rm GeV}$ as a representative example (right). The sum of cocktail simulations and model calculations is compared in invariant mass and transverse momentum to the experimental data for all BES-I energies in Chapter 5 (c.f. Figure 5.2 and Figure 5.6).

The total of HMBT and QGP calculations in Figure 4.10 (left) exhibits very similar shape with only little structure for all BES-I energies. The single contributions are hence only displayed for $\sqrt{s_{\rm NN}}$ = 19.6 GeV to demonstrate that hadronic in-medium modifications dominate up to $M_{\rm ee} \sim 1~{\rm GeV/c^2}$ beyond which thermal radiation from the QGP phase takes over. Since the latter originates from earlier emission times and higher temperatures, its smaller slope parameter allows it to reach higher invariant masses than the hadronic sources. However, in this intermediate mass regime (IMR), the QGP signal competes with the continuum from correlated semi-leptonic charmed decays (c.f. Figure 4.4) even though it prevails over Drell-Yan contributions up to the J/ ψ mass.

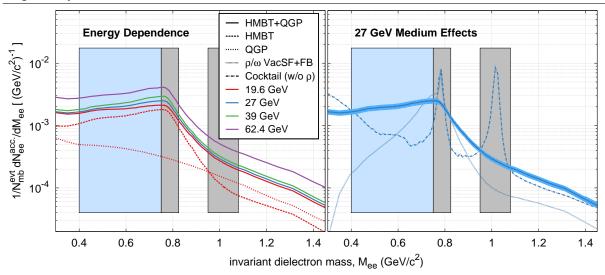
Figure 4.10 (right) compares the HMBT+QGP in-medium invariant mass distributions at $\sqrt{s_{\rm NN}}$ = 27 GeV to the hadronic cocktail without freeze-out ρ -meson as well as to ρ/ω vacuum spectral functions propagated through the fireball (VacSF+FB). In the ρ/ω and ϕ mass regions (grey boxes) the medium effects are unfortunately hidden under the respective freeze-out contributions even though the ρ/ω resonance structure experiences a rather strong suppression (c.f. change from short dashed to solid line versus dash-dotted line in left grey box). Due to its already discussed inertness to in-medium modifications, this is especially true for the ϕ -meson for which such effects are basically unobservable with the available experimental statistics (omitted in the figure).

However, the comparison also reveals two promising regions for the medium effects to be detected in the invariant mass spectra. On the one hand, in the mass region below the ρ/ω resonances from 0.4 to 0.75 GeV/c² (blue boxes, identical to Figure 5.2 and Figure 5.3) as well as in the region between ρ/ω and ϕ , the dominant contribution to the total yield is caused by (hadronic) in-medium effects rather than freeze-out decays (cocktail). Moreover, almost the entire effect in these regions is rooted in the broadening of the ρ -meson's spectral function [114] with a contributed yield as much as three times larger than the cocktail at $M_{ee} = 0.6$ GeV/c² (c.f. enhancement ratios in Figure 5.3 right). In the IMR ($M_{ee} > 1.1$ GeV/c²), on the other hand,

the in-medium contributions from the hadronic and QGP phases jointly amount to a dielectron yield comparable in size and shape to the $c\bar{c}$ continuum.

It should be emphasized at this point that the preceding conclusions on in-medium hadronic and QGP effects have been reached without prior knowledge of their comparison to experimental data in Chapter 5 and can hence be considered true predictions with respect to observable consequences on dielectron spectra.

Figure 4.10 Dielectron invariant mass spectra of in-medium effects in hadronic and QGP phases after fireball evolution. (left) Energy dependence of HMBT+QGP calculations at all BES-I energies (solid lines) with single contributions representatively depicted for 19.6 GeV (dashed and dotted lines). (right) Comparison of predicted in-medium effects at 27 GeV to cocktail simulation without freeze-out ρ (dash-dotted) and to fireball-propagated ρ/ω vacuum spectral functions (dense dotted). The blue band denotes a systematic uncertainty of 10% assigned empirically on the total in-medium distribution based on theorists' estimates.



Chapter 5

Results and Discussion

This chapter presents the results of this study's energy-dependent analysis of dielectron production in combination with the according published results at top RHIC energy ($\sqrt{s_{NN}}$ = 200 GeV, [16]). The results cover invariant mass (M_{ee}) and transverse momentum (p_T) spectra of characteristic mass regions as well as their comparison to simulations and model calculations allowing for the detailed discussion of their physics interpretation. The Low-Mass-Region (LMR, M_{ee} < 1.1 GeV/c²) as one of the particularly interesting regions is highlighted by studying the energy dependence of observed excess yields and enhancement ratios over the cocktail with respect to previous measurements, relation to total baryon density, and expectations for BES-II.

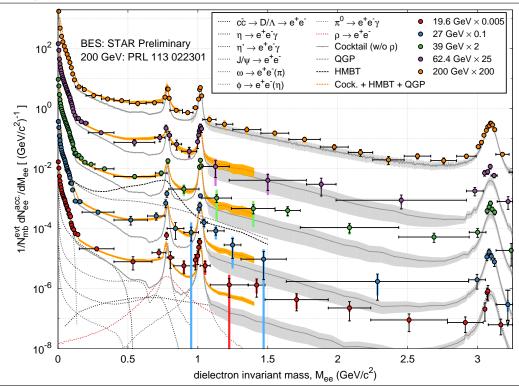
Figure 5.1 depicts the efficiency-corrected invariant mass spectra of all STAR dielectron measurements in 0-80% minimum bias Au+Au collisions enabling a systematic study of dielectron production for the wide energy range from about SPS up to top RHIC energies, namely $\sqrt{s_{\rm NN}}$ = 19.6 - 200 GeV. The peak structures of the π^0 mesons' Dalitz decay and especially the direct decays of the ω -, ϕ - and J/ψ -mesons are nicely identified in the experimental spectra despite the rather poor signal-to-background ratio in the ω/ϕ mass region (see Section 2.4). The quality of the data allows for the invariant mass spectra to be measured up to $M_{ee} \sim 3.5$ GeV/c^2 . The scaling factors in Table 5.1 are used to scale the cocktail simulations described in Section 4.1 to the experimental spectra in the π^0 region (M_{ee} < 0.1 GeV/c²). The choice of employing scaling factors is justified in light of the difficulties involved in the determination of cocktail yields ¹ as well as the efficiency correction of the data (Chapter 3). It also allows for a more meaningful comparison to model calculations above the π^0 mass region since neither conclusions regarding the absolute excess nor regarding the enhancement factors, for instance, should be biased by a mass-independent overall scaling of the spectra. As for the magnitude of the scaling factors, it should be noted that even the spectra at $\sqrt{s_{\rm NN}}$ = 200 GeV require an adjustment of about 10% despite very high statistics and low(er) systematic uncertainties. The scaling factors for BES-I energies are thus not only within reach of the respective systematic uncertainties (see uncertainties in Table 5.1) but also within acceptable limits as empirically expected from the measurement at top RHIC energy.

Table 5.1: Scaling factors F of cocktail to data below 0.1 GeV/ c^2 of the invariant mass spectrum for all BES-I and top RHIC energies. Errors are combined statistical and systematic uncertainties with the former negligible due to the abundant π^0 signal.

$\sqrt{s_{ m NN}}$	19.6 GeV	27 GeV	39 GeV	62.4 GeV	200 GeV
F	$0.83 {\pm} 0.13$	0.82 ± 0.12	$0.87 {\pm} 0.14$	0.87 ± 0.13	0.90 ± 0.09

¹ Note: STAR's latest $\pi/K/p$ yields are not published and their systematic uncertainties still under evaluation.

Figure 5.1 Efficiency-corrected invariant mass dielectron spectra for 0-80% minimum bias Au+Au collisions at BES-I and top RHIC energies compared to cocktail simulations and model calculations [3, 206]. In addition to the total cocktail (grey), the single hadronic freeze-out contributions are depicted for 19.6 GeV (dotted lines). For 39 GeV, the two model contributions from hadronic gas (HMBT) and QGP phase (dashed lines) are shown next to the total expected yield (orange band).



The cocktail simulations generally show good agreement with the data over the entire mass range covered with sufficient statistics during BES-I. In the LMR, though, and as previously reported by other measurements (see Section 1.3), all spectra consistently exhibit a sizeable excess over the cocktail. Contributions from direct ρ decays after freeze-out using a simple Breit-Wigner shape are depicted for comparison at $\sqrt{s_{\rm NN}}$ = 19.6 GeV. However, they are not included in the total cocktails used in this chapter since they by far do not account for the magnitude of the enhancement [213]. Instead, the in-medium model calculations treat the full evolution of the ρ -meson including the appropriate amount of freeze-out decays (see Section 4.2) and hence need to be added on top of the cocktail without any ρ contributions. In particular, the scenario of a broadened ρ spectral function resulting from Hadronic Many-Body Theory (HMBT) together with QGP contributions [3, 206], consistently describes the invariant mass dependence of dielectron LMR yields from SPS to top RHIC energies within systematic uncertainties. In the IMR, these model calculations also yield a visible contribution on top of the cocktail resulting in an improved agreement with the data. This is possibly the first measurement indicative of IMR in-medium effects emerging in the BES-I energy regime. HMBT and QGP contributions are especially sizeable at lower BES-I energies where the $c\bar{c}$ cross sections in elementary collisions $(\sigma_{c\bar{c}}^{NN})$ fall off steeply.

However, substantial conclusions on the possible observation of QGP radiation in this mass region are not only constrained by the limited statistics in this region and the large uncertainties on $\sigma_{c\bar{c}}^{NN}$, but also difficult due to the unknown medium effects on the charm continuum (see Chapter 6) as well as the correlated background contributions from π^0 decays in jets (details see Section 2.4). Without adequate statistics in the mass region above about 1.1 GeV/c², the latter impedes the precise normalization of mixed event to same event background dis-

tributions, and the former is indistinguishable from the data even in the simple case of decorrelated charm pairs causing changes in the mass slope. Conclusive measurement of QGP radiation would also require the study of $T_{\rm eff}$ versus invariant mass which has proven challenging already at $\sqrt{s_{\rm NN}}=200$ GeV with superior statistics and systematics. The BES-I dielectron results for the IMR presented here, drive most of the motivation for BES-II since they reiterate the importance of measuring the $c\bar{c}$ -continuum in detail. The improved beam luminosity hopefully enhances statistics sufficiently enough to even allow for energy-dependent $T_{\rm eff}$ measurements of the QGP. The present study not only constitutes the first dielectron results available in heavy-ion collisions at BES-I energies but also enables novel comparisons within STAR of the $\phi \to ee$ and $\phi \to KK$ decay channels, for instance, or of the J/ψ to results obtained using electro-magnetic calorimeters at intermediate p_T .

Figure 5.2 LMR e⁺e⁻ spectrum exhibiting excess yields over the entire BES-I energy range up to the top RHIC energy. The color code is identical to Figure 5.1 showing good agreement of HMBT and QGP model calculations with LMR dielectron yields. Also depicted for comparison is the alternative scenario of ρ/ω vacuum spectral functions (VacSF) propagated through the fireball (FB). Note that ρ model calculations also include freeze-out contributions. Figure 5.3 makes detailed comparisons of the scenarios to the excess. The blue regions denote the mass range used for the calculation of integrated excess yields and enhancement factors in Figure 5.4 (0.4 < M_{ee} < 0.75 GeV/c²).

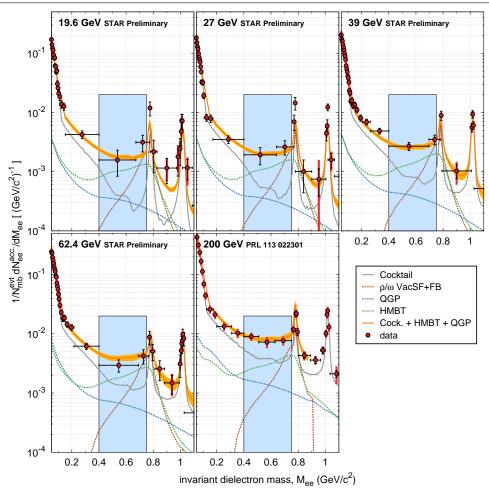
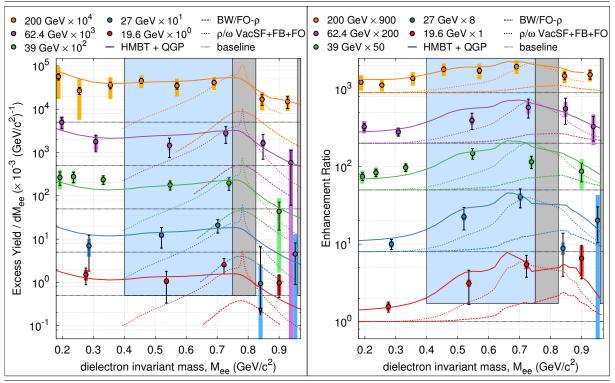


Figure 5.2 gives more detailed insights into the mass region of the dielectron spectra between the π^0 tail and beyond the ϕ resonance, exhibiting sizeable excess yields over the cocktail of hadronic (freeze-out) sources. In their consistent description over a wide range of energies by the in-medium model calculations, contributions primarily due to the broadened in-medium

 ρ spectral function in HMBT clearly dominate over contributions from the QGP in the mass region 0.4 to 0.75 GeV/ c^2 (blue rectangles). Hence, the measured excess yields are rooted in the ρ meson modifications mainly governed by interactions with baryons in the late-stage but hot and dense hadronic phase. Moreover, the model calculations of the yields from the two contributing phases in this scenario indicate a smooth increasing evolution with beam energy and only minor changes in their spectral shape. An alternative scenario is to assume a vacuum spectral function for the ρ and ω mesons un-modified by the medium. The resulting invariant mass spectra after integrating the according rates over the fireball evolution and adding the contributions from freeze-out ρ decays on top, are included in Figure 5.2 (brown dashed line) for comparison to the broadened ρ spectral function scenario. The respective shape already suggests by eye that this scenario is insufficient to describe the required yields in the mass region of the excess. In this context, studying the cocktail-subtracted excess yields (data minus cocktail) and cocktail-normalized enhancement ratios (data divided by cocktail) in Figure 5.3 draws a clearer picture.

Figure 5.3 Invariant mass dependence of absolute LMR excess yields (left) and LMR enhancement ratios (right) over cocktail compared to in-medium, vacuum and bare freeze-out scenarios. The mass regions in which freeze-out ω and ϕ decays are highly dominant, are masked out for clarity (grey boxes). Also note, that the energies are shifted against each other on a logarithmic scale for better visualization. Black dotted horizontal lines denote the according baselines of 0.5×10^{-3} and 1 for excess yields and enhancement ratios, respectively. All systematic uncertainties are combined into uncertainties on the experimental data points. The regions highlighted in blue are used in Figure 5.4 to derive integrated excess yields and enhancement factors.



The absolute excess yields below the ω meson evidently increase smoothly with beam energy (see Table 5.2) and exhibit an approximately constant dependence on invariant mass. Both observations are consistently described by the yields predicted in HMBT and QGP calculations, which are favored at all energies by the data over the scenarios using fireball-propagated vacuum spectral functions or bare freeze-out ρ decays. The same conclusion can be reached from the enhancement ratios in this mass region, which allow for visually improved statistical and

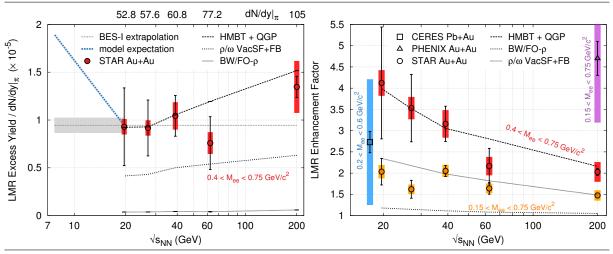
systematic uncertainties but convolute relative differences in the energy dependence of cocktail and data. Still, the energy-dependent measurement of excess yields and enhancement ratios corroborates the preceding conclusion that the broadened ρ scenario provides a consistent description in good agreement with the data over a wide energy range.

Table 5.2: Excess yields from HMBT+QGP integrated over LMR (blue box in Figure 5.3 left).

${\sqrt{s_{ m NN}}}$	19.6 GeV	27 GeV	39 GeV	62.4 GeV	200 GeV
$(\times 10^{-3})$	0.65	0.72	0.82	1.2	1.8

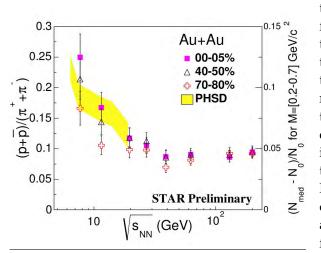
The quality of the STAR data also allows for the systematic measurement of integrated LMR enhancement factors and excess yields with respect to their energy dependence in the BES-I energy regime. Due to the approximately constant dependence on invariant mass, these integrated measures are suitable to quantify the energy dependence of the LMR dielectron production yields with respect to the cocktail in Figure 5.4. The mass region 0.4 - 0.75 GeV/c² is chosen as basis to derive the integrated observables since it avoids STAR's limited acceptance and hence steep decline in detector efficiency for $p_T < 0.2~{\rm GeV/c}$, but is still broad enough in range to gather sufficient statistics while not being influenced by the tail of the π^0 distribution.

Figure 5.4 (Left) Measured BES-I and top RHIC energy LMR excess yields normalized to the respective $dN/dy|_{\pi}$ denoted for each energy in the top margin. The grey dashed line and box represent the average excess yield from BES-I projected into the BES-II regime with the size of the uncertainty taken from 200 GeV. The blue dashed line depicts the expected trend of the LMR excess in the BES-II regime as suggested by the according quantity in PHSD calculations (see Figure 5.5). (Right) LMR enhancement factors measured at STAR's BES-I in Au+Au in comparison to Pb+Au measurements by CERES at SPS and Au+Au by PHENIX and STAR at top RHIC energy. The STAR BES-I enhancement factors are derived for two different mass regions for comparison. The energy dependence of the different theoretical scenarios explained in the text is depicted, too.



The measured LMR excess yields in Figure 5.4 (left) are normalized to the invariant pion yields at the respective energy which allows for the comparison to the energy dependence of the total baryon density in Figure 5.5.

Figure 5.5 Energy dependence of total baryon density in Au+Au collisions using the total proton-to-pion ratio as proxy. The BES-II energy regime is overlaid with the expected trend from PHSD for the dielectron excess yield in $M_{ee} = 0.2 - 0.7 \text{ GeV/c}^2$ [21, 22] (yellow band).



In general, protons/pions are the most abundant baryons/mesons emanating from and routinely measured in a heavy-ion collision. The proton-to-pion ratio $(p + \bar{p})/(\pi^+ +$ π^{-}) is about 1/5 at SPS energies and decreases to about 1/10 at RHIC energies as opposed to a ratio of about 1 at AGS energies. Hence, at SPS as well as RHIC energies mesons are the dominating particle species controlling the freeze-out conditions [214] which also makes the proton-to-pion ratio a valid estimator for the total baryon density. This is important in the discussion of LMR excess yields since inmedium modifications to the ρ spectral function are expected to depend on total instead of net baryon density due to the seeming CP invariance of the strong interaction (see Section 4.2 and Section 2.7.1 in [10]). The study in Figure 5.4 (left) does not reveal a strong energy dependence of the excess yield in line with the approximately constant total baryon density for BES-I energies as observed in Figure 5.5.

A possible energy-dependent enhancement which would thus be directly related to earlier creation times, seems to be hidden due the emission of LMR dielectrons during phases driven by hadronic densities and due to the integration of the according rates over the system's temperature evolution profile.

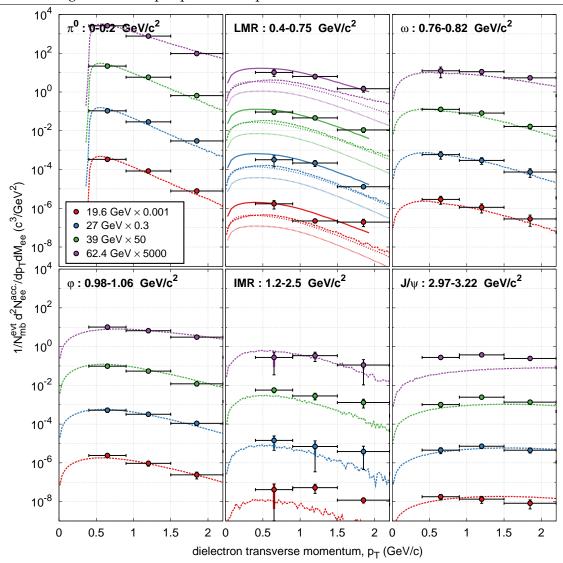
The agreement in energy dependence of measured LMR excess yields and total baryon density in BES-I further raises the interesting question of which trend to expect for the BES-II energy regime. ρ -meson based PHSD calculations [21, 22] predict a relative increase of the expected excess yield $(N_{\rm med}-N_0)/N_0$ in $M_{\rm ee}=0.2$ - 0.7 GeV/c² by about a factor of two which is consistent with the according increase in the measured total baryon densities below $\sqrt{s_{\rm NN}}=20$ GeV in Figure 5.5. This trend is translated to Figure 5.4 (left) and compared to the average excess yield extrapolated from the BES-I regime. Systematic uncertainties from $\sqrt{s_{\rm NN}}=200$ GeV are associated with the extrapolation since statistical errors are expected to be small in BES-II with RHIC's improved luminosities at the community's disposal. It shows that STAR should be able to continue studying the LMR excess yield's trend with decreasing beam energy and its (possible) correlation with total baryon density [23].

The extraction of enhancement factors in Figure 5.4 (right) allows for the comparison to the previously reported results of CERES and PHENIX. Despite different experimental acceptances, the STAR results reach general consistency with CERES at $\sqrt{s_{\rm NN}}$ = 17 GeV while providing higher quality measurements. In comparison to PHENIX, however, the results show a sizeable discrepancy which is not fully resolved yet, since neither the projection of STAR's results into the PHENIX acceptance, nor the detailed comparison of cocktail simulations provide satisfactory explanations ([16], also see Section 1.3).

In the mass range of $0.4 - 0.75 \text{ GeV/c}^2$, STAR's measurements of excess yields as well as enhancements factors are compared to the different theoretical scenarios used in the context of Figure 5.2 and Figure 5.3. Along with the excess yields, one observes an increasing enhance-

ment factor with decreasing energy in agreement with the HMBT in-medium ρ -meson calculations. As a result, the preceding conclusion of a broadened ρ spectral function as preferred scenario for the enhancement, is further supported in its energy dependence by the agreement of the data over the wide BES-I energy range. Hence, for the first time since the NA60 dimuon measurements, its findings regarding LMR enhancement are also confirmed in the dielectron sector with the added bonus of consistency in energy dependence.

Figure 5.6 Efficiency-corrected p_T dielectron spectra in 0-80% minimum bias Au+Au collisions measured by STAR at BES-I energies in six characteristic mass regions of the invariant mass spectrum. Solid lines in the LMR compare the p_T -dependence of LMR yields to the expectations from the total of cocktail and model. Dashed and dotted lines in this region represent the respective contributions (cocktail, HMBT, QGP) to the total LMR yield. Dashed lines in the other mass regions denote p_T spectra as expected from cocktail simulations.



In Figure 5.6, STAR's measurements are extended to the p_T dependence of dielectron production in six characteristic regions of the invariant mass spectrum. Note that, though available in Section 2.4.2, the lowest p_T bin is omitted since it is severely influenced by STAR's acceptance hole and hence suffers large systematic uncertainties during the efficiency correction. The comparison of the enhancement's p_T dependence to medium modifications allows for more resilient conclusions about its source since transverse momentum and invariant mass together cover the full phase space available to dielectrons. In line with the invariant mass

dependence of Figure 5.1, overall consistency with the cocktail and also with the scenario of an in-medium broadened ρ spectral function in the LMR is observed at all BES-I energies. This further strengthens the conclusion of the latter being the correct description for the LMR excess at these energies.

In the projected momentum range, the p_T spectra in Figure 5.6 show an approximately exponential shape. When represented as transverse mass distributions, their inverse slope can be interpreted as the effective temperature T_{eff} of the expanding medium. The observed continuous decrease in slope over the six different invariant mass regions is characteristic for dielectrons emanating from all stages of the expansion and reveals the time-ordered nature of the different dielectron sources [213]. The slopes (T_{eff}) of the p_T spectra in Figure 5.6 also decrease (increase) faster up to the ρ/ω pole mass region than from the ϕ to the J/ψ mass regions beyond 1 GeV/c². Though not directly observed here for the dielectron excess due to insufficient statistics, this is reminiscent of the observations made for the dimuon excess in Figure 1.8c: T_{eff} rises linearly with M_{ee} up to the ρ -meson mass but stays below its expected trend. Referring to the same figure, it is argued in [213] that this is "consistent with radial flow of an in-medium hadronlike source, namely $\pi\pi\to\rho$, decaying continuously into lepton pairs". It is further consistent with expectations that maximal radial flow is reached by the ρ due to the its maximal coupling to pions (c.f. T_{eff} vs. β in Section 1.2).

All the above observations in the dielectrons' M_{ee} and p_T distributions reiterate their unique sensitivity to the space and time evolution dynamics of a heavy ion collision.

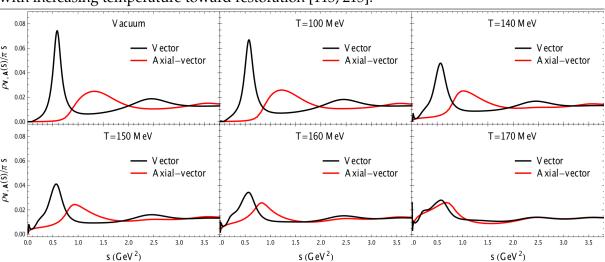


Figure 5.7 Vector (ρ) and axial-vector (a_1) in-medium spectral functions gradually merging with increasing temperature toward restoration [113, 215].

In summary, the results of this thesis can cumulatively be taken as an indication for the *universal* nature of the source underlying the observed enhancement in LMR dielectron production. The theoretical scenario of a broadened ρ spectral function seems to be serving well to describe this source which itself fuels the required progress on the theory side to thoroughly connect the measured ρ spectral function to its chiral partner and arrive at the long-awaited conclusions on possible chiral symmetry restoration. For instance, the authors of [113, 215] subsequently pose the question whether the in-medium vector (ρ) spectral functions describing the dilepton data presented in this chapter, are theoretically compatible with χ SR. Satisfying theoretical constraints and Lattice QCD results, they find a smooth reduction of the a_1 meson's mass and a large increase in its width with increasing temperature (Figure 5.7). The axial-vector spectral function ultimately merges with the vector spectral function which they argue establishes a direct and compatible connection of dileptons and χ SR. They admit that microscopic calculations of the a_1 are imperative and efforts in this direction are ongoing at the time of this writing.

Chapter 6

Summary and Outlook

Quantum Chromo Dynamics (QCD) has emerged [1] as a very successful theory to predict and confirm the properties of the phases in which nuclear matter exists at various temperatures and baryon densities (see Section 1.1). In the QCD vacuum, quarks and gluons are confined into color-neutral hadrons and the global chiral symmetry of the QCD Lagrangian is spontaneously broken [2] which explains the basic features of the experimental hadron spectrum [3]. At sufficiently high temperatures and baryon densities, nuclear matter is expected to undergo a transition into the Quark-Gluon-Plasma (QGP) consisting of deconfined quarks and gluons as the determining degrees of freedom, and accompanied by chiral symmetry restoration [4]. Such fundamental properties of QCD matter can be studied in ultra-relativistic heavy-ion collisions [5, 6] producing a relatively large volume of high energy and nucleon densities as existent in the early universe (see Section 1.2). During its subsequent expansion and cooling, the hot and dense matter created in these collisions goes through multiple stages of QCD phases before hadronizing and freezing out into the observable particles of the QCD vacuum [7]. Measurement of the elliptic flow of mesons and baryons, for instance, sheds light on the thermalization time scale of the medium as well as the degree of collective expansion driven by a possibly partonic source [8, 9]. It is imperative, however, to observe and comprehensively measure (smoking-gun) signals for the two fundamental QCD characteristics of deconfinement and chiral symmetry restoration. Annihilation of $q\bar{q}$ pairs in a thermally equilibrated deconfined QCD medium would result in thermal electromagnetic radiation (directly from the QGP), and modifications of vector meson spectral functions in the medium could reveal precursor effects of the disappearance of the QCD vacuum structure, respectively [10, 11]. The discussion of the latter connection in Section 1.3 identifies the requirement of a coordinated effort from both the theoretical and experimental side to strengthen the conclusions on (partial) chiral symmetry restoration based on dielectron measurements of the ρ spectral function.

Dileptons are unique bulk-penetrating tools in this regard since they penetrate through the surrounding medium with negligible interaction and are created throughout the entire system evolution starting at the early bulk stages (see Figure 1.6). The pairs' invariant mass (M_{ee}) and transverse momentum (p_T) distributions are reminiscent of their time-ordered emission and hence sensitive to the system's evolution dynamics. The Low-Mass- (LMR) and Intermediate-Mass-Regions (IMR) of dielectron spectra, in particular, promise access to the in-medium modified ρ spectral function as well as the effective QGP temperature, respectively, provided for the latter that the contribution by a possibly medium-modified charm continuum is known [12]. A multitude of experiments at SIS18, SPS and RHIC have taken on the challenging task to measure these rare probes in a heavy-ion environment (see Section 1.3.1). CERES has first observed a sizeable and unexplained excess yield in the LMR over a cocktail of expected hadronic sources [13]. NA60's results from high-quality dimuon measurements have identified the broadened ρ spectral function as the favorable scenario to explain the LMR excess, and partonic sources

as dominant in the IMR [14]. PHENIX followed with dielectron measurements at top RHIC energy exhibiting a significant LMR enhancement and good agreement of IMR dielectron production with a charm continuum as expected from N_{bin} -scaled p+p collisions [15]. As opposed to the NA60 results, the former could not be explained in size by the existing model calculations even when exhausting the available parameter space. Measurements of dielectron production at the same energy by STAR at RHIC resulted in a more moderate enhancement consistent with NA60 measurements and with model calculations based on in-medium broadened ρ spectral functions [16]. Note that in the low temperature and high baryon density regime, HADES confirmed the *DLS puzzle* with a measured LMR enhancement factor of about 2 - 3 [17, 18].

The two preceding paragraphs set the stage for the extensive study of dielectron production presented in this thesis. Enabled by the addition of the TOF detector system completed in 2010, STAR provides excellent PID, low material budget, full azimuthal acceptance at mid-rapidity, and wide p_T coverage [19]. Especially in combination with the first phase of the Beam Energy Scan (BES-I) at RHIC [20], STAR presents the unprecedented opportunity for an energydependent study of dielectron production within a homogeneous experimental environment closing the wide gap in the QCD phase diagram between SPS and top RHIC energies (see Section 1.4). This thesis concentrates on the analysis of the beam energies 19.6, 27, 39, and 62.4 GeV recorded in Au+Au collisions during BES-I providing sufficient statistics for such a study (see Chapter 2). In conjunction with the published STAR results at top RHIC energy, this provides the first comprehensive energy-dependent dataset that will also most likely be the only one available in this energy regime for the forseeable future given the enormous effort involved in obtaining it 1 . The results of this thesis (see Chapter 5) include M_{ee} - and p_T -spectra for the four beam energies measured in 0-80% minimum-bias Au+Au collisions with high statistics up to 3.5 GeV/c^2 and 2.2 GeV/c, respectively. Their comparison with cocktail simulations of hadronic sources reveals a sizeable and steadily increasing excess yield in the LMR at all beam energies which cannot be described by ρ/ω vacuum spectral functions propagated through the fireball expansion and much less by the according bare freeze-out contributions. Good agreement over the entire energy range as well as in M_{ee} and p_T shape is instead reached with model calculations within Hadronic Many-Body Theory (HMBT) based on an in-medium broadened ρ spectral function. This contribution dominates in the LMR over $q\bar{q}$ contributions from the QGP and hence universally serves well as the underlying source of the measured enhancement for the entire RHIC energy regime. It also means that most of the enhancement is governed by interactions of the ρ meson with thermal resonance excitations in the late(r)-stage hot and dense hadronic phase. This conclusion is supported by the energy-dependent measurement of integrated LMR excess yields normalized to the invariant pion yields as well as LMR enhancement factors. The former do not exhibit a strong dependence on beam energy as expected from the approximately constant total baryon density above 20 GeV, and the latter show agreement with the CERES measurement at SPS energy despite different detector acceptances while providing higher quality data. The consistency in excess yields and with model calculations measured by STAR over the wide RHIC energy regime makes a strong case for LMR enhancements on the order of a factor 2 - 3 rather than 5 or more.

The energy-dependence of the integrated LMR excess yields allows for an interesting projection into the second phase of the Beam Energy Scan (BES-II). For the energy regime below 20 GeV, measurements of the total baryon density as well as ρ -meson based PHSD calculations suggest an increase of about a factor of two in LMR excess [21, 22]. High-statistics measurements in BES-II should provide enough accuracy to study these predictions and further strengthen our understanding of the LMR enhancement and its underlying source [23]. Besides enhanced statistics, BES-II will provide improved tracking due to the proposed iTPC upgrade,

 $^{^{1}}$ STAR will continue to take high statistics data at $\sqrt{s_{NN}}$ < 20 GeV during BES Phase-II.

and improved capabilities for the measurement of dimuons, for instance. In the present study, reliable conclusions on QGP radiation in the IMR are unfortunately primarily constrained by the available statistics, the uncertainties in $c\bar{c}$ cross sections in nucleon-nucleon collision, and possible medium-modifications of the charm continuum through decorrelation of the e^+/e^- decay daughters. Measurements during BES-II, however, will enable the study of the charm continuum and hence indirectly QGP radiation due to the recently completed upgrades of the HFT and MTD detector subsystems. This is especially important for the LMR since the $c\bar{c}$ contribution to the total cocktail in the 0.4 - 0.7 GeV/ c^2 mass region increases from about 20% at 19.6 GeV up to about 60% at 200 GeV.

In conclusion, STAR's measurements during BES-I provide high-quality datasets essential to improve the understanding of the LMR enhancement regarding its M_{ee} , p_T and energy dependence. The study of its centrality dependence in the near future would complete the extractable results and could reveal new information about the energy dependence of the fireball's life time. The scenario of broadened in-medium ρ spectral functions has proven to not only serve well as dominating underlying source but also to be *universal* in nature since it quantitatively and qualitatively explains the LMR enhancements measured over the wide range from SPS to top RHIC energies. The extent of the results presented here enables a more solid discussion of its relation to chiral symmetry restoration from a theoretical point of view. High-statistics measurements at BES-II hold the promise to confirm these conclusions along with the LMR enhancement's relation to total baryon density with decreasing beam energy.

Part II

Software: STAR and Open-Source Projects

Chapter 7

Contribution of STAR Software Modules

7.1 StV0TofCorrection: TOF Correction of Off-Vertex Decays

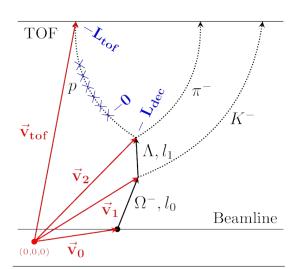
Abstract

The class described in this chapter provides member functions to correct the time-of-flight of daughter particles originating from V_0 decays. The underlying algorithm is based on the reconstruction of mother decay particles. Detailed studies performed by applying the algorithm to Λ - and Ω -decays, demonstrate its background rejection power and prove it to work as expected. As an additional feature, a default cut on the particles' corrected mass is implemented and can be applied by the user to improve the signal-to-noise ratio. The source code of this work has been developed in the last quarter of 2010 and is part of the StBTofUtil [24] module in the official STAR CVS code repository since January 2011. The latest revision of the class implementation is from December 2013. A version of this chapter from December 2010 has been made available to the STAR collaboration as an internal report [25, 26]. This work was supported by the German Exchange Service DAAD.

To identify the species of detected particles, their mass is calculated by means of their velocity β . For this purpose, the particles' time-of-flight (TOF) from their decay vertex to a matched hit in the TOF detector is required. In the case of very short-lived particles their decay vertex can be assumed to coincide with the event vertex. However, due to the non-negligible decay length of V_0 particles, a TOF correction has to be applied to the emanating daughter particles which can be achieved by calculating the time-of-flight for the reconstructed unstable mother particles. By subsequently applying a cut on the corrected mass, a higher ratio of those decay particles can be obtained which actually fit the V_0 decay topology. The class StVOTofCorrection described in this chapter provides the necessary tools for such V_0 TOF corrections. It has been developed for the usage within STAR's analysis framework StRoot. This chapter first explains the implemented algorithm and subsequently tests it by means of Λ - and Ω -decays. It concludes by demonstrating the general usage of StVOTofCorrection accompanied by examples of its application.

Figure 7.1 illustrates the TOF correction algorithm. Blue crosses schematically denote single TPC hits of the proton track. The first TPC hit is taken as origin for the path length measure. The variables used to correct the time-of-flight of a proton produced in the decay chain $\Omega^- \to \Lambda K^- \to p\pi^- K^-$ are shown as well. Using this example the general TOF correction algorithm implemented in the *StV0TofCorrection* class is explained in the following.

Figure 7.1 Sketch for β correction.



Let v_0 be the 3d-vector from the global origin of the cartesian coordinate system to the event vertex, $v_{1,2}$ the 3d-vectors to the decay vertices of Ω/Λ and v_{tof} the 3d-vector to the TOF hit matched with the proton track. Then, the decay lengths $l_i = |v_{i+1} - v_i|$ of Ω/Λ and their velocities

$$\beta_i = \sqrt{1/(1 + (M_i c/p_i)^2)}$$

with M_i the invariant masses and p_i the reconstructed momenta of Ω/Λ , can be used to calculate the Ω/Λ time-of-flights $\Delta t_i = l_i \beta_i c$. For the decay lengths, the mother particle tracks are assumed to be straight regardless of their charge. Deviations caused by this assumption were investigated and found to be negligible. Consequently, the original

proton time-of-flight TOF_p can be corrected via TOF_p' = TOF_p - $\Sigma\Delta'$ t_i'. The use of $\beta_p c = L_p'$ TOF_p and $m_p c = p\sqrt{\beta_p^{-2} - 1}$ provides a way to recalculate the proton mass with its corrected time-of-flight if the corresponding path length L_p' is known. Latter is deduced by evaluating the points on the proton helix which correspond to the distance of closest approach (dca) to TOF hit and Δ decay vertex, respectively. Therefore a function written by Δ . Schmah was adapted to the needs of the class. It iteratively determines the dca of a point to a helix and returns the corresponding path lengths. Given the path lengths on the proton helix to the TOF hit (L_{tof}) and the Δ decay vertex (L_{dec}) the corrected proton path length amounts to $L_p' = L_{tof} - L_{dec}$. Finally, a cut on the corrected proton mass can be applied to reject protons which do not fit the given decay topology. By this means the signal-to-noise ratio can be increased significantly. The preceding discussion holds for all types of V_0 decays independent of particle species or number of decay steps. Therefore, the algorithm has been implemented with unlimited and variable number of function arguments to assure a most general usage.

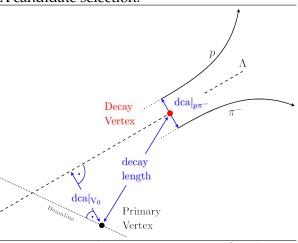
In the following the class functionality and its features are investigated taking the decay $\Lambda \to p\pi^-$ in Au+Au collisions at 7.7 GeV as an example due to its sufficient statistics. For decay reconstruction the set of cuts listed in the following table is used resulting in 34 M candidate combinations.

Table 7.1: Summary of cuts applied for Λ candidate selection

Event Vertex	PID TPC dE/dx	
Vz < 70 cm & Vr < 2 cm	$n\sigma_p < 4 \& n\sigma_\pi < 4$	
Track Properties	Topology	
nHitsFit > 14	decay length > 4 cm	
nHitsRatio > 0	$dca(V_0) < 2.5 cm$	
dca(p) > 0.5 cm & dca(π^-) > 1 cm	dca(p π^-) < 2.5 cm	
0.1	$1.06 < M_{\rm inv}(~p~\pi~) < 1.19~{\rm GeV/c^2}$	

To gain access to the different effects of TOF correction the candidates sample is divided into three sub-samples: In Sub-Sample I only $p\pi$ combinations with β information for both particles are selected to check whether the algorithm works and whether the PID can be improved. In the Sub-Sample I all other cases where a TOF correction is possible are gathered to answer the question of how many candidates can be restored. The last subsample comprises the residual $p\pi$ combinations which do not provide any TOF information. See Table 7.2 for further clarification. The boolean values indicate whether the specific information is available for the track or not.

Figure 7.2 Illustration of cut variables used for Λ candidate selection.



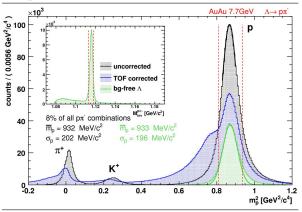
Note that there are cases where TOF information is available for the track but no β information. This is connected to the fact that the timing information for global tracks is not reliable and therefore omitted on MicroDST level.

Table 7.2: List of Sub-Samples

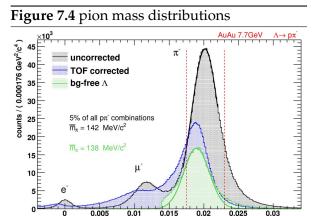
$P_{p} TOF_{\pi}$	F_{π}	TOF_pTOF_π	$\beta_p \beta_{\pi}$
11 Sub-Sample I		*	11
0 & 1 1	1	10 & 11	10
1 & 1 1 Sub-Sample II	1 Sub-Sample II	01&11	0 1
01&11	:11	10 & 01 & 11	0 0
0 0 Sub-Sample III	Sub-Sample III	0 0	0 0

Figure 7.3 shows a comparison of mass distributions for protons steming from $\Lambda \to p\pi^-$ decays. For the sample with available β information for each decay track, distributions are plotted with (blue) and without (black) applied TOF correction. A scaled mass distribution (green) for a background-free Λ sample (inlet) is shown as well. The cut applied on the p π invariant mass is 1.113 - 1.118 GeV/ c^2 . Solid lines represent Gaussian functions fitted in the range $0.83 < m^2 < 0.9 \, GeV^2/c^4$. Resulting parameters are given in corresponding colors. Red dashed lines indicate the applied mass cuts for particle identification. The percentages given in this and the following figures are

Figure 7.3 Proton mass distributions for subsample I



based on the total initial number of $p\pi$ combinations. No differentiation has been made regarding the changing momentum resolution. As its main feature the TOF correction algorithm changes the mass distributions with respect to the origin of the particle: the distribution of protons which do not fit the specific decay topology are shifted to lower masses and broadened see the shoulder of the blue distribution. Whereas true protons stay at their original mass. This can be proven by generating a background-free Λ sample using tighter and additional cuts - see inlet in Figure 7.3. The Gaussian function fitted to the resulting scaled mass distribution is not shifted and its extrapolation does not reveal any underlying or broadened structure. Applying a cut on the squared proton mass inreases the separation power of Λ - and non- Λ -daughters.

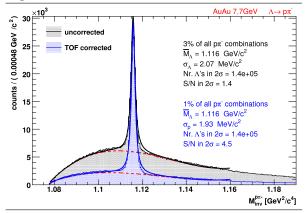


The pion mass distributions after the proton mass cut are shown in Figure 7.4 using identical color code. The aforementioned cut on the proton mass is already applied. Here the non- Λ -daughters can only be seen as tails at the lower mass end of the pion distribution not allowing a separation as clear as for protons. However more important, the mean pion mass is shifted by $3 \text{ MeV}/c^2$ to its nominal mass. Thus, using the TOF correction algorithm accounts for the systematically off pion mass intrinsically.

Figure 7.5 compares the $p\pi$ invariant mass spectra with (blue) and without (black) applied TOF correction algorithm. The distributions are fitted with Breit-Wigner + higher order polynomial functions (solid). There are two major improvements to be emphasized:

 $m_{\pi^*}^2 \left[GeV^2/c^4 \right]$

Figure 7.5 $p\pi$ invariant mass distributions



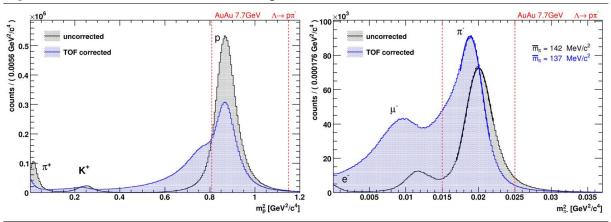
- The number of reconstructed Λ's stays constant which proves that mainly non-Λ-daughters have been rejected by the new proton and pion particle identification.
- The signal-to-background ratio improves by more than a factor 3. A comparable effect can be seen for the case of incomplete TOF information. This nicely shows the background rejection power of the algorithm for the cases of TOF information being available.

Unfortunately, the current sub-sample only covers 8% of the total number of Λ can-

didates. The residual sub-samples therefore dominate the signal-to-background ratio with respect to the overall achievable improvements.

Figure 7.6 shows the mass distributions for sub-sample II with (blue) and without (black) applied TOF correction. Red dashed lines indicate the mass cuts used for particle identification. In general, the distributions for both particles indicate the same features as discussed in the previous section, i.e. non-decay-daughter separation and pion pole mass shift. However, in addition a gain of 35% can be observed for the pions in a 2σ range around the respective mean masses. These are pions whose time-of-flight was intrinsically reconstructed by the algorithm using the matched TOF hit but which originally did not have a β information associated (see Table 7.2). For this sub-sample, particle identification cuts on the proton and pion mass have been applied as well (indicated by red dashed lines in Figure 7.6).

Figure 7.6 mass distributions for sub-sample II



The comparison of the resulting $p\pi^-$ invariant mass distributions is shown in Figure 7.7. Even for the current statistically dominant sub-sample (60%) a significant improvement (factor 2.3) in signal-to-background ratio can be observed suffering only a small signal loss. Latter could mainly be caused by the fact that the applied mass cuts have rather been chosen in favor of the uncorrected distributions.

The final $p\pi^-$ invariant mass spectrum is shown in Figure 7.8. The corrected spectrum shows a slightly smaller width and a non-significant decrease of 10% in the number of Λ s.

Regarding the signal-to-background ratio an overall improvement of approx. 40% is achieved. The comparably lower gain in contrast to *Sub-Sample I* and *Sub-Sample II* is due to the poor signal-to-background ratio of the sub-sample in which no TOF correction is possible at all. Nevertheless these improvements show the importance of applying a TOF correction to the tracks of V₀ decay particles regarding background suppression.

In addition to the preceding Λ analysis the TOF correction algorithm was applied to the decay $\Omega^- \to \Lambda K^- \to p \pi^- K^-$. The corresponding plots can be found in Figure 7.9. Applying to-noise ratio by a factor of 1.5 in this case.

Figure 7.7 Comparison of Λ invariant mass spectra with and without TOF correction

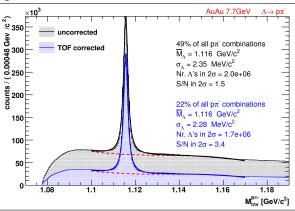
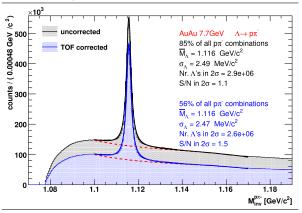
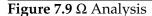
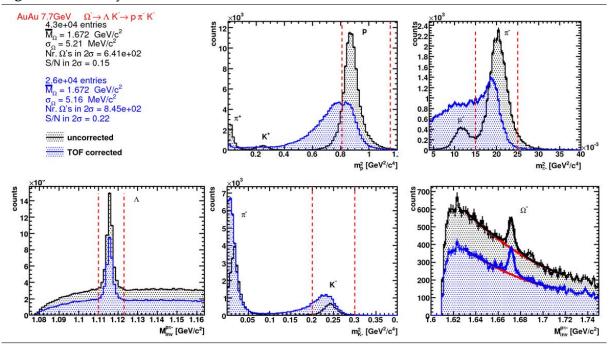


Figure 7.8 Overall influence of TOF correction on the Λ signal



ing plots can be found in Figure 7.9. Applying a TOF correction results in an increase of signal-to-noise ratio by a factor of 1.5 in this case





In general, the class is supposed to be initiated once by calling its constructor. The member functions <code>setVectors3D</code>, <code>setMotherTracks</code> and <code>correctBeta</code> are afterwards used multiple times for the TOF correction of each decay particle. Hence, these member functions have to be invoked for each combination of daughter particles in the following order. Remember to call these functions each time as a block.

setVectors3D(v0)(v1)...(vn)(vtof)

This function sets all the space vectors needed for TOF correction. The function arguments v0...vtof are all of type StThreeVectorD and define the vectors to the following space points.

- v0: event vertex / primary vertex
- v1...vn: vertices in decay chain resulting in the final particle to be corrected
- vtof: TOF hit

Special care has to be taken of the vectors' ordering: Start with the event vertex and add the vertex vectors as you follow the decay chain to the final particle and its TOF hit. The final argument of setVectors3D always corresponds to the TOF hit vector.

The event vertex does not change on a candidate-by-candidate basis, of course. Nonetheless, it is given to setVectors3D as an argument to simplify the implementation and to minimize the functions to be called by the user. Make sure to start TOF correction only if a TOF hit for the particle exists! Carefully check the original time-of-flights given as an argument to the correctBeta function!

The operator () is overloaded to allow for a variable number of arguments to be given to the function and pack them into an inline container sequentially. Thus, make sure to put each function argument inside brackets as indicated in above.

Starting gcc 4.3 the so called *variadic templates* were included in the compiler. These function templates accept a variable number of arguments (*parameter rack*) which can be accessed and unpacked via the ellipsis (...) operator. This approach would have been a more elegant way to implement the class. Unfortunately, variadic templates will only be understood within the new C++0x standard which presumably will be published at the end of 2011.

setMotherTracks(t0)...(tn-1)

Call this function to set the reconstructed 4-momentum vectors t0...tn-1 of type StL orentzVector for all mother particles. Keep the warning in setVectors3D in mind! The number of arguments given should be smaller by 2 compared to setVectors3D. If not, the code compiles nevertheless but results in an error message during runtime.

correctBeta(helix,tof,betacorr)

This is the main function of the class. It takes the helix of type StPhysicalHelixD and the original time-of-flight tof of the particle to be TOF corrected and writes the corrected particle velocity into betacorr. The variable betacorr can afterwards be used to calculate a new particle mass and utilize it for particle identification. Alternatively, correctBeta can be called as correctBeta (helix, tof, betacorr, p, enum) with p the particle's momentum and enum the particle species. In this form a default hard-coded m^2 -cut is applied to the particle's mass and the result returned as boolean value (enum definition: 0 = pi, 1 = K, 2 = p).

clearContainers()

This function needs to be called to clear all inline containers before TOF correcting the next particle. To assure the filling of a clean container, allocated memory and pointers are deleted in this function. It could be done automatically after the TOF correction is finished. However, the user is encouraged to do it manually to have a more memorizable and controllable block of functions.

Section B.1 gives two examples of how to use the StVOTofCorrection class and its member functions. The first example shows the case of correcting a particle with one mother particle and the second the case of two mother particles. Both examples are illustrated in Figure 7.1.

7.2 StBadRdosDb: Database Interface for TPC missing RDOs

The class <code>StBadRdosDb</code> has been developed to use information about the TPC's number of missing read-out boards (RDO) during a physics analysis. The data taken in runs 10 & 11 are divided into <code>run ranges</code> with equal number of missing RDOs and the result stored in a custom database format. <code>StBadRdosDb</code> can then be used to acquire the current run range given a specific run id. This is especially helpful for analyses which rely on stable detector conditions throughout a beam time and thus are sensitive to a run-range-dependent efficiency correction. Upon request by <code>STAR</code>'s physics working group for bulk correlations, <code>StBadRdosDb</code> has been announced to the collaboration [27] and made available in the <code>STAR</code> CVS [28] as well as the author's code repository [216]. The <code>makeRunList.pl</code> script used to generate official <code>STAR</code> run lists for each beam time and available in a common area of <code>STAR</code> scripts [217] has been modified to query the central <code>STAR</code> database for the number of missing RDOs per subsequent run and the according <code>TPC</code> sectors and RDO id's. It has been extended to deal with 2010 as well as 2011 data. The queried dataset is reduced to the list of run id's at which the number of missing RDOs changes. Given the correct trigger setup name and year the <code>genBadRdosDb.pl</code> script is executed as

\$ perl genBadRdosDb.pl AuAu39_production 2011

See the RunLog browser [218] for information on the trigger setup name. For convenience, the code repository contains a bash script to (re-)generate all database files: database/genAll. sh. If database files for upcoming beam energies are generated one should make sure that the trigger selection in the genBadRdosDb.pl script covers all runs needed in the respective data analysis. The <code>StBadRdosDb</code> class does not require any STAR libraries to be loaded and solely relies on ROOT. It provides the following member functions to retrieve information about missing RDOs and their respective run ranges. For their usage see the <code>testStBadRdosDb.C</code> ROOT macro.

Int_t GetRunRange(Int_t runid);

This function is considered the main purpose of the *StBadRdosDb* implementation. It returns the run range index for a given run id.

Int_t GetNrRunRanges() { return NrRanges;}

A helper function returning the total number of run ranges. It can be used to define arrays and histogram ranges for run-range dependent analyses.

Int_t GetNrBadRdos(Int_t run_range);

An informational function returning the number of missing RDOs for a given run range.

Int_t GetSector(Int_t run_range, Int_t nrdo);

Get Sector returns the sector to which a specific missing RDO with index nrdo in run range run_range belongs.

Int_t GetNrBadRdosSector(Int_t runid, Int_t sector);

retrieves the number of missing RDOs for a specific run id and sector.

Int_t GetFirstId(Int_t rr) { return prun[rr];}

Helper function to get the first run id in the database for a specific run range.

Table 7.3 lists an examplatory database file used by the member functions of *StBadRdosDb* to provide information about the missing RDOs of a specific beam time. All energies for the years 2010 and 2011 have been included in the database (Section B.2). Each line in the database files indicates the start of a run range containing run id's with equal number of missing RDOs. The second column shows the number of missing RDOs in this range followed by the according number of RDO *identifiers*. Each identifier encodes the missing RDO's sector and identification number (format: sector.id). These identifiers are encoded in genBadRdosDb.pl and decoded in the class member functions GetSector and GetNrBadRdosSector.

RunID	# bad RDOs	RDO identifiers (sector.id)
11148001	3	17.01 23.02 23.08
11151010	4	11.10 17.01 23.02 23.08
11151028	3	17.01 23.02 23.08
11151040	4	17.01 21.11 23.02 23.08
11151080	5	01.07 17.01 21.11 23.02 23.08
11152053	6	01.07 07.05 17.01 21.11 23.02 23.08
11153012	7	01.07 01.09 07.05 17.01 21.11 23.02 23.08
11156032	8	01.07 01.09 07.05 09.03 17.01 21.11 23.02 23.08
11158011	9	01.07 01.09 07.05 09.03 11.01 17.01 21.11 23.02 23.08

Table 7.3: StBadRdosDb database file for 11 GeV recorded during run 10.

7.3 StRunIdEventsDb: Database Interface for Run Id Indexing

StRunIdEventsDb has been developed to facilitate handling the run-dependent studies for the multiple beam energies analyzed in Part I of this thesis. The class implementation provides a mapping from a specific run id to its corresponding index for all energies of STAR's beam energy scan during runs 10 & 11. Moreover, the number of events can be retrieved on a runby-run basis for each trigger at all energies.

Analogous to Section 7.2 the perl script <code>genRunIdEventsDb.pl</code> is used to generate the database files. The following literal block - which also serves as configuration file for the

StRunIdEventsDb class - lists all triggers for a specific combination of energy and year. Figure 7.10 shows database excerpts for 39 and 62 GeV with index, run id, and corresponding number of events per trigger. The full database and the code are available in the author's code repository [219].

database/config

Figure 7.10 database excerpts for 39 and 62 GeV

	-				
[058	6] 11112017	00474150	00045887	00023399	00499950
[058	7] 11112018	00473755	00046888	00024117	00499989
[058	8] 11112019	00476851	00047345	00023548	00499916
[058	9] 11112020	00478675	00048222	00023583	00499951
[059	0] 11112021	00477492	00051072	00024213	00499887
[059	1] 11112022	00319775	00035458	00016388	00341242
[059	2] 11112023	00476084	00054814	00023762	00499047
>	loaded RunIdEventsDb'	s database_39 wi	th 593 RunIds		
7070	3] 11098051	00136672	00000000	00037889	00263639
[076	4] 11098052	00140473	00000000	00035999	00257227
[076	5] 11098053	00142025	00000000	00034440	00254305
[076	6] 11098054	00144032	00000000	00032893	00251295
[076	7] 11098055	00081684	00000000	00016386	00135279
[076	8] 11098056	00095806	00000000	00018140	00156450
	loaded RunIdEventsDb'	s database_62 wi	th 709 RunIds		

StRunIdEventsDb has been implemented as a singleton class to avoid repeated loading of the database into memory. Hence, the constructors are declared private and a public member function is added which decides on returning a pointer to a newly created instance of StRunIdEventsDb or to an already existing one. To assure singleton behavior this pointer is declared a private static member. It therefore suffices to initialize the class and load the database via

```
StRunIdEventsDb* db = StRunIdEventsDb::Instance(mEnergy, mYear);
```

The following class member functions are implemented to communicate with the database.

```
Int_t getTotalNrRunIds() { return mNrRunIds;}
    get the total number of run id's

Int_t getRunIdIndex(const Int_t& runid);
    get the index for a specific run id

Int_t getRunId(Int_t ind);
    get the run id for a specific index

Int_t getNrEvents(string tn, Int_t runid);
    get the number of events for a specific runid and trigger name

void printAllTrigNames();
    print all trigger names available for this energy and year

string getTrigName(Int_t n);
    get a single trigger name according to the index of printAllTrigNames()
```

Chapter 8

Transition of STAR CVS to a modern Revision Control System

The use of a revision control system to track the changes of its code basis is essential to the progress of a software development project. STAR is in no way different to other large technology companies in that many submodules exist for STAR's detector subsystems with different people responsible for each of them. Regarding one of the largest experiments in heavy ion physics, however, there is progress made not only in terms of pure software improvements for data analyses but also an ever increasing amount of submodules needs to be added each year accompanying STAR's detector upgrades. Still, along with the data itself, code used to process the data taken during previous beam times needs to be available to ensure reproducibility of published results and possible reproduction of DSTs when new knowledge is acquired or bugs identified. In addition, running experiments like STAR involves a myriad of custom-built tools needed for tasks such as data acquisition and backup, online monitoring and analysis, database organization and interfaces, detector alignment and calibration, track reconstruction and detector matching during data production, Monte Carlo simulations, ticket/issue submission, documentation, and publications. Hence, STAR's code organization closely resembles the development structure and release cycles of other large software products with hierarchical work flows and a policy which requires all code to be made accessible to all collaborators. On top, most of the data analysis in STAR is conducted on multiple remote computing sites at all of which identical code deployments have to be guaranteed despite differing development environments.

All this requires maintaining a centralized revision control system like the *Concurrent Versions System* (CVS) [220] which currently is STAR's system of choice. Since its beginnings, STAR has collected an immense amount of code and developed a workflow heavily centered around CVS with many tweaks to customize it. Even though other centralized successors (Subversion, for instance) have been released to overcome some of CVS's shortcomings, STAR's very active data taking and publication cycle have not allowed for a transition to newer systems. However, with the rise of distributed revision control systems like *git* [221] for instance, the many advantages of modern revision control systems do seem to make a re-evaluation of STAR's current system necessary. Some of these advantages include instant and cheap creation and deletion of branches, branch merging and rebasing, working without connection to the remote (central) repository, significantly compressed repository sizes, fast repository cloning, temporary stashing of changes as well as selective staging and committing.

There exist many distributed revision control systems but especially *git* has gained traction and became very popular through the immersion of social coding and with it an increased number of open source contributions. Judging by the popularity of it, *git* seems to be best suited to support a developer's workflow as it encourages frequent commits and work on parallel feature branches. Thus, likewise in STAR, collaborators seem to prefer the use of *git*

for their private analysis code development which starts to increasingly collide with or at least inhibit the contribution to STAR's central CVS repository. In general, due to the expensive nature of branching in CVS most of the code developed by the physicists in STAR seems to stay untracked in their home directories and unshared through the designated user areas in STAR's CVS. It therefore seems to be time for an overhaul of STAR's revision control system and a transition to one of the modern distributed systems.

The following two requirements need to be kept in mind, though. First, STAR's policy requires *git* as a distributed revision control system to be used in a centralized but modular manner. A spread of the entire STAR software with each checkout through many home directories is unfavorable. Second, concerns about manpower almost dictate the use of already available and established open source solutions particularly because the transition would have to happen during ongoing operations. At the same time, these solutions should have a good chance of long-term support or be already stable enough for STAR not to depend on their fate.

This chapter will not discuss the merits of one revision control system over the other but give a specific suggestion on how a transition could be carried out with the best chance of going through smoothly. It is assumed that *git* would become the new revision control system of choice without discussing its advantages or disadvantages when compared to other distributed systems. This chapter concentrates on the execution of a transition from CVS to *git* by demonstrating that history conversion of all STAR CVS submodules is feasible via *cvs2git* and by introducing *gerrit* as the new review system for future code changes and gateway for all sorts of interactions with the central repository. This includes providing the necessary scripts and instructions as well as deploying an instance of the review system on a remote server for demonstration purposes. *cgit* is proposed as a replacement for *cvsweb* as web service to browse the repository.

Section 8.1 motivates and explains the proposed solution and Section 8.2 discusses a list of requirements in the framework of the proposed solution. In Section 8.3 *gerrit* is set up on a remote server with *cgit* as external browser, STAR's CVS is converted into multiple git repositories, synchronized to the remote server and added to *gerrit*. Finally, Section 8.4 gives instructions on how to interact with the demonstration deployment as an end user. Note that this chapter is of special importance to STAR as it introduces a solution for modernizing its revision control system. It will serve as documentation to accompany the migration to the new system and provide references to documentation to ease the user's transition from CVS to *git*.

Introductory Comment on Git for CVS Users. Git is commit based with all the rest being almost exclusively pointers. Each commit has a parent, and each branch is based on a commit. That's why git is light in committing and branching. A tag in git, for instance, is only a pointer to a single commit and as such a direct connection to go back to a certain point in time. In general, git is fundamentally different from CVS in that its revisions **are** snapshots of the directory at a given point in time unlike CVS where everything is file based. Git for instance, records file renames and moves perfectly fine.

8.1 Proposed Solution: Git + Repo + Gerrit + CGit

Due to the distributed nature of *git* the concept of submodules is not equivalent to CVS. Submodules in CVS can be checked out and committed to separately while the minimum *unit* for a checkout is defined by one *git* repository. Submodules in *git* [222] are generally used for foreign libraries which evolve entirely separately but on which the software itself depends on. They are not checked out together with a *git* repository but need to be initialized and synchronized separately. The day-to-day usage of *git* submodules has some serious trip falls and is rather cumbersome which is why the community tends to avoid them. Hence, the "imitation" of a central CVS repository with *git* is better realized using independent *git* sub-repositories whose interplay is controlled via a wrapper script and a configuration file. This way multiple

sub-repositories can be checked out and worked on simultaneously while global tagging and branching is maintained by the wrapper script.

Google's Android Open Source Project (AOSP) has this issue already resolved and developed such a wrapper script in python called *repo* [223]. It uses a so-called manifest configuration file in xml format to organize the structural layout of the project and the remote location of the repositories as well as coordinated checkouts of specific versions. It does not replace *git* but operates "on top of git" [224]. AOSP's workflow is directly applicable to STAR's as it is general enough to serve as a template for any major collaborative software development project. AOSP's workflow using *repo* is very well documented [225] and with its millions of lines of code well-proven in an heavy software development environment. These are good credentials for STAR to use it and not to fear its near-term obsolescence.

The same counts for *gerrit* [226], a web-based code review tool which controls all the interaction with the single *git* repositories including amongst others merging patches into the master branch [227]. *Gerrit* achieves this control mechanism by running ssh and http daemons on two different non-standard ports. Not only does it provide a stream-lined, documented and self-sustained code review, its configuration also covers many aspects of centralized collaboration code development. For instance, it provides automated builds via the Jenkins trigger [228] and code changes will only be accepted and merged if they pass the build process and according (unit) tests. It includes email notifications, sign-offs etc. and even a REST API [229].

The standard repository browser *gitweb* comes with every *git* installation by default and can be configured to be used in *gerrit*. It is suggested, however, to use the *cgit* browser [230] instead which is more feature-rich and easily exchangeable with *gitweb* in *gerrit*. *cgit* is written in C and includes caching if desired, both of which make it extremely fast and very responsive. *cgit* is straight-forward to set up and its development is very active. In March 2013 it has been selected by the Linux Kernel as its primary repository browser [231, 232].

In a nutshell, git + repo + gerrit + cgit gives STAR the best chances to succeed in a CVS to Git migration while significantly modernizing its workflow and code review.

8.2 STAR specific Requirements and Requests

In the following a list of requirements and requests which are specific to STAR is discussed. These items have been identified as important questions to STAR through discussion with the project leader of STAR's software & computing group, Dr. Jerome Lauret (jlauret@bnl.gov).

Centralized Workflow with Feature and Development Branches

In the past, the lack of convenient use of feature and temporary branches in CVS has caused users to maintain copies of entire CVS submodules of StRoot/ in their designated user area at offline/users/. The user areas do not serve the purpose of maintaining official STAR code until it is ready to be committed into the main branch. They exist as an area for users to share code which is not STAR official but still of interest for the entire collaboration. Thus, the new system has to enable the use of development and feature branches for the user to work on while still within the central repository. Also, the new platform has to take care of the organization of these parallel branches in terms of sharing, reviewing and merging with the main branch and core development.

These concerns and appearances of "offline-branching" and inconvenient parallel development are what caused the development of *git* in the first place. Together with *repo* and *gerrit* as tools to organize the interplay of many git repositories as well as the parallel coding of multiple developers, the new system proposed in Section 8.1 covers all possible aspects of such a development environment in a very convenient and well documented manner. See the quick intro of *gerrit* for a standard "life of a patch" [227].

Moreover, even though *git* is of distributed nature all code committing must be encouraged to go to a central repository. This principle is enforced by STAR rules and must not

be violated when switching to a new revision control system. Here again, the usage of many git repositories as a joint central entity is the main purpose for the development of *gerrit* by AOSP as outlined in Section 8.1. *Gerrit* serves as the sole gateway to the repositories and while it is possible to push directly to the git repositories behind *gerrit* and thus entirely circumvent the review, this is not desired and can be switched off completely.

Authentication and Authorization

In contrary to a publicly accessible open source project such as AOSP, strict authentication and authorization mechanisms have to be enforced in STAR. These methods have to be consistent with BNL policies. For instance, users without valid RCF account are not to be allowed write access to repositories served by the new platform.

In its default setup *gerrit* manages users and its logins via the OpenID mechanism. Internally users are organized in groups with specific access rights globally or on a per project basis. *Gerrit* provides ACL authorization like CVS does but its capabilities allow very fine grained and extensive control of the repositories and its branches (see [233]). For authentication already existing kerberos accounts can be used instead of OpenID. This is not in the scope of the demonstration deployment of this chapter as it would only be possible to implement on a dedicated server at BNL with access to krb5.keytab [234]. This needs to be explored after the user's reception of the new system has been reviewed. Hence for simplicity, the demonstration deployment of the *gerrit* instance in this chapter will only be based on a single user login (*protected*) and multiple associated e-mail addresses and ssh-keys (see Section 8.4).

Two aspects of authentication and authorization will have to be evaluated in the future. First, having an automated mechanism to port the current CVS access rules (karma) into *gerrit* would be favorable to preserve access rights to repositories and branches. Second, CVS currently does not have truely public areas which are not subject to STAR's access control. STAR might profit if such areas would be realizable with the new platform enabling STAR collaborators to participate in community work.

gitolite [235] is an alternative AA system to setup access controlled hosting of git repositories. Access on per project and per branch basis is configured via a dedicated gitolite-admin repository with a central configuration file and public ssh-keys. It integrates very well with cgit, too, and repo can still be used to organize multiple git repositories at once. Without a gerrit instance, however, repo upload is redundant, of course. Gitolite is a very good option for the hosting of git repositories with a small number of developers who organize the control of a small amount of development and feature branches themselves and do not need automated code review nor continuous build integration. Thus, to secure the long-term stability of code organization and review in STAR gerrit seems to be better suited.

Demonstration Deployment and Trial Phase

For the final migration to *git* and the associated deployment of the *gerrit* platform a phase of daily incremental conversion of CVS to *git* history would not necessarily be required. During a trial phase with a *gerrit* demonstration deployment — as is the goal of this chapter — CVS and *git* could run in parallel and even diverge. The demonstration deployment of this chapter will already put in place a full conversion of STAR's CVS repository for users to play with. In addition, it shall encourage the involvement of the people responsible for each repository to thoroughly check their converted history. This should help in identifying failed conversions of single commits as well as possible merging or splitting of historically linked CVS submodules into *git* repositories. Following this feedback, these requests can be scripted into the automated conversion (see Section 8.3) before a date is scheduled for the final migration at which the STAR's CVS repository is retired for good.

Repository Browser

The core of STAR's developer team is long-time used to the *cvsweb* experience of browsing code and its history. The proposed repository browser *cgit* already provides a large set of features and comes very close to the conception of browsing code in STAR. Contrary to STAR's CVS, the new system will not have the entire STAR CVS repository and all its submodules mangled into one big *git* repository but split them up into many smaller ones organized by the *repo* script. Thus, the *cgit* browser will serve these repositories as independent unrelated entities. It allows, however, to organize the repositories into categories which significantly facilitates the browsing. Pagination can be switched off such that the general layout of the *cgit* browser will look like the Linux Kernel's [232]. *CGit* further features sorting the repository listing on its landing page based on name, description, owner and idle time. Together with the very fast search function, the list of repositories can quickly be reduced to the ones of interest to the user.

Still, *cgit* is an open source project and thus helpful features like "Expand/Collapse Categories" can be suggested to the community or contributed. As for the representation of a repository itself in *cgit*, functionalities present in *cvsweb* are mostly implemented in *cgit* [236], too, but will need some getting used to on the user's side.

In the author's opinion only *GitLab* [237] would be a serious alternative candidate to use as repository browser. Rather than only being a repository browser, however, it aims at being an open source alternative to the popular *GitHub* social coding platform [238]. Hence, it does not fit STAR's requirements to interface with *gerrit* as well as *cgit* does.

8.3 Migration from CVS to new System

This section documents in detail the steps to be taken to first set up a gerrit instance on a remote server with cgit as an external repository browser (Section 8.3.1) and then convert the CVS submodules StRoot, kumacs, pams, StDb, StarDb, asps, QtRoot, StarVMC and mgr into git repositories (Section 8.3.2). The converted repositories will also be added to the gerrit review system.

The demonstration deployment of gerrit in this section will only rely on a simple single sign-on via HTTP authorization. The credentials are chosen to be the common ones for access to usual STAR protected areas. This allows all STAR collaborators to interact with the system with administrator priviledges given that they add their ssh-key to the *STAR Protected* user on gerrit as described below. However, it still restricts read access to STAR's code to its collaborators only. This is by design such that all collaborators contributing to the STAR code repository can try out the new system before a production deployment with fine-grained access control is started.

The gerrit instance which will be set up in the following will also be used to serve all scripts and configuration files necessary for the deployment in a dedicated repository named *git4star*. Thus on all sites and for all users interacting with the gerrit review system a dedicated ssh-key pair has to be generated and its public key uploaded to the *STAR Protected* user on gerrit ¹. This needs to be done for end users uploading changes as well as admins converting CVS repos and creating projects. The source codes for the shell scripts are also appended to this thesis in Section B.3.

Last, the following entry needs to be added for the *gerrit4star* host to ~/.ssh/config. After that connecting to gerrit via ssh gerrit4star should present itself with a welcome message and exit. All the subsections in this section assume that the reader can clone the *git4star* repository via git clone gerrit4star:git4star on all sites.

Host=gerrit4star
Hostname=gerrit4star.the-huck.com

¹ http://gerrit4star.the-huck.com/#/settings/ssh-keys

```
User=<replace-with-STAR-Protected-username>
Port=29418
IdentityFile=~/.ssh/<replace-with-ssh-key-name>
IdentitiesOnly=yes
```

8.3.1 On the Web Server

Assumptions

Gerrit runs under a dedicated *gerrit4star* user at the domain http://gerrit4star.the-huck.com with the external cgit browser at http://cgit4star.the-huck.com.

Apache Configuration

As super-user, setup a name-based virtual host to serve cgit at http://cgit4star.the-huck.com [239] and second one with reverse proxy and HTTP authentication for the gerrit review system at http://gerrit4star.the-huck.com (see [240, 241]). Restrict access to both by adding the *STAR Protected* user to htpasswd and including the appropriate section in the apache configuration. This user will later be used as single sign-on and thus administrator login to gerrit as well as for all repository interaction through ssh (see above's ~/. ssh/config). Example cgit4star.the-huck.com and gerrit4star.the-huck.com apache configuration files are available in the git4star script repository (see following step).

Get *git4star* script repository

```
As gerrit4star user, clone the git4star script directory: git clone gerrit4star:git4star $HOME/git4star
```

Setup cgit browser

The following will clone, init, config and install cgit [242]. It will configure the cgit.cgi script to be installed in \$CGIT_SCRIPT_PATH and anything else in \$prefix. Adjust both in cgit.conf to reflect your web server setup.

```
git clone git://git.zx2c4.com/cgit $HOME/cgit
cd cgit && git submodule init && git submodule update
# copy cgit config file
cp $HOME/git4star/cgit.conf $HOME/cgit/
make -j4
# switch user if 'gerrit4star' doesn't have sudo perms
# go back to 'gerrit4star' user afterwards
sudo make install
# copy cgitrc to $CGIT_CONFIG (see cgit.conf)
cp $HOME/git4star/cgitrc $prefix/etc/cgitrc
# go to http://cgit4star.the-huck.com to see whether cgit runs
# ignore "no repositories found" message
```

Install gerrit

The code below downloads, installs and configures the HTTP proxy for gerrit [243]. The <code>configureHttpProxy.sh</code> script also starts the ssh and http daemons. http://cgit4star.the-huck.com should now list an <code>AllProjects.git</code> repository which appears to be empty and visiting http://gerrit4star.the-huck.com should now show the gerrit welcome page after logging in using the <code>STAR</code> protected credentials. Fill out "Full Name" as well as optionally register an e-mail and add a ssh-key.

```
cd $HOME # for gerrit4star user
wget https://gerrit-releases.storage.googleapis.com/gerrit-2.6.1.war
```

```
# the following batch install will raise a FAILED notice but that's \lower
java -jar gerrit-2.6.1.war init --batch -d $HOME/gerrit_review
~/git4star/configureHttpProxy.sh
```

Configure CGit as external browser

Gerrit will still show links to its internally handle gitweb browser. Running \$HOME/qit 4star/configureCGit.sh configures cgit as external browser instead of gitweb. For the final \$HOME/gerrit_review/etc/gerrit.config see the \$HOME/git4star/ gerrit.config file in the git4star script repository. Check the cgit links for AllProje cts.git in gerrit after configuration to confirm a correct configuration.

Final Step

Set additional access rights "Create Reference" and "Push Merge Commit" for administrators under refs/* at http://gerrit4star.the-huck.com/#/admin/projects/All-Projects,access. This is later needed to push the newly converted CVS repositories directly into gerrit.

8.3.2 In a Working Directory at BNL with CVSROOT Access

Assumptions

All of the following code will be executed within a dedicated working directory. Access to the *git4star* script repository is assumed as well.

```
<WORKDIR> = /star/institutions/lbl/huck/star_cvs2git/
```

Convert STAR CVS

The following code downloads and unpacks cvs2git [244]. The CVS submodules StRoot, kumacs, pams, StDb, StarDb, asps, QtRoot, StarVMC and mgr are then converted to git via the convertStarCVS.sh script. Make sure to check the environment variables in this script before executing it!

```
cd <WORKDIR> && git clone gerrit4star:git4star
wget http://cvs2svn.tigris.org/files/documents/1462/49237/cvs2svn ↔
   -2.4.0.tar.qz
tar -xvzf cvs2svn-2.4.0.tar.gz
cd git4star
# the following converts all repos and takes about 1.5h!
./convertStarCVS.sh | tee cvs2git.log
```

Two remarks on the conversion of CVS to git. First, the conversion of STAR's CVS repository to git for production deployment of gerrit would require a list of all CVS committers in the format *username* : *Full Name* <*E-Mail*> to be fed into the conversion. This list would map usernames to the format in which git uses them because each git commit requires the committer to provide an e-mail address, too. This is due to the principle that committers should minimally be reachable by e-mail. Such a list could be either generated by using the finger command or direct access to a database at BNL providing this information. Second, a general freely choosable "cvs2git" user including name and e-mail would need to be provided during the conversion. This user gets used for commits for which CVS does not record the original author. More information about these details can be found in the my.cvs2git.options file in the *git4star* script repository.

Create and upload Gerrit Projects

Running createGerritProjects.sh in \$workdir/git4star creates all projects in gerrit and pushes the according repositories to gerrit. The script also adds sign-off and change-id requirements to all projects in gerrit.

Write Manifest for repo

When executing the writeManifest.sh script a default manifest named default. xml is generated based on the converted CVS repositories which can later be used to initialize the STAR repository for the use with the *repo* script (see Section 8.4).

	git (MB)	CVS (MB)
StRoot	363	480
kumacs	14.8	1.74
pams	37.6	128
StDb	6.47	4.58
StarDb	199	576
asps	16.1	47.5
QtRoot	16.3	12.5
StarVMC	47.5	116
mgr	4.66	5.93
total	705	1373

Table 8.1: Overview of repository sizes

8.4 End User Instructions for Gerrit Demonstration Deployment

Setup Gerrit Access

Add ssh-key to *STAR Protected* user in gerrit as describe in the introduction part of this section. Run ssh gerrit4star to check whether you see the welcome message and thus are able to connect to gerrit correctly. Add your git-config e-mail address to the *STAR Protected* user at http://gerrit4star.the-huck.com/#/settings/contact and confirm it via the link in the e-mail sent to you. Put the following into your ~/.gitconfig.

```
[review "http://gerrit4star.the-huck.com"]
  username = protected
```

Setup, init and start sync'ing with repo

First install the *repo* script as described in [245]. A good introduction and overview of the usage of *repo* and the associated workflow can be found in [246, 247]. To get started, create an empty directory to hold your working files.

```
mkdir MyStarProjects && cd MyStarProjects
```

The manifest specifies where the various repositories included in the STAR repository will be placed within your working directory. Init your working directory using the default.xml in the *git4star* script repository:

```
repo init -u gerrit4star:git4star --config-name
```

When prompted, configure *repo* with your full name and the email you added above to the *STAR Protected* user in gerrit. ALL projects can be pulled down to your working directory as specified in the default manifest by running a simple repo sync. However, this is not desired in most cases. The *repo* script allows for only a list of gerrit projects to be synchronized via

repo sync StRoot-StAnalysisMaker StRoot-StHbtMaker

Start Work and Upload Changes for Review

The workflow of *repo* together with gerrit is very well documented in [248, 249]. Start a new development branch in all the repos you sync'ed via

```
repo start <br/>branchname> --all
```

Change to the git repository of your choice, start playing around, change files and when you are done, commit everything via

```
git commit -a -s -m "commit message"
```

Add your ssh-key to the ssh-agent (ssh-add ~/.ssh-key-name>) and upload your changes to gerrit for review via a simple

```
repo upload
```

Check repo help for more. Screenshots of Gerrit and CGit for STAR are appended in Section B.4.

Chapter 9

Open Source Contribution of Physics Analysis and Documentation Tools

9.1 ckon: Automatic Build Tool for ROOT Analyses

ROOT [164] allows for the automatic compilation of shared libraries using the ACLiC compiler [250]. This is very convenient for the quick use of compiled libraries in CINT but the organization of code developed for a physics analysis project would be cumbersome regarding its size and the resulting intra-project library dependencies. On top, ROOT-based shared libraries are mostly invoked through a macro and not a compiled program. The latter significantly improves the quality of a software project. Most bugs are detectable during compilation and not runtime and run control can be extended through command line options and arguments. This avoids constant recompilation due to hard-coding of I/O variables, for instance, and facilitates the use in shell scripts. Writing Makefiles for each library and program on the other hand is a difficult, time-consuming and repetitive task. This section is dedicated to a comprehensive solution of this issue.

On all computing sites STAR provides the user with the perl script *cons* to automatically compile shared libraries which rely on ROOT as well as StRoot software. However, *cons* is somewhat outdated and does not provide flexible configuration options. It covers a standard source code layout in which each subdirectory of *StRoot* is compiled into a library. For custom configuration like deeper structures which would need *cons* to recursively scan directories, for instance, the user needs to modify the *cons* script itself. Moreover, it is not straight-forward to set up on a local machine when StRoot software is not even needed. The author hence uses Autoconf and its simplified Makefile-"language" to automatically generate Makefiles specific to the underlying operating system. Autoconf is well established amongst software looking to be platform independent and provides GNU's known "configure / make / make install" workflow including distribution package management ("make clean / make distclean / make dist").

This is a first step towards an easy-to-maintain project layout but still requires the setup of Automake-Makefiles with library-specific naming conventions. This task is already streamlined when compared to manually writing Makefiles but still is error-prone and very repetitive. The latter, however, makes the entire process wrapable into the dedicated software tool *ckon*. On top of relieving the user from any duty to write Makefiles at all, this tool makes it easy to include foreign code or third-party libraries as well as the user's own core utility and database classes based on a simple project-specific YAML configuration file. All which is needed to build an entire project is <code>ckon setup && ckon</code> with the user deciding on the source directory's layout.

The following first outlines the usage of GNU's autoconf in conjunction with ROOT which is based on a talk given by the author at the Junior's Day of the STAR Collaboration Meeting

in November 2011 at LBNL. Find the talk titled "An example-driven introduction to using autoconf/automake (& Doxygen) for the organization of C++ data analysis software within the CERN ROOT framework" published on speakerdeck.com [29]. The automatic build tool *ckon* is subsequently introduced which was developed by the author to automate the suggested autoconf-based workflow for ROOT. Even though doxygen support is discussed in the presentation the reader is referred to Section 9.3 in which the author opts for Asciidoc to cover documentation of a physics analysis project.

The listing below demonstrates a possible layout for a simple ROOT analysis using Autoconf. The according source code is published at [251]. For references, see [252-257].

- configure.ac required for ./configure script
- Automake-Makefile for generating the main program bin/runhSimple
- source code for main program to control the class behavior. decodes options and re-initializes argc/argv for TRint
- hSimple class based on \$ROOTSYS/tutorials/hsimple.C [258]
- same for Options class [259]. for demonstration purposes only (better use Boost's program_options)
- 6 install program in bin/ and run it:

```
autoreconf -v --force --install && ./configure && make
runhSimple "out/hsimple.root"
runhSimple -N 1000000 "out/hsimple.root"
runhSimple -O "pics/test.png" "out/hsimple.root"
runhSimple -N 20000 -O "pics/test.png" "out/hsimple.root"
```

build & package distribution management

```
make dist # generate tarball
make clean # remove build files
make distclean # remove everything generated by automake
```

ckon is a C++ build tool which automatically takes care of compilation, dictionary generation and linking of programs and libraries developed for data analyses within the CERN ROOT analysis framework [164]. Given a source directory it recursively parses header include statements to figure out which libraries the main programs need to be linked to. It uses automake/autoconf [260] to be platform independent and GNU install compliant. In addition,

m4 macros [261] are automatically downloaded and the according compiler flags included based on a list of boost [262] libraries provided in the config file. For the purpose of YAML database usage, a m4 macro can be downloaded during setup to link against the yaml-cpp library [263]. The project's source code has been published on github [264] with the according documentation at [265]. It was written by the author of this thesis with invaluable contributions by Hiroshi Masui. It is released under the MIT License [266] and requires the following list of software already installed on the system: m4/1.4.6, autoconf/2.68, automake/1.11.4, libtool/2.4, boost/1.50, libcurl/7.27.0. Install *ckon* via

```
git clone https://github.com/tschaume/ckon.git
cd ckon && ./installCkon <install-path>
# replace install-path> with an install path in your PATH
# see './installCkon -h' for help
# see './configure --help' for configuration options
```

Shown below are the generic command line options which can be given to *ckon*. The long option <code>--ckon_cmd</code> is implemented as optional positional option to run the setup, clean all compilation products (i.e. <code>make clean</code>) and globally install libraries and programs (i.e. <code>make install</code>).

```
Generic Options:

-h [ --help ] show this help

-v [ --verbose ] verbose output

-j arg call make w/ -j <cores>

--ckon_cmd arg none | setup | clean | install | dry

Positional Arguments:
ckon setup # init dir, run the setup (mandatory)
ckon # build all
ckon clean # clean all build products
ckon install # install libraries (beta)
ckon dry # only generate automake's pseudo-makefiles
```

Run ckon setup to generate the files *configure.ac* and *.autom4te.cfg* (both autoconf specific with no need for modifications) as well as *ckon.cfg*. Modify the latter to resemble your directory structure and linker options. Simply remove the lines/options you do not need, thus using the default options.

The following options can be set on the command line or preferably in *ckon.cfg*. Optionally, a file named *ckonignore* with a list of strings to be ignored during the build process, can be created in the working directory. Wildcards are not supported (yet). Instead, each path currently processed by *ckon* will be checked against the strings/lines in *ckonignore*. If one of the strings in *ckonignore* is contained in the currently scanned path, the path is ignored/skipped.

```
Configuration:
-s [ --suffix ] arg add suffix + in LinkDef.h (bool)
-y [ --yaml ] arg use yaml
--ckon.src_dir arg source dir
--ckon.exclSuffix arg no + suffix
--ckon.NoRootCint arg no dictionary
--ckon.prog_subdir arg progs subdir
--ckon.build_dir arg build dir
--ckon.install_dir arg install dir
--ckon.cppflags arg add CPPFLAGS
--ckon.boost arg boost libraries
```

In addition, unregistered options of the form ldadd.prog_name are allowed to use for adding LDFLAGS to the linker of specific programs. The given string/value is added verbatim in LDADD. Unregistered options are only allowed in *ckon.cfg*. For instance, link the programs

genCharmContrib and dedxCut versus Pythia6 [267] and RooFit [178] by adding the following to ckon.cfg.

```
[ldadd]
genCharmContrib=-lPhysics -lEG -lEGPythia6 # link pythia
dedxCut=-lRooFit -lRooFitCore -lMinuit # link roofit
```

ckon.boost is set during ckon setup to use and link against specific boost libraries. Try not to run rootcint (ckon.NoRootCint) on the library if compilation fails.

Since version 0.4 *ckon* allows for the automatic download of a *yaml.m4* macro during <code>ckon setup</code> to link against the yaml-cpp library [263]. Please submit an issue [268] if the macro does not find the yaml-cpp library after you installed it. This added functionality should not break anything if you choose not to use YAML during <code>ckon setup</code>.

For the recursive header scan to work, make sure that all include directives for C++ and ROOT headers are enclosed in <...>! Only your local/private headers should be enclosed in "...". Otherwise *ckon* will fail reporting a basic_string::_S_create error.

Put header and source files for each library into a separate folder in <code>ckon.src_dir</code>. Running <code>ckon</code> should automagically take the right action for the current status of your build directory (no need to run <code>ckon clean</code> before re-compilation). Makefiles and LinkDef's are generated automatically based on the contents and timestamps in the <code>ckon.src_dir</code> directory. A typical directory structure is shown in Section B.5 using the current defaults for illustration purposes.

9.2 ccsgp: Publication-ready Plots with Gnuplot and Python

ccsgp [269] is a plotting library based on gnuplot-py which wraps the necessary calls to gnuplot-py into one function called make_plot. The keyword arguments to make_plot provide easy control over the plot-by-plot dependent options while reasonable defaults for legend, grid, borders, font sizes, terminal etc. are handled internally. By providing the data in a default and reasonable format, the user does not need to deal with the details of "gnuplot'ing" nor the internals of the gnuplot-py interface library. Every call of make_plot dumps an ascii representation of the plot in the terminal and generates the eps hardcopy original. The eps figure is also converted automatically into pdf, png and jpg formats for easy inclusion in presentations and papers. In addition, the user can decide to save the data contained in each image into hdf5 files for easy access via numpy. The function repeat_plot allows the user replot a specific graph with different properties, like axis ranges for instance. The make_panel user function facilitates plotting of 1D- or 2D-panel images with merged axes. The library allows for the generation of identical plots independent of the data input source (ROOT, YAML, ascii, pickle, hdf5, etc.) using the full power of python. The name ccsgp stands for Carbon Capture and Sequestration GnuPlot as this library started off in the context of CCS research [270]. The package ccsgp_get_started [271, 272] provides a sample setup to get started with ccsgp. ccsgp is initialized as a module and its usage demonstrated with dedicated functions in the examples module. Helpful utility functions are also included to complement the features of ccsqp. Installation and implementation details for both, ccsqp and ccsqp_get_started, are appended in Section B.6.

9.3 wp-pdf: Setup/Tools for Physics Analysis Homepage and Note

During the STAR review process of physics analyses for publication detailed reports have to be provided to the committee in form of a homepage as well as in pdf-format. Usually, this means twice the workload for presenting the same content. The markup language AsciiDoc and the python script *blogpost* both developed by S. Rackham are the ideal tools to separate writing and compiling information from its presentational form [273]. The content only exists in text files

which are pushed to a Wordpress instance for display in html or which can be converted into a docbook [274] to generate an analysis note. The a2x tool-chain takes care of this process [275]. Text-based source files also make it possible to track progress and changes with a revision control system. This approach significantly reduces the workload while at the same time improves the quality of the analysis note and corresponding homepage by using the tools optimized for the respective task.

In this section the collection of commands required to achieve this goal is condensed into a small Makefile providing descriptive targets. This makes it very convenient to update Word-Press pages from the command line as well as create the corresponding pdf versions. The instructions are tuned to the usage of the Wordpress instance in the context of a high energy physics analysis.

wp-pdf has been announced on Asciidoc's mailing list [276] and a public demonstration page which uses the AsciiDoc userguide itself has been deployed at http://asciidoc.the-huck.com. The following instructions and the Makefile are also published on github [277]. On a side note, images can quite comfortably be organized and served remotely ¹ by using git-annex [278, 279].

setup wordpress

- configure apache [239]
- create mysql database [280]
- install Wordpress [281]
- add upgrade constants to wp-config.php [282] (see Section B.7)
- change to www-data owner: sudo chown -R www-data: www-data public/
- install Foghorn theme, adjust *Appearance* → *Theme Options*
- install the following wordpress plugins: Options Framework, Disable Comments, CMS Page Order, Multi-level Navigation Plugin, WP Google Fonts (font: Gentium Book Basic), WP PHP widget, MathJax-Latex (change options: Force Load, Use wp-latex syntax?, Use MathJax CDN?)
- set up Sidebar in Appearance → Widgets:
 Search, Section Index, PHP Widget (see Section B.7)
- go to *Settings* → *Permalinks* and use post name as URL
- after pushing front page, go to *Settings* \rightarrow *Reading* and choose it as static front page

install blogpost

The official README and source code of blogpost can be found at [283, 284]. The author of this thesis implemented two changes on top of blogpost version 0.9.5: First, allow more than the 10 last most recent posts/pages to show up in info and second, a bugfix for inline-latex via the config macro [285]. This customized version is available on github [286] along with install instructions in its README file.

prepare for deployment

In the working directory adjust docinfo.xml. If you will be including images, create a symbolic link named images linking to the image directory and/or adjust Makefile (see Section B.7).

use Makefile for hp, pdf & latex

Let *wp-pdf* do the "magic":

```
make make pdf make hp
```

¹ see http://downloads.the-huck.com

```
make latex
make out/Introduction/Introduction.txt
make clean
```

After publishing a page for the first time, use $Pages \rightarrow Page$ Order to arrange pages.

9.4 rmrg: Automization Class and Program for ROOTs hadd

rmrg is a command line program to merge ROOT Trees and Histograms with additional features and increased control currently missing in ROOT's hadd [30]. Primarily,

- automatic file-list generation based on an input directory scan
- step-by-step verbose TTree and Histogram merging
- options for number of files to merge at once and minimum file size

This tool was developed to be included as afterburner in the PicoDst production at LBNL. Small output files would be merged on a run-by-run basis which provides a homogenous land-scape of input files to relieve the queueing systems of the batch farms. The code is published on github [287].

Part III Appendix

Chapter 10

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Chapter 11

Xenon Excimer Lamp for HADES RICH

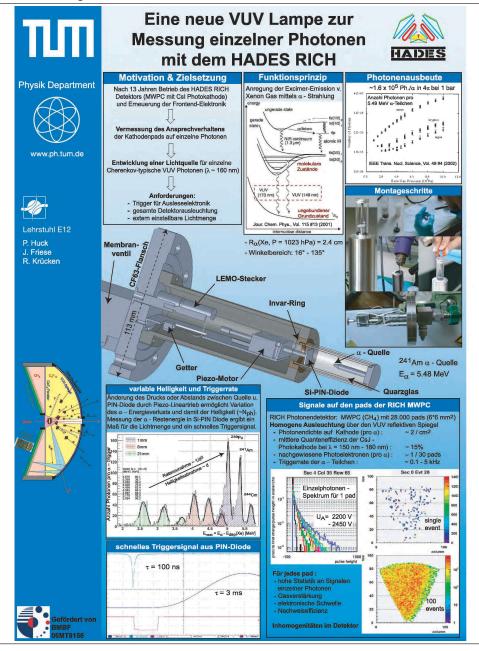
- Dec '09 Jul '10, Kruecken, Friese (TU Munich)
- DPG spring meeting 2001, abstract submission ¹, poster ²
- new VUV lamp for single photon measurement with HADES RICH
- Hardware development and design project
- 13 years of HADES RICH operation (MWPC w/CsI photo cathode) and renewal of Frontend electronics
 - necessitates measurement of cathode pads response on single photons
 - develop light source for single cherenkov typical VUV photons (160nm)
- requirements:
 - trigger for readout electronics
 - isotropic and full detector coverage
 - externally adjustable light emission/tuning
- technique: Xenon Excimer Emission via alpha radiation (2.4cm radiation length)
- R&D and design
 - diaphragm valve
 - flange for RICH mounting
 - LEMO readout electronics and external control
 - getters for Xenon gas purity improvements through heating
 - piezo motor for light emission control
 - invar inlet for Quarz glass metal connection
 - 241Am alpha radiation source
 - Si-PiN-Diode for triggering (fast trigger signal 100ns)
- assembly steps in cleanroom (glas-metal soldering)
- energy deposition measurements for variable light output and trigger rate
- on-site RICH MWPC pad-by-pad signals / measurements (voltage dependence ...)

¹ http://www.dpg-verhandlungen.de/year/2011/conference/muenster/part/hk/session/39/contribution/-

² http://www.star.bnl.gov/protected/lfspectra/huck/Talks/DPG11_poster_druck.jpg

- single photon spectra
- homogenous RICH MWPC illumination through reflection on VUV mirror
- photon density, mean quantum efficiency, number of photo-electrons, trigger rate
- pad-by-pad: high statistics, gas amplification, thresholds, detection efficiency

Figure 11.1 DPG11 poster



Appendix A

Physics

A.1 Technical FAQs

Relevant URLs

- cgit.the-huck.com: version-controlled code & data repositories ¹
- downloads.the-huck.com/star: download page containing all pictures, talks etc
- star.the-huck.com: central analysis webpage
- Analysis Chain for raw data [288].

Designated Data Repository

The dielectron_data_protected repository provided at [289] contains all necessary text files to go through a step-by-step comparison with the raw data analysis and the efficiency correction as well as the final physics plots. The included README is a good starting point explaining directory structure and notations. For the comparison of background ratio plots at 19 GeV, for instance, the README refers to rawdata/19 subdirectory. Same for the single track efficiencies. M_{ee} -dependent ratios are also included (rgm, rmm, rpp) along with the acceptance correction factor (ac). Efficiency-corrected data is collected in the input sub-directories of examples/ (mostly gp_panel).

¹ clone any repo via git clone http://protected@cgit.the-huck.com/<repo-name>

A.2 Bad Run Tables

Table A.1: List of rejected runs at BES-I energies in StRefMultCorr and refined for this analysis.

	S+ PofM	ultCorr		additional RunIDs rejected						
20	10		11	19.6 GeV	62.4 GeV					
11080072	11095005	12113091	12136034	12113082	27 GeV 12172044	39 GeV 11102107	11080055			
11081023	11095006	12114007	12136054	12113082	12172045	11105033	11080056			
11081025	11095009	12114035	12138005	12113084	12172046	11100000	11080057			
11082012	11095010	12114078	12138017	12113085	12172048		11080062			
11082012	11095010	12111070	12138021	12113086	12172049		11080063			
11082046	11095011	12114072	12146004	12113087	12172049		11080067			
11082056	11095012	1211110	12146006	12113088	12172057		11080071			
11082057	11095014	12115009	12146007	12113089	12172058		11080071			
11084009	11095011	12115011	12146008	12113091	12172030		11081001			
11084011	11095022	12115016	12151035	12114026	12174037		11081003			
11084012	11095022	12115018	12153002	12115026	12174048		11081004			
11084013	11095048	12115019	12153004	12117010	12174054		11081025			
11084020	11095050	12115020	12153007	12119009	12175062		11081034			
11084021	11095051	12115022	12153013	12119011	12175089		11081037			
11084035	11095061	12115023	12157038	12119015	12175094		11081052			
11084044	11095062	12115062	12157051	12119016	12176047		11081053			
11084064	11095063	12115073	12158040	12119017	12176057		11081054			
11085015	11095064	12115093	12158041	12119018	12176058		11081058			
11085025	11095082	12115094	12158054	12119020	12176066		11084049			
11085030	11095087	12116012	12158056	12119021	12176067		11084064			
11085046	11096024	12116054	12158057	12119023	12176068		11084069			
11085055	11096039	12117010	12162055	12119024	12176071		11084070			
11085056	11096043	12117016	12162056	12119025	12178059		11085001			
11085057	11096044	12117020	12162057	12119027	12178078		11085050			
11086005	11097093	12117065	12162058	12119028	12178094		11085051			
11086007	11099124	12119040	12164037	12119040	12178123		11085052			
11087001	11100002	12119042	12164078		12179002		11085054			
11087002	11100045	12120017	12164079		12179063		11085055			
11087003	11101046	12120026	12166002		12179083		11086001			
11087004	11102012	12121017	12166003				11086002			
11088013	11102051	12121022	12167015				11086003			
11089026	11102052	12121034	12167024				11086005			
11089028	11102053	12121050	12167052				11086007			
11089029	11102054	12121067	12168002				11086011			
11089055	11102055	12122019	12168009				11086019			
11089068	11102058	12127003	12168022				11086022			
11089072	11103035	12127010	12168077				11086043			
11091007	11103056	12127011	12170044				11087058			
11091015	11103058	12127017	12170045				11087059			
11091021	11103092	12127018	12170054				11087065			
11091078	11103093	12127032	12170056				11089054			
11092010	11105052	12128025	12172050				11092014			
11092011	11105053	12132043	12172051				11092032			
11092012	11105054	12132061	12172055				11093075			
11092032	11105055	12133018	12173030				11093077			
11092033	11107007	12134023	12173031				11093078			
11092034	11107042	12136005	12173032				11093081			
11092067	11107057	12136006	12173033				11093083			
11092096	11107061	12136014	12173034				11093086			
11093001	11107065	12136017	12174067				11093087			
11094016	11107074	12136022	12174085				11093088			
11094017	11108101	12136023	12175062				11093089			
11094018	11109013	12136024	12175087				11093090			
11094019	11109077	12136025	12175113				11093091			
11094020	11109088	12136027	12175114				11094001			
11094021	11109090	12136028	12175115				11094002			

Table A.1: (continued)

11094022 11109127 12136029 12176044 11094004 11094023 11110013 12136031 11094004 11094007 11094027 11110073 11095024 11095022 11094028 111110184 11095027 11094044 11111085 11095027 11094044 11111085 11095029 11094045 12176051 11095029 11094046 12177015 11095030 11094047 12177015 1109506 11094050 12177092 1109506 11094051 12177092 1109506 11094052 12177106 1109507 11094053 12177106 1109507 11094075 1217803 1109507 11094075 1217803 1109507 11095002 12178005 11096007 11095002 12178005 11096007 11095003 1217809 1109601 11095004 12178120 1109601 11096015 11096018 11096016 11096018 11096018 1109607 </th <th></th> <th></th> <th></th> <th></th> <th></th> <th></th>						
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11096096 11096108						
11096108						
11097102						
						11097102

A.3 Run QA Figures

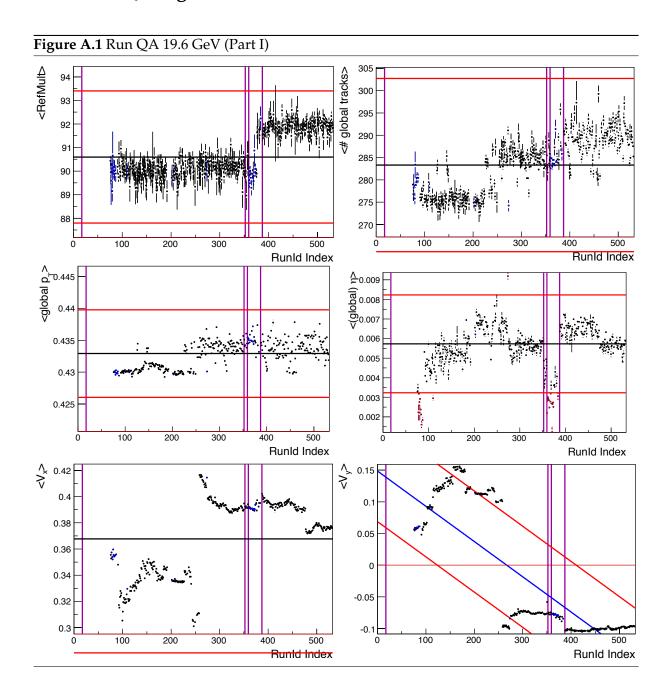


Figure A.2 Run QA 19.6 GeV (Part II)

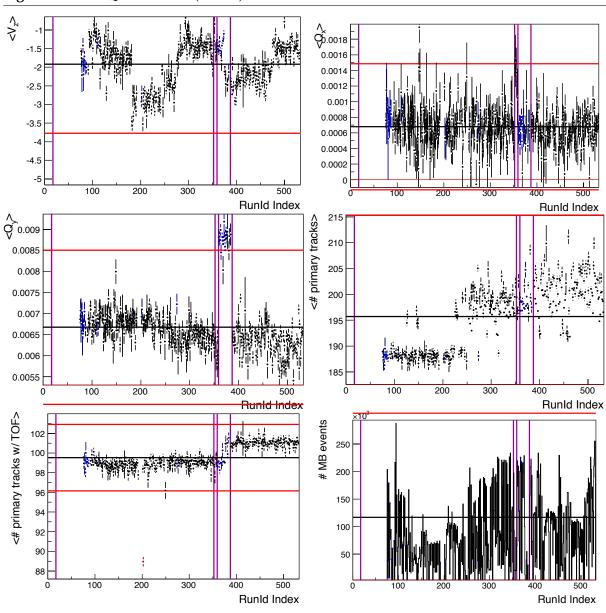


Figure A.3 Run QA 27 GeV (Part I)

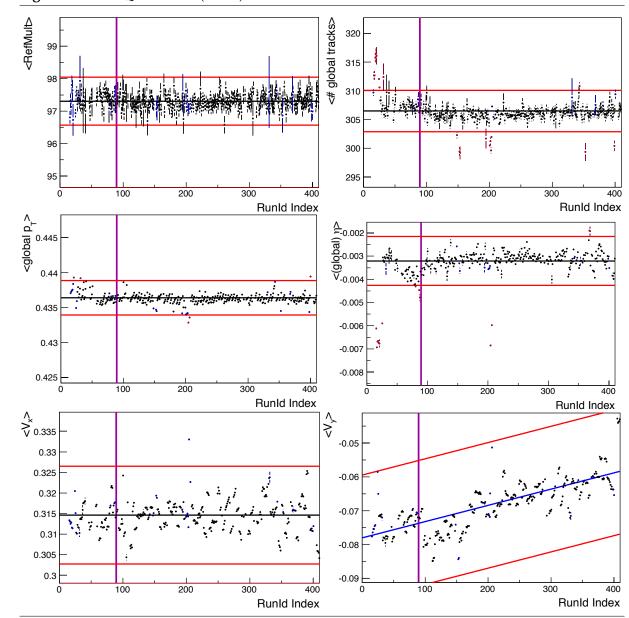
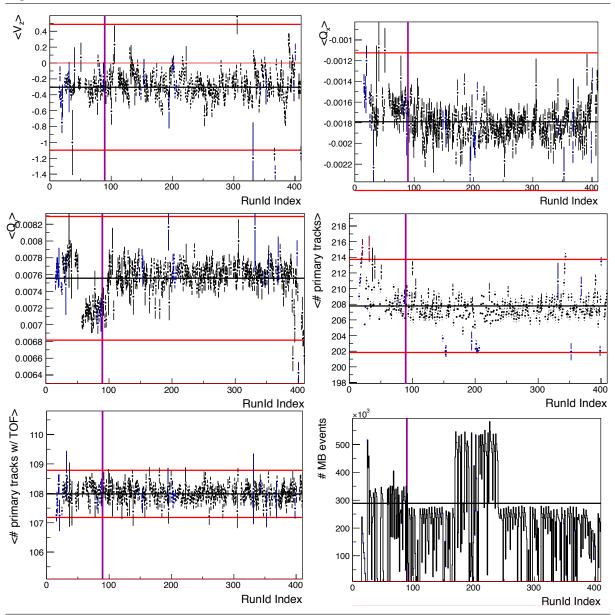


Figure A.4 Run QA 27 GeV (Part II)



100

200

300

500

600

Runid Index

700

Figure A.5 Run QA 39 GeV (Part I) <RefMult> <# global tracks> 350 109 345 108 340 107 335 106 330 105 325 104 320 103 100 100 400 400 200 500 600 200 600 500 RunId Index Runld Index ^_0.455 d o 0.45 0.445 (global) ما> (global) ما> (global) ما> 0.435 0.002 t profile 0.43 0.425 -0.002 0.42 -0.004 0.415 100 100 400 400 500 600 200 300 600 700 500 Runld Index **Runld Index** ∧-0.035 √
 0.32 ₹ -0.04 -0.045 0.31 -0.05 -0.055 0.3 -0.06 -0.065 0.29 -0.07 -0.075 0.28 -0.08 200 400 700

100

300

400

600

Runld Index

Figure A.6 Run QA 39 GeV (Part II)

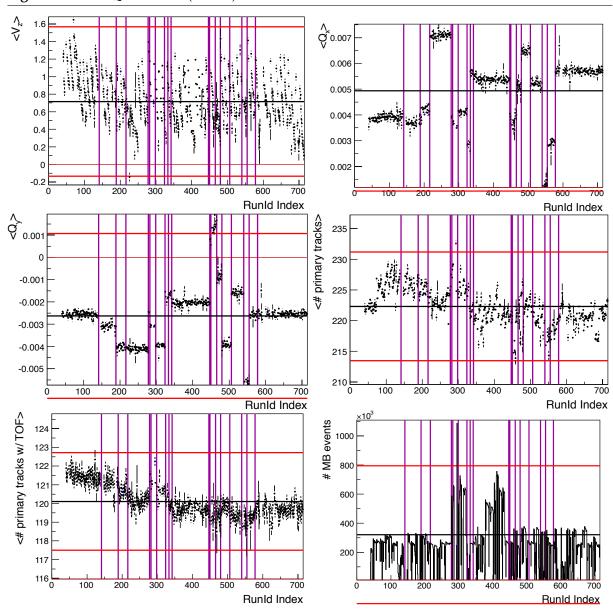
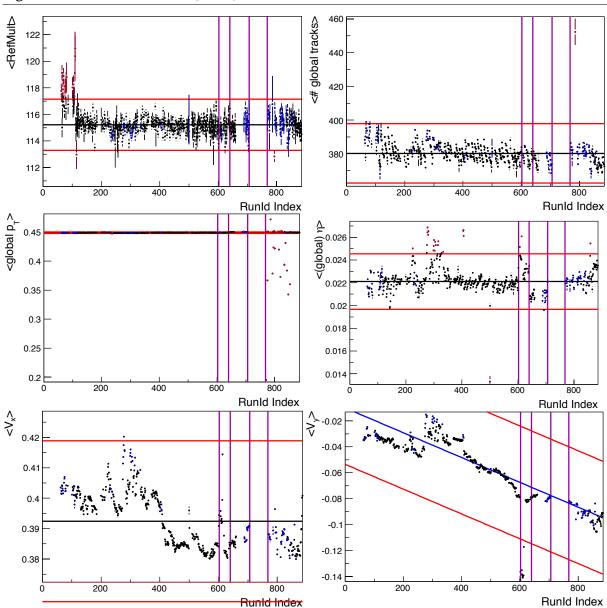
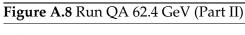
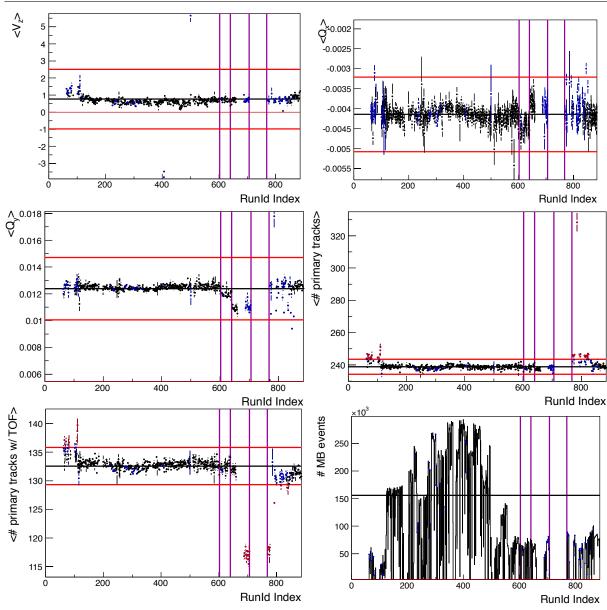


Figure A.7 Run QA 62.4 GeV (Part I)







A.4 Particle Identification Figures

Figure A.9 TOF Selection of positrons (left column) and electrons (right column) for all BES-I energies. For a detailed description see Figure 2.12.

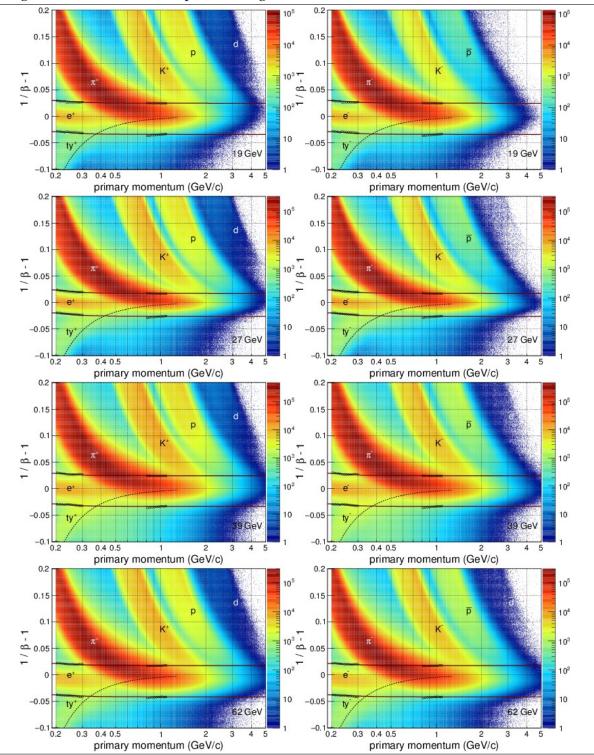


Figure A.10 TPC energy loss and selection of positrons (left column) and electrons (right column) at $\sqrt{s_{\rm NN}}$ = 19.6 GeV and 27 GeV with and without TOF selection (Figure A.9). For a detailed description see Figure 2.14.

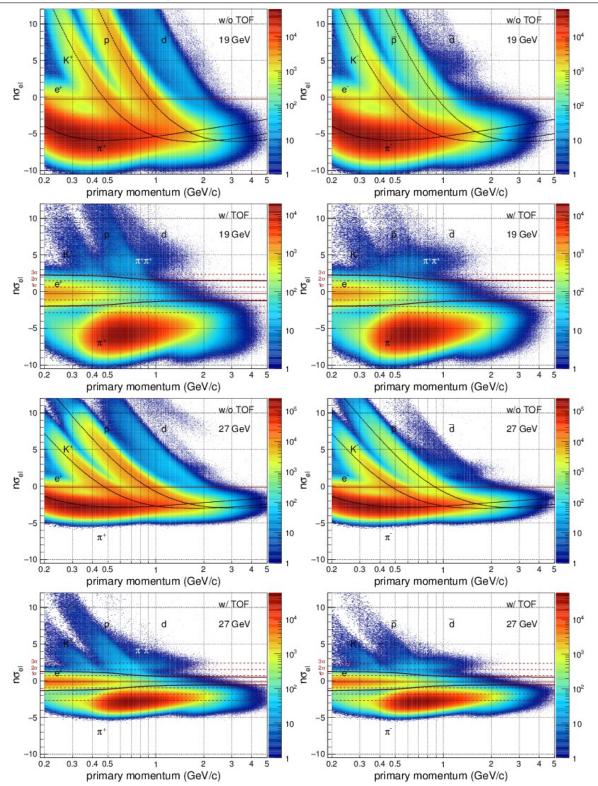
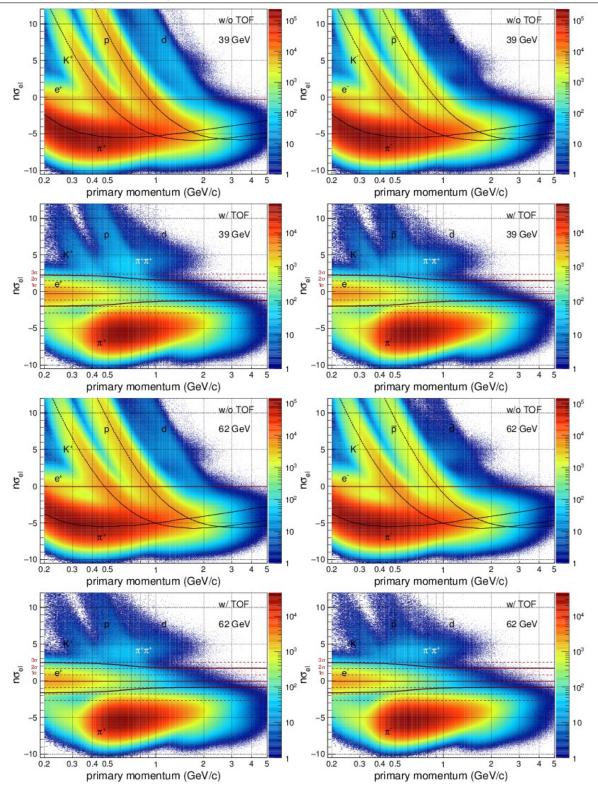


Figure A.11 TPC energy loss and selection of positrons (left column) and electrons (right column) at $\sqrt{s_{NN}}$ = 39 GeV and 62.4 GeV with and without TOF selection (Figure A.9). For a detailed description see Figure 2.14.



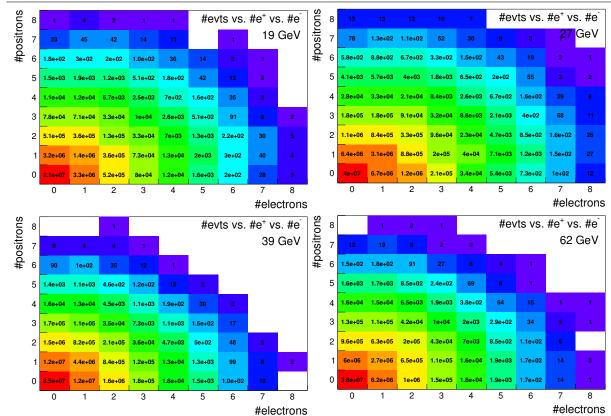


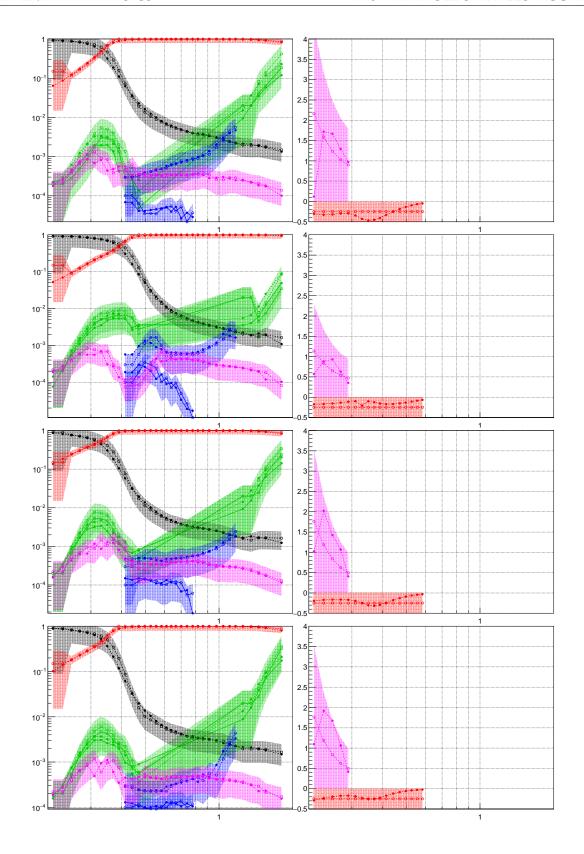
Figure A.12 Number of events for combinations of number of e⁺/e⁻ at all BES-I energies.

A.5 Particle Samples Figures

This section is organized in columns for each energy and rows increasing with momentum. It first shows all multi-gaussian fits to pure K, p, merged- π , and π samples followed by the simultaneous multi-particle fits to $n\sigma_{el}$ distributions. The grey boxes denote the $n\sigma_{el}$ selection criterium used to identify electrons/positrons. The final page of this section shows the momentum dependence of the free (but properly initialized and constrained) fit parameters, namely yield fractions (top) and few correctional shifts/widths (bottom). Only a representative sample of the fits is included here. For the full selection see the supporting information [290].

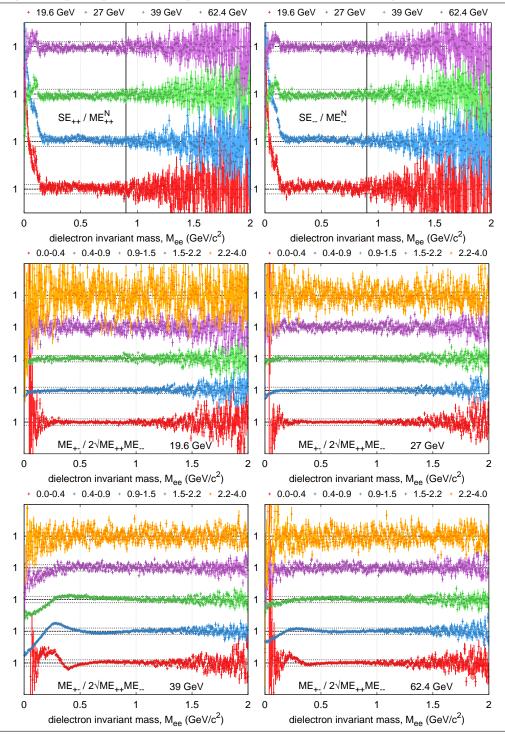






A.6 Pair Reconstruction Figures

Figure A.13 (top row) SE/ME^N like-sign ratios for the identification of the normalization range. (remaining rows) p_T -dependent acceptance correction factors. See Figure 2.24.



A.7 ISR pT spectra in p+p

data: http://www.star.bnl.gov/protected/lfspectra/huck/html/ppspectra_data/code: http://cgit.the-huck.com/cgit.cgi/Obsolete/tree/PPptSpectra deduce $\eta/\pi 0$ ratio from ISR/Fermilab data

make own $\omega \& \varphi$ pT spectra from dielectron measurement or simply use m_T scaling compare to available data in 39 GeV after scaling: π^0 , $\phi \to KK$ (check $\pi 0$ yield in AuAu via # participants scaling from p+p)

Phys. Lett. B 194 (1987) 4, Nucl. Phys. B 209 (1982) 309-320, Nucl. Phys. B 158 (1979) 1-10 Phys. Lett. B 79 (1978), Nucl. Phys. B 124 (1977) 1-11, Phys. Lett. B 64 (1976)

Nucl. Phys. B 116 (1976) 77-98, Phys. Rev. Lett 40 (1978) 684, Phys. Rev. Lett. 38 (1977) 112

Nucl. Phys. B 106 (1976) 1-30, Nucl. Phys. B 100 (1975) 237-290, Nucl. Phys. B 98 (1975) 49-72

Phys. Lett. B 55 (1975) 232, Nucl. Phys. B 87 (1975) 19-40, Phys. Lett. B 47 (1973) 75

Phys. Lett. B 47 (1973) 275, Phys. Lett. B 46 (1973) 471, Phys. Rev. Lett. 31 (1973) 413

Phys. Lett. 44B (1973) 521

Figure A.14 ISR spectra

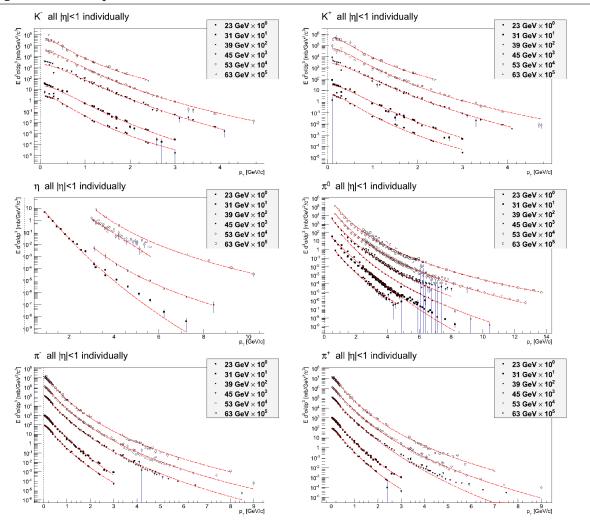


Figure A.15 Notes on ISR Spectra (Levy misses -1 exponent)



ISR/Fermilab data & remarks

ISR@CERN measured p+p at $\sqrt{s} = 23, 31, 45, 53, 63 \,\text{GeV}$

Phys. Lett. B 194 (1987) 4 Nucl. Phys. B 209 (1982) 309-320 Nucl. Phys. B 158 (1979) 1-10 Phys. Lett. B 79 (1978) Nucl. Phys. B 124 (1977) 1-11 Phys. Lett. B 64 (1976) Nucl. Phys. B 116 (1976) 77-98 Phys. Rev. Lett 40 (1978) 684 Phys. Rev. Lett. 38 (1977) 112 Nucl. Phys. B 106 (1976) 1-30 Nucl. Phys. B 100 (1975) 237-290 Nucl. Phys. B 98 (1975) 49-72 Phys. Lett. B 55 (1975) 232 Nucl. Phys. B 87 (1975) 19-40 Phys. Lett. B 47 (1973) 75 Phys. Lett. B 47 (1973) 275

Phys. Lett. B 46 (1973) 471

Phys. Rev. Lett. 31 (1973) 413 Phys. Lett. 44B (1973) 521

E706@Fermilab p+p at $E_{kin} = 530$, 800 GeV/c. Corresponds to $\sqrt{s} = 31.5$, 38.8 GeV!

Phys. Rev. D 68 (2003) 052001

 \Rightarrow ca. 90 datasets for π , K, η with $|\eta| < 1$ (mostly small windows around midrapidity)

Levy Fit Function [PRC 71, 064902] best description over entire p_T range $\frac{1}{2\pi p_T} \frac{d^2 N}{dy \, dp_T} = \frac{dN}{dy} \frac{(n-1)(n-2)}{2\pi n T (nT + m_0(n-2))}$ pt weight [NIM A 355 (1995) 541-547] correct pt for wide pt bins assuming local $exp(-bp_T)$ $p_T^{corr} = p_T^{low} + (\ln(b\Delta p_T) - \ln(1 - \exp(-b\Delta p_T)))/b$

all rapidities plotted independently

→ average each energy over rapidity range!



Simulation Input

General Idea

scaling of particle ratios from p+p to Au+Au is available at 200 GeV

- → assume scaling to be energy independent
- \rightarrow scale particle ratios from p+p@ISR/Fermilab to Au+Au w/ same scaling factors
- → use in cocktail simulation for 39(27,62) GeV

particle ratios at 200 GeV and resulting scaling factors (based on PHENIX [PRC 81, 034911] and STAR measurements)

particle	ratio in Au+Au (Yifei, Xin)	ratio in p+p (Bingchu)	scaling factor			
π^0	1.0	1.0	1.0			
η	0.1125	0.1327	0.8478			
ρ	0.17	0.17	1.0			
ω	0.08985	0.1041	0.8631			
ϕ	0.0258	0.01351	1.9083			
η'	0.02144	0.03182	0.6738			
J/ψ	0.0221	1.9e-5	1.163e3			

Patrick Huck

Soft Hadron Meeting, LBNL (08/22/2011) 7 / 13

A.8 Efficiency Tables

Table A.2: $p_T/\eta/\phi$ -dependent Combined Detector & Track Quality Efficiencies ε with statistical uncertainties. Only an excerpt is listed here with the full table in the supporting information [290].

			10.4.0	ZoV.	27.0	CoV.	$arepsilon \pm \Delta arepsilon_{ m st}$		62.4 GeV		
p_T	η	ϕ	19.6 C e ⁻	∍ev e ⁺	27 G e ⁻	ev e+		GeV e ⁺	62.4 e ⁻	Gev e ⁺	
0.3	-0.875	170 E	e 61±4	e' 63±4	e 67±3	e' 66±3	e ⁻ 25±3	e ' 2±1	e 64±3	e' 64±3	
0.5	-0.875 -0.875	-172.5 -172.5	61 ± 4 68 ± 4	60±4	67 ± 3 62 ± 3	75±3	25±3 61±3	$(0\pm 4)e-01$	64 ± 3 74 ± 3	54 ± 3	
0.5	-0.875 -0.875	-172.5 -172.5	74 ± 4	53±4	59±3	80±3	73±3	12±2	74 ± 3 76 ± 3	54±3 51±3	
0.7	-0.875	-172.5 -172.5		49 ± 4	58±3	83±2	75±3	23±2	70 ± 3 74 ± 3	50±3	
1.1	-0.875	-172.5 -172.5	70±4 77±3	54 ± 4	57±3	77 ± 3	75±3	33±3	74±3 79±3	53±3	
1.3	-0.875	-172.5	75±3	52±4	56 ± 3	76 ± 3	73 ± 3 72 ± 3	42±3	78±3	46±3	
1.5	-0.875	-172.5	73 ± 3 73 ± 4	57±4	60 ± 3	83±3	75±3	33±3	81±3	50±3	
1.7	-0.875	-172.5	74 ± 4	56±4	61±3	81±3	77±3	43±3	79±3	52±3	
1.9	-0.875	-172.5		47 ± 4	59±3	81±3	77±3	43±3	79±3	54±3	
0.3	-0.875	-157.5		60 ± 4	66 ± 3	73±3	56±3	31±3	72 ± 3	60±3	
0.5	-0.875	-157.5		63±4	76±3	68±3	62±3	2±1	61±3	72±3	
0.7	-0.875	-157.5		67 ± 4	78±3	64 ± 3	51±3	$(0\pm 4)e-01$	53±3	74 ± 3	
0.9	-0.875	-157.5		73±4	78±3	54±3	27±3	$(0\pm 4)e-01$	48±3	77±3	
1.1	-0.875	-157.5	51±4	71±4	80±3	55±3	21±2	0±0	52±3	78±3	
1.3	-0.875	-157.5	51±4	70 ± 4	78±3	55±3	17±2	$(0\pm 4)e-01$	62±3	76 ± 3	
1.5	-0.875	-157.5		67±4	84 ± 2	57±3	10 ± 2	0.02 ± 0.34	52±3	73 ± 3	
1.7	-0.875	-157.5		83±3	81±3	56±3	10 ± 2	$(0\pm 4)e-01$	55±3	73±3	
1.9	-0.875	-157.5	52 ± 4	75±3	81 ± 3	58 ± 3	9±2	0±0	56 ± 3	76 ± 3	
0.3	-0.875	-142.5	58 ± 4	68 ± 4	71 ± 3	64 ± 3	40 ± 3	56±3	61±3	56 ± 4	
0.5	-0.875	-142.5	77 ± 4	60 ± 4	62±3	75 ± 3	3 ± 1	55±3	71 ± 3	57±3	
0.7	-0.875	-142.5	77 ± 3	59 ± 4	60±3	81 ± 3	0 ± 0	35 ± 3	76 ± 3	54 ± 3	
0.9	-0.875	-142.5	82 ± 3	49 ± 4	57±3	81 ± 3	0 ± 0	22 ± 2	74 ± 3	56 ± 3	
1.1	-0.875	-142.5	72 ± 3	51 ± 4	55 ± 3	77 ± 3	$0.4 {\pm} 0.5$	15 ± 2	77 ± 3	50 ± 3	
1.3	-0.875	-142.5	69 ± 4	$48{\pm}4$	58 ± 3	80 ± 3	0.02 ± 0.37	12±2	75 ± 3	59 ± 3	
1.5	-0.875	-142.5	$64{\pm}4$	57 ± 4	55 ± 3	77 ± 3	$(0\pm 4)e-01$	9±2	77 ± 3	63 ± 3	
1.7	-0.875	-142.5	72 ± 4	56 ± 4	60 ± 3	81 ± 3	0 ± 0	8±2	76 ± 3	59 ± 3	
1.9	-0.875	-142.5	69 ± 3	57 ± 4	61±3	79 ± 3	0 ± 0	7 ± 2	82 ± 3	55 ± 3	
0.3	-0.875	-127.5	63 ± 4	59 ± 4	64 ± 3	64 ± 3	2 ± 1	43 ± 3	65 ± 3	45 ± 3	
0.5	-0.875	-127.5		67 ± 4	78 ± 3	66 ± 3	$0.4 {\pm} 0.5$	48 ± 3	50 ± 3	51 ± 3	
0.7	-0.875	-127.5		71 ± 4	84 ± 2	62 ± 3	14 ± 2	64 ± 3	44 ± 3	60 ± 3	
0.9	-0.875	-127.5		65 ± 4	78 ± 3	57 ± 3	15 ± 2	66 ± 3	43 ± 3	58 ± 3	
1.1	-0.875	-127.5	52 ± 4	74 ± 3	81±3	52±3	26 ± 3	62 ± 3	43 ± 3	69 ± 3	
1.3	-0.875	-127.5	59 ± 4	78±3	83±3	63±3	32±3	65±3	47 ± 3	67 ± 3	
1.5	-0.875	-127.5	54 ± 4	72±4	79±3	54±3	37±3	58±3	45 ± 3	60±3	
1.7	-0.875	-127.5	57±4	70±4	76±3	62±3	39±3	61±3	49±4	66±3	
1.9	-0.875	-127.5		74±3	80±3	53±3	44±3	62±3	47±3	63±3	
0.3	-0.875	-112.5	57±4	62±4			13±2	68±3	37±3	53±3	
0.5	-0.875	-112.5	65±4				46±3	56±3	52±3	49±4	
0.7	-0.875	-112.5			55±3		61±3	46±3	66±3	36±3	
0.9	-0.875	-112.5			61±3		60±3	48±3	62±3	41±3	
1.1	-0.875	-112.5			59±3		60±3	48±3	63±3	46±3	
1.3	-0.875	-112.5	74±3				63±3	51±3	64±3	43±3	
1.5	-0.875	-112.5			59±3		55±3	44±3	67±3	46±3	
1.7	-0.875	-112.5			61±3 60±3		63±3	45±3	69±3	46±4	
1.9	-0.875	-112.5					65±3	45±3	65±3	49 ± 4	
0.3 0.5	-0.875 -0.875	-97.5 -97.5			58±3 78±3		$42\pm 3 \ 47\pm 3$	61±3 75±3	46 ± 4 49 ± 3	51 ± 3 60 ± 3	
0.5	-0.875 -0.875	-97.5 -97.5			78±3 81±3		47 ± 3 47 ± 3	75±3 81±2	49±3 50±3	60±3 69±3	
0.7	-0.875 -0.875	-97.5 -97.5			80±3		47 ± 3 44 ± 3	83±2	30±3 44±3	71±3	
1.1	-0.875 -0.875	-97.5 -97.5	63 ± 4				50 ± 3	79±2	50 ± 3	67±3	
1.1	-0.875	-97.5 -97.5			82±3		55±3	86±2	50±3	68±3	
1.5	-0.875 -0.875	-97.5 -97.5			81±3		65±3	88±2	50±3 51±3	72±3	
1.7	-0.875	-97.5 -97.5	50 ± 4 59 ± 4				54 ± 3	86±2	47 ± 3	72±3 72±3	
1./	0.070	71.0	しノエヨ	.010	0110	0110	0110	0012	1, 10	,	

Table A.2: (continued)

1.9	-0.875	-97.5	55 ± 4	72 ± 4	72 ± 3	61 ± 3	66 ± 3	81 ± 2	53 ± 3	75 ± 3
0.3	-0.875	-82.5	60 ± 4	$40{\pm}4$	66 ± 3	63 ± 3	59 ± 3	75 ± 3	47 ± 3	66 ± 3
0.5	-0.875	-82.5	73 ± 4	46 ± 4	59 ± 3	75 ± 3	72 ± 3	62 ± 3	62 ± 3	55 ± 3
0.7	-0.875	-82.5	69 ± 4	47 ± 4	54 ± 3	80 ± 3	83 ± 2	60±3	63 ± 3	46 ± 3
0.9	-0.875	-82.5	72 ± 3	$44{\pm}4$	51 ± 3	84 ± 3	80 ± 2	59 ± 3	68 ± 3	48 ± 3
1.1	-0.875	-82.5	71 ± 4	45 ± 4	53 ± 3	81 ± 3	85 ± 2	58 ± 3	72 ± 3	$48{\pm}4$
1.3	-0.875	-82.5	78 ± 4	46 ± 4	58 ± 3	75 ± 3	82 ± 2	60±3	73 ± 3	48 ± 3
1.5	-0.875	-82.5	80 ± 3	58 ± 4	58 ± 3	81 ± 3	$84{\pm}2$	62 ± 3	67 ± 3	53 ± 3
1.7	-0.875	-82.5	76 ± 4	51 ± 4	57 ± 3	83 ± 3	$84{\pm}2$	69±3	69 ± 3	50 ± 3
1.9	-0.875	-82.5	78 ± 4	$48{\pm}4$	61 ± 3	78 ± 3	80 ± 2	60±3	70 ± 3	48 ± 3
0.3	-0.875	-67.5	62 ± 4	36 ± 4	58 ± 3	75 ± 3	71 ± 3	26 ± 3	54 ± 3	24 ± 3
0.5	-0.875	-67.5	$48{\pm}4$	33 ± 4	65 ± 3	63 ± 3	68 ± 3	$78{\pm}2$	58 ± 3	65 ± 3
0.7	-0.875	-67.5	$46{\pm}4$	36 ± 4	72 ± 3	61 ± 3	68 ± 3	$88{\pm}2$	56 ± 3	80 ± 3
0.9	-0.875	-67.5	$41{\pm}4$	$40{\pm}4$	68 ± 3	60 ± 3	64 ± 3	91 ± 2	50 ± 3	74 ± 3
1.1	-0.875	-67.5	39 ± 4	$44{\pm}4$	73 ± 3	59 ± 3	62 ± 3	91 ± 2	57 ± 3	75 ± 3
1.3	-0.875	-67.5	41 ± 4	40 ± 4	77 ± 3	61±3	67 ± 3	$88{\pm}2$	55 ± 3	76 ± 3
1.5	-0.875	-67.5	31 ± 3	$44{\pm}4$	71 ± 3	57 ± 3	68 ± 3	90±2	56 ± 3	78 ± 3
1.7	-0.875	-67.5	33 ± 4	49 ± 4	71 ± 3	60 ± 3	65 ± 3	89 ± 2	58 ± 3	79 ± 3
1.9	-0.875	-67.5	35 ± 4	49 ± 4	75 ± 3	53±3	63±3	91 ± 2	60 ± 3	77 ± 3
0.3	-0.875	-52.5	33 ± 4	39 ± 4	41 ± 3	58 ± 3	77 ± 3	1 ± 1	58 ± 3	0 ± 0
0.5	-0.875	-52.5	30 ± 4	41 ± 4	50 ± 3	69 ± 3	85 ± 2	2 ± 1	71 ± 3	3 ± 1
0.7	-0.875	-52.5	33 ± 4	$40{\pm}4$	44 ± 3	68 ± 3	91±2	16 ± 2	73 ± 3	15 ± 2
0.9	-0.875	-52.5	38 ± 4	$40{\pm}4$	47 ± 3	71 ± 3	$88{\pm}2$	32 ± 3	82 ± 3	32 ± 3
1.1	-0.875	-52.5	41 ± 4	38 ± 4	48 ± 3	69 ± 3	$88{\pm}2$	41 ± 3	76 ± 3	37 ± 3
1.3	-0.875	-52.5	$44{\pm}4$	39 ± 4	53±3	72 ± 3	89 ± 2	47 ± 3	83±3	38 ± 3
1.5	-0.875	-52.5	39 ± 4	39 ± 4	53 ± 3	79 ± 3	$88{\pm}2$	49 ± 3	79 ± 3	44 ± 3
1.7	-0.875	-52.5	$46{\pm}4$	41 ± 4	51±3	70 ± 3	88 ± 2	53±3	76 ± 3	50 ± 3
1.9	-0.875	-52.5	47 ± 4	42 ± 4	57±3	71 ± 3	89 ± 2	58±3	83 ± 2	45 ± 3
0.3	-0.875	-37.5	39 ± 4	34 ± 4	35 ± 3	53±3	75 ± 3	30 ± 3	61±3	10 ± 2
0.5	-0.875	-37.5	32 ± 4	47 ± 4	47 ± 3	40 ± 3	57±3	0.7 ± 0.6	44 ± 3	$0.5 {\pm} 0.4$
0.7	-0.875	-37.5	32 ± 4	53 ± 4	51 ± 3	37 ± 3	40 ± 3	$0.8 {\pm} 0.6$	28 ± 3	0 ± 0
0.9	-0.875	-37.5	31 ± 4	47 ± 4	54 ± 3	32 ± 3	25±3	0.03 ± 0.37	19 ± 3	0 ± 0
1.1	-0.875	-37.5	36 ± 4	$48{\pm}4$	55 ± 3	37 ± 3	16 ± 2	0 ± 0	13 ± 2	0 ± 0
1.3	-0.875	-37.5	32 ± 4	53 ± 4	57±3	37 ± 3	15 ± 2	$(0\pm 4)e-01$	9 ± 2	0 ± 0
1.5	-0.875	-37.5	41 ± 4	58 ± 4	52±3	41 ± 3	8±2	0±0	8 ± 2	0 ± 0
1.7	-0.875	-37.5	36 ± 4	52 ± 4	55 ± 3	35 ± 3	11 ± 2	$(0\pm 4)e-01$	5±1	0 ± 0
1.9	-0.875	-37.5	38 ± 4	57 ± 4	57±3	43 ± 3	8±2	0±0	$4{\pm}1$	0 ± 0

Table A.3: TOF Matching (ε_{TOF}) and Total Track (ε_{tot}) Efficiencies for η < 0. Only an excerpt is listed here with the full table in the supporting information [290].

r)												$arepsilon_{tot} \pm \Delta arepsilon_{stat} \pm \Delta arepsilon_{syst}$							
ŀ	T	η	ϕ	19.	-	27		39		62.	_	19.60	GeV	27 G	eV	39 G	eV	62.4 (GeV	
				Ge'			V		•	Ge										
																		e		
0).21-	-0.875	-172.5	40	39	42	42	43	34	32	31	$22_{\pm 1\pm 3}$	$24_{\pm 2\pm 5}$	$28_{\pm 1\pm 4}$	$26_{\pm 1 \pm 3}$	$3_{\pm1\pm0.4}$	$1_{\pm 0.4 \pm 0.4}$	$418_{\pm 1\pm 3}$	$20_{\pm 1.0 \pm 3}$	
0).23-	-0.875	-172.5	48	45	49	50	52	50	41	37	$27_{\pm 2\pm 3}$	$28_{\pm 2\pm 5}$	$33_{\pm 2\pm 4}$	$31_{\pm 2\pm 3}$	$6_{\pm1\pm0.7}$	$2_{\pm 0.5 \pm 0.5}$	$424_{\pm 1\pm 3}$	$23_{\pm1\pm3}$	
0).25-	-0.875	-172.5	54	50	53	56	57	36	48	40	$31_{\pm 2\pm 3}$	$30_{\pm 2 \pm 5}$	$36_{\pm 2\pm 4}$	$35_{\pm 2\pm 3}$	$8_{\pm1\pm1.0}$	$1_{\pm 0.4 \pm 0.4}$	$328_{\pm 2\pm 3}$	$25_{\pm1\pm3}$	
0).27-	-0.875	-172.5	59	51	56	61	66	0	53	43	$34_{\pm 2\pm 4}$	$31_{\pm 2\pm 4}$	$37_{\pm 2\pm 4}$	$39_{\pm 2\pm 3}$	$12_{\pm 2\pm 1}$	$0_{\pm0\pm0}$	$31_{\pm 2\pm 4}$	$27_{\pm1\pm3}$	
0).29-	-0.875	-172.5	60	55	59	62	63	0	53	46	$35_{\pm 2\pm 4}$	$33_{\pm 2\pm 4}$	$39_{\pm 2\pm 4}$	$40_{\pm 2\pm 3}$	$14_{\pm 2 \pm 2}$	$0_{\pm0\pm0}$	$32_{\pm 2\pm 4}$	$28_{\pm 1\pm 3}$	
0	.31-	-0.875	-172.5	64	55	59	66	66	0	57	47	$37_{\pm 2\pm 4}$	$33_{\pm 2\pm 4}$	$39_{\pm 2\pm 4}$	$43_{\pm 2\pm 3}$	$17_{\pm 2 \pm 2}$	$0_{\pm0\pm0}$	$35_{\pm 2\pm 4}$	$28_{\pm 1\pm 3}$	
0	.33-	-0.875	-172.5	63	59	63	65	59	0	56	51	$37_{\pm 2\pm 4}$	$35_{\pm 2\pm 4}$	$41_{\pm 2\pm 4}$	$43_{\pm 2\pm 3}$	$17_{\pm 2\pm 2}$	$0_{\pm0\pm0}$	$34_{\pm 2\pm 4}$	$30_{\pm 2\pm 4}$	
0	.35-	-0.875	-172.5	63	60	65	65	58	0	56	52	$38_{\pm 2\pm 4}$	$35_{\pm 2\pm 4}$	$42_{\pm 2\pm 5}$	$43_{\pm 2\pm 3}$	$19_{\pm 2 \pm 2}$	$0_{\pm0\pm0}$	$35_{\pm 2\pm 4}$	$30_{\pm 2\pm 4}$	
0	.37-	-0.875	-172.5	65	60	65	67	61	0	58	52	$39_{\pm 2\pm 4}$	$35_{\pm 2\pm 4}$	$41_{\pm 2\pm 4}$	$46_{\pm 2\pm 3}$	$22_{\pm 2\pm 2}$	$0_{\pm0\pm0}$	$36_{\pm 2\pm 4}$	$29_{\pm 2\pm 4}$	
0	.39-	-0.875	-172.5	65	62	66	67	62	0	58	55	$40_{\pm 2\pm 4}$	$36_{\pm2\pm4}$	$42_{\pm 2\pm 4}$	$46_{\pm 2\pm 3}$	$24_{\pm 2\pm 3}$	$0_{\pm0\pm0}$	$37_{\pm 2\pm 4}$	$30_{\pm 2\pm 4}$	
0	.42-	-0.875	-172.5	63	66	71	64	60	0	56	59	$38_{\pm 2\pm 4}$	$38_{\pm 2\pm 4}$	$44_{\pm 2 \pm 5}$	$44_{\pm 2\pm 3}$	$26_{\pm 2\pm 3}$	$0_{\pm0\pm0}$	$36_{\pm 2\pm 4}$	$31_{\pm 2\pm 4}$	
0	0.46-	-0.875	-172.5	63	67	72	66	62	0	57	60	$39_{\pm 2\pm 4}$	$38_{\pm 2 \pm 4}$	$43_{\pm 2 \pm 4}$	$46\pm2\pm3$	$31_{\pm 2 \pm 4}$	$0_{\pm 0 \pm 0}$	$37_{\pm 2\pm 4}$	$30_{\pm 2 \pm 4}$	
0).5 -	-0.875	-172.5	64	69	73	66	63	0	57	61	$40_{\pm 2\pm 4}$	$38_{\pm 2\pm 4}$	$42_{\pm 2\pm 3}$	$46_{\pm 2\pm 3}$	$35_{\pm 2\pm 3}$	$0_{\pm 0 \pm 0}$	$37_{\pm 1 \pm 3}$	$29_{\pm 2 \pm 2}$	
0	.54-	-0.875	-172.5	62	71	76	64	61	72	56	63	$38_{\pm 2\pm 4}$	$38_{\pm 2\pm 4}$	$43_{\pm 2\pm 3}$	$44_{\pm 2\pm 3}$	$35_{\pm 2\pm 3}$	$2_{\pm 0.5 \pm 0.5}$	$_{3}36_{\pm1\pm3}$	$29_{\pm 2 \pm 2}$	
0	.58-	-0.875	-172.5	61	71	76	63	61	70	56	63	$38_{\pm 2\pm 4}$	$36_{\pm 2\pm 4}$	$41_{\pm 2\pm 3}$	$44_{\pm 2\pm 3}$	$36_{\pm 2\pm 3}$	$3_{\pm 0.6 \pm 0.6}$	$536_{\pm 1\pm 3}$	$29_{\pm 2\pm 2}$	

Table A.3: (continued)

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0.62 - 0.875 \quad -172.5 \quad 62 \quad 68 \quad 73 \quad 64 \quad 62 \quad 49 \quad 56 \quad 61 \quad 39_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 4} \quad 39_{\pm 2 \pm 3} \quad 44_{\pm 2 \pm 3} \quad 37_{\pm 1 \pm 3} \quad 3_{\pm 0.6 \pm 0.7} \\ 36_{\pm 1 \pm 3} \quad 27_{\pm 2 \pm 2} \quad 27_{\pm 2 \pm 2}
 0.66 - 0.875 - 172.5
                                                                                                                                                                                  64\ 66\ 71\ 66\ 64\ 49\ 58\ 58\ 41_{\pm2\pm4}\ 32_{\pm2\pm3}\ 37_{\pm2\pm3}\ 45_{\pm2\pm3}\ 40_{\pm1\pm3}\ 4_{\pm0.7\pm1.0}37_{\pm1\pm3}\ 25_{\pm2\pm2}
 0.7 - 0.875 - 172.5
                                                                                                                                                                                  64 \ 66 \ 70 \ 66 \ 64 \ 56 \ 58 \ 58 \ 41_{\pm 2 \pm 4} \ 31_{\pm 2 \pm 3} \ 36_{\pm 2 \pm 3} \ 45_{\pm 2 \pm 3} \ 41_{\pm 1 \pm 3} \ 6_{\pm 0.9 \pm 1} \ 37_{\pm 1 \pm 3} \ 25_{\pm 2 \pm 2}
                                                                                                                                                                                  65\ 65\ 70\ 67\ 64\ 60\ 58\ 59\ 41_{\pm 2\pm 4}\ 30_{\pm 2\pm 3}\ 35_{\pm 2\pm 3}\ 45_{\pm 2\pm 3}\ 41_{\pm 1\pm 3}\ 7_{\pm 1\pm 2}\quad 37_{\pm 1\pm 3}\ 25_{\pm 2\pm 2}
 0.74 - 0.875 - 172.5
 0.78 - 0.875 - 172.5
                                                                                                                                                                                  64 \ 69 \ 73 \ 66 \ 63 \ 63 \ 58 \ 62 \ 40_{\pm 2 \pm 4} \ 31_{\pm 2 \pm 3} \ 36_{\pm 2 \pm 3} \ 45_{\pm 1 \pm 3} \ 40_{\pm 1 \pm 3} \ 9_{\pm 1 \pm 2} \ 36_{\pm 1 \pm 3} \ 26_{\pm 2 \pm 2}
                                                                                                                                                                                  63\  \, 70\  \, 74\  \, 65\  \, 62\  \, 65\  \, 57\  \, 62\  \, 39_{\pm2\pm4}\  \, 31_{\pm2\pm3}\  \, 36_{\pm2\pm3}\  \, 44_{\pm1\pm3}\  \, 40_{\pm1\pm4}\  \, 10_{\pm1\pm3}\  \, 35_{\pm1\pm3}\  \, 26_{\pm2\pm3}
 0.82 - 0.875 - 172.5
                                                                                                                                                                                  63 \ 69 \ 73 \ 64 \ 62 \ 66 \ 57 \ 62 \ 38_{\pm 2 \pm 4} \ 30_{\pm 2 \pm 3} \ 35_{\pm 2 \pm 3} \ 44_{\pm 1 \pm 3} \ 40_{\pm 1 \pm 4} \ 12_{\pm 1 \pm 3} \ 35_{\pm 1 \pm 3} \ 26_{\pm 2 \pm 3}
 0.86 - 0.875
                                                                                                  -172.5
                                                                                                                                                                                  63\ 68\ 73\ 65\ 63\ 67\ 57\ 61\ 38_{\pm 2 \pm 4}\ 29_{\pm 2 \pm 3}\ 35_{\pm 2 \pm 3}\ 44_{\pm 1 \pm 3}\ 40_{\pm 1 \pm 4}\ 13_{\pm 1 \pm 3}\ 35_{\pm 1 \pm 3}\ 25_{\pm 2 \pm 3}
 0.9 - 0.875
                                                                                                  -172.5
                                                                                                                                                                                63\ 68\ 73\ 65\ 63\ 67\ 57\ 61\ 39_{\pm 2 \pm 4}\ 29_{\pm 2 \pm 3}\ 35_{\pm 2 \pm 3}\ 43_{\pm 1 \pm 3}\ 40_{\pm 1 \pm 4}\ 14_{\pm 1 \pm 3}\ 35_{\pm 1 \pm 3}\ 25_{\pm 2 \pm 3}
 0.94 - 0.875 - 172.5
 0.98 - 0.875 \quad -172.5 \quad 64 \quad 66 \quad 72 \quad 64 \quad 63 \quad 68 \quad 57 \quad 60 \quad 40_{\pm 2 \pm 4} \quad 29_{\pm 2 \pm 3} \quad 34_{\pm 2 \pm 3} \quad 42_{\pm 1 \pm 3} \quad 40_{\pm 1 \pm 4} \quad 16_{\pm 2 \pm 4} \quad 35_{\pm 1 \pm 3} \quad 25_{\pm 2 \pm 3} \quad 
 1.1 \ \ -0.875 \quad \  -172.5 \quad \  66 \quad 62 \quad 68 \quad 66 \quad 65 \quad 65 \quad 59 \quad 57 \quad 43_{\pm 2 \pm 5} \ 29_{\pm 2 \pm 4} \ 31_{\pm 2 \pm 3} \ 41_{\pm 2 \pm 5} \ 41_{\pm 1 \pm 6} \quad 18_{\pm 2 \pm 6} \ 38_{\pm 1 \pm 5} \ 25_{\pm 2 \pm 4} 
                                                                                                                                                                                69\ 65\ 69\ 70\ 67\ 69\ 60\ 58\ 44_{\pm 2\pm 5}\ 29_{\pm 2\pm 4}\ 30_{\pm 2\pm 3}\ 42_{\pm 2\pm 5}\ 41_{\pm 2\pm 6}\ 25_{\pm 2\pm 8}\ 38_{\pm 1\pm 5}\ 22_{\pm 2\pm 4}
 1.3 -0.875 -172.5
 1.5 - 0.875 - 172.5
                                                                                                                                                                                  68\ 68\ 72\ 72\ 67\ 72\ 61\ 60\ 43_{\pm2\pm5}\ 33_{\pm2\pm8}\ 34_{\pm2\pm5}\ 47_{\pm1\pm10}42_{\pm2\pm7}\ 20_{\pm2\pm7}\ 40_{\pm1\pm7}\ 24_{\pm2\pm5}
 1.7 -0.875 -172.5
                                                                                                                                                                                65\ 73\ 76\ 69\ 65\ 72\ 59\ 63\ 41_{\pm2\pm8}\ 34_{\pm2\pm7}\ 36_{\pm2\pm5}\ 43_{\pm1\pm11}42_{\pm1\pm7}\ 26_{\pm2\pm9}\ 37_{\pm1\pm6}\ 27_{\pm2\pm5}
 1.9 - 0.875 - 172.5
                                                                                                                                                                                  63\ 73\ 76\ 68\ 65\ 72\ 59\ 63\ 38_{\pm2\pm8}\ 29_{\pm2\pm6}\ 35_{\pm2\pm5}\ 43_{\pm1\pm11}42_{\pm1\pm7}\ 26_{\pm2\pm9}\ 38_{\pm1\pm6}\ 27_{\pm2\pm5}
 0.21 - 0.875 - 157.5
                                                                                                                                                                                41\  \  \, 38\  \  \, 40\  \  \, 42\  \  \, 43\  \  \, 30\  \  \, 34\  \  \, 31\  \  \, 28_{\pm 1 \pm 4}\  \  \, 22_{\pm 1 \pm 3}\  \  \, 24_{\pm 1 \pm 3}\  \  \, 31_{\pm 1 \pm 4}\  \  \, 22_{\pm 1 \pm 3}\  \  \, 13_{\pm 1 \pm 2}\  \  \, 24_{\pm 1 \pm 4}\  \  \, 16_{\pm 1 \pm 3}
                                                                                                                                                                                  46\ \ 46\ \ 49\ \ 48\ \ 45\ \ 37\ \ 39\ \ 39\ \ 31_{\pm 2 \pm 4}\ 27_{\pm 2 \pm 3}\ \ 30_{\pm 2 \pm 3}\ \ 35_{\pm 1 \pm 4}\ \ 24_{\pm 1 \pm 3}\ \ 15_{\pm 1 \pm 2}\ \ 28_{\pm 1 \pm 4}\ \ 21_{\pm 1 \pm 3}
 0.23 - 0.875 - 157.5
 0.25 - 0.875 - 157.5
                                                                                                                                                                                  50\ 51\ 54\ 51\ 49\ 43\ 42\ 45\ 34_{\pm2\pm4}\ 30_{\pm2\pm3}\ 34_{\pm2\pm3}\ 38_{\pm1\pm4}\ 26_{\pm1\pm3}\ 16_{\pm1\pm2}\ 30_{\pm1\pm4}\ 25_{\pm1\pm3}
 0.27 - 0.875 - 157.5
                                                                                                                                                                                  52 \ 56 \ 59 \ 54 \ 50 \ 48 \ 45 \ 50 \ 35_{\pm 2 \pm 4} \ 33_{\pm 2 \pm 3} \ 37_{\pm 2 \pm 4} \ 39_{\pm 1 \pm 4} \ 26_{\pm 1 \pm 3} \ 16_{\pm 1 \pm 2} \ 31_{\pm 1 \pm 4} \ 28_{\pm 2 \pm 4}
 0.29 - 0.875 - 157.5
                                                                                                                                                                                  56 \ 58 \ 60 \ 57 \ 53 \ 50 \ 49 \ 52 \ 36_{\pm 2 \pm 4} \ 34_{\pm 2 \pm 3} \ 39_{\pm 2 \pm 4} \ 41_{\pm 2 \pm 4} \ 28_{\pm 2 \pm 4} \ 16_{\pm 1 \pm 2} \ 33_{\pm 1 \pm 4} \ 29_{\pm 2 \pm 4}
 0.31 - 0.875 - 157.5
                                                                                                                                                                                  56\ 62\ 65\ 58\ 52\ 56\ 50\ 55\ 36_{\pm 2 \pm 4}\ 36_{\pm 2 \pm 3}\ 42_{\pm 2 \pm 4}\ 41_{\pm 2 \pm 4}\ 28_{\pm 1 \pm 4}\ 16_{\pm 1 \pm 2}\ 33_{\pm 2 \pm 4}\ 32_{\pm 2 \pm 4}
                                                                                                                                                                                  60\ 61\ 64\ 61\ 56\ 58\ 53\ 54\ 37_{\pm 2 \pm 4}\ 35_{\pm 2 \pm 3}\ 42_{\pm 2 \pm 4}\ 43_{\pm 2 \pm 4}\ 31_{\pm 2 \pm 4}\ 15_{\pm 1 \pm 2}\ 35_{\pm 2 \pm 4}\ 32_{\pm 2 \pm 4}
 0.33 - 0.875 - 157.5
                                                                                                                                                                                  63\ 62\ 65\ 63\ 57\ 62\ 55\ 56\ 38_{\pm2\pm4}\ 36_{\pm2\pm3}\ 43_{\pm2\pm4}\ 44_{\pm2\pm4}\ 31_{\pm2\pm4}\ 14_{\pm1\pm2}\ 36_{\pm2\pm4}\ 33_{\pm2\pm4}
 0.35 - 0.875 - 157.5
                                                                                                                                                                                  62\ 65\ 67\ 63\ 56\ 74\ 55\ 58\ 37_{\pm 2 \pm 4}\ 38_{\pm 2 \pm 3}\ 46_{\pm 2 \pm 4}\ 44_{\pm 2 \pm 4}\ 31_{\pm 2 \pm 4}\ 15_{\pm 1 \pm 2}\ 35_{\pm 2 \pm 4}\ 35_{\pm 2 \pm 4}
 0.37-0.875 -157.5
                                                                                                                                                                                  64\ 65\ 66\ 65\ 58\ 79\ 57\ 57\ 37_{\pm 2 \pm 4}\ 38_{\pm 2 \pm 3}\ 45_{\pm 2 \pm 4}\ 44_{\pm 2 \pm 4}\ 32_{\pm 2 \pm 4}\ 13_{\pm 1 \pm 2}\ 36_{\pm 2 \pm 4}\ 35_{\pm 2 \pm 4}
 0.39 - 0.875 - 157.5
 0.42 - 0.875 - 157.5
                                                                                                                                                                                  69\ 62\ 64\ 70\ 62\ 82\ 61\ 56\ 39_{\pm 2\pm 4}\ 36_{\pm 2\pm 3}\ 45_{\pm 2\pm 4}\ 47_{\pm 2\pm 4}\ 35_{\pm 2\pm 4}\ 10_{\pm 1\pm 1}\ 37_{\pm 2\pm 4}\ 34_{\pm 2\pm 4}
 0.46 - 0.875 - 157.5
                                                                                                                                                                                  69\ 63\ 65\ 70\ 63\ 20\ 63\ 56\ 37_{\pm3\pm3}\ 37_{\pm2\pm3}\ 46_{\pm2\pm4}\ 46_{\pm2\pm4}\ 36_{\pm2\pm4}\ 1_{\pm0.3\pm0.2}36_{\pm2\pm4}\ 35_{\pm1\pm5}
 0.5 - 0.875 - 157.5
                                                                                                                                                                                  70 63 66 71 63 0
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 0.54 - 0.875 - 157.5
                                                                                                                                                                                  72 60 64 73 65 0
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                                                                                                                                                                                  73 60 63 74 66 0
 0.58 - 0.875 - 157.5
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 0.62 - 0.875
 0.66 - 0.875
                                                                                                    -157.5
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 0.7 - 0.875
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 0.74 - 0.875
                                                                                                  -157.5
                                                                                                                                                                                  67 63 66 68 65 0
 0.78 - 0.875 - 157.5
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 0.82 - 0.875 - 157.5
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 0.86 - 0.875 - 157.5
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 0.9 - 0.875 - 157.5
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 0.94 - 0.875 - 157.5
                                                                                                                                                                                  68 60 64 69 67 0
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 0.98-0.875 -157.5 68 59 65 68 66 0
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 1.1 -0.875 -157.5 65 62 67 65 65 0
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 1.3 -0.875 -157.5 65 67 69 66 63 0
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 1.5 \ -0.875 \ \ -157.5 \ \ 66 \ \ 67 \ \ 69 \ \ 69 \ \ 62 \ \ 0 \ \ 59 \ \ 59 \ \ 29_{\pm 2 \pm 4} \ 38_{\pm 2 \pm 9} \ \ 46_{\pm 1 \pm 6} \ \ 31_{\pm 2 \pm 7} \ \ 5_{\pm 0.9 \pm 0.9} 0_{\pm 0 \pm 0}
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 1.7 \ \ -0.875 \quad \  -157.5 \quad \  71 \quad 65 \quad 69 \quad 72 \quad 78 \quad 0 \quad \  63 \quad 58 \quad 32_{\pm 2 \pm 6} \ 46_{\pm 2 \pm 9} \ 43_{\pm 1 \pm 6} \ 31_{\pm 2 \pm 8} \ 7_{\pm 1 \pm 1} \quad \  0_{\pm 0 \pm 0}
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 0.21 - 0.875 \quad -142.5 \quad 40 \quad 40 \quad 40 \quad 41 \quad 32 \quad 43 \quad 34 \quad 45 \quad 19_{\pm 2 \pm 3} \quad 27_{\pm 1 \pm 5} \quad 30_{\pm 1 \pm 3} \quad 24_{\pm 1 \pm 3} \quad 18_{\pm 1 \pm 3} \quad 24_{\pm 1 \pm 4} \quad 18_{\pm 1 \pm 3} \quad 23_{\pm 2 \pm 4} \quad 23_{\pm 4} \quad 2
 0.23 - 0.875 \quad -142.5 \quad 48 \quad 46 \quad 46 \quad 49 \quad 41 \quad 48 \quad 43 \quad 47 \quad 24_{\pm 2 \pm 3} \quad 31_{\pm 2 \pm 5} \quad 34_{\pm 1 \pm 3} \quad 29_{\pm 2 \pm 3} \quad 21_{\pm 1 \pm 3} \quad 26_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 25_{\pm 2 \pm 4} \quad 24_{\pm 1 \pm 4} \quad 
 0.25 - 0.875 \quad -142.5 \quad 53 \quad 50 \quad 50 \quad 54 \quad 48 \quad 50 \quad 50 \quad 49 \quad 27_{\pm 2 \pm 3} \quad 34_{\pm 2 \pm 5} \quad 36_{\pm 2 \pm 4} \quad 33_{\pm 2 \pm 3} \quad 23_{\pm 2 \pm 3} \quad 27_{\pm 2 \pm 4} \quad 28_{\pm 2 \pm 4} \quad 26_{\pm 2 \pm 4} \quad 26_{\pm 2 \pm 4} \quad 28_{\pm 4
 0.27 - 0.875 \quad -142.5 \quad 57 \quad 52 \quad 53 \quad 59 \quad 54 \quad 49 \quad 55 \quad 51 \quad 30_{\pm 2 \pm 3} \quad 35_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 4} \quad 36_{\pm 2 \pm 3} \quad 24_{\pm 2 \pm 3} \quad 27_{\pm 2 \pm 4} \quad 31_{\pm 2 \pm 4} \quad 27_{\pm 2 \pm 4} \quad 
 0.29 - 0.875 \quad -142.5 \quad 58 \quad 56 \quad 57 \quad 60 \quad 57 \quad 52 \quad 55 \quad 54 \quad 32_{\pm 2 \pm 3} \quad 37_{\pm 2 \pm 4} \quad 40_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 3} \quad 23_{\pm 2 \pm 3} \quad 28_{\pm 2 \pm 4} \quad 32_{\pm 2 \pm 4} \quad 29_{\pm 4
 0.31 - 0.875 \quad -142.5 \quad 62 \quad 56 \quad 57 \quad 64 \quad 64 \quad 52 \quad 59 \quad 54 \quad 35_{\pm 2 \pm 3} \quad 36_{\pm 2 \pm 4} \quad 40_{\pm 2 \pm 4} \quad 41_{\pm 2 \pm 4} \quad 24_{\pm 2 \pm 3} \quad 28_{\pm 2 \pm 4} \quad 35_{\pm 2 \pm 4} \quad 29_{\pm 4
 0.33 - 0.875 \quad -142.5 \quad 60 \quad 61 \quad 61 \quad 63 \quad 67 \quad 56 \quad 58 \quad 57 \quad 35_{\pm 2 \pm 4} \quad 39_{\pm 2 \pm 4} \quad 42_{\pm 2 \pm 4} \quad 40_{\pm 2 \pm 4} \quad 22_{\pm 2 \pm 3} \quad 30_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 4} \quad 30_{\pm 4 \pm 4} \quad 
 0.35 - 0.875 \quad -142.5 \quad 61 \quad 62 \quad 63 \quad 63 \quad 70 \quad 57 \quad 58 \quad 58 \quad 37_{\pm 2 \pm 4} \quad 39_{\pm 2 \pm 4} \quad 43_{\pm 2 \pm 4} \quad 41_{\pm 2 \pm 4} \quad 21_{\pm 2 \pm 2} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 5} \quad 
 0.37 - 0.875 \quad -142.5 \quad 64 \quad 62 \quad 63 \quad 65 \quad 83 \quad 56 \quad 61 \quad 58 \quad 39_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 4} \quad 41_{\pm 2 \pm 4} \quad 43_{\pm 2 \pm 4} \quad 21_{\pm 2 \pm 2} \quad 30_{\pm 2 \pm 4} \quad 37_{\pm 2 \pm 5} \quad 30_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 4} \quad 48_{\pm 2 \pm 4} \quad 
 0.39 - 0.875 \quad -142.5 \quad 63 \quad 64 \quad 64 \quad 65 \quad 85 \quad 58 \quad 60 \quad 60 \quad 40_{\pm 2 \pm 4} \quad 39_{\pm 2 \pm 4} \quad 42_{\pm 2 \pm 4} \quad 44_{\pm 2 \pm 4} \quad 19_{\pm 2 \pm 2} \quad 31_{\pm 2 \pm 4} \quad 37_{\pm 2 \pm 5} \quad 31_{\pm 2 \pm 5} \quad 
 0.42 - 0.875 \quad -142.5 \quad 60 \quad 69 \quad 69 \quad 62 \quad 81 \quad 63 \quad 58 \quad 64 \quad 39_{\pm 2 \pm 4} \quad 41_{\pm 3 \pm 4} \quad 44_{\pm 2 \pm 4} \quad 42_{\pm 2 \pm 4} \quad 13_{\pm 1 \pm 2} \quad 33_{\pm 2 \pm 5} \quad 36_{\pm 2 \pm 5} \quad 33_{\pm 2 \pm 5} \quad 
 0.46 - 0.875 \quad -142.5 \quad 62 \quad 70 \quad 70 \quad 64 \quad 53 \quad 64 \quad 59 \quad 65 \quad 42_{\pm 2 \pm 4} \quad 40_{\pm 3 \pm 4} \quad 42_{\pm 2 \pm 4} \quad 44_{\pm 2 \pm 4} \quad 5_{\pm 0.7 \pm 0.6} \\ 33_{\pm 2 \pm 5} \quad 37_{\pm 2 \pm 5} \quad 33_{\pm 2 \pm 5}
                                                                                                                                                                                  62\ 71\ 71\ 64\ 65\ 63\ 60\ 65\ 44_{\pm 2\pm 4}\ 39_{\pm 3\pm 4}\ 41_{\pm 2\pm 2}\ 45_{\pm 2\pm 4}\ 2_{\pm 0.9\pm 0.1}32_{\pm 2\pm 4}\ 38_{\pm 2\pm 4}\ 33_{\pm 2\pm 4}
 0.5 - 0.875 - 142.5
 0.54 - 0.875 \quad -142.5 \quad 60 \quad 74 \quad 74 \quad 62 \quad 0 \quad 66 \quad 58 \quad 67 \quad 42_{\pm 2 \pm 4} \quad 40_{\pm 3 \pm 4} \quad 41_{\pm 2 \pm 2} \quad 43_{\pm 2 \pm 4} \quad 0_{\pm 0 \pm 0} \quad 30_{\pm 2 \pm 4} \quad 37_{\pm 2 \pm 4} \quad 33_{\pm 4}
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Table A.3: (continued)

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0.7 \ \ -0.875 \quad \  -142.5 \quad \  63 \quad 69 \quad 69 \quad 65 \quad 0 \quad \  65 \quad 61 \quad 62 \quad 42_{\pm 2 \pm 4} \quad 36_{\pm 2 \pm 3} \quad 35_{\pm 2 \pm 2} \quad 44_{\pm 1 \pm 4} \quad 0_{\pm 0 \pm 0} \quad \  20_{\pm 2 \pm 2} \quad 39_{\pm 1 \pm 4} \quad 28_{\pm 2 \pm 3} \quad 38_{\pm 2 \pm 3} \quad 38_{\pm 2 \pm 2} \quad 48_{\pm 2 \pm 3} \quad 38_{\pm 2 \pm 2} \quad 48_{\pm 2 \pm 3} \quad 38_{\pm 2 \pm 2} \quad 38_
   0.74 - 0.875 \quad -142.5 \quad 63 \quad 69 \quad 69 \quad 65 \quad 0 \quad 65 \quad 61 \quad 61 \quad 43_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 3} \quad 35_{\pm 2 \pm 2} \quad 44_{\pm 1 \pm 4} \quad 0_{\pm 0 \pm 0} \quad 18_{\pm 2 \pm 2} \quad 39_{\pm 1 \pm 4} \quad 28_{\pm 2 \pm 3} \quad 38_{\pm 2 \pm 3} \quad 38_{\pm 2 \pm 2} \quad 48_{\pm 2 \pm 3} \quad 18_{\pm 2 \pm 2} \quad 18
   0.78 - 0.875
                                                                                                                                                                                                                  -142.5
                                                                                                                                                                                                                                                                                                                                                                                                  62\ 71\ 71\ 64\ 0\ 69\ 60\ 63\ 42_{\pm 2\pm 4}\ 34_{\pm 2\pm 3}\ 35_{\pm 2\pm 2}\ 43_{\pm 1\pm 3}\ 0_{\pm 0\pm 0}\ 17_{\pm 2\pm 2}\ 37_{\pm 1\pm 4}\ 29_{\pm 2\pm 3}
                                                                                                                                                                                                                         -142.5 \quad 61 \quad 72 \quad 72 \quad 63 \quad 0 \quad 71 \quad 59 \quad 64 \quad 42_{\pm 2 \pm 4} \quad 33_{\pm 2 \pm 3} \quad 35_{\pm 2 \pm 2} \quad 42_{\pm 1 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 16_{\pm 2 \pm 3} \quad 36_{\pm 1 \pm 4} \quad 29_{\pm 2 \pm 4} \quad 38_{\pm 4} \quad 
   0.82 - 0.875
   0.86 - 0.875
                                                                                                                                                                                                                      -142.5 \quad 62 \quad 73 \quad 72 \quad 63 \quad 0 \quad 70 \quad 59 \quad 64 \quad 43_{\pm 2 \pm 4} \quad 32_{\pm 2 \pm 3} \quad 34_{\pm 2 \pm 2} \quad 42_{\pm 1 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 15_{\pm 2 \pm 3} \quad 36_{\pm 1 \pm 4} \quad 29_{\pm 2 \pm 4} \quad 39_{\pm 2 \pm 4} \quad 29_{\pm 4} \quad 29
   0.9 - 0.875
                                                                                                                                                                                                                         -142.5 \quad 62 \quad 71 \quad 72 \quad 63 \quad 0 \quad 69 \quad 59 \quad 63 \quad 44_{\pm 2 \pm 4} \quad 31_{\pm 2 \pm 3} \quad 34_{\pm 2 \pm 2} \quad 42_{\pm 1 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 13_{\pm 1 \pm 2} \quad 36_{\pm 1 \pm 4} \quad 29_{\pm 2 \pm 4} \quad 31_{\pm 2 \pm 3} \quad 34_{\pm 2 \pm 2} \quad 42_{\pm 1 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 13_{\pm 1 \pm 2} \quad 36_{\pm 1 \pm 4} \quad 29_{\pm 2 \pm 4} \quad 31_{\pm 2 \pm 3} \quad 34_{\pm 2 \pm 2} \quad 42_{\pm 1 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 13_{\pm 1 \pm 2} \quad 36_{\pm 1 \pm 4} \quad 29_{\pm 2 \pm 4} \quad 31_{\pm 2 \pm 3} \quad 34_{\pm 2 \pm 2} \quad 42_{\pm 1 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 13_{\pm 1 \pm 2} \quad 36_{\pm 1 \pm 4} \quad 29_{\pm 2 \pm 4} \quad 31_{\pm 2 \pm 3} \quad 34_{\pm 2 \pm 2} \quad 42_{\pm 1 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 13_{\pm 1 \pm 2} \quad 36_{\pm 1 \pm 4} \quad 29_{\pm 2 \pm 4} \quad 31_{\pm 2 \pm 3} \quad 34_{\pm 2 \pm 2} \quad 42_{\pm 1 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 13_{\pm 1 \pm 2} \quad 36_{\pm 1 \pm 4} \quad 29_{\pm 2 \pm 4} \quad 31_{\pm 2 \pm 3} \quad 34_{\pm 2 \pm 2} \quad 42_{\pm 1 \pm 3} \quad 34_{\pm 2 \pm 2} \quad 34_{\pm 2 \pm 4} \quad 34_{\pm 4 \pm 4} \quad 34_{\pm 4
                                                                                                                                                                                                                         -142.5 \quad 62 \quad 70 \quad 72 \quad 63 \quad 0 \quad 68 \quad 60 \quad 63 \quad 42_{\pm 2 \pm 4} \quad 30_{\pm 2 \pm 3} \quad 33_{\pm 2 \pm 2} \quad 41_{\pm 1 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 12_{\pm 1 \pm 2} \quad 36_{\pm 1 \pm 4} \quad 28_{\pm 2 \pm 4} \quad 30_{\pm 1 \pm 4} \quad 28_{\pm 2 \pm 4} \quad 30_{\pm 1 \pm 4} \quad 28_{\pm 2 \pm 4} \quad 30_{\pm 1 \pm 4} \quad 30
0.94 - 0.875
                                                                                                                                                                                                                         -142.5 \quad 63 \quad 70 \quad 72 \quad 62 \quad 0 \quad 66 \quad 59 \quad 62 \quad 42_{\pm 2 \pm 4} \quad 30_{\pm 2 \pm 3} \quad 33_{\pm 2 \pm 2} \quad 40_{\pm 1 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 11_{\pm 1 \pm 2} \quad 36_{\pm 1 \pm 4} \quad 27_{\pm 2 \pm 4} \quad 30_{\pm 1 \pm 4} \quad 27_{\pm 2 \pm 4} \quad 27_{\pm 4}
0.98 - 0.875
                                                                                                                                                                                                                         1.1 -0.875
   1.3 -0.875
                                                                                                                                                                                                                         -142.5 \quad 67 \quad 71 \quad 70 \quad 70 \quad 0 \quad 67 \quad 62 \quad 61 \quad 36_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 8} \quad 30_{\pm 2 \pm 4} \quad 42_{\pm 2 \pm 9} \quad 0_{\pm 0 \pm 0} \quad 5_{\pm 0.9 \pm 2} \quad 39_{\pm 2 \pm 8} \quad 31_{\pm 2 \pm 7} \quad 39_{\pm 2 \pm 8} \quad 3
   1.5 - 0.875
                                                                                                                                                                                                                      -142.5 \quad 64 \quad 74 \quad 74 \quad 66 \quad 0 \quad 84 \quad 61 \quad 64 \quad 39_{\pm 2\pm 8} \quad 35_{\pm 3\pm 7} \quad 34_{\pm 2\pm 5} \quad 42_{\pm 1\pm 11} \\ 0_{\pm 0\pm 0} \quad 6_{\pm 1\pm 2} \quad 37_{\pm 1\pm 6} \quad 30_{\pm 2\pm 6} \quad 38_{\pm 3\pm 7} \quad 38_{\pm 3\pm 
   1.7 - 0.875
   0.23 - 0.875
                                                                                                                                                                                                                  -127.5 \quad 46 \quad 48 \quad 49 \quad 45 \quad 60 \quad 43 \quad 39 \quad 45 \quad 29_{\pm 2 \pm 3} \quad 26_{\pm 2 \pm 4} \quad 29_{\pm 2 \pm 3} \quad 29_{\pm 1 \pm 3} \quad 2_{\pm 0.6 \pm 0.3} \\ 17_{\pm 1 \pm 3} \quad 26_{\pm 1 \pm 5} \quad 19_{\pm 1 \pm 3} \quad 29_{\pm 1 \pm 3}
   0.25 - 0.875 \quad -127.5 \quad 49 \quad 54 \quad 54 \quad 49 \quad 75 \quad 50 \quad 43 \quad 52 \quad 31_{\pm 2 \pm 3} \quad 30_{\pm 2 \pm 4} \quad 33_{\pm 2 \pm 3} \quad 31_{\pm 2 \pm 3} \quad 2_{\pm 0.7 \pm 0.3} \\ 20_{\pm 1 \pm 3} \quad 28_{\pm 1 \pm 5} \quad 22_{\pm 2 \pm 3} \quad 20_{\pm 1 \pm 3}
                                                                                                                                                                                                                      -127.5 \quad 52 \quad 59 \quad 59 \quad 52 \quad 100 \quad 58 \quad 46 \quad 58 \quad 32_{\pm 2 \pm 3} \quad 33_{\pm 2 \pm 4} \quad 36_{\pm 2 \pm 4} \quad 33_{\pm 2 \pm 3} \quad 2_{\pm 1 \pm 0.3} \quad 24_{\pm 2 \pm 3} \quad 29_{\pm 1 \pm 5} \quad 25_{\pm 2 \pm 4} \quad 20_{\pm 1 \pm 5} 
   0.27 - 0.875
   0.29 - 0.875
                                                                                                                                                                                                                      -127.5 \quad 56 \quad 60 \quad 60 \quad 55 \quad 0 \quad 61 \quad 51 \quad 60 \quad 34_{\pm 2 \pm 3} \quad 33_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 4} \quad 35_{\pm 2 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 25_{\pm 2 \pm 3} \quad 32_{\pm 1 \pm 5} \quad 25_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 4} \quad 38
   0.31 - 0.875
                                                                                                                                                                                                                         -127.5 \quad 56 \quad 63 \quad 64 \quad 55 \quad 0 \quad 64 \quad 52 \quad 63 \quad 34_{\pm 2 \pm 3} \quad 36_{\pm 2 \pm 4} \quad 41_{\pm 2 \pm 4} \quad 35_{\pm 2 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 27_{\pm 2 \pm 4} \quad 32_{\pm 2 \pm 5} \quad 27_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 28_{\pm 2 \pm 4} \quad 28_{\pm 2 \pm 5} \quad 28
   0.33 - 0.875
                                                                                                                                                                                                                         -127.5 \quad 60 \quad 63 \quad 63 \quad 60 \quad 0 \quad 61 \quad 56 \quad 61 \quad 36_{\pm 2 \pm 3} \quad 36_{\pm 2 \pm 4} \quad 41_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 26_{\pm 2 \pm 4} \quad 33_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 4} \quad 26_{\pm 2 \pm 5} \quad 26
                                                                                                                                                                                                                      -127.5 \quad 62 \quad 63 \quad 64 \quad 61 \quad 0 \quad 62 \quad 58 \quad 61 \quad 36_{\pm 2 \pm 3} \quad 37_{\pm 2 \pm 4} \quad 43_{\pm 2 \pm 4} \quad 39_{\pm 2 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 26_{\pm 2 \pm 4} \quad 33_{\pm 2 \pm 4} \quad 27_{\pm 2 \pm 4}
   0.35 - 0.875
   0.37 - 0.875 \quad -127.5 \quad 62 \quad 66 \quad 67 \quad 61 \quad 0 \quad 65 \quad 58 \quad 64 \quad 36_{\pm 2 \pm 3} \quad 39_{\pm 2 \pm 4} \quad 45_{\pm 2 \pm 4} \quad 39_{\pm 2 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 28_{\pm 2 \pm 4} \quad 33_{\pm 2 \pm 4} \quad 28_{\pm 4} 
   0.39 - 0.875 \quad -127.5 \quad 63 \quad 65 \quad 66 \quad 62 \quad 0 \quad 64 \quad 60 \quad 63 \quad 36_{\pm 2 \pm 3} \quad 39_{\pm 2 \pm 4} \quad 46_{\pm 2 \pm 4} \quad 39_{\pm 2 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 27_{\pm 2 \pm 4} \quad 32_{\pm 2 \pm 4} \quad 28_{\pm 4} \quad 28
   0.42 - 0.875 \quad -127.5 \quad 68 \quad 62 \quad 63 \quad 67 \quad 0 \quad 60 \quad 63 \quad 61 \quad 38_{\pm 2 \pm 3} \quad 37_{\pm 2 \pm 4} \quad 44_{\pm 2 \pm 4} \quad 42_{\pm 2 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 26_{\pm 2 \pm 4} \quad 32_{\pm 2 \pm 4} \quad 27_{\pm 4} 
   0.46 - 0.875 \quad -127.5 \quad 69 \quad 64 \quad 64 \quad 68 \quad 0 \quad 62 \quad 63 \quad 62 \quad 37_{\pm 2 \pm 3} \quad 39_{\pm 2 \pm 4} \quad 46_{\pm 2 \pm 4} \quad 42_{\pm 2 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 27_{\pm 2 \pm 4} \quad 30_{\pm 2 \pm 4} \quad 28_{\pm 2 \pm 4} \quad 28_{\pm 2 \pm 4} \quad 48_{\pm 4} 
   0.5 -0.875
                                                                                                                                                                                                                  -127.5 \quad 69 \quad 64 \quad 65 \quad 68 \quad 0 \quad 64 \quad 63 \quad 64 \quad 36_{\pm 2 \pm 3} \quad 40_{\pm 2 \pm 4} \quad 47_{\pm 2 \pm 3} \quad 42_{\pm 2 \pm 3} \quad 0_{\pm 0 \pm 0} \quad 28_{\pm 2 \pm 3} \quad 28_{\pm 2 \pm 3} \quad 29_{\pm 2 \pm 3}
   0.54 - 0.875
                                                                                                                                                                                                                  -127.5
                                                                                                                                                                                                                                                                                                                                                                                               72 \ 62 \ 63 \ 71 \ 68 \ 61 \ 66 \ 62 \ 38_{\pm 3 \pm 3} \ 38_{\pm 2 \pm 4} \ 46_{\pm 2 \pm 3} \ 42_{\pm 2 \pm 3} \ 2_{\pm 0.5 \pm 0.3} 28_{\pm 2 \pm 3} \ 28_{\pm 2 \pm 3} \ 28_{\pm 2 \pm 3}
                                                                                                                                                                                                                         -127.5
   0.58 - 0.875
                                                                                                                                                                                                                                                                                                                                                                                                  73 \ 61 \ 63 \ 71 \ 77 \ 62 \ 67 \ 61 \ 38_{\pm 3 \pm 3} \ 38_{\pm 2 \pm 4} \ 45_{\pm 1 \pm 3} \ 41_{\pm 2 \pm 3} \ 4_{\pm 0.8 \pm 0.5} \ 30_{\pm 2 \pm 4} \ 27_{\pm 2 \pm 3} \ 29_{\pm 2 \pm 4}
                                                                                                                                                                                                                                                                                                                                                                                                  71 \ 62 \ 63 \ 70 \ 64 \ 63 \ 66 \ 62 \ 37_{\pm 2 \pm 3} \ 38_{\pm 2 \pm 4} \ 45_{\pm 1 \pm 3} \ 39_{\pm 2 \pm 3} \ 5_{\pm 0.8 \pm 0.7} \ 32_{\pm 2 \pm 4} \ 26_{\pm 2 \pm 3} \ 30_{\pm 2 \pm 4}
   0.62 - 0.875
                                                                                                                                                                                                                  -127.5
   0.66 - 0.875
                                                                                                                                                                                                                             -127.5
                                                                                                                                                                                                                                                                                                                                                                                                  68\ 64\ 65\ 66\ 54\ 65\ 64\ 63\ 36_{\pm2\pm3}\ 40_{\pm2\pm4}\ 47_{\pm1\pm3}\ 36_{\pm2\pm3}\ 5_{\pm0.8\pm0.9}34_{\pm2\pm4}\ 24_{\pm2\pm3}\ 31_{\pm2\pm4}
                                                                                                                                                                                                                                                                                                                                                                                               67 \ 65 \ 65 \ 67 \ 61 \ 65 \ 63 \ 36_{\pm 2 \pm 3} \ 40_{\pm 2 \pm 4} \ 47_{\pm 1 \pm 3} \ 35_{\pm 2 \pm 3} \ 8_{\pm 1 \pm 1} \quad 36_{\pm 2 \pm 4} \ 24_{\pm 2 \pm 2} \ 32_{\pm 2 \pm 4}
   0.7 - 0.875
                                                                                                                                                                                                                                -127.5
                                                                                                                                                                                                                      0.74 - 0.875
   0.78 - 0.875
   0.82 - 0.875
0.86 - 0.875
0.9 - 0.875
                                                                                                                                                                                                                  -127.5
0.94-0.875 -127.5
                                                                                                                                                                                                                                                                                                                                                                                                  70 62 64 69 73 62 71 61 33_{\pm 2\pm 3} 36_{\pm 2\pm 4} 41_{\pm 1\pm 3} 31_{\pm 2\pm 2} 11_{\pm 1\pm 2} 34_{\pm 2\pm 6} 25_{\pm 2\pm 3} 30_{\pm 2\pm 5}
0.98 - 0.875 \quad -127.5 \quad 69 \quad 61 \quad 65 \quad 68 \quad 73 \quad 62 \quad 71 \quad 61 \quad 32_{\pm 2 \pm 3} \quad 36_{\pm 2 \pm 4} \quad 41_{\pm 1 \pm 3} \quad 30_{\pm 2 \pm 2} \quad 12_{\pm 1 \pm 2} \quad 34_{\pm 2 \pm 6} \quad 25_{\pm 2 \pm 3} \quad 31_{\pm 2 \pm 5} \quad 
1.1 \;\; -0.875 \;\; -127.5 \;\; 67 \;\; 65 \;\; 67 \;\; 64 \;\; 69 \;\; 66 \;\; 68 \;\; 64 \;\; 30_{\pm 2 \pm 3} \;\; 41_{\pm 2 \pm 6} \;\; 43_{\pm 1 \pm 4} \;\; 27_{\pm 2 \pm 4} \;\; 15_{\pm 2 \pm 3} \;\; 34_{\pm 2 \pm 9} \;\; 24_{\pm 2 \pm 3} \;\; 36_{\pm 2 \pm 7} \;\; 36_{\pm 2 \pm 7} \;\; 38_{\pm 2 \pm 7} \;\; 28_{\pm 1 \pm 1} \;\; 28_{\pm 1} 
1.3 \ \ -0.875 \quad \  -127.5 \quad \  \  68 \quad 69 \quad 70 \quad 67 \quad 72 \quad 69 \quad 69 \quad 65 \quad 34_{\pm 2 \pm 3} \quad 46_{\pm 2 \pm 6} \quad 45_{\pm 1 \pm 4} \quad 33_{\pm 2 \pm 4} \quad 19_{\pm 2 \pm 4} \quad 38_{\pm 2 \pm 10} \quad 26_{\pm 2 \pm 4} \quad 35_{\pm 2 \pm 6} \quad 35_{\pm 2 \pm 6} \quad 10^{-1} \quad 10^
   1.5 \ \ -0.875 \quad \  -127.5 \quad \  69 \quad 70 \quad 69 \quad 68 \quad 76 \quad 69 \quad 71 \quad 65 \quad 31_{\pm 2 \pm 3} \quad 43_{\pm 2 \pm 10} \\ 42_{\pm 1 \pm 6} \quad 29_{\pm 2 \pm 6} \quad 24_{\pm 2 \pm 4} \quad 34_{\pm 2 \pm 10} \\ 26_{\pm 2 \pm 5} \quad 32_{\pm 2 \pm 8} \quad 24_{\pm 2 \pm 10} \quad 24_{\pm 2 \pm 10} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_{\pm 2 \pm 5} \\ 26_{\pm 2 \pm 5} \quad 26_
   1.7 \;\; -0.875 \quad -127.5 \quad 72 \;\; 67 \;\; 68 \;\; 72 \;\; 78 \;\; 67 \;\; 77 \;\; 63 \;\; 34_{\pm 2 \pm 7} \;\; 40_{\pm 2 \pm 8} \;\; 40_{\pm 1 \pm 6} \;\; 35_{\pm 2 \pm 9} \;\; 26_{\pm 2 \pm 5} \;\; 34_{\pm 2 \pm 11} \;\; 30_{\pm 2 \pm 5} \;\; 33_{\pm 2 \pm 7} \;\; 33
1.9 \ -0.875 \ -127.5 \ 74 \ 68 \ 68 \ 73 \ 79 \ 67 \ 77 \ 63 \ 34_{\pm 2 \pm 7} \ 43_{\pm 2 \pm 9} \ 42_{\pm 1 \pm 6} \ 30_{\pm 2 \pm 8} \ 29_{\pm 2 \pm 5} \ 35_{\pm 2 \pm 11} \ 29_{\pm 2 \pm 5} \ 32_{\pm 2 \pm 7} \ 43_{\pm 2 \pm 7} \ 43_{\pm 2 \pm 9} \ 42_{\pm 1 \pm 6} \ 30_{\pm 2 \pm 8} \ 29_{\pm 2 \pm 5} \ 35_{\pm 2 \pm 11} \ 29_{\pm 2 \pm 5} \ 32_{\pm 2 \pm 7} \ 43_{\pm 2 \pm 7} \ 43_{\pm 2 \pm 9} \ 42_{\pm 1 \pm 6} \ 43_{\pm 2 \pm 8} \ 29_{\pm 2 \pm 5} \ 35_{\pm 2 \pm 11} \ 29_{\pm 2 \pm 5} \ 32_{\pm 2 \pm 7} \ 43_{\pm 2 \pm 7} \ 43_{\pm 2 \pm 9} \ 42_{\pm 1 \pm 6} \ 43_{\pm 2 \pm 8} \ 43_{\pm 2 \pm 1} \ 43_{\pm 2 \pm 1}
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Table A.4: TOF Matching (ε_{TOF}) and Total Track (ε_{tot}) Efficiencies for $\eta > 0$. Only an excerpt is listed here with the full table in the supporting information [290].

n_				$arepsilon_{ ext{TC}}$)F					$arepsilon_{tot} \pm \Delta arepsilon_{stat} \pm \Delta arepsilon_{syst}$							
p_T η	ϕ	19.6	27	,	39)	62.	4	19.6 ($^{\circ}$ oV	27 G	αV	39 G	ωV	62.4 ($\gamma_{o}V$	
		GeV	Ge	V	Ge	V	Ge	V	19.0 (3E V	27 G	ev	39 G	ie v	02.4	JE V	
		e- e+	e-	e^{+}	e-	e^{+}	e-	e^{+}	e-	e^+	e-	e^+	e ⁻	e^+	e ⁻	e^+	
0.21 0.125	-172.5	56 57	54	58	56	59	53	55	$47_{\pm 2\pm 4}$	$50_{\pm 1 \pm 4}$	$51_{\pm 0.9\pm}$	50 _{±1±3}	$44_{\pm 1 \pm 5}$	$48_{\pm1\pm6}$	$45_{\pm1\pm5}$	$44_{\pm 1\pm 5}$	
0.23 0.125	-172.5	59 60	58	61	60	63	57	59	$50_{\pm 2\pm 4}$	$53_{\pm 2\pm 4}$	$54_{\pm 1.0 \pm}$	53 _{±1±4}	$47_{\pm 1 \pm 5}$	$50_{\pm1\pm7}$	$47_{\pm 1 \pm 5}$	$47_{\pm 2\pm 6}$	
0.25 0.125	-172.5	61 63	62	63	62	66	58	62	$52_{\pm 2\pm 4}$	$56_{\pm 2\pm 4}$	$57_{\pm 1 \pm 5}$	$55_{\pm1\pm4}$	$49_{\pm 1 \pm 5}$	$51_{\pm 2\pm 7}$	$49_{\pm 1 \pm 5}$	$49_{\pm 2 \pm 6}$	
0.27 0.125	-172.5	64 63	62	65	65	67	61	62	$55_{\pm 2\pm 4}$	$56_{\pm 2\pm 4}$	$57_{\pm 1 \pm 5}$	$58_{\pm1\pm4}$	$52_{\pm1\pm6}$	$51_{\pm 2\pm 7}$	$51_{\pm1\pm5}$	$49_{\pm 2 \pm 6}$	
0.29 0.125	-172.5	64 66	65	65	66	69	61	63	$55_{\pm 2\pm 4}$	$58_{\pm 2\pm 4}$	$59_{\pm 1 \pm 5}$	$57_{\pm 1\pm 4}$	$52_{\pm1\pm6}$	$51_{\pm 2\pm 7}$	$51_{\pm1\pm5}$	$50_{\pm 2 \pm 6}$	
0.31 0.125	-172.5	67 64	64	68	69	68	64	62	$58_{\pm 2\pm 4}$	$57_{\pm 2\pm 4}$	$58_{\pm 1 \pm 5}$	$61_{\pm1\pm4}$	$55_{\pm 2\pm 6}$	$49_{\pm 2\pm 7}$	$53_{\pm1\pm5}$	$49_{\pm 2 \pm 6}$	
0.33 0.125	-172.5	65 68	66	66	67	71	62	65	$57_{\pm 2\pm 4}$	$60_{\pm 2\pm 4}$	$60_{\pm 1 \pm 5}$	$59_{\pm 1 \pm 4}$	$54_{\pm1\pm6}$	$51_{\pm 2\pm 7}$	$52_{\pm1\pm5}$	$51_{\pm 2\pm 6}$	
0.35 0.125	-172.5	66 67	66	67	67	71	63	65	$58_{\pm 2\pm 4}$	$59_{\pm 2\pm 4}$	$60_{\pm 1 \pm 5}$	$60_{\pm 1 \pm 4}$	$54_{\pm 1 \pm 6}$	$50_{\pm 2\pm 7}$	$53_{\pm1\pm5}$	$51_{\pm 2 \pm 6}$	
0.37 0.125	-172.5	69 65	65	69	70	70	66	64	$61_{\pm 2 \pm 4}$	58 + 2 + 4	58+1+5	63+1+4	57_{+2+6}	$48_{\pm 2\pm 6}$	$55_{\pm 1\pm 6}$	$50_{\pm 2\pm 6}$	

Table A.4: (continued)

```
-172.5
                                                                                                               69\ 66\ 65\ 69\ 70\ 71\ 66\ 65\ 62_{\pm1\pm4}\ 58_{\pm2\pm4}\ 58_{\pm1\pm5}\ 63_{\pm1\pm4}\ 57_{\pm2\pm6}\ 48_{\pm2\pm6}\ 55_{\pm1\pm6}\ 51_{\pm2\pm6}
0.39 0.125
                                                                   -172.5
0.42\ 0.125
                                                                                                               67 \ 68 \ 67 \ 68 \ 74 \ 64 \ 67 \ 60_{\pm 1 \pm 4} \ 60_{\pm 2 \pm 4} \ 59_{\pm 1 \pm 5} \ 62_{\pm 1 \pm 4} \ 55_{\pm 1 \pm 6} \ 48_{\pm 2 \pm 6} \ 53_{\pm 1 \pm 5} \ 52_{\pm 2 \pm 6}
0.46 0.125
                                                                   -172.5
                                                                                                               70 \ 66 \ 65 \ 70 \ 70 \ 72 \ 67 \ 66 \ 63_{\pm 1 \pm 5} \ 58_{\pm 2 \pm 4} \ 57_{\pm 1 \pm 5} \ 65_{\pm 1 \pm 4} \ 58_{\pm 1 \pm 6} \ 44_{\pm 2 \pm 6} \ 55_{\pm 1 \pm 6} \ 51_{\pm 2 \pm 6}
0.5 0.125
                                                                   -172.5
                                                                                                               71 \ 66 \ 65 \ 71 \ 71 \ 72 \ 68 \ 66 \ 65_{\pm 1 \pm 4} \ 57_{\pm 1 \pm 3} \ 57_{\pm 2 \pm 3} \ 66_{\pm 1 \pm 3} \ 59_{\pm 1 \pm 4} \ 42_{\pm 2 \pm 5} \ 56_{\pm 1 \pm 4} \ 51_{\pm 2 \pm 4}
0.54 \ 0.125
                                                                   -172.5
                                                                                                               69 \ 68 \ 68 \ 69 \ 69 \ 75 \ 66 \ 68 \ 62_{\pm 1 \pm 4} \ 58_{\pm 2 \pm 3} \ 58_{\pm 2 \pm 3} \ 64_{\pm 1 \pm 3} \ 57_{\pm 1 \pm 4} \ 43_{\pm 2 \pm 5} \ 54_{\pm 1 \pm 4} \ 50_{\pm 2 \pm 4}
                                                                                                               68\ 68\ 68\ 69\ 68\ 75\ 66\ 68\ 62_{\pm1\pm4}\ 56_{\pm2\pm3}\ 57_{\pm2\pm3}\ 64_{\pm1\pm3}\ 57_{\pm1\pm4}\ 43_{\pm2\pm5}\ 54_{\pm1\pm4}\ 48_{\pm2\pm4}
0.58 \ 0.125
                                                                   -172.5
0.62\ 0.125
                                                                   -172.5
                                                                                                               70\ 66\ 66\ 70\ 70\ 72\ 67\ 65\ 62_{\pm 1 \pm 4}\ 53_{\pm 2 \pm 3}\ 54_{\pm 2 \pm 3}\ 64_{\pm 1 \pm 3}\ 58_{\pm 1 \pm 4}\ 41_{\pm 2 \pm 5}\ 54_{\pm 1 \pm 4}\ 44_{\pm 2 \pm 4}
0.66\ 0.125
                                                                   -172.5
                                                                                                               72 \ 64 \ 64 \ 72 \ 72 \ 70 \ 69 \ 65 \ 63_{\pm 2 \pm 4} \ 50_{\pm 2 \pm 3} \ 51_{\pm 2 \pm 3} \ 65_{\pm 1 \pm 3} \ 60_{\pm 1 \pm 4} \ 39_{\pm 2 \pm 5} \ 55_{\pm 1 \pm 4} \ 42_{\pm 2 \pm 4}
                                                                                                               72\ 64\ 64\ 72\ 72\ 70\ 69\ 65\ 63_{\pm 2 \pm 4}\ 48_{\pm 2 \pm 3}\ 50_{\pm 2 \pm 3}\ 65_{\pm 1 \pm 3}\ 60_{\pm 1 \pm 4}\ 39_{\pm 2 \pm 4}\ 55_{\pm 1 \pm 4}\ 40_{\pm 2 \pm 3}
0.7 0.125
                                                                   -172.5
                                                                   -172.5
                                                                                                               72\ 64\ 64\ 72\ 72\ 69\ 69\ 65\ 62_{\pm 2 \pm 4}\ 47_{\pm 2 \pm 3}\ 48_{\pm 2 \pm 3}\ 64_{\pm 0.9 \pm 6}0_{\pm 1 \pm 4}\ 39_{\pm 2 \pm 4}\ 54_{\pm 1 \pm 4}\ 39_{\pm 2 \pm 3}
0.74\ 0.125
                                                                                                               70\ 66\ 67\ 72\ 70\ 72\ 68\ 67\ 60_{\pm 1 \pm 4}\ 48_{\pm 2 \pm 3}\ 48_{\pm 2 \pm 3}\ 62_{\pm 0.9 \pm 5}9_{\pm 1.0 \pm 4}40_{\pm 2 \pm 5}\ 53_{\pm 1 \pm 4}\ 40_{\pm 2 \pm 3}
                                                                   -172.5
0.78 \ 0.125
                                                                   -172.5
                                                                                                               68\ 67\ 67\ 69\ 68\ 73\ 66\ 68\ 59_{\pm 1 \pm 4}\ 47_{\pm 2 \pm 3}\ 47_{\pm 2 \pm 3}\ 60_{\pm 0.8 \pm} \\ 58_{\pm 0.9 \pm 6}40_{\pm 2 \pm 7}\ 51_{\pm 1 \pm 4}\ 40_{\pm 2 \pm 5}
0.82\ 0.125
                                                                   -172.5
                                                                                                               69\ 67\ 68\ 69\ 68\ 73\ 66\ 68\ 59_{\pm1\pm4}\ 46_{\pm2\pm3}\ 46_{\pm2\pm3}\ 59_{\pm0.7\pm}\\ 58_{\pm0.9\pm6}\ 40_{\pm2\pm7}\ 51_{\pm1\pm4}\ 39_{\pm2\pm5}
0.86\ 0.125
                                                                   -172.5
                                                                                                               69\ 66\ 67\ 70\ 68\ 72\ 66\ 68\ 59_{\pm 1 \pm 4}\ 45_{\pm 2 \pm 3}\ 44_{\pm 2 \pm 2}\ 59_{\pm 0.7 \pm 5}8_{\pm 0.8 \pm 6}40_{\pm 2 \pm 7}\ 50_{\pm 1 \pm 4}\ 38_{\pm 2 \pm 5}
0.9 0.125
                                                                   -172.5
                                                                                                               69\ 67\ 68\ 70\ 68\ 72\ 66\ 69\ 59_{\pm1\pm4}\ 46_{\pm2\pm3}\ 44_{\pm2\pm2}\ 58_{\pm0.8\pm5}7_{\pm0.8\pm6}39_{\pm2\pm7}\ 50_{\pm1\pm4}\ 39_{\pm2\pm5}
0.94\ 0.125
                                                                   -172.5
                                                                                                               69\ 65\ 66\ 69\ 68\ 71\ 65\ 68\ 58_{\pm1\pm4}\ 45_{\pm2\pm3}\ 43_{\pm2\pm2}\ 57_{\pm0.8\pm}\\ 56_{\pm0.9\pm6}38_{\pm2\pm7}\ 50_{\pm1\pm4}\ 38_{\pm2\pm5}
0.98 \ 0.125
                                                                                                               71\ 63\ 63\ 72\ 70\ 68\ 68\ 64\ 59_{\pm 1\pm 6}\ 44_{\pm 2\pm 5}\ 42_{\pm 1\pm 4}\ 56_{\pm 1\pm 7}\ 57_{\pm 1.0\pm 8}36_{\pm 2\pm 10}\ 51_{\pm 1\pm 6}\ 36_{\pm 2\pm 6}
1.1 0.125
                                                                   -172.5
                                                                   -172.5
                                                                                                               72\ 63\ 64\ 73\ 72\ 68\ 68\ 65\ 61_{\pm1\pm6}\ 41_{\pm2\pm4}\ 37_{\pm2\pm3}\ 56_{\pm0.9\pm5}8_{\pm0.9\pm9}40_{\pm2\pm11}\ 50_{\pm1\pm6}\ 37_{\pm2\pm6}
1.3 0.125
1.5 0.125
                                                                   -172.5
                                                                                                               73 \ 67 \ 67 \ 73 \ 71 \ 71 \ 69 \ 68 \ 61_{\pm 1.0 \pm 4} 3_{\pm 2 \pm 10} 39_{\pm 2 \pm 5} \ 58_{\pm 0.7 \pm 5} 8_{\pm 0.9 \pm 9} 41_{\pm 2 \pm 12} \ 52_{\pm 1 \pm 9} \ 38_{\pm 2 \pm 9}
1.7 0.125
                                                                   -172.5
                                                                                                               70\ 72\ 71\ 71\ 69\ 74\ 67\ 71\ 56_{\pm 1\pm 11}46_{\pm 2\pm 9}\ 45_{\pm 2\pm 6}\ 54_{\pm 0.8\pm}53_{\pm 1\pm 8}\ 43_{\pm 2\pm 13}\ 50_{\pm 1\pm 7}\ 39_{\pm 2\pm 8}
1.9 0.125
                                                                   -172.5
                                                                                                               71 \ 72 \ 72 \ 70 \ 68 \ 75 \ 66 \ 72 \ 59_{\pm 1 \pm 11} 45_{\pm 2 \pm 9} \ 43_{\pm 2 \pm 6} \ 53_{\pm 0.8 \pm 5} 55_{\pm 0.8 \pm 8} 43_{\pm 2 \pm 13} \ 49_{\pm 1 \pm 7} \ 40_{\pm 2 \pm 8}
0.21\ 0.125
                                                                   -157.5
                                                                                                               55 \ 56 \ 57 \ 56 \ 57 \ 53 \ 55 \ 51_{\pm 0.9 \pm} \\ \phi 0_{\pm 1 \pm 4} \ 51_{\pm 1.0 \pm} \\ \phi 2_{\pm 1 \pm 3} \ 46_{\pm 1 \pm 5} \ 42_{\pm 1 \pm 6} \ 50_{\pm 0.7 \pm 5} \\ 41_{\pm 2 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 2.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 5} \ 50_{\pm 0.7 \pm 5} \\ \phi 1_{\pm 1.0 \pm 
0.23\ 0.125
                                                                   -157.5
                                                                                                               59 \ 60 \ 60 \ 61 \ 60 \ 61 \ 57 \ 59 \ 54_{\pm 1 \pm 4} \ 54_{\pm 1 \pm 4} \ 56_{\pm 1 \pm 5} \ 56_{\pm 1 \pm 3} \ 50_{\pm 1 \pm 5} \ 45_{\pm 2 \pm 6} \ 53_{\pm 0.8 \pm 5} 44_{\pm 2 \pm 5}
                                                                                                               62\ 61\ 61\ 64\ 62\ 62\ 60\ 59\ 57_{\pm1\pm4}\ 55_{\pm1\pm4}\ 57_{\pm1\pm5}\ 58_{\pm1\pm3}\ 52_{\pm1\pm6}\ 45_{\pm2\pm6}\ 55_{\pm0.9\pm5}45_{\pm2\pm5}
0.25\ 0.125
                                                                   -157.5
0.27\ 0.125
                                                                                                               62\ 63\ 64\ 63\ 62\ 65\ 60\ 61\ 57_{\pm 1 \pm 4}\ 57_{\pm 1 \pm 4}\ 60_{\pm 1 \pm 5}\ 57_{\pm 1 \pm 3}\ 52_{\pm 1 \pm 6}\ 47_{\pm 2 \pm 6}\ 55_{\pm 1.0 \pm 5}46_{\pm 2 \pm 6}
                                                                   -157.5
                                                                                                               65 \ 63 \ 63 \ 66 \ 65 \ 64 \ 63 \ 61 \ 59_{\pm 1 \pm 4} \ 56_{\pm 1 \pm 4} \ 59_{\pm 1 \pm 5} \ 60_{\pm 1 \pm 3} \ 54_{\pm 1 \pm 6} \ 47_{\pm 2 \pm 6} \ 56_{\pm 1 \pm 6} \ 47_{\pm 2 \pm 6}
0.29\ 0.125
                                                                   -157.5
                                                                                                               64\ 65\ 66\ 65\ 63\ 68\ 62\ 64\ 59_{\pm 1 \pm 4}\ 58_{\pm 1 \pm 4}\ 62_{\pm 1 \pm 6}\ 59_{\pm 1 \pm 3}\ 53_{\pm 1 \pm 6}\ 49_{\pm 2 \pm 7}\ 55_{\pm 1 \pm 5}\ 49_{\pm 2 \pm 6}
0.31\ 0.125
                                                                   -157.5
0.33\ 0.125
                                                                   -157.5
                                                                                                               66\ 64\ 65\ 68\ 66\ 66\ 65\ 62\ 61_{\pm1\pm4}\ 58_{\pm1\pm4}\ 61_{\pm1\pm6}\ 61_{\pm1\pm3}\ 55_{\pm1\pm6}\ 47_{\pm2\pm6}\ 57_{\pm1\pm6}\ 48_{\pm2\pm6}
0.35 0.125
                                                                   -157.5
                                                                                                               67 \ 64 \ 66 \ 68 \ 67 \ 65 \ 63 \ 61_{\pm 1 \pm 4} \ 58_{\pm 1 \pm 4} \ 62_{\pm 1 \pm 6} \ 62_{\pm 1 \pm 3} \ 56_{\pm 1 \pm 6} \ 48_{\pm 2 \pm 6} \ 56_{\pm 1 \pm 5} \ 49_{\pm 2 \pm 6}
                                                                                                                65 \ 67 \ 69 \ 67 \ 65 \ 70 \ 63 \ 65 \ 59_{\pm 1 \pm 4} \ 61_{\pm 1 \pm 4} \ 65_{\pm 1 \pm 6} \ 60_{\pm 1 \pm 3} \ 54_{\pm 1 \pm 6} \ 50_{\pm 2 \pm 7} \ 54_{\pm 1 \pm 5} \ 51_{\pm 2 \pm 6}
0.37 0.125
                                                                   -157.5
                                                                                                                66 \ 68 \ 68 \ 67 \ 66 \ 70 \ 64 \ 65 \ 60_{\pm 1 \pm 4} \ 61_{\pm 1 \pm 4} \ 65_{\pm 1 \pm 6} \ 61_{\pm 1 \pm 3} \ 55_{\pm 1 \pm 6} \ 49_{\pm 2 \pm 7} \ 54_{\pm 1 \pm 5} \ 51_{\pm 2 \pm 6}
0.39 0.125
                                                                   -157.5
0.42\ 0.125
                                                                   -157.5
                                                                                                               70\ 66\ 67\ 70\ 69\ 69\ 67\ 64\ 63_{\pm1\pm4}\ 59_{\pm1\pm4}\ 64_{\pm1.0\pm}63_{\pm1\pm3}\ 57_{\pm1\pm6}\ 48_{\pm2\pm6}\ 55_{\pm1\pm5}\ 51_{\pm2\pm6}
0.46\ 0.125
                                                                   -157.5
                                                                                                               69 \ 69 \ 70 \ 70 \ 68 \ 72 \ 67 \ 66 \ 61_{\pm 1 \pm 4} \ 62_{\pm 1 \pm 4} \ 66_{\pm 1 \pm 6} \ 62_{\pm 1 \pm 3} \ 56_{\pm 1 \pm 6} \ 50_{\pm 2 \pm 7} \ 53_{\pm 2 \pm 5} \ 53_{\pm 2 \pm 6}
                                                                                                               68\ 69\ 71\ 69\ 67\ 73\ 66\ 66\ 60_{\pm 2\pm 4}\ 62_{\pm 1\pm 4}\ 67_{\pm 1.0\pm} \\ 62_{\pm 1\pm 3}\ 56_{\pm 1\pm 4}\ 49_{\pm 2\pm 6}\ 50_{\pm 2\pm 3}\ 53_{\pm 1\pm 5}
0.5 \quad 0.125
                                                                   -157.5
                                                                                                               70 \ 67 \ 69 \ 72 \ 70 \ 69 \ 65 \ 61_{\pm 2 \pm 4} \ 60_{\pm 1 \pm 4} \ 65_{\pm 0.9 \pm 6} \\ 2_{\pm 1 \pm 3} \ 56_{\pm 2 \pm 4} \ 48_{\pm 2 \pm 5} \ 51_{\pm 2 \pm 3} \ 52_{\pm 1 \pm 4}
0.54\ 0.125
                                                                   -157.5
                                                                   -157.5
                                                                                                               70 \ 67 \ 69 \ 71 \ 71 \ 70 \ 64 \ 60_{\pm 2 \pm 4} \ 60_{\pm 1 \pm 4} \ 64_{\pm 0.9 \pm 6} 0_{\pm 2 \pm 2} \ 54_{\pm 2 \pm 4} \ 47_{\pm 2 \pm 5} \ 50_{\pm 2 \pm 3} \ 52_{\pm 1 \pm 4}
0.58 \ 0.125
                                                                  -157.5
0.62\ 0.125
                                                                                                               69\ 69\ 70\ 70\ 70\ 72\ 68\ 66\ 58_{\pm 2\pm 4}\ 61_{\pm 1\pm 4}\ 65_{\pm 0.9\pm}\\ 56_{\pm 2\pm 2}\ 50_{\pm 2\pm 4}\ 48_{\pm 2\pm 5}\ 47_{\pm 2\pm 3}\ 54_{\pm 1\pm 5}
                                                                                                               66\ 70\ 71\ 67\ 67\ 74\ 65\ 67\ 54_{\pm 2\pm 4}\ 62_{\pm 1\pm 4}\ 65_{\pm 0.9\pm} \\ \mathfrak{z}1_{\pm 2\pm 2}\ 46_{\pm 2\pm 3}\ 49_{\pm 2\pm 6}\ 43_{\pm 2\pm 3}\ 55_{\pm 1\pm 5}
0.66\ 0.125
                                                                   -157.5
                                                                                                               65\ \ 70\ \ 71\ \ 67\ \ 67\ \ 74\ \ 65\ \ 67\ \ 52_{\pm 2\pm 3}\ \ 61_{\pm 1\pm 4}\ \ 64_{\pm 0.9\pm} \\ 49_{\pm 2\pm 2}\ \ 44_{\pm 2\pm 3}\ \ \ 48_{\pm 2\pm 6}\ \ \ 42_{\pm 2\pm 3}\ \ 55_{\pm 1\pm 5}
0.7 0.125
                                                                   -157.5
                                                                                                              65\ 70\ 71\ 67\ 67\ 74\ 65\ 67\ 51_{\pm2\pm3}\ 60_{\pm1\pm4}\ 63_{\pm0.9\pm}\\ 48_{\pm2\pm2}\ 43_{\pm2\pm3}\ 49_{\pm2\pm6}\ 41_{\pm2\pm3}\ 54_{\pm1\pm5}
                                                                   -157.5
0.74\ 0.125
                                                                   -157.5 \quad 67 \quad 68 \quad 69 \quad 68 \quad 69 \quad 71 \quad 67 \quad 65 \quad 51_{\pm 2 \pm 3} \quad 58_{\pm 1 \pm 3} \quad 59_{\pm 0.9 \pm 4} \\ 8_{\pm 2 \pm 2} \quad 43_{\pm 2 \pm 3} \quad 47_{\pm 2 \pm 5} \quad 42_{\pm 2 \pm 3} \quad 51_{\pm 1 \pm 4} \quad 8_{\pm 2 \pm 3} \quad 48_{\pm 2 \pm 4} \quad 48_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 5} \quad 48_{\pm 5} \quad 8_{\pm 1 \pm 4} \quad 8_{\pm 2 \pm 5} \quad 8_{\pm 1 \pm 4} \quad 8_{\pm 2 \pm 5} \quad 8_{\pm 1 \pm 5}
0.78 \ 0.125
                                                                   -157.5 \quad 69 \quad 67 \quad 68 \quad 71 \quad 71 \quad 71 \quad 69 \quad 64 \quad 51_{\pm 2 \pm 3} \quad 56_{\pm 1 \pm 3} \quad 58_{\pm 0.9 \pm 34} \\ 9_{\pm 2 \pm 2} \quad 43_{\pm 2 \pm 4} \quad 47_{\pm 2 \pm 9} \quad 43_{\pm 2 \pm 3} \quad 50_{\pm 1 \pm 6} \quad 50_{\pm 1 \pm 6} \quad 10_{\pm 1 \pm 6} 
0.82 0.125
                                                                                                               68\ 66\ 67\ 71\ 71\ 70\ 68\ 64\ 50_{\pm 2\pm 3}\ 55_{\pm 1\pm 3}\ 57_{\pm 0.9\pm} 48_{\pm 2\pm 2}\ 42_{\pm 2\pm 4}\ 48_{\pm 2\pm 9}\ 42_{\pm 2\pm 3}\ 49_{\pm 1\pm 6}
0.86\ 0.125
                                                                   -157.5
                                                                   -157.5
                                                                                                               69\ 66\ 67\ 70\ 71\ 70\ 68\ 63\ 49_{\pm2\pm3}\ 55_{\pm1\pm3}\ 55_{\pm1.0\pm} 47_{\pm2\pm2}\ 41_{\pm2\pm4}\ 48_{\pm2\pm9}\ 42_{\pm2\pm3}\ 48_{\pm1\pm6}
0.9 0.125
                                                                                                               68\ 65\ 66\ 70\ 70\ 70\ 64\ 47_{\pm 2\pm 3}\ 54_{\pm 1\pm 3}\ 54_{\pm 0.9\pm} \\ 46_{\pm 2\pm 2}\ 40_{\pm 2\pm 4}\ 48_{\pm 2\pm 9}\ 40_{\pm 2\pm 3}\ 49_{\pm 1\pm 6}
0.94 0.125
                                                                                                               67\ 65\ 67\ 70\ 71\ 70\ 68\ 63\ 46_{\pm2\pm3}\ 54_{\pm1\pm3}\ 54_{\pm0.9\pm3} \\ 54_{\pm2\pm2}\ 40_{\pm2\pm4}\ 48_{\pm2\pm9}\ 40_{\pm2\pm3}\ 49_{\pm1\pm6}
0.98 0.125
                                                                   -157.5 \quad 65 \quad 68 \quad 69 \quad 66 \quad 68 \quad 73 \quad 65 \quad 66 \quad 42_{\pm 2 \pm 4} \quad 56_{\pm 1 \pm 6} \quad 55_{\pm 0.8 \pm 9} \\ 41_{\pm 2 \pm 5} \quad 36_{\pm 2 \pm 5} \quad 51_{\pm 2 \pm 14} \quad 35_{\pm 2 \pm 4} \quad 51_{\pm 1.0 \pm 8} \quad 51_{\pm 1.0 \pm 8} \quad 51_{\pm 1.0 \pm 8} \quad 51_{\pm 1.0 \pm 1} \quad 
1.1 0.125
                                                                   -157.5 \quad 62 \quad 68 \quad 69 \quad 65 \quad 68 \quad 74 \quad 64 \quad 66 \quad 42_{\pm 2 \pm 4} \quad 57_{\pm 1.0 \pm 5} \\ 2_{\pm 1.0 \pm 5} \\ 2_{\pm 1.0 \pm 4} \\ 9_{\pm 2 \pm 5} \quad 34_{\pm 2 \pm 5} \quad 49_{\pm 2 \pm 13} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 4} \quad 49_{\pm 1 \pm 8} \\ 37_{\pm 4} \quad 49_{\pm 4} \\ 37_{\pm 4} \quad 49_{\pm 4} \\ 49_{\pm 
1.3 0.125
1.5 0.125
                                                                   -157.5 \quad 64 \quad 67 \quad 66 \quad 70 \quad 73 \quad 66 \quad 65 \quad 40_{\pm 2 \pm 4} \quad 55_{\pm 1 \pm 12} \\ 51_{\pm 0.9 \pm} \\ \mathcal{F}7_{\pm 2 \pm 8} \quad 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 50_{\pm 0.9 \pm 11} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 2 \pm 6} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15} \quad 49_{\pm 1 \pm 15} \\ 37_{\pm 1 \pm 15
                                                                   -157.5 \quad 68 \quad 66 \quad 66 \quad 71 \quad 76 \quad 71 \quad 69 \quad 64 \quad 39_{\pm 2 \pm 7} \quad 53_{\pm 1 \pm 10} \\ 51_{\pm 0.7 \pm 7} \\ 41_{\pm 2 \pm 11} \\ 39_{\pm 2 \pm 6} \quad 45_{\pm 2 \pm 14} \quad 40_{\pm 2 \pm 6} \quad 47_{\pm 1 \pm 9} 
1.7 0.125
1.9 0.125
                                                                   -157.5
                                                                                                              69\ 66\ 67\ 73\ 76\ 71\ 71\ 64\ 43_{\pm2\pm8}\ 53_{\pm1\pm10}50_{\pm1.0\pm}43_{\pm2\pm11}39_{\pm2\pm6}\ 46_{\pm2\pm14}\ 42_{\pm2\pm6}\ 48_{\pm1.0\pm9}
                                                                                                               57 \ 55 \ 55 \ 58 \ 56 \ 56 \ 54 \ 54 \ 52_{\pm 1 \pm 5} \ 51_{\pm 0.9 \pm 5} \\ 2_{\pm 0.9 \pm 5} 54_{\pm 1.0 \pm 4} 9_{\pm 1 \pm 5} \ 45_{\pm 1 \pm 6} \ 45_{\pm 1 \pm 5} \ 39_{\pm 2 \pm 4}
0.21 0.125
                                                                   -142.5
0.23 0.125
                                                                   -142.5
                                                                                                              61 \ 59 \ 60 \ 61 \ 61 \ 61 \ 58 \ 59 \ 56_{\pm 1 \pm 5} \ 55_{\pm 1 \pm 4} \ 57_{\pm 1.0 \pm 5} \ 57_{\pm 1 \pm 4} \ 52_{\pm 1 \pm 6} \ 48_{\pm 1 \pm 6} \ 49_{\pm 1 \pm 5} \ 42_{\pm 2 \pm 5}
0.25 0.125
                                                                   -142.5
                                                                                                               63 \ 61 \ 63 \ 63 \ 62 \ 64 \ 60 \ 61 \ 57_{\pm 1 \pm 5} \ 57_{\pm 1 \pm 4} \ 59_{\pm 1 \pm 5} \ 58_{\pm 1 \pm 4} \ 52_{\pm 1 \pm 6} \ 50_{\pm 1 \pm 7} \ 50_{\pm 1 \pm 5} \ 44_{\pm 2 \pm 5}
                                                                   -142.5
0.27 0.125
                                                                                                               65 \ 61 \ 63 \ 65 \ 66 \ 64 \ 62 \ 61 \ 59_{\pm 1 \pm 5} \ 56_{\pm 1 \pm 4} \ 59_{\pm 1 \pm 5} \ 60_{\pm 1 \pm 4} \ 54_{\pm 1 \pm 6} \ 50_{\pm 1 \pm 7} \ 52_{\pm 1 \pm 5} \ 44_{\pm 2 \pm 5}
                                                                   -142.5
                                                                                                              64\ 63\ 66\ 64\ 66\ 62\ 63\ 58_{\pm1\pm5}\ 58_{\pm1\pm4}\ 62_{\pm1\pm5}\ 59_{\pm1\pm4}\ 54_{\pm1\pm6}\ 51_{\pm2\pm7}\ 52_{\pm1\pm5}\ 45_{\pm2\pm5}
0.29 0.125
                                                                                                               67 \ 62 \ 65 \ 67 \ 69 \ 65 \ 62 \ 60_{\pm 1 \pm 5} \ 57_{\pm 1 \pm 4} \ 61_{\pm 1 \pm 5} \ 62_{\pm 1 \pm 4} \ 56_{\pm 1 \pm 6} \ 50_{\pm 2 \pm 7} \ 54_{\pm 1 \pm 6} \ 44_{\pm 2 \pm 5}
0.31 0.125
                                                                                                               64 \ 65 \ 68 \ 65 \ 67 \ 68 \ 64 \ 65 \ 58_{\pm 1 \pm 5} \ 59_{\pm 1 \pm 4} \ 63_{\pm 1 \pm 5} \ 59_{\pm 1 \pm 4} \ 53_{\pm 1 \pm 6} \ 51_{\pm 2 \pm 7} \ 53_{\pm 1 \pm 5} \ 46_{\pm 2 \pm 5}
0.33 0.125
0.35 \ 0.125
                                                                   -142.5
                                                                                                               65 \ 68 \ 68 \ 68 \ 68 \ 65 \ 68 \ 65 \ 58_{\pm 1 \pm 5} \ 59_{\pm 1 \pm 4} \ 63_{\pm 1 \pm 5} \ 59_{\pm 1 \pm 4} \ 54_{\pm 2 \pm 6} \ 51_{\pm 2 \pm 7} \ 54_{\pm 1 \pm 6} \ 46_{\pm 2 \pm 5}
0.37 0.125
                                                                   -142.5
                                                                                                               67 \ 63 \ 66 \ 68 \ 72 \ 66 \ 67 \ 63 \ 60_{\pm 1 \pm 5} \ 57_{\pm 1 \pm 4} \ 61_{\pm 1 \pm 5} \ 62_{\pm 1 \pm 4} \ 55_{\pm 2 \pm 6} \ 49_{\pm 2 \pm 7} \ 56_{\pm 1 \pm 6} \ 45_{\pm 2 \pm 5}
                                                                   -142.5 \quad 67 \quad 64 \quad 67 \quad 67 \quad 72 \quad 67 \quad 64 \quad 60_{\pm 1 \pm 5} \quad 58_{\pm 1 \pm 4} \quad 62_{\pm 1 \pm 5} \quad 61_{\pm 1 \pm 4} \quad 55_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 7} \quad 56_{\pm 1 \pm 6} \quad 45_{\pm 2 \pm 5} \quad 61_{\pm 1 \pm 6} \quad 61_{\pm
0.39 0.125
                                                                   -142.5 \quad 64 \quad 67 \quad 70 \quad 65 \quad 70 \quad 70 \quad 65 \quad 67 \quad 57_{\pm 1 \pm 5} \quad 59_{\pm 1 \pm 4} \quad 64_{\pm 1 \pm 5} \quad 59_{\pm 1 \pm 4} \quad 52_{\pm 2 \pm 6} \quad 51_{\pm 2 \pm 7} \quad 54_{\pm 1 \pm 6} \quad 47_{\pm 2 \pm 5} \quad 59_{\pm 1 \pm 4} \quad 59_{\pm 1 \pm 4} \quad 59_{\pm 1 \pm 4} \quad 59_{\pm 1 \pm 6} \quad 
0.42 \ 0.125
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Table A.4: (continued)

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-142.5 \quad 66 \quad 65 \quad 68 \quad 67 \quad 73 \quad 68 \quad 68 \quad 66 \quad 58_{\pm 2 \pm 5} \quad 57_{\pm 2 \pm 4} \quad 62_{\pm 1 \pm 5} \quad 60_{\pm 1 \pm 4} \quad 52_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 6} \quad 56_{\pm 1 \pm 6} \quad 46_{\pm 2 \pm 5} \quad 57_{\pm 2 \pm 6} \quad 60_{\pm 1 \pm 6} \quad 
  0.460.125
                                                                                                                                                                                                  -142.5
  0.5 \quad 0.125
                                                                                                                                                                                                                                                                                                                                   67 \ 65 \ 68 \ 68 \ 74 \ 68 \ 68 \ 66 \ 58_{\pm 2 \pm 5} \ 56_{\pm 2 \pm 4} \ 61_{\pm 1 \pm 3} \ 60_{\pm 1 \pm 3} \ 51_{\pm 2 \pm 4} \ 47_{\pm 2 \pm 5} \ 56_{\pm 1 \pm 4} \ 45_{\pm 2 \pm 3}
                                                                                                                                                                                                  -142.5
                                                                                                                                                                                                                                                                                                                                   64\ 67\ 71\ 65\ 72\ 71\ 66\ 68\ 56_{\pm 1\pm 5}\ 58_{\pm 2\pm 4}\ 62_{\pm 1\pm 3}\ 59_{\pm 1\pm 3}\ 49_{\pm 2\pm 3}\ 48_{\pm 2\pm 5}\ 54_{\pm 1\pm 4}\ 44_{\pm 2\pm 3}
  0.54 \ 0.125
                                                                                                                                                                                                  -142.5
                                                                                                                                                                                                                                                                                                                                   64\ 68\ 71\ 65\ 72\ 71\ 66\ 68\ 56_{\pm 1\pm 5}\ 57_{\pm 2\pm 4}\ 61_{\pm 1\pm 3}\ 59_{\pm 1\pm 3}\ 49_{\pm 2\pm 3}\ 46_{\pm 2\pm 5}\ 53_{\pm 1\pm 4}\ 42_{\pm 2\pm 3}
  0.58 \ 0.125
     0.62 0.125
                                                                                                                                                                                                  -142.5 \quad 66 \quad 66 \quad 69 \quad 66 \quad 73 \quad 70 \quad 67 \quad 67 \quad 58_{\pm 1 \pm 5} \quad 55_{\pm 2 \pm 4} \quad 58_{\pm 1 \pm 3} \quad 60_{\pm 1 \pm 3} \quad 50_{\pm 2 \pm 3} \quad 44_{\pm 2 \pm 5} \quad 53_{\pm 1 \pm 4} \quad 39_{\pm 2 \pm 3} \quad 50_{\pm 1 \pm 4} \quad 50_{\pm 1 \pm 3} \quad 50_{\pm 2 \pm 3} \quad 50_{\pm 1 \pm 4} \quad 
     0.660.125
                                                                                                                                                                                                                                                                                                                                68\ 64\ 68\ 68\ 75\ 69\ 69\ 65\ 60_{\pm 1 \pm 5}\ 52_{\pm 2 \pm 4}\ 55_{\pm 1 \pm 3}\ 61_{\pm 1 \pm 3}\ 51_{\pm 2 \pm 4}\ 41_{\pm 2 \pm 5}\ 54_{\pm 1 \pm 4}\ 35_{\pm 2 \pm 3}
                                                                                                                                                                                                  -142.5 \quad 68 \quad 64 \quad 67 \quad 68 \quad 76 \quad 69 \quad 69 \quad 65 \quad 59_{\pm 1 \pm 5} \quad 51_{\pm 2 \pm 4} \quad 54_{\pm 1 \pm 3} \quad 61_{\pm 0.9 \pm} \\ 50_{\pm 2 \pm 4} \quad 40_{\pm 2 \pm 4} \quad 54_{\pm 1 \pm 4} \quad 33_{\pm 2 \pm 3} \quad 61_{\pm 1 \pm 4} \quad 54_{\pm 1 \pm 4} \quad 61_{\pm 1 \pm 4} \quad 
  0.7 \quad 0.125
  0.74 \ 0.125
                                                                                                                                                                                                  -142.5 \quad 69 \quad 65 \quad 68 \quad 69 \quad 76 \quad 69 \quad 69 \quad 65 \quad 60_{\pm 1 \pm 5} \quad 50_{\pm 2 \pm 3} \quad 52_{\pm 2 \pm 2} \quad 60_{\pm 0.9 \pm} \\ 51_{\pm 2 \pm 4} \quad 39_{\pm 2 \pm 4} \quad 53_{\pm 1 \pm 4} \quad 33_{\pm 2 \pm 3} \quad 33_{\pm 2 \pm 3} \quad 50_{\pm 1} \quad 5
                                                                                                                                                                                                  -142.5 \quad 66 \quad 66 \quad 70 \quad 67 \quad 74 \quad 72 \quad 67 \quad 67 \quad 58_{\pm 1 \pm 5} \quad 50_{\pm 2 \pm 3} \quad 52_{\pm 2 \pm 2} \quad 57_{\pm 0.9 \pm} \\ 50_{\pm 2 \pm 4} \quad 40_{\pm 2 \pm 4} \quad 51_{\pm 1 \pm 4} \quad 35_{\pm 2 \pm 3} \quad 50_{\pm 2 \pm 3} \quad 50_{\pm 2 \pm 3} \quad 50_{\pm 2 \pm 4} \quad 50_{\pm 4 \pm 4} \quad 
     0.780.125
                                                                                                                                                                                                  -142.5 \quad 65 \quad 68 \quad 71 \quad 65 \quad 72 \quad 73 \quad 66 \quad 68 \quad 56_{\pm 1 \pm 5} \quad 50_{\pm 2 \pm 3} \quad 51_{\pm 2 \pm 2} \quad 55_{\pm 0.9 \pm 3} \\ 49_{\pm 2 \pm 5} \quad 40_{\pm 2 \pm 7} \quad 50_{\pm 1 \pm 4} \quad 36_{\pm 2 \pm 4} \quad 50_{\pm 1 \pm 4} \quad 50_{\pm 1 \pm 4} \quad 50_{\pm 2 \pm 4} \quad 50_{\pm 1 \pm 4} 
  0.82\ 0.125
                                                                                                                                                                                                  -142.5 \quad 66 \quad 68 \quad 72 \quad 66 \quad 72 \quad 73 \quad 65 \quad 67 \quad 57_{\pm 1 \pm 5} \quad 48_{\pm 2 \pm 3} \quad 50_{\pm 2 \pm 2} \quad 54_{\pm 0.9 \pm} \\ 50_{\pm 2 \pm 5} \quad 39_{\pm 2 \pm 7} \quad 49_{\pm 1 \pm 4} \quad 36_{\pm 2 \pm 4} \quad 36_{\pm 2 \pm 4} \quad 48_{\pm 1} \quad 36_{\pm 2} \quad 48_{\pm 2} \quad 48_{\pm 1} \quad 4
  0.86\ 0.125
                                                                                                                                                                                                  -142.5 \quad 66 \quad 68 \quad 71 \quad 66 \quad 72 \quad 72 \quad 65 \quad 67 \quad 56_{\pm 1.0 \pm 5}47_{\pm 2 \pm 3} \quad 48_{\pm 2 \pm 2} \quad 54_{\pm 1.0 \pm 5}51_{\pm 2 \pm 5} \quad 37_{\pm 2 \pm 7} \quad 49_{\pm 1 \pm 4} \quad 36_{\pm 2 \pm 4} \quad 36_{\pm 2 \pm 4} \quad 48_{\pm 2 \pm 2} \quad 54_{\pm 1.0 \pm 5}51_{\pm 2 \pm 5} \quad 37_{\pm 2 \pm 7} \quad 49_{\pm 1 \pm 4} \quad 36_{\pm 2 \pm 4} \quad 48_{\pm 2 \pm 2} \quad 48_{\pm 2 \pm 2} \quad 54_{\pm 1.0 \pm 5}51_{\pm 2 \pm 5} \quad 37_{\pm 2 \pm 7} \quad 49_{\pm 1 \pm 4} \quad 36_{\pm 2 \pm 4} \quad 48_{\pm 2 \pm 2} \quad 48_{\pm 2 \pm 3} \quad 48_{\pm 2 \pm 4} \quad 48_{\pm 4} \quad 4
  0.9 0.125
  0.94 \ 0.125
                                                                                                                                                                                                  -142.5 \quad 65 \quad 68 \quad 71 \quad 65 \quad 72 \quad 71 \quad 65 \quad 66 \quad 56_{\pm 1 \pm 5} \quad 46_{\pm 2 \pm 3} \quad 47_{\pm 2 \pm 2} \quad 53_{\pm 0.9 \pm} \\ 50_{\pm 2 \pm 5} \quad 37_{\pm 2 \pm 7} \quad 49_{\pm 1 \pm 4} \quad 35_{\pm 2 \pm 4} \quad 48_{\pm 1 \pm 4} \quad 48_{\pm 2 \pm 5} \quad 
                                                                                                                                                                                                  -142.5 \quad 66 \quad 67 \quad 71 \quad 65 \quad 72 \quad 71 \quad 65 \quad 66 \quad 55_{\pm 1 \pm 5} \quad 45_{\pm 2 \pm 3} \quad 46_{\pm 2 \pm 2} \quad 52_{\pm 0.9 \pm} \\ 50_{\pm 2 \pm 5} \quad 36_{\pm 2 \pm 7} \quad 49_{\pm 1 \pm 4} \quad 34_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 4} \quad 34_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 4} \quad 34_{\pm 2 \pm 4} \quad 49_{\pm 1 \pm 4} \quad 
  0.98 \ 0.125
     1.1 0.125
                                                                                                                                                                                                  -142.5 \quad 67 \quad 64 \quad 67 \quad 68 \quad 75 \quad 67 \quad 68 \quad 63 \quad 55_{\pm 1 \pm 6} \quad 43_{\pm 2 \pm 5} \quad 42_{\pm 1 \pm 3} \quad 54_{\pm 0.9 \pm} \\ \mathcal{5}1_{\pm 2 \pm 8} \quad 34_{\pm 2 \pm 9} \quad 52_{\pm 1 \pm 6} \quad 32_{\pm 2 \pm 5} \quad 34_{\pm 2 \pm 9} \quad 54_{\pm 1 \pm 1} \quad 34_{\pm 2 \pm 1}
                                                                                                                                                                                                  -142.5 \quad 69 \quad 64 \quad 67 \quad 69 \quad 76 \quad 67 \quad 68 \quad 63 \quad 56_{\pm 1 \pm 6} \quad 40_{\pm 2 \pm 4} \quad 40_{\pm 2 \pm 3} \quad 52_{\pm 1.0 \pm} \\ 51_{\pm 2 \pm 8} \quad 32_{\pm 2 \pm 9} \quad 50_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 30_{\pm 2 \pm 5} \quad 30_{\pm 1 \pm 6} \quad 
     1.3 0.125
                                                                                                                                                                                                  -142.5 \quad 68 \quad 67 \quad 69 \quad 69 \quad 75 \quad 70 \quad 68 \quad 65 \quad 57_{\pm 1 \pm 7} \quad 41_{\pm 2 \pm 9} \quad 40_{\pm 2 \pm 5} \quad 54_{\pm 0.8 \pm 4} \\ 7_{\pm 2 \pm 7} \quad 36_{\pm 2 \pm 11} \quad 52_{\pm 1 \pm 9} \quad 33_{\pm 2 \pm 7} \quad 36_{\pm 2 \pm 11} \quad 52_{\pm 1 \pm 9} \quad 33_{\pm 2 \pm 7} \quad 36_{\pm 2 \pm 11} \quad 52_{\pm 1 \pm 9} \quad 33_{\pm 2 \pm 7} \quad 36_{\pm 2 \pm 11} \quad 52_{\pm 1 \pm 9} \quad 33_{\pm 2 \pm 7} \quad 36_{\pm 2 \pm 11} \quad 52_{\pm 1 \pm 9} \quad 33_{\pm 2 \pm 7} \quad 36_{\pm 2 \pm 11} \quad 52_{\pm 1 \pm 9} \quad 33_{\pm 2 \pm 7} \quad 36_{\pm 2 \pm 11} \quad 52_{\pm 1 \pm 9} \quad 33_{\pm 2 \pm 7} \quad 36_{\pm 2 \pm 11} \quad 52_{\pm 1 \pm 9} \quad 33_{\pm 2 \pm 7} \quad 36_{\pm 2 \pm 11} \quad 52_{\pm 1 \pm 9} \quad 33_{\pm 2 \pm 7} \quad 36_{\pm 2 \pm 11} \quad 52_{\pm 1 \pm 9} \quad 33_{\pm 2 \pm 7} \quad 36_{\pm 2 \pm 11} \quad 52_{\pm 1 \pm 9} \quad 33_{\pm 2 \pm 7} \quad 36_{\pm 2 \pm 11} \quad 36_{\pm 11} \quad 3
     1.5 0.125
     1.7 0.125
                                                                                                                                                                                                  -142.5 \quad 67 \quad 71 \quad 74 \quad 68 \quad 73 \quad 75 \quad 66 \quad 70 \quad 56_{\pm 1 \pm 11} \\ 44_{\pm 2 \pm 9} \quad 43_{\pm 2 \pm 6} \quad 52_{\pm 0.7 \pm 14} \\ 8_{\pm 2 \pm 7} \quad 37_{\pm 2 \pm 11} \\ 49_{\pm 1 \pm 7} \quad 35_{\pm 2 \pm 7} 
     1.9 0.125
                                                                                                                                                                                                  -142.5 \quad 67 \quad 72 \quad 75 \quad 67 \quad 73 \quad 76 \quad 66 \quad 70 \quad 54_{\pm 1 \pm 11} 47_{\pm 2 \pm 9} \quad 46_{\pm 2 \pm 6} \quad 50_{\pm 0.8 \pm 48} 8_{\pm 2 \pm 7} \quad 39_{\pm 2 \pm 12} \quad 47_{\pm 1 \pm 7} \quad 35_{\pm 2 \pm 7} \quad 38_{\pm 2 \pm 7} \quad 48_{\pm 1 \pm 12} \quad 48_{\pm 1 \pm 13} \quad 48_{
  0.21 0.125
                                                                                                                                                                                                  -127.5 \quad 55 \quad 41 \quad 43 \quad 58 \quad 58 \quad 57 \quad 52 \quad 54 \quad 48_{\pm 1 \pm 4} \quad 36_{\pm 1 \pm 4} \quad 40_{\pm 0.8 \pm 5} \\ 42_{\pm 1.0 \pm 4} \\ 41_{\pm 2 \pm 5} \quad 42_{\pm 1 \pm 6} \quad 44_{\pm 1 \pm 4} \quad 36_{\pm 2 \pm 5} \quad 42_{\pm 1 \pm 6} \quad 44_{\pm 1 \pm 4} \quad 36_{\pm 2 \pm 5} \quad 48_{\pm 1 \pm 4} \quad 40_{\pm 1.8 \pm 5} \\ 41_{\pm 1.0 \pm 4} \\ 41_{\pm 1.0
                                                                                                                                                                                                  -127.5 \quad 58 \quad 57 \quad 57 \quad 61 \quad 62 \quad 60 \quad 57 \quad 58 \quad 51_{\pm 1 \pm 4} \quad 49_{\pm 1 \pm 4} \quad 53_{\pm 1 \pm 5} \quad 56_{\pm 1 \pm 3} \quad 43_{\pm 2 \pm 5} \quad 45_{\pm 2 \pm 6} \quad 47_{\pm 1 \pm 5} \quad 39_{\pm 2 \pm 5}
     0.23 0.125
     0.25 0.125
                                                                                                                                                                                                  -127.5 \quad 60 \quad 60 \quad 60 \quad 63 \quad 66 \quad 62 \quad 60 \quad 59 \quad 53_{\pm 1 \pm 4} \quad 52_{\pm 2 \pm 4} \quad 56_{\pm 1 \pm 5} \quad 58_{\pm 1 \pm 3} \quad 46_{\pm 2 \pm 5} \quad 46_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 39_{\pm 2 \pm 5} \quad 39_{\pm 2 \pm 5} \quad 48_{\pm 1 \pm 3} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 
                                                                                                                                                                                                  -127.5 \quad 59 \quad 63 \quad 63 \quad 62 \quad 66 \quad 65 \quad 60 \quad 62 \quad 52_{\pm 1 \pm 4} \quad 55_{\pm 2 \pm 4} \quad 59_{\pm 1 \pm 5} \quad 57_{\pm 1 \pm 3} \quad 45_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 49_{\pm 2 \pm 5} \quad 41_{\pm 2 \pm 5} \quad 
     0.27 0.125
                                                                                                                                                                                                  -127.5 \quad 61 \quad 63 \quad 63 \quad 64 \quad 69 \quad 65 \quad 62 \quad 62 \quad 54_{\pm 1 \pm 4} \quad 55_{\pm 2 \pm 4} \quad 59_{\pm 1 \pm 5} \quad 59_{\pm 1 \pm 3} \quad 46_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 6} \quad 50_{\pm 2 \pm 5} \quad 41_{\pm 2 \pm 5}
     0.29 0.125
                                                                                                                                                                                                  -127.5 \quad 59 \quad 65 \quad 66 \quad 62 \quad 67 \quad 68 \quad 60 \quad 65 \quad 52_{\pm 1 \pm 4} \quad 57_{\pm 2 \pm 4} \quad 62_{\pm 1 \pm 5} \quad 57_{\pm 1 \pm 3} \quad 45_{\pm 2 \pm 5} \quad 50_{\pm 2 \pm 7} \quad 48_{\pm 2 \pm 5} \quad 43_{\pm 2 \pm 5} \quad 43_{\pm 2 \pm 5} \quad 68_{\pm 2 \pm 5} \quad 48_{\pm 2 \pm 5} \quad 
     0.31 0.125
                                                                                                                                                                                                  -127.5 \quad 63 \quad 64 \quad 64 \quad 65 \quad 71 \quad 67 \quad 63 \quad 63 \quad 56_{\pm 1 \pm 4} \quad 56_{\pm 2 \pm 4} \quad 60_{\pm 1 \pm 5} \quad 60_{\pm 1 \pm 3} \quad 47_{\pm 2 \pm 5} \quad 49_{\pm 2 \pm 6} \quad 50_{\pm 2 \pm 5} \quad 42_{\pm 2 \pm 5}
  0.33\ 0.125
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  0.35 \ 0.125
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     0.37 0.125
                                                                                                                                                                                                                                                                                                                                   62 \ 67 \ 64 \ 70 \ 71 \ 63 \ 66 \ 55_{\pm 1 \pm 4} \ 59_{\pm 2 \pm 4} \ 63_{\pm 1 \pm 6} \ 59_{\pm 1 \pm 3} \ 46_{\pm 2 \pm 5} \ 51_{\pm 2 \pm 7} \ 49_{\pm 2 \pm 5} \ 44_{\pm 2 \pm 5}
                                                                                                                                                                                                                                                                                                                                   62 \ 67 \ 67 \ 64 \ 71 \ 70 \ 63 \ 66 \ 55_{\pm 1 \pm 4} \ 59_{\pm 2 \pm 4} \ 63_{\pm 1 \pm 6} \ 60_{\pm 1 \pm 3} \ 46_{\pm 2 \pm 5} \ 51_{\pm 2 \pm 7} \ 49_{\pm 2 \pm 5} \ 44_{\pm 2 \pm 5}
  0.39 0.125
                                                                                                                                                                                                  -127.5
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  0.42\ 0.125
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     0.46 0.125
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  0.5 \quad 0.125
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                                                                                                                                                                                                                                                                                                                                   69\ 66\ 68\ 71\ 77\ 69\ 68\ 65\ 58_{\pm2\pm4}\ 58_{\pm1\pm4}\ 63_{\pm0.9\pm}\ 64_{\pm1\pm3}\ 46_{\pm2\pm3}\ 50_{\pm2\pm6}\ 47_{\pm2\pm3}\ 43_{\pm2\pm4}
  0.54\ 0.125
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  0.58 \ 0.125
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  0.62\ 0.125
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  0.74\ 0.125
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  0.78 0.125
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  0.82\ 0.125
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  0.86 0.125
                                                                                                                                                                                                                                                                                                                                68\ 65\ 67\ 70\ 75\ 69\ 67\ 65\ 48_{\pm 2\pm 3}\ 56_{\pm 1\pm 3}\ 55_{\pm 1.0\pm} \\ 50_{\pm 2\pm 2}\ 37_{\pm 2\pm 4}\ 51_{\pm 1\pm 9}\ 34_{\pm 2\pm 3}\ 45_{\pm 1\pm 6}
  0.9 0.125
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  0.94\ 0.125
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  0.98 0.125
                                                                                                                                                                                                  -127.5 \quad 64 \quad 68 \quad 69 \quad 67 \quad 71 \quad 72 \quad 65 \quad 67 \quad 41_{\pm 2 \pm 4} \quad 56_{\pm 1 \pm 6} \quad 56_{\pm 0.8 \pm 3} \\ 9_{\pm 2 \pm 5} \quad 35_{\pm 2 \pm 5} \quad 52_{\pm 1 \pm 14} \quad 33_{\pm 2 \pm 4} \quad 42_{\pm 2 \pm 7} \quad 33_{\pm 2 \pm 7} \quad 43_{\pm 1 \pm 1} 
  1.1 0.125
                                                                                                                                                                                                  -127.5 \quad 64 \quad 68 \quad 70 \quad 66 \quad 72 \quad 73 \quad 65 \quad 68 \quad 39_{\pm 2 \pm 4} \quad 56_{\pm 1 \pm 6} \quad 55_{\pm 0.8 \pm} \\ 39_{\pm 2 \pm 5} \quad 33_{\pm 2 \pm 5} \quad 53_{\pm 1 \pm 14} \quad 31_{\pm 2 \pm 4} \quad 45_{\pm 1 \pm 7} \quad 31_{\pm 1 \pm 7} \quad 43_{\pm 1 \pm 7} \quad
     1.3 0.125
                                                                                                                                                                                                  -127.5 \quad 66 \quad 68 \quad 70 \quad 68 \quad 74 \quad 72 \quad 66 \quad 68 \quad 45_{\pm 2 \pm 5} \quad 57_{\pm 0.9 \pm 15} \\ 4_{\pm 0.7 \pm 17} 9_{\pm 2 \pm 8} \quad 39_{\pm 2 \pm 6} \quad 53_{\pm 1 \pm 16} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 2 \pm 6} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 1 \pm 10} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 1 \pm 10} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 1 \pm 10} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 1 \pm 10} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 1 \pm 10} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 1 \pm 10} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 1 \pm 10} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 1 \pm 10} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 1 \pm 10} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 1 \pm 10} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 1 \pm 10} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 1 \pm 10} \quad 44_{\pm 1 \pm 10} \\ 32_{\pm 1 \pm 10} \quad 44_{\pm 10} \\ 32_{\pm 10} \quad 44_{\pm 10} \\ 32_{\pm 10}
     1.5 0.125
                                                                                                                                                                                                  -127.5 \quad 69 \quad 67 \quad 68 \quad 73 \quad 78 \quad 70 \quad 70 \quad 66 \quad 48_{\pm 2 \pm 9} \quad 57_{\pm 0.7 \pm 1} \\ 27_{\pm 0.8 \pm 7} \quad 43_{\pm 2 \pm 11} \\ 42_{\pm 2 \pm 6} \quad 50_{\pm 1 \pm 15} \quad 34_{\pm 2 \pm 5} \quad 43_{\pm 1 \pm 8} \quad 43_{\pm 1 \pm 8} \quad 43_{\pm 1 \pm 1} 
  1.7 0.125
                                                                                                                                                                                                  -127.5 73 68 68 75 78 70 70 67 46_{+2+9} 57_{+1+11} 52_{+0,9\pm} 40_{+2+10} 41_{+2\pm} 51_{\pm1\pm} 43_{\pm2\pm} 44_{\pm1\pm} 41_{\pm2\pm} 41_{\pm1\pm}
1.9 0.125
```

Table A.5: η -/ ϕ -dependence of systematic uncertainties $\Delta \varepsilon$, scaling factors F, and reduced χ^2 for the determination of TOF Matching Efficiencies.

			19	9.6 (GeV				2	27 G	eV				3	9 G	eV				62	2.4 (GeV	,	
η	ϕ		e ⁻			e^+			e ⁻			e^+			e ⁻			e^+			e ⁻			e^+	
·		$\Delta arepsilon$	F	χ^2	$\Delta arepsilon$	F	χ^2	$\Delta arepsilon$	F	χ^2	$\Delta arepsilon$	F	χ^2	$\Delta arepsilon$	F	χ^2	$\Delta \varepsilon$	F	χ^2	$\Delta \varepsilon$	F	χ^2	$\Delta \varepsilon$	F	χ^2
-0.875	-172.5	6	1.18	1.3	7	1.16	1.9	5	1.22	1.7	4	1.19	1.2	3	1.12	0.9	11	1.16	1.7	4	1.11	1.2	3	1.09	0.8
-0.875	-157.5	6	1.18	1.2	4	1.15	0.9	4	1.18	1.2	5	1.18	1.5	4	1.14	1.9	2	1.21	1.2	4	1.12	1.1	4	1.10	1.0
-0.875	-142.5	6	1.16	0.8	6	1.19	1.3	3	1.18	0.9	5	1.16	1.7	4	1.30	1.3	4	1.17	1.5	5	1.18	1.1	6	1.09	1.5
-0.875	-127.5	5	1.19	1.0	7	1.19	1.5	4	1.18	0.9	5	1.15	1.8	8	1.22	0.9	3	1.14	0.8	6	1.17	1.4	6	1.05	, 1.6

Table A.5: (continued)

-0.875 $-112.5 \quad 8 \quad 1.16 \ 1.9 \ 8 \quad 1.13 \ 1.2 \ 4 \quad 1.14 \ 1.1 \ 4 \quad 1.15 \ 1.0 \ 5 \quad 1.23 \ 1.3 \ 4 \quad 1.18 \ 0.8 \ 8 \quad 1.12 \ 2.1 \ 6 \quad 1.19 \ 1.8 \ 1.8 \ 1.8 \ 1.8 \ 1.12 \ 1.18 \ 1.8 \ 1.12 \ 1.18 \$ -0.875 $6 \quad 1.14 \ 1.4 \ 8 \quad 1.17 \ 1.7 \ 4 \quad 1.17 \ 1.0 \ 4 \quad 1.20 \ 1.1 \ 5 \quad 1.16 \ 1.4 \ 4 \quad 1.23 \ 1.0 \ 6 \quad 1.09 \ 1.2 \ 5 \quad 1.17 \ 1.1$ -0.875-82.5 $15 \ 1.28 \ 2.5 \ 10 \ 1.22 \ 1.6 \ 5 \ 1.14 \ 1.1 \ 5 \ 1.14 \ 1.1 \ 4 \ 1.19 \ 1.4 \ 4 \ 1.19 \ 1.9 \ 7 \ 1.15 \ 1.8 \ 3 \ 1.05 \ 0.9$ $8 \quad 1.33 \ 1.5 \ 8 \quad 1.14 \ 1.1 \ 4 \quad 1.13 \ 1.5 \ 5 \quad 1.12 \ 2.0 \ 4 \quad 1.19 \ 1.5 \ 3 \quad 1.17 \ 0.8 \ 7 \quad 1.11 \ 1.7 \ 4 \quad 1.09 \ 0.8$ -0.875-67.5-0.875-52.5 $1.16 \ 1.0 \ 13 \ 1.12 \ 2.5 \ 4 \quad 1.11 \ 1.1 \ 5 \quad 1.25 \ 1.2 \ 3 \quad 1.23 \ 1.2 \ 7 \quad 1.25 \ 0.7 \ 13 \ 1.31 \ 1.4 \ 12 \ 1.00 \ 1.4$ -0.875-37.511 1.20 1.4 12 1.22 1.6 7 1.13 1.4 6 1.21 1.4 4 1.22 2.0 1 1.18 0.3 5 1.20 1.1 4 1.13 0.4 -0.875-22.5 $10\ \ 1.13\ \ 1.3\ \ 10\ \ 1.33\ \ 1.7\ \ 4\ \ \ 1.30\ \ 0.6\ \ 5\ \ \ \ 1.14\ \ 1.0\ \ 4\ \ \ \ 1.24\ \ 1.9\ \ 2\ \ \ \ 1.17\ \ 1.0\ \ 8\ \ \ \ 1.17\ \ 1.5\ \ 8\ \ \ \ 1.11\ \ 2.0$ -0.875-7.5 $8 \quad 1.13 \ 1.6 \ 8 \quad 1.28 \ 1.6 \ 5 \quad 1.21 \ 1.1 \ 6 \quad 1.13 \ 1.2 \ 12 \ 1.14 \ 1.2 \ 3 \quad 1.08 \ 1.6 \ 14 \ 1.14 \ 1.7 \ 10 \ 1.17 \ 0.9$ -0.8757.5 1.19 1.5 6 1.16 1.2 3 1.19 0.8 4 1.14 1.8 4 1.09 1.1 3 1.14 1.5 5 1.05 1.5 8 1.09 2.4 22.5 1.11 0.8 4 1.19 1.3 5 1.17 2.0 6 1.13 2.8 4 1.13 2.0 5 1.06 2.9 4 -0.8751.21 1.3 5 -0.87537.5 1.16 1.6 6 1.15 2.0 5 1.12 1.6 4 1.15 1.4 5 1.11 2.3 4 1.17 1.8 5 1.07 1.3 1.18 1.1 7 52.5 $1.17 \ 1.5 \ 4 \quad 1.16 \ 1.3 \ 4 \quad 1.16 \ 1.3 \ 4 \quad 1.18 \ 1.2 \ 4 \quad 1.10 \ 1.3 \ 4 \quad 1.16 \ 1.1 \ 4 \quad 1.07 \ 1.0$ -0.8751.20 1.3 7 67.5 -0.8751.14 1.6 5 1.10 1.1 6 1.14 2.7 4 1.13 1.2 4 1.19 1.2 4 1.08 1.3 4 1.14 0.9 6 1.10 1.3 -0.87582.5 1.16 1.5 7 1.19 1.5 5 1.14 1.6 6 1.15 2.0 4 1.12 1.5 7 1.12 2.3 4 1.07 0.7 7 -0.87597.5 1.18 1.6 8 1.16 1.7 4 1.17 0.8 7 1.13 1.6 7 1.13 1.8 5 1.20 1.6 9 1.12 1.7 6 1.14 1.2 -0.875112.5 1.12 1.2 6 1.21 1.0 4 1.19 0.7 4 1.12 1.3 6 1.09 1.2 3 1.15 0.7 5 1.08 1.2 5 1.12 1.1 1.15 1.6 7 1.13 1.8 5 1.14 1.5 4 1.13 1.4 4 1.10 1.7 4 1.19 1.6 4 1.08 1.1 4 1.12 1.3 -0.875127.5 -0.875142.5 1.16 1.5 5 1.16 1.4 3 1.17 1.0 4 1.15 1.5 3 1.13 1.3 3 1.16 1.2 4 1.12 1.5 3 1.15 0.8 -0.875157.5 1.14 1.2 7 1.17 1.6 5 1.16 1.7 4 1.16 1.1 4 1.15 1.5 4 1.16 1.6 4 1.15 1.6 4 1.17 1.3 -0.875172.5 1.19 1.3 6 1.18 1.6 5 1.16 1.7 5 1.18 2.0 4 1.13 1.0 4 1.15 1.1 4 1.11 1.3 3 1.14 1.0 -0.625-172.55 1.12 1.6 3 1.10 0.5 4 1.11 1.8 3 1.10 1.2 3 1.05 1.4 7 1.06 1.6 3 1.09 1.2 3 1.07 1.2 -0.625-157.55 1.12 1.2 4 1.10 0.9 4 1.08 1.9 4 1.09 2.1 3 1.08 1.3 1 1.07 0.5 3 1.07 1.3 4 1.09 2.2 -0.625-142.5 $4 \quad 1.11 \ 0.8 \ 5 \quad 1.11 \ 1.4 \ 4 \quad 1.11 \ 2.0 \ 2 \quad 1.07 \ 0.9 \ 3 \quad 1.12 \ 2.0 \ 3 \quad 1.07 \ 1.2 \ 3 \quad 1.06 \ 1.2 \ 4 \quad 1.08 \ 1.5$ -127.56 1.13 1.5 5 1.11 1.4 3 1.09 1.5 3 1.07 1.5 6 1.20 1.1 3 1.06 1.5 4 1.07 1.6 3 1.07 1.3 -0.625-0.625-112.54 1.10 1.3 6 1.15 1.5 4 1.11 1.8 4 1.09 1.3 4 1.07 1.2 3 1.07 1.3 4 1.08 1.3 4 1.08 1.2 -97.5 $5 \quad 1.12 \ 1.1 \ 5 \quad 1.12 \ 1.5 \ 3 \quad 1.09 \ 1.1 \ 3 \quad 1.09 \ 1.0 \ 5 \quad 1.09 \ 2.0 \ 3 \quad 1.09 \ 1.0 \ 4 \quad 1.08 \ 1.4 \ 4 \quad 1.09 \ 1.2 \ 1.0 \$ -0.625-0.625-82.5 $6\quad 1.15\ 1.1\ 7\quad 1.11\ 1.3\ 5\quad 1.11\ 1.9\ 4\quad 1.08\ 1.4\ 4\quad 1.07\ 1.4\ 3\quad 1.09\ 1.4\ 4\quad 1.08\ 1.3\ 3\quad 1.06\ 1.1$ -0.625-67.5 $6\quad 1.17\ 1.4\ 8\quad 1.06\ 2.0\ 3\quad 1.09\ 1.3\ 3\quad 1.11\ 1.2\ 3\quad 1.06\ 1.6\ 3\quad 1.06\ 1.2\ 4\quad 1.03\ 0.6\ 4\quad 1.06\ 1.6$ -0.625-52.57 1.16 1.4 5 1.14 1.0 4 1.06 1.1 5 1.09 1.8 3 1.09 1.7 7 1.10 1.4 7 1.01 0.9 11 1.14 1.4 -0.625-37.56 1.10 0.9 9 1.11 1.8 5 1.11 1.8 3 1.12 1.3 3 1.08 2.2 1 1.10 0.5 3 1.07 0.9 3 1.06 0.9 -22.51.15 1.0 5 1.15 1.5 5 1.09 1.8 2 1.12 1.3 2 1.10 1.9 5 -0.6255 1.10 0.8 5 1.15 1.4 6 -0.625-7.51.13 1.4 3 1.11 0.9 3 1.08 1.5 7 1.12 0.9 3 1.06 1.7 8 1.09 1.1 6 1.08 1.9 6 -0.6257.5 5 1.12 1.3 3 1.10 1.2 4 1.08 1.5 2 1.04 0.8 2 1.07 1.2 4 1.08 2.5 5 1.08 1.7 1.12 1.7 5 1.12 1.0 3 1.11 1.3 4 1.09 1.5 7 -0.62522.5 4 $1.10\ 0.7\ 4$ 1.07 5.9 3 1.05 1.9 4 1.08 1.8 4 1.06 1.2 1.09 1.1 3 1.12 1.2 4 1.08 1.9 3 1.06 1.7 2 1.07 1.7 4 -0.62537.5 5 1.09 1.5 5 1.07 1.7 4 1.05 1.4 5 $1.11\ 1.7\ 3\quad 1.08\ 0.7\ 3\quad 1.11\ 1.4\ 3\quad 1.09\ 1.1\ 2\quad 1.10\ 1.0\ 2\quad 1.08\ 1.5\ 3\quad 1.08\ 1.3\ 4\quad 1.08\ 1.8$ -0.62552.5 67.5 5 $1.10 \ 1.2 \ 5 \quad 1.10 \ 1.6 \ 4 \quad 1.12 \ 1.9 \ 4 \quad 1.08 \ 1.8 \ 2 \quad 1.09 \ 1.2 \ 3 \quad 1.07 \ 1.2 \ 4 \quad 1.06 \ 1.4 \ 3 \quad 1.08 \ 1.4$ -0.625-0.62582.5 5 $1.11\ 1.7\ 6$ $1.07\ 1.5\ 4$ $1.11\ 1.3\ 4$ $1.09\ 1.3\ 3$ $1.10\ 1.0\ 3$ $1.09\ 1.5\ 4$ $1.08\ 1.6\ 4$ $1.06\ 1.3$ 7 1.13 1.8 5 1.09 1.1 4 1.12 1.1 4 1.10 1.2 5 1.10 1.7 2 1.11 1.0 5 1.08 1.3 4 1.06 1.0 -0.62597.5 112.5 5 1.10 1.0 5 1.07 1.1 4 1.09 1.3 3 1.09 1.0 4 1.08 1.3 3 1.07 0.9 3 1.06 0.6 3 1.05 1.2 -0.625-0.625127.5 $6 \quad 1.11 \ 1.8 \ 4 \quad 1.08 \ 1.2 \ 4 \quad 1.11 \ 1.7 \ 3 \quad 1.08 \ 1.6 \ 3 \quad 1.07 \ 1.8 \ 2 \quad 1.09 \ 0.7 \ 3 \quad 1.06 \ 1.4 \ 4 \quad 1.08 \ 2.1$ 5 1.10 1.2 5 1.09 2.6 3 1.11 1.3 4 1.11 2.7 2 1.09 1.2 3 1.08 2.0 3 1.08 1.8 3 1.07 1.4 -0.625142.5 157.5 1.12 1.2 6 1.11 1.6 2 1.10 0.9 3 1.07 1.3 3 1.09 1.8 2 1.08 0.9 3 1.07 1.2 3 1.08 1.2 -0.625-0.625172.5 $4 \quad 1.10 \ 1.0 \ 6 \quad 1.11 \ 2.0 \ 3 \quad 1.11 \ 1.3 \ 2 \quad 1.11 \ 0.9 \ 2 \quad 1.08 \ 1.3 \ 3 \quad 1.06 \ 1.1 \ 4 \quad 1.08 \ 1.7 \ 3 \quad 1.06 \ 1.5$ -0.375-172.53 1.12 0.9 4 1.11 1.2 3 1.09 1.2 3 1.08 0.9 3 1.07 1.4 5 1.02 1.3 3 1.05 1.5 3 1.07 1.8 -0.375-157.54 1.10 1.1 4 1.09 1.2 4 1.09 1.8 3 1.07 1.0 2 1.08 0.8 3 1.10 2.0 3 1.07 1.2 3 1.07 1.1 -142.5-0.3754 1.09 1.3 5 1.08 1.4 4 1.09 2.2 4 1.10 2.0 2 1.09 1.0 3 1.06 1.4 3 1.06 1.2 3 1.05 1.0 $-127.5 \quad 5 \quad 1.11 \ 1.4 \ 3 \quad 1.09 \ 0.8 \ 3 \quad 1.10 \ 1.2 \ 3 \quad 1.07 \ 1.2 \ 5 \quad 1.13 \ 0.9 \ 2 \quad 1.06 \ 1.0 \ 3 \quad 1.05 \ 1.3 \ 3 \quad 1.05 \ 1.1$ -0.375 $-112.5 \quad 5 \quad 1.11 \ 1.3 \ 4 \quad 1.11 \ 1.1 \ 4 \quad 1.09 \ 1.5 \ 3 \quad 1.08 \ 1.1 \ 4 \quad 1.09 \ 1.6 \ 2 \quad 1.06 \ 1.0 \ 3 \quad 1.07 \ 1.0 \ 4 \quad 1.04 \ 1.6$ -0.375-0.375-97.5 $4 \quad 1.14 \ 1.1 \ 4 \quad 1.06 \ 0.8 \ 4 \quad 1.08 \ 2.0 \ 4 \quad 1.09 \ 1.8 \ 3 \quad 1.10 \ 1.0 \ 4 \quad 1.09 \ 1.8 \ 3 \quad 1.05 \ 1.4 \ 3 \quad 1.05 \ 0.8$ $5 \quad 1.08 \; 1.3 \; 6 \quad 1.12 \; 1.5 \; 5 \quad 1.11 \; 2.1 \; 4 \quad 1.06 \; 1.8 \; 3 \quad 1.07 \; 1.2 \; 3 \quad 1.07 \; 1.2 \; 3 \quad 1.07 \; 1.1 \; 4 \quad 1.05 \; 1.6$ -0.375-82.5 $6 \quad 1.08 \; 1.9 \; 4 \quad 1.07 \; 1.2 \; 3 \quad 1.10 \; 1.6 \; 4 \quad 1.08 \; 1.5 \; 3 \quad 1.08 \; 2.0 \; 3 \quad 1.05 \; 1.4 \; 5 \quad 1.09 \; 1.2 \; 3 \quad 1.02 \; 0.9$ -0.375-67.5-0.375-52.54 1.11 0.7 7 1.06 1.9 4 1.09 1.8 3 1.07 1.0 3 1.07 2.9 4 1.09 0.9 7 1.04 1.1 11 0.95 1.3 -0.375-37.55 $1.10\ 1.4\ 6\quad 1.08\ 1.1\ 4\quad 1.09\ 1.2\ 5\quad 1.09\ 2.2\ 3\quad 1.08\ 1.9\ 2\quad 1.10\ 1.3\ 5\quad 1.08\ 2.0\ 4\quad 1.09\ 2.2$ -0.375-22.56 1.11 1.2 4 1.11 0.8 5 1.09 1.6 6 1.09 2.1 2 1.11 1.2 3 1.08 2.8 4 1.05 1.8 3 -0.375-7.51.06 1.1 4 1.08 1.3 4 1.06 1.5 6 1.08 1.0 2 1.06 1.0 12 1.04 2.1 8 1.08 1.6 4 1.10 1.1 5 -0.3751.09 1.0 3 1.11 0.9 2 1.07 0.7 3 1.06 1.4 2 7.5 1.09 1.2 4 1.06 2.0 4 1.01 1.3 4 -0.37522.5 1.08 1.3 3 1.09 1.4 3 1.07 1.5 6 1.06 5.2 2 1.06 1.3 3 5 1.11 1.3 4 1.04 1.7 3 -0.37537.5 5 1.05 1.4 5 1.12 1.4 4 1.09 1.5 3 1.07 1.2 3 1.07 2.2 2 1.07 1.5 4 1.05 1.8 3 1.09 1.0 4 1.07 2.3 3 1.09 1.6 3 -0.37552.5 5 1.09 1.7 4 1.08 1.2 2 1.06 1.9 3 1.09 1.6 2 67.5 1.07 1.9 3 1.10 1.2 3 1.06 1.3 3 1.07 1.6 3 1.04 1.1 4 -0.3755 1.08 2.1 5 1.08 1.4 3 1.07 1.4 $5 \quad 1.10 \ 2.0 \ 4 \quad 1.08 \ 0.9 \ 4 \quad 1.11 \ 1.4 \ 3 \quad 1.09 \ 1.3 \ 3 \quad 1.10 \ 2.1 \ 3 \quad 1.07 \ 1.2 \ 3 \quad 1.07 \ 1.3 \ 4 \quad 1.06 \ 1.4$ 82.5 -0.375

Table A.5: (continued)

-0.375	97.5	5	1.09 1.1 7	1.10 1.7 4	1.07 1.5 4	1.09 1.7 3	1.07 1.3 3	1.06 0.9 4	1.07 1.5 5	1.06 1.6
-0.375	112.5	4	1.09 1.1 4	1.08 0.8 4	1.10 1.8 3	1.07 1.0 3	1.07 0.8 3	1.08 1.2 4	1.10 1.3 4	1.06 2.0
-0.375	127.5	4	1.09 1.4 5	1.10 1.1 3	1.09 1.2 3	1.08 1.1 3	1.05 1.7 3	1.09 1.8 4	1.06 2.5 3	1.07 1.2
-0.375	142.5	4	1.12 1.1 3	1.08 1.2 3	1.08 1.3 3	1.10 1.9 3	1.08 1.9 2	1.07 1.3 3	1.08 1.5 3	1.06 1.2
-0.375	157.5	4	1.10 1.3 3	1.08 0.9 3	1.10 1.7 3	1.08 1.4 3	1.07 1.3 3	1.08 1.2 3	1.07 1.2 3	1.08 1.5
-0.375	172.5	3	$1.10\ 1.0\ 4$	$1.09\ 1.4\ 4$	1.11 2.1 3	1.10 1.6 2	1.08 1.5 2	1.05 1.1 2	1.07 0.7 3	$1.05 \ 1.5$
-0.125	-172.5	4	1.07 1.2 4	1.08 1.1 4	1.08 1.8 3	1.05 1.4 3	1.06 1.5 3	1.09 0.8 2	1.07 1.2 2	1.07 1.2
-0.125	-157.5	4	1.10 1.2 4	1.07 1.1 4	1.09 2.0 3	1.05 1.0 3	1.08 2.1 3	1.08 1.6 3	1.06 1.6 2	1.05 0.9
-0.125	-142.5	4	1.10 1.3 5	1.09 1.5 2	1.09 1.0 3	1.07 1.3 3	1.07 1.3 2	1.05 1.0 3	$1.05 \ 1.5 \ 4$	1.03 1.7
-0.125	-127.5	5	1.09 1.7 4	1.06 1.0 2	1.08 0.9 3	1.06 1.4 5	1.08 1.6 2	1.05 0.7 4	1.03 1.8 2	1.04 0.5
-0.125	-112.5	4	1.10 0.9 5	1.12 1.2 3	1.07 1.3 3	1.05 1.0 4	1.05 1.3 2	1.03 1.1 4	1.03 1.5 3	1.04 1.4
-0.125	-97.5	6	1.08 2.1 4	1.06 0.9 3	1.09 0.9 3	1.07 0.9 3	1.04 1.2 3	1.03 1.5 3	$1.06 \ 1.4 \ 4$	1.02 1.6
-0.125	-82.5	6	1.02 1.4 7	1.07 1.4 3	1.10 1.2 3	1.07 1.2 3	1.10 1.4 3	1.06 1.3 4	1.06 1.4 3	1.03 1.1
-0.125	-67.5	4	1.07 1.2 4	1.09 0.7 2	1.10 1.0 3	1.09 0.9 3	1.09 1.8 3	1.04 1.3 4	1.01 1.3 4	1.04 1.6
-0.125	-52.5	6	1.03 1.5 6	1.05 1.7 3	1.07 1.0 4	1.10 1.2 3	1.08 1.8 3	1.06 1.0 4	0.95 1.3 6	$1.07 \ 1.4$
-0.125	-37.5	5	1.06 1.2 5	1.07 1.2 4	1.13 1.4 4	1.12 1.6 2	1.09 1.3 3	1.08 1.5 3	1.03 1.2 3	1.06 1.2
-0.125	-22.5	6	1.08 1.2 5	1.09 1.4 3	1.12 1.1 3	1.10 0.9 2	1.10 0.8 2	1.09 1.7 4	1.07 1.6 4	1.04 1.6
-0.125	-7.5	5	$1.10\ 1.4\ 4$	1.03 1.1 5	$1.08\ 1.5\ 4$	1.08 1.6 4	1.06 1.0 2	1.07 1.3 6	1.04 1.5 5	0.95 1.1
-0.125	7.5	5	1.09 1.8 5	1.08 1.5 3	1.09 1.5 2	1.08 0.9 3	1.07 1.6 2	1.08 1.1 4	1.07 1.3 5	1.02 1.9
-0.125	22.5	5	1.08 1.4 3	1.03 0.6 3	1.08 1.2 3	1.09 1.4 4	1.07 3.6 2	1.06 1.1 4	1.03 1.6 3	1.05 1.4
-0.125	37.5	3	$1.10\ 0.9\ 4$	1.07 1.3 3	1.09 1.5 3	1.06 0.9 3	1.07 1.9 3	1.06 1.8 3	1.08 0.9 3	$1.05 \ 1.4$
-0.125	52.5	4	1.10 0.8 4	1.06 0.6 3	1.08 1.6 3	1.05 1.3 2	1.09 1.3 2	1.06 1.2 5	1.07 2.5 3	1.03 1.1
-0.125	67.5	4	1.07 1.1 4	1.06 0.9 3	1.09 1.1 2	1.07 0.8 2	1.06 1.3 3	1.08 1.1 3	1.04 1.0 3	1.06 1.0
-0.125	82.5	5	1.10 1.5 3	$1.05 \ 0.9 \ 4$	1.07 1.8 3	1.06 1.1 2	$1.08 \ 1.1 \ 4$	1.07 2.3 3	1.02 0.9 3	$1.07 \ 1.0$
-0.125	97.5	5	1.05 1.2 4	1.08 0.9 4	1.08 2.0 4	1.04 1.1 3	1.08 1.1 3	1.08 0.9 4	1.06 1.0 4	1.05 1.5
-0.125	112.5	5	1.09 1.7 6	1.09 2.0 3	1.08 1.3 3	1.04 0.9 3	1.09 1.2 3	1.05 1.4 4	1.04 1.5 3	1.04 1.0
-0.125	127.5	4	1.11 1.0 3	1.07 0.6 3	1.11 1.6 2	1.07 1.1 3	1.07 1.9 2	1.06 1.2 3	1.07 1.1 3	$1.05 \ 1.1$
-0.125	142.5	3	1.09 0.7 4	1.08 1.9 4	1.09 2.0 3	1.08 1.0 3	1.08 2.1 3	1.06 1.9 4	1.06 2.4 2	1.07 0.9
-0.125	157.5	3	1.09 0.7 5	1.06 1.3 3	1.10 1.6 3	1.06 1.7 2	1.06 1.1 3	1.06 1.9 4	1.06 2.1 3	1.06 1.4
-0.125	172.5	4	1.11 1.5 3	1.09 0.6 3	1.06 1.7 3	1.08 1.4 3	1.08 1.9 3	1.05 1.6 3	1.07 1.2 3	$1.06 \ 1.5$
0.125	-172.5	5	1.09 1.5 4	1.09 1.0 3	1.07 1.3 3	1.08 1.6 2	1.08 1.7 2	1.08 1.3 3	1.07 1.8 3	1.07 1.4
0.125	-157.5	4	1.07 1.6 4	1.07 1.1 3	1.08 2.0 2	1.08 0.8 2	1.06 1.1 2	1.05 1.4 2	1.07 0.7 3	1.04 1.7
0.125	-142.5	6	1.09 1.7 4	1.05 1.2 3	1.09 1.2 3	1.07 1.2 2	1.09 1.3 2	1.06 1.2 3	1.08 1.1 2	$1.06 \ 0.5$
0.125	-127.5	4	1.07 1.2 4	1.06 1.1 3	1.06 1.2 2	1.08 0.8 3	1.10 1.6 2	1.07 1.4 2	1.06 0.9 3	1.06 1.2
0.125	-112.5	4	1.08 1.5 6	1.07 2.3 3	1.08 1.4 3	1.07 1.7 3	1.07 1.8 2	1.08 1.3 3	1.08 1.7 3	1.08 1.0
0.125	-97.5	4	$1.10\ 1.4\ 4$	$1.07 \ 1.0 \ 4$	1.06 1.4 3	1.07 1.4 2	1.08 1.3 2	1.08 1.0 3	1.08 1.3 3	1.05 1.3
0.125	-82.5	7	1.10 1.8 5	1.11 1.1 2	1.07 0.8 3	1.04 1.1 3	1.06 1.4 3	$1.07\ 1.4\ 4$	1.07 1.2 4	1.06 1.7
	-67.5									
0.125		4	1.10 1.1 5	1.11 1.1 3	1.06 1.2 3	1.06 1.2 2	1.08 1.4 3	1.05 1.5 3	1.10 1.4 3	1.06 1.7
0.125	-52.5	6	1.13 1.6 4	1.11 1.3 2	1.09 0.7 3	1.07 0.7 3	1.08 2.3 3	1.07 2.1 3	1.09 1.3 3	$1.05 \ 1.1$
0.125	-37.5	4	1.11 0.8 5	1.13 1.4 6	1.02 2.1 5	1.05 1.4 2	1.09 1.5 2	1.07 1.3 4	1.07 2.1 4	1.06 1.6
0.125	-22.5	6	1.10 1.5 3	1.13 0.6 3	1.09 1.0 3	1.07 0.8 2	1.08 1.2 3	1.06 1.6 4	1.04 2.1 3	1.09 0.8
0.125	-7.5	4	$1.07\ 0.9\ 4$	1.09 1.2 3	1.05 0.9 3	1.08 0.9 3	1.08 2.3 4	1.04 3.7 3	1.07 0.9 3	1.07 1.8
0.125	7.5	4	1.09 1.0 6	1.08 2.1 4	1.10 2.0 2	1.06 0.9 3	1.07 2.3 3	1.07 1.5 4	1.05 1.9 3	1.08 1.6
0.125	22.5	4	1.12 1.4 4	1.06 1.2 2	1.07 0.7 3	1.08 1.8 2	1.06 1.8 3	1.05 2.4 3	1.08 1.5 2	1.06 0.9
0.125	37.5	5	1.08 1.2 4	1.07 1.1 4	1.09 2.0 3	1.08 1.2 3	1.09 1.2 3	1.06 1.2 3	1.07 1.1 3	1.07 2.0
0.125	52.5	5	1.07 1.5 4	1.06 1.4 3	1.08 1.3 3	1.05 1.2 3	1.07 1.5 3	1.03 1.5 3	1.07 1.5 3	1.01 1.2
0.125	67.5	4	1.08 1.0 5	1.09 1.3 3	1.08 1.6 3	1.07 1.4 3	1.09 2.6 3	1.07 1.4 3	1.06 1.7 3	1.07 1.5
0.125	82.5	4	1.08 0.9 3	1.03 0.7 3	1.06 1.1 2	1.10 0.8 3	1.07 1.6 3	1.05 0.9 3	$1.07\ 1.6\ 4$	1.03 1.9
0.125	97.5	6	1.06 1.6 5	1.10 1.0 4	1.09 1.5 4	1.06 1.3 3	1.05 0.9 4	1.10 1.3 4	$1.07 \ 1.1 \ 4$	$1.09 \ 1.4$
0.125	112.5	4	1.13 1.4 5	1.08 1.3 3	1.08 1.3 4	1.08 1.9 2	1.08 1.3 2	1.10 1.1 3	1.06 0.9 4	1.05 2.1
0.125	127.5	5	1.12 1.5 5	1.08 1.3 3	1.07 1.3 2	1.04 1.0 2	1.10 1.6 2	1.08 1.6 3	1.04 1.5 2	1.06 1.0
0.125	142.5	4	1.08 1.4 3	1.06 1.1 3	1.08 1.7 3	1.06 1.7 3	1.11 1.1 2	1.06 1.8 3	1.08 1.5 2	1.07 1.3
0.125	157.5	5	1.09 1.2 3	1.07 1.1 3	1.07 1.4 2	1.06 1.2 4	1.06 2.0 2	1.08 0.9 3	1.07 2.1 3	1.07 1.2
0.125	172.5	3	1.09 0.9 4	1.06 1.0 3	1.08 1.2 2	1.06 1.0 3	1.07 2.2 2	1.05 1.2 3	1.08 1.3 3	1.04 1.2
0.375	-172.5	5	1.06 1.8 4	1.08 1.2 3	$1.10\ 1.4\ 4$	1.09 1.6 2	1.06 1.0 2	1.07 1.9 2	1.07 0.9 3	1.06 1.1
0.375	-157.5	4	1.07 1.1 5	1.07 2.0 3	1.09 1.3 3	1.08 1.2 3	1.10 3.0 2	1.06 1.6 3	1.07 1.1 3	1.05 1.3
0.375	-142.5	5	1.09 1.5 4	1.06 1.3 4	1.10 2.2 2	1.08 0.9 3	1.06 1.8 2	1.08 1.6 3	1.06 1.3 3	1.06 1.5
0.375	-127.5	5	1.13 2.0 4	1.08 0.8 3	$1.08\ 1.5\ 4$	1.06 1.5 2	1.09 1.3 2	1.06 1.8 3	1.08 1.1 3	1.06 1.6
0.375	-112.5	5	1.10 1.6 6	1.08 1.9 3	1.08 1.1 3	1.06 1.1 2	1.08 1.1 3	1.07 1.6 4	1.07 1.7 2	1.07 1.0
0.375	-97.5	5	1.07 1.8 6	1.07 1.9 4	1.09 2.1 3	1.06 1.3 3	1.07 1.3 3	1.07 2.4 3	1.07 1.2 3	1.09 2.0
0.375	-82.5	6	1.11 1.6 5	$1.10\ 1.4\ 4$	1.08 1.6 3	1.10 1.2 3	1.08 1.7 3	$1.07\ 1.5\ 4$	1.08 1.8 2	1.06 0.7
0.375	-67.5	5	1.08 1.9 4	1.05 1.0 4	1.09 1.8 3	1.10 1.1 3	1.07 1.5 2	1.06 1.6 3	1.09 1.9 3	1.06 2.1
	20	_		1						

Table A.5: (continued)

0.375	-52.5	3	$1.10\ 0.6\ 4$	1.09 1.3 4	1.10 1.5 5	1.12 1.5 2	1.08 1.3 2	1.09 1.5 3	1.07 1.3 3	1.08 1.6
0.375	-37.5	4	1.09 1.0 5	1.10 2.0 4	1.11 1.3 3	1.10 0.9 2	1.10 1.9 2	1.07 1.6 4	1.09 2.2 3	1.06 1.0
0.375	-22.5	5	1.11 1.7 5	$1.10\ 1.7\ 4$	1.12 1.2 4	1.07 1.3 3	1.08 1.8 2	1.05 1.2 3	1.08 1.9 2	1.06 1.2
0.375	-7.5	6	1.13 2.1 4	1.10 1.4 4	1.08 1.2 3	1.08 1.3 3	1.08 1.6 2	1.08 1.3 3	1.06 1.5 3	1.04 1.4
0.375	7.5	6	1.11 2.0 5	1.08 1.5 4	1.11 2.1 3	1.08 1.8 2	1.08 1.8 2	1.09 1.4 4	1.07 1.8 3	1.08 1.6
0.375	22.5	4	$1.10\ 1.4\ 5$	1.07 1.3 4	1.08 2.7 2	1.08 0.9 2	1.09 1.0 3	1.06 1.7 4	1.08 1.5 3	$1.05 \ 1.4$
0.375	37.5	4	1.08 1.0 5	1.12 1.4 3	1.10 1.2 2	1.07 1.0 3	1.09 1.5 3	1.07 1.3 3	1.05 1.0 4	1.06 1.8
0.375	52.5	4	1.11 1.2 5	1.07 1.5 3	1.08 1.1 3	1.07 1.4 3	1.07 1.4 2	1.06 1.1 3	1.07 1.7 3	1.05 1.5
0.375	67.5	5	1.11 1.1 5	1.09 1.4 4	1.10 1.7 2	1.07 1.0 3	1.08 2.7 3	1.08 2.1 4	1.07 2.1 3	1.09 2.3
0.375	82.5	5	1.12 1.2 4	1.08 0.8 3	1.08 2.3 3	1.07 1.3 3	1.06 1.9 4	1.04 1.8 4	1.07 1.8 4	1.07 1.6
0.375	97.5	5	1.11 0.8 8	1.09 2.3 4	1.08 1.6 3	1.07 0.9 4	1.08 2.1 6	1.09 1.9 5	1.06 1.4 3	1.07 1.4
0.375	112.5	4	1.11 0.9 4	$1.07 \ 1.1 \ 4$	1.09 2.0 4	1.08 1.4 2	1.08 1.7 2	1.08 1.3 4	1.07 1.6 3	$1.04 \ 1.5$
0.375	127.5	3	1.09 0.8 4	1.08 1.2 4	1.10 1.4 3	1.07 1.6 2	1.11 1.2 3	1.08 2.0 3	1.07 1.4 3	1.09 1.1
0.375	142.5	4	1.07 1.5 3	1.08 0.8 3	1.08 1.5 3	1.09 1.5 3	1.11 1.1 3	1.07 2.2 3	1.08 1.6 3	1.06 1.1
0.375	157.5	5	1.11 1.9 5	1.08 1.6 3	1.10 1.3 3	1.08 1.2 3	1.05 1.1 3	1.07 2.8 4	1.07 1.7 3	$1.08\ 1.4$
0.375	172.5	3	1.12 0.8 4	1.08 0.9 3	1.08 1.6 3	1.08 1.2 3	1.08 2.0 3	1.06 1.9 3	1.10 1.3 3	1.06 1.6
0.625	-172.5	5	1.13 1.4 4	1.09 0.9 3	1.11 1.7 3	1.09 1.4 3	1.08 1.7 4	1.06 2.3 3	1.08 1.3 3	1.07 1.4
0.625	-157.5	6	1.10 1.5 4	1.11 1.4 4	1.11 1.7 3	1.10 1.3 3	1.09 1.8 2	1.07 1.8 3	1.08 1.3 3	1.04 1.5
0.625	-142.5	5	1.11 1.5 4	1.10 1.1 5	1.13 2.1 4	1.09 1.3 3	1.07 1.6 2	1.08 1.6 4	1.08 1.5 3	$1.09\ 1.4$
0.625	-127.5	4	1.11 0.8 5	1.11 1.3 4	1.10 1.6 4	1.09 1.6 3	1.08 1.5 3	1.09 1.6 3	1.10 1.0 2	1.09 0.5
0.625	-112.5	5	1.12 1.4 6	1.06 1.4 4	1.08 1.3 2	1.10 0.7 2	1.09 1.0 3	1.08 1.7 4	1.06 1.6 3	1.08 1.1
0.625	-97.5	6	1.11 1.5 6	1.12 1.5 5	1.09 1.9 3	1.08 1.2 3	1.08 1.4 3	1.08 1.7 3	1.10 1.4 3	1.07 1.3
0.625	-82.5	5	1.07 0.9 5	1.05 1.1 4	1.08 1.2 4	1.11 1.6 3	1.08 1.6 3	1.08 1.8 4	1.07 1.9 3	1.09 0.8
0.625	-67.5	5	1.08 1.4 5	1.13 1.3 4	1.12 1.6 3	1.08 1.4 2	1.09 1.2 3	1.08 1.7 3	1.10 0.9 3	1.07 1.1
0.625	-52.5	5	1.10 1.2 5	1.11 1.3 4	$1.07\ 0.8\ 4$	1.11 1.1 3	1.08 1.9 4	1.09 3.3 3	1.06 1.6 2	1.06 1.1
0.625	-37.5	5	1.11 1.4 4	1.08 1.4 5	1.11 1.1 4	1.08 0.9 3	1.09 2.1 3	1.07 2.3 4	1.09 2.3 3	1.05 1.3
0.625	-22.5	4	1.10 1.1 3	1.07 0.8 4	1.12 1.6 4	1.07 0.8 3	1.07 1.6 2	1.06 1.0 3	1.08 1.3 3	1.05 1.1
0.625	-7.5	5	1.12 2.0 3	1.08 0.8 5	1.12 1.5 4	1.09 1.3 3	1.08 1.9 2	1.07 1.1 4	1.10 2.2 2	1.07 0.8
0.625	7.5	4	1.09 1.1 4	1.11 1.2 4	1.12 2.1 3	1.07 1.2 2	1.10 1.3 2	1.09 1.5 3	1.08 1.0 3	$1.07 \ 1.0$
0.625	22.5	4	1.12 0.8 5	1.10 1.8 4	1.12 1.3 3	1.09 1.2 3	1.09 2.2 3	1.08 2.3 4	1.08 1.8 3	1.07 1.3
0.625	37.5	4	1.10 1.0 5	1.07 1.8 4	1.11 2.1 3	1.07 1.4 2	1.09 1.2 3	1.07 1.8 3	1.06 1.2 3	1.09 1.4
0.625	52.5	5	1.10 1.3 6	1.11 2.3 3	1.11 1.2 4	1.07 2.1 3	1.08 1.4 3	$1.05 \ 1.7 \ 4$	$1.07 \ 1.5 \ 4$	1.07 2.1
0.625	67.5	5	1.09 1.4 5	1.10 1.3 3	1.11 1.3 3	1.10 1.2 4	1.09 2.7 3	1.09 2.0 4	1.07 1.7 4	1.08 1.7
0.625	82.5	4	1.12 0.9 5	1.07 1.0 4	1.10 1.2 3	1.11 0.8 3	1.09 1.4 3	1.07 1.3 4	1.05 1.9 5	1.04 2.3
0.625	97.5	7	1.11 1.3 5	$1.06\ 0.8\ 4$	1.10 1.6 4	1.09 1.4 3	1.09 1.9 4	1.13 0.9 5	1.10 1.7 3	1.08 0.9
0.625	112.5	5	1.09 0.9 4	1.07 0.9 3	1.09 0.8 5	1.08 1.5 3	1.08 2.2 2	1.11 1.1 3	1.09 0.9 3	1.06 1.1
0.625	127.5	4	1.09 1.2 4	1.09 1.0 4	1.11 1.7 3	1.09 1.4 2	1.13 1.4 3	1.07 1.8 3	1.06 1.5 3	1.07 1.3
0.625	142.5	5	1.11 1.7 5	1.11 1.4 3	1.09 1.3 3	1.08 1.4 4	1.11 1.5 3	1.07 1.8 4	1.07 1.5 2	1.05 1.2
0.625	157.5	5	$1.14\ 1.6\ 4$	1.09 1.0 3	1.12 1.1 4	$1.08 \ 1.4 \ 4$	1.07 2.7 3	1.07 2.4 3	1.07 1.2 2	$1.06\ 0.6$
0.625	172.5	5	1.14 1.4 5	1.09 1.1 4	1.09 1.6 3	1.10 1.5 3	1.10 2.0 3	1.07 1.7 3	1.10 1.9 3	1.08 1.5
		7								
0.875	-172.5	/	1.21 1.4 7	1.12 1.5 4	1.12 1.2 4	1.12 1.2 3	1.17 1.8 2	1.12 1.0 4	1.11 1.3 3	1.09 0.8
0.875	-157.5	6	1.15 1.0 7	$1.08 \ 1.5 \ 4$	1.15 1.0 4	1.12 0.9 4	1.15 2.4 2	1.14 1.1 5	1.12 1.7 4	$1.10\ 1.4$
0.875	-142.5	6	1.16 1.0 5	1.10 0.9 4	1.12 0.9 4	1.12 0.9 3	1.17 1.2 3	1.11 1.2 4	1.13 1.4 5	1.06 1.5
0.875	-127.5	6	1.19 1.2 6	1.11 1.1 4	1.18 1.2 4	1.16 1.0 3	1.18 1.2 3	1.11 1.3 4	1.11 1.0 5	1.09 1.8
0.875	-112.5	6	1.15 1.3 5	1.05 1.0 5	1.16 1.4 3	1.17 0.7 3	1.17 1.1 3	1.13 1.7 5	1.12 0.9 5	1.11 1.5
0.875	-97.5	7	1.20 1.3 6	1.18 1.1 5	1.10 1.2 4	1.17 1.0 3	1.13 1.5 3	$1.17\ 0.9\ 4$	1.10 1.0 5	1.11 2.2
0.875	-82.5	7	1.16 1.1 8	1.08 1.4 5	1.19 1.3 4	1.13 1.0 3	1.13 0.8 4	1.17 1.4 5	1.10 1.1 4	1.08 1.0
0.875	-67.5	6	1.22 1.2 6	1.21 1.3 4	1.18 1.2 5	1.11 1.4 3	1.18 1.2 3	1.19 1.5 4	1.11 1.6 5	1.08 1.8
0.875	-52.5	5	1.13 1.0 6	$1.18 \ 1.4 \ 4$	1.13 0.8 7	1.29 1.1 2	1.20 1.1 3	1.18 1.2 4	1.14 1.7 3	1.08 0.8
0.875	-37.5	9	1.20 2.2 6	1.14 1.6 7	1.14 1.3 7	1.31 1.7 3	1.18 1.5 3	$1.14\ 1.5\ 4$	1.11 1.5 3	1.10 1.6
0.875	-22.5	6	1.13 1.3 5	1.15 1.1 7	1.27 1.8 6	1.08 1.2 3	1.16 1.1 2	1.15 1.0 4	1.14 1.1 4	1.12 1.2
0.875	-7.5	4	1.21 1.0 6	1.17 0.9 7	1.26 1.5 6	1.12 1.4 2	1.14 0.9 3	1.23 1.5 4	1.07 1.6 4	1.14 1.2
0.875	7.5	6	1.19 1.3 6	1.15 1.4 5	1.19 1.7 4	1.17 1.4 2	1.15 1.2 2	1.22 0.9 4	$1.09\ 1.4\ 4$	1.08 1.1
0.875	22.5	7	1.16 1.7 5	1.18 0.8 5	1.17 1.5 5	1.15 1.5 3	1.19 1.6 2	1.17 0.7 5	1.11 1.5 4	1.11 1.4
0.875	37.5	5	1.20 1.1 5	1.18 0.9 4	1.20 1.3 3	1.15 1.0 2	1.16 1.1 3	1.13 1.1 3	1.11 1.1 5	1.10 1.6
0.875	52.5	5	1.16 0.9 5	$1.18 \ 1.4 \ 4$	1.20 1.1 5	1.19 1.8 3	1.11 1.9 3	1.12 1.1 5	1.12 1.9 3	1.09 1.0
0.875	67.5	6	1.12 1.0 6	1.14 1.3 5	1.16 1.8 4	1.12 1.2 3	1.15 1.7 3	1.16 2.4 4	1.12 1.4 4	1.12 1.2
0.875	82.5	8	1.19 1.8 7	1.13 1.1 6	1.14 1.6 5	1.14 1.7 4	1.12 1.2 4		1.08 1.3 5	1.11 1.3
								1.15 1.2 5		
0.875	97.5	9	1.15 1.6 7	1.14 1.4 5	1.15 1.0 5	1.13 1.0 5	1.14 1.8 9	1.26 1.9 6	1.10 1.4 5	1.07 1.1
0.875	112.5	8	1.21 1.5 5	1.14 0.8 5	1.18 1.4 5	1.14 1.6 3	1.18 1.7 5	1.16 2.1 5	1.14 1.1 5	1.10 1.6
0.875	127.5	7	1.17 2.0 7	1.16 2.0 4	1.17 1.3 3	1.15 0.9 3	1.18 1.6 3	1.17 1.5 4	1.18 1.4 4	1.13 1.5
0.875	142.5									
		6	1.17 1.3 4	1.20 0.9 5	1.18 1.7 4	1.15 1.6 9	1.19 1.8 2	1.16 1.1 4	1.09 1.7 3	1.06 1.3

Table A.5: (continued)

0.875	157.5	7	1.16 1.4 8	1.24 2.3 3	1.14 0.8 5	1.12 1.6 4	1.18 1.5 3	1.17 1.3 3	1.14 1.1 3	$1.07 \ 0.8$
0.875	172.5	8	1.20 2.5 4	$1.17\ 0.9\ 4$	1.14 1.7 6	1.14 2.2 3	1.19 1.8 3	1.16 1.1 3	$1.10\ 0.9\ 4$	1.12 1.3

Table A.6: p-dependence of TPC Selection Efficiencies

				c ⊥ A	c .			
n	19.6	GeV	27 (ε±Δ GeV	$\varepsilon_{ m syst}$ 39 (GeV	62.4	GeV
p	e ⁻	e ⁺	e ⁻	е ⁺	e ⁻	e ⁺	e ⁻	e ⁺
0.20399	97.4±0.6	97.5±0.2	99.6±0.1	99.5±0.0	97.2±0.5	97.2±0.3	96.3±0.1	96.2±0.1
0.212128	97.1 ± 0.6 97.4 ± 0.6	97.5 ± 0.2	99.6 ± 0.1	99.5 ± 0.0	97.2 ± 0.5	97.1 ± 0.3	96.3 ± 0.1	96.1 ± 0.1
0.220591	97.1 ± 0.6	97.4 ± 0.2	99.5 ± 0.1	99.5 ± 0.0	97.2 ± 0.5	97.1 ± 0.3	96.2 ± 0.1	96.1 ± 0.1
0.229391	97.3 ± 0.6	97.4 ± 0.2	99.5 ± 0.1	99.5 ± 0.0	97.1 ± 0.5	97.1 ± 0.3	96.2 ± 0.1	96.1 ± 0.1
0.238543	97.3 ± 0.6	97.4 ± 0.2	99.5 ± 0.1	99.5 ± 0.0	97.1 ± 0.5	97.1 ± 0.3	96.2 ± 0.1	96.0 ± 0.1
0.24806	97.3 ± 0.6	97.1 ± 0.2	99.5 ± 0.1	99.5 ± 0.0	97.1 ± 0.5	97.1 ± 0.3	96.2 ± 0.1	96.0 ± 0.1
0.257956	97.3 ± 0.6	97.4 ± 0.2	99.5 ± 0.1	99.5 ± 0.0	97.1 ± 0.5	97.0 ± 0.3	96.1±0.1	96.0 ± 0.1
0.268248	97.2 ± 0.6	97.1 ± 0.2 97.3 ± 0.2	99.5 ± 0.1	99.5 ± 0.0	97.0 ± 0.5	97.0 ± 0.3	96.1 ± 0.1	95.9 ± 0.1
0.278949	97.2 ± 0.6	97.3 ± 0.2	99.5 ± 0.1	99.5 ± 0.0	97.0 ± 0.5	97.0 ± 0.3	96.0 ± 0.1	95.9 ± 0.1
0.290078	97.2 ± 0.6	97.3 ± 0.2	99.5 ± 0.1	99.4 ± 0.0	97.0 ± 0.5	96.9 ± 0.3	96.0 ± 0.1	95.8 ± 0.1
0.301651	97.1 ± 0.6	97.2 ± 0.2	99.4 ± 0.1	99.4 ± 0.0	96.9 ± 0.5	96.9 ± 0.3	95.9 ± 0.1	95.8 ± 0.1
0.313686	97.1 ± 0.6	97.2 ± 0.2	99.4 ± 0.1	99.4 ± 0.0	96.9 ± 0.5	96.8 ± 0.3	95.9 ± 0.1	95.7 ± 0.1
0.3262	97.0 ± 0.6	97.1 ± 0.2	99.4 ± 0.1	99.4 ± 0.0	96.8 ± 0.5	96.8 ± 0.3	95.8 ± 0.1	95.7 ± 0.1
0.339214	97.0 ± 0.6	97.1 ± 0.2	99.4 ± 0.1	99.4 ± 0.0	96.8 ± 0.6	96.7 ± 0.3	95.7 ± 0.1	95.6 ± 0.1
0.352747	96.9 ± 0.6	97.0 ± 0.2	99.3±0.1	99.3±0.0	96.7 ± 0.6	96.7 ± 0.3	95.7 ± 0.1	95.5 ± 0.1
0.36682	96.9 ± 0.6	97.0 ± 0.2	99.3±0.1	99.3±0.0	96.6±0.6	96.6 ± 0.3	95.6 ± 0.1	95.4 ± 0.1
0.381455	96.8±0.6	96.9 ± 0.2	99.3±0.1	99.2±0.0	96.6±0.6	96.5 ± 0.3	95.5 ± 0.1	95.3 ± 0.1
0.396673	96.7±0.7	96.8 ± 0.2	99.2 ± 0.1	99.2±0.0	96.5 ± 0.6	96.4 ± 0.3	95.3±0.1	95.2 ± 0.1
0.412499	96.6 ± 0.7	96.7 ± 0.2	99.1±0.1	99.1±0.0	96.3±0.6	96.3±0.3	95.2 ± 0.1	95.0 ± 0.1
0.428955	96.5 ± 0.7	96.6 ± 0.2	99.1±0.2	99.0±0.0	96.2±0.6	96.2 ± 0.3	95.1 ± 0.1	94.9 ± 0.1
0.446069	96.3±0.7	96.4 ± 0.2	99.0±0.2	98.9 ± 0.0	96.1 ± 0.6	96.0±0.3	94.9 ± 0.1	94.7 ± 0.1
0.463865	96.2 ± 0.7	96.3 ± 0.2	98.8 ± 0.2	98.8±0.0	95.9 ± 0.6	95.8 ± 0.3	94.7 ± 0.1	94.5 ± 0.1
0.482371	96.0 ± 0.7	96.1 ± 0.2	98.7 ± 0.2	98.7 ± 0.0	95.7 ± 0.7	95.6 ± 0.4	94.4 ± 0.1	94.2 ± 0.1
0.501616	95.7 ± 0.8	95.9 ± 0.2	$98.5 {\pm} 0.2$	98.5 ± 0.0	95.5 ± 0.7	95.4 ± 0.4	94.1 ± 0.1	93.9 ± 0.1
0.521628	95.5 ± 0.8	95.6 ± 0.2	98.3 ± 0.2	98.3 ± 0.1	95.2 ± 0.7	95.1 ± 0.4	93.8 ± 0.1	93.6 ± 0.1
0.542438	95.1 ± 0.8	95.3 ± 0.2	98.0 ± 0.3	98.0 ± 0.1	$94.8 {\pm} 0.7$	$94.8 {\pm} 0.4$	93.3 ± 0.1	93.1 ± 0.1
0.564079	$94.8 {\pm} 0.8$	94.9 ± 0.2	97.6 ± 0.3	97.6 ± 0.1	$94.5 {\pm} 0.7$	$94.4 {\pm} 0.4$	92.9 ± 0.1	92.7 ± 0.1
0.586583	$94.4 {\pm} 0.9$	$94.5 {\pm} 0.2$	97.2 ± 0.3	97.1 ± 0.1	94.0 ± 0.8	$94.0 {\pm} 0.4$	92.3 ± 0.1	92.1 ± 0.1
0.609986	93.9 ± 0.9	94.0 ± 0.2	96.6 ± 0.4	96.5 ± 0.1	$93.5 {\pm} 0.8$	$93.5 {\pm} 0.4$	91.7 ± 0.1	91.5 ± 0.2
0.634321	93.3 ± 1.0	93.5 ± 0.3	95.9 ± 0.4	95.8 ± 0.1	93.0 ± 0.8	92.9 ± 0.5	91.1 ± 0.1	90.8 ± 0.2
0.659628	$92.8{\pm}1.0$	93.0 ± 0.3	95.1 ± 0.5	95.0 ± 0.1	92.4 ± 0.9	92.3 ± 0.5	$90.4 {\pm} 0.2$	90.1 ± 0.2
0.685944	92.2 ± 1.0	92.4 ± 0.3	$94.1 {\pm} 0.5$	94.1 ± 0.1	$91.8 {\pm} 0.9$	91.7 ± 0.5	89.7 ± 0.2	$89.4 {\pm} 0.2$
0.71331	91.6 ± 1.1	$91.8 {\pm} 0.3$	93.2 ± 0.5	93.1 ± 0.1	91.2 ± 0.9	$91.1 {\pm} 0.5$	88.9 ± 0.2	88.7 ± 0.2
0.741768	91.1 ± 1.1	91.2 ± 0.3	92.1 ± 0.6	92.1 ± 0.1	90.6 ± 0.9	$90.6 {\pm} 0.5$	88.2 ± 0.2	88.0 ± 0.2
0.771361	$90.5 {\pm} 1.1$	90.7 ± 0.3	91.1 ± 0.6	91.0 ± 0.1	$90.1 {\pm} 1.0$	90.0 ± 0.5	87.6 ± 0.2	87.3 ± 0.2
0.802135	90.0 ± 1.1	90.2 ± 0.3	90.1 ± 0.7	90.0 ± 0.1	$89.5 {\pm} 1.0$	89.5 ± 0.5	87.0 ± 0.2	86.7 ± 0.2
0.834136	$89.5 {\pm} 1.2$	89.8 ± 0.3	89.1 ± 0.7	89.0 ± 0.2	89.1 ± 1.0	89.0 ± 0.5	$86.4 {\pm} 0.2$	86.1 ± 0.2
0.867415	89.1 ± 1.2	89.3 ± 0.3	88.2 ± 0.7	$88.1 {\pm} 0.2$	$88.6 {\pm} 1.0$	$88.6 {\pm} 0.6$	85.9 ± 0.2	85.6 ± 0.2
0.902021	$88.7 {\pm} 1.2$	88.9 ± 0.3	87.3 ± 0.7	87.2 ± 0.2	$88.2 {\pm} 1.0$	88.2 ± 0.6	85.4 ± 0.2	85.1 ± 0.2
0.938007	$88.4 {\pm} 1.2$	88.6 ± 0.3	86.5 ± 0.7	$86.4 {\pm} 0.2$	87.9 ± 1.0	87.8 ± 0.6	85.0 ± 0.2	$84.7 {\pm} 0.2$
0.97543	$88.1 {\pm} 1.2$	88.3 ± 0.3	85.7 ± 0.8	85.6 ± 0.2	87.5 ± 1.0	87.5 ± 0.6	$84.6 {\pm} 0.2$	84.3 ± 0.2
1.01434	87.8 ± 1.2	88.0 ± 0.3	85.0 ± 0.8	84.9 ± 0.2	87.3 ± 1.1	87.2 ± 0.6	84.3 ± 0.2	84.0 ± 0.2
1.05481	87.5 ± 1.2	87.7 ± 0.3	$84.4 {\pm} 0.8$	84.3 ± 0.2	87.0 ± 1.1	86.9 ± 0.6	84.0 ± 0.2	83.7 ± 0.2
1.09689	87.3 ± 1.2	87.5 ± 0.3	83.8 ± 0.8	83.7 ± 0.2	86.7 ± 1.1	86.7 ± 0.6	83.7 ± 0.2	83.4 ± 0.2
1.14066	87.0 ± 1.2	87.3 ± 0.3	83.2 ± 0.8	83.1 ± 0.2	86.5 ± 1.1	$86.4 {\pm} 0.6$	$83.4 {\pm} 0.2$	83.1 ± 0.2
1.18616	86.8 ± 1.2	87.1 ± 0.3	82.7 ± 0.8	82.6 ± 0.2	86.3 ± 1.1	86.2 ± 0.6	83.2 ± 0.2	82.9 ± 0.2
1.23349	86.7 ± 1.2	86.9 ± 0.3	82.3 ± 0.8	82.2 ± 0.2	86.1 ± 1.1	86.1 ± 0.6	83.0 ± 0.2	82.7 ± 0.2
1.2827	86.5 ± 1.3	86.7 ± 0.3	$81.8 {\pm} 0.8$	81.7 ± 0.2	86.0 ± 1.1	85.9 ± 0.6	82.8 ± 0.2	82.5 ± 0.2
1.33387	86.4 ± 1.3	86.6 ± 0.3	$81.4 {\pm} 0.8$	81.3 ± 0.2	85.8 ± 1.1	85.7 ± 0.6	82.6 ± 0.2	82.3 ± 0.2
1.38709	86.2 ± 1.3	86.5 ± 0.3	81.1 ± 0.8	81.0 ± 0.2	85.7 ± 1.1	85.6 ± 0.6	82.5 ± 0.2	82.1 ± 0.2
1.44242	86.1 ± 1.3	86.3 ± 0.3	80.7 ± 0.8	80.6 ± 0.2	85.5 ± 1.1	85.5 ± 0.6	82.3 ± 0.2	82.0 ± 0.2
1.49997	86.0 ± 1.3	86.2 ± 0.3	80.4 ± 0.8	80.3 ± 0.2	85.4 ± 1.1	85.3 ± 0.6	82.2 ± 0.2	81.9 ± 0.2

Table A.6: (continued)

1.55981	85.9 ± 1.3	86.1 ± 0.3	$80.1 {\pm} 0.8$	80.0 ± 0.2	$85.3 {\pm} 1.1$	85.2 ± 0.6	82.1 ± 0.2	81.7 ± 0.2
1.62204	85.8 ± 1.3	86.0 ± 0.3	79.9 ± 0.9	79.8 ± 0.2	85.2 ± 1.1	85.1 ± 0.6	81.9 ± 0.2	81.6 ± 0.2
1.68675	85.7 ± 1.3	85.9 ± 0.3	79.6 ± 0.9	79.5 ± 0.2	85.1 ± 1.1	85.0 ± 0.6	$81.8 {\pm} 0.2$	$81.5 {\pm} 0.2$
1.75405	85.6 ± 1.3	85.8 ± 0.3	79.4 ± 0.9	79.3 ± 0.2	85.0 ± 1.1	85.0 ± 0.6	81.7 ± 0.2	$81.4 {\pm} 0.2$
1.82403	85.5 ± 1.3	85.8 ± 0.3	79.2 ± 0.9	79.1 ± 0.2	85.0 ± 1.1	84.9 ± 0.6	81.6 ± 0.2	81.3 ± 0.2
1.8968	85.4 ± 1.3	85.7 ± 0.3	79.0 ± 0.9	78.9 ± 0.2	84.9 ± 1.1	$84.8 {\pm} 0.6$	81.5 ± 0.2	81.2 ± 0.2
1.97247	85.4 ± 1.3	85.6 ± 0.3	78.8 ± 0.9	78.7 ± 0.2	$84.8 {\pm} 1.1$	$84.7 {\pm} 0.6$	81.5 ± 0.2	$81.1 {\pm} 0.2$
2.05116	85.3 ± 1.3	85.5 ± 0.3	78.6 ± 0.9	78.5 ± 0.2	$84.7 {\pm} 1.1$	84.7 ± 0.6	$81.4 {\pm} 0.2$	81.1 ± 0.2

Table A.7: Dielectron (pair) efficiencies.

M_{ee}	p_T			$\varepsilon_{ m syst}$	
		19.6 GeV	27 GeV	39 GeV	62.4 GeV
0.002	0.2	0.0 ± 0	0.0 ± 0	0.0 ± 0	0.0 ± 0
0.0055	0.2	0.0 ± 0	0.0 ± 0	0.0 ± 0	0.0±0
0.0085	0.2	0.0±0	0.0±0	0.0±0	0.0±0
0.025	0.2	19.4 ± 2.5	19.8 ± 2.5	$9.4{\pm}1.7$	$12.7{\pm}2.2$
0.055	0.2	18.8 ± 2.5	$20.4{\pm}2.6$	11.5 ± 2.1	12.3±2.1
0.115	0.2	20.3±2.7	21.9 ± 2.7	12.5 ± 2.3	$13.7{\pm}2.4$
0.22	0.2	22.7 ± 3.0	23.2 ± 2.9	14.2 ± 2.6	15.4 ± 2.7
0.34	0.2	23.8 ± 3.0	24.7 ± 3.0	$14.7{\pm}2.6$	16.4 ± 2.8
0.45	0.2	24.4 ± 3.1	25.2 ± 3.1	15.1 ± 2.7	16.7 ± 2.9
0.55	0.2	26.4 ± 3.2	27.4 ± 3.3	16.2 ± 2.9	18.3 ± 3.1
0.65	0.2	27.9 ± 3.3	29.1 ± 3.4	17.2 ± 3.0	19.4 ± 3.2
0.75	0.2	29.0 ± 3.4	30.3 ± 3.4	17.9 ± 3.1	20.1 ± 3.2
0.85	0.2	29.6 ± 3.4	31.0 ± 3.4	18.2 ± 3.1	20.7 ± 3.2
0.95	0.2	29.8 ± 3.3	31.4 ± 3.2	18.3 ± 3.0	20.7 ± 3.1
1.05	0.2	29.6 ± 3.2	31.1 ± 3.0	18.2 ± 2.8	$20.4{\pm}2.8$
1.15	0.2	29.0 ± 3.1	30.3 ± 2.7	17.9 ± 2.7	19.9 ± 2.6
1.4	0.2	26.9 ± 2.9	27.4 ± 2.3	16.8 ± 2.5	$18.3 {\pm} 2.4$
1.8	0.2	$24.2 {\pm} 2.7$	23.2 ± 2.1	15.5 ± 3.1	16.2 ± 2.5
2.2	0.2	22.7 ± 3.0	20.9 ± 2.5	14.8 ± 3.9	15.3 ± 2.9
2.6	0.2	22.4 ± 3.6	20.0 ± 3.2	14.9 ± 4.6	15.1 ± 3.3
3.0	0.2	22.7 ± 4.8	20.0 ± 4.3	15.2 ± 5.0	15.3 ± 3.9
3.35	0.2	23.1 ± 5.8	20.1 ± 5.3	15.4 ± 5.2	15.5 ± 4.1
0.002	0.7	19.3 ± 2.2	20.3 ± 2.2	11.4 ± 2.0	13.3 ± 2.1
0.0055	0.7	20.1 ± 2.3	21.0 ± 2.3	12.2 ± 2.1	14.2 ± 2.2
0.0085	0.7	$20.8 {\pm} 2.4$	21.8 ± 2.4	12.5 ± 2.1	14.8 ± 2.3
0.025	0.7	24.1 ± 2.7	25.2 ± 2.8	14.5 ± 2.5	16.8 ± 2.6
0.055	0.7	26.6 ± 3.0	27.6 ± 3.1	16.0 ± 2.8	18.5 ± 2.9
0.115	0.7	28.1 ± 3.2	29.2 ± 3.2	17.0 ± 2.9	19.6 ± 3.1
0.22	0.7	28.7 ± 3.3	29.9 ± 3.3	17.7 ± 3.0	20.1 ± 3.2
0.34	0.7	28.5 ± 3.3	29.7 ± 3.3	17.7 ± 3.0	20.0 ± 3.1
0.45	0.7	28.3 ± 3.3	29.6 ± 3.2	17.4 ± 2.9	19.8 ± 3.1
0.55	0.7	28.2 ± 3.2	29.4 ± 3.1	17.2 ± 2.9	19.5 ± 3.0
0.65	0.7	28.0 ± 3.2	29.2 ± 3.1	17.2 ± 2.8	19.3 ± 2.9
0.75	0.7	27.6 ± 3.1	$28.7{\pm}2.9$	17.1 ± 2.8	19.0 ± 2.8
0.85	0.7	27.4 ± 3.1	$28.2 {\pm} 2.8$	16.9 ± 2.8	$18.8 {\pm} 2.8$
0.95	0.7	27.2 ± 3.1	27.8 ± 2.7	16.9 ± 2.9	18.7 ± 2.8
1.05	0.7	27.1 ± 3.0	27.6 ± 2.7	17.0 ± 2.9	18.6 ± 2.7
1.15	0.7	26.9 ± 3.0	27.2 ± 2.6	17.0 ± 3.0	$18.4 {\pm} 2.7$
1.4	0.7	26.1 ± 3.0	25.9 ± 2.5	16.6 ± 3.2	17.8 ± 2.7
1.8	0.7	24.5 ± 3.1	$23.4{\pm}2.6$	15.8 ± 3.6	$16.5{\pm}2.8$
2.2	0.7	23.3 ± 3.5	21.5 ± 3.0	$15.4 {\pm} 4.1$	15.7 ± 3.1
2.6	0.7	22.9 ± 4.2	20.5 ± 3.8	15.2 ± 4.6	15.4 ± 3.5
3.0	0.7	23.0 ± 5.0	20.3 ± 4.5	$15.4 {\pm} 4.9$	15.5 ± 3.7
3.35	0.7	23.3 ± 5.3	$20.3 {\pm} 4.8$	15.6 ± 4.9	15.6 ± 3.8
0.002	1.2	18.9 ± 2.1	19.1 ± 1.8	11.7 ± 2.1	13.2 ± 1.9
0.0055	1.2	19.5 ± 2.2	19.5±1.9	$12.1{\pm}2.2$	13.6 ± 2.0
0.0085	1.2	20.4 ± 2.3	$20.7{\pm}2.0$	12.7 ± 2.3	14.3 ± 2.1

Table A.7: (continued)

0.025	1.2	23.3 ± 2.6	23.6 ± 2.3	$14.5{\pm}2.6$	16.3 ± 2.4
0.055	1.2	25.6 ± 2.8	25.9 ± 2.5	15.9 ± 2.8	17.8 ± 2.6
0.115	1.2	26.9 ± 3.0	27.2 ± 2.6	16.9 ± 3.0	$18.7 {\pm} 2.8$
0.22	1.2	27.9 ± 3.1	$28.1 {\pm} 2.7$	17.7 ± 3.2	19.5 ± 2.9
0.34	1.2	27.7 ± 3.1	27.9 ± 2.7	17.6 ± 3.2	19.2 ± 2.9
0.45	1.2	27.4 ± 3.1	27.5 ± 2.7	17.3 ± 3.1	18.9 ± 2.8
0.55	1.2	27.1 ± 3.1	27.1 ± 2.7	17.0 ± 3.1	18.6 ± 2.8
0.65	1.2	26.7 ± 3.1	26.7 ± 2.7	16.7 ± 3.1	18.3 ± 2.8
0.75	1.2	26.3 ± 3.1	26.2 ± 2.7	16.5 ± 3.2	18.0 ± 2.8
0.85	1.2	25.9 ± 3.1	25.8 ± 2.7	16.3 ± 3.2	17.7 ± 2.8
0.95	1.2	25.5 ± 3.1	25.2±2.7	16.1 ± 3.3	17.4 ± 2.9
1.05	1.2	25.3±3.2	24.8 ± 2.8	16.1 ± 3.4	17.3±2.9
1.15	1.2	25.1 ± 3.3	24.5 ± 2.9	16.1±3.6	17.1 ± 3.0
1.4	1.2	25.1 ± 3.6	24.2 ± 3.2	16.2±3.8	17.1 ± 3.2
1.8	1.2	24.8 ± 4.1	23.4 ± 3.7	16.2 ± 4.1	16.9 ± 3.4
2.2 2.6	1.2	24.0 ± 4.4	22.2 ± 4.0	16.0 ± 4.3	16.3 ± 3.4
2.6 3.0	1.2 1.2	23.5 ± 4.5 23.3 ± 4.3	21.2 ± 4.0 20.6 ± 3.7	15.8 ± 4.3 15.7 ± 4.2	15.9 ± 3.3 15.7 ± 3.2
3.35	1.2	23.3 ± 4.3 23.3 ± 4.2	20.0 ± 3.7 20.4 ± 3.6	15.7 ± 4.2 15.8 ± 4.1	15.7 ± 3.2 15.7 ± 3.1
0.002	1.2	17.3 ± 2.5	16.4 ± 2.3	13.8 ± 4.1 11.5 ± 2.8	13.7 ± 3.1 11.9 ± 2.2
0.002	1.9	17.3 ± 2.3 18.0 ± 2.7	17.2 ± 2.5	11.3 ± 2.6 12.1 ± 2.9	11.9 ± 2.2 12.6 ± 2.4
0.0035	1.9	18.8 ± 2.8	17.2 ± 2.5 17.8 ± 2.5	12.4 ± 3.0	12.0 ± 2.4 12.9 ± 2.4
0.0005	1.9	21.5 ± 3.2	20.5 ± 2.9	14.2 ± 3.4	15.0 ± 2.8
0.055	1.9	23.6 ± 3.5	22.4 ± 3.2	15.6 ± 3.8	16.4 ± 3.1
0.115	1.9	24.8 ± 3.7	23.6 ± 3.4	16.5 ± 4.0	17.3 ± 3.2
0.22	1.9	25.9 ± 3.9	24.7 ± 3.5	17.3 ± 4.2	18.1 ± 3.4
0.34	1.9	26.1 ± 3.9	24.8±3.6	17.3 ± 4.2	18.0 ± 3.4
0.45	1.9	25.9 ± 3.9	24.6 ± 3.6	17.1 ± 4.2	17.9 ± 3.4
0.55	1.9	25.7 ± 3.9	24.4 ± 3.6	16.7 ± 4.1	17.6 ± 3.4
0.65	1.9	25.6 ± 3.9	24.2 ± 3.6	$16.5{\pm}4.1$	17.5 ± 3.4
0.75	1.9	25.5 ± 4.0	24.2 ± 3.6	16.3 ± 4.0	17.4 ± 3.4
0.85	1.9	25.4 ± 4.0	24.0 ± 3.7	$16.2 {\pm} 4.0$	17.2 ± 3.4
0.95	1.9	25.2 ± 4.1	23.8 ± 3.7	$16.1 {\pm} 4.0$	17.1 ± 3.4
1.05	1.9	25.0 ± 4.1	23.6 ± 3.8	16.0 ± 4.0	17.0 ± 3.3
1.15	1.9	24.9 ± 4.1	23.4 ± 3.8	16.0 ± 4.0	16.9 ± 3.3
1.4	1.9	$24.7 {\pm} 4.2$	23.2 ± 3.8	16.0 ± 3.9	16.8 ± 3.3
1.8	1.9	24.6 ± 4.1	22.9 ± 3.7	16.2 ± 3.8	16.7 ± 3.1
2.2	1.9	24.5 ± 3.9	22.5 ± 3.4	16.3 ± 3.6	16.6 ± 2.9
2.6	1.9	24.0 ± 3.7	21.7 ± 3.1	16.2 ± 3.4	16.3 ± 2.7
3.0	1.9	23.7 ± 3.6	21.0 ± 3.0	16.1±3.5	16.0 ± 2.7
3.35	1.9	23.5 ± 3.7	20.6 ± 3.0	16.1 ± 3.5	15.9 ± 2.7
0.002	3.1	17.0 ± 2.6	15.3 ± 2.2	11.9 ± 2.5	11.8 ± 2.0
0.0055	3.1	17.8 ± 2.7	16.1 ± 2.3	12.4 ± 2.5	12.4 ± 2.0
0.0085 0.025	3.1 3.1	$18.4{\pm}2.7$ $21.1{\pm}3.1$	$16.8{\pm}2.4$ $19.1{\pm}2.7$	12.8 ± 2.6 14.7 ± 3.0	$12.9{\pm}2.1$ $14.7{\pm}2.4$
0.025	3.1	21.1 ± 3.1 23.1 ± 3.4	19.1 ± 2.7 20.9 ± 2.9	14.7 ± 3.0 16.1 ± 3.3	14.7 ± 2.4 16.1 ± 2.6
0.033	3.1	23.1 ± 3.4 24.2 ± 3.6	20.9 ± 2.9 21.8 ± 3.1	16.1 ± 3.5 16.8 ± 3.5	16.1 ± 2.0 16.9 ± 2.8
0.22	3.1	25.2 ± 3.8	22.8 ± 3.2	17.5 ± 3.6	17.6 ± 2.9
0.34	3.1	25.6 ± 3.8	23.1 ± 3.2	17.7 ± 3.6	17.8 ± 2.9
0.45	3.1	25.6 ± 3.8	23.1 ± 3.2 23.1 ± 3.2	17.7 ± 3.6	17.8 ± 2.9
0.55	3.1	25.6 ± 3.8	23.1 ± 3.2	17.5 ± 3.6	17.7 ± 2.9
0.65	3.1	25.5 ± 3.8	23.0 ± 3.2	17.3 ± 3.5	17.5 ± 2.9
0.75	3.1	25.3 ± 3.8	22.9 ± 3.2	17.1 ± 3.5	17.4 ± 2.8
0.85	3.1	25.2 ± 3.8	22.7 ± 3.2	16.8 ± 3.4	17.3 ± 2.8
0.95	3.1	25.1 ± 3.7	22.7 ± 3.1	16.7 ± 3.4	17.2 ± 2.8
1.05	3.1	25.1 ± 3.7	22.7 ± 3.1	16.6 ± 3.3	17.1 ± 2.8
1.15	3.1	25.1 ± 3.7	22.6 ± 3.1	16.4 ± 3.3	17.0 ± 2.8
1.4	3.1	24.9 ± 3.7	22.4 ± 3.0	16.3 ± 3.2	16.9 ± 2.7
1.8	3.1	24.7 ± 3.6	22.2 ± 2.9	16.2 ± 3.1	16.7 ± 2.7
2.2	3.1	24.5 ± 3.5	22.0 ± 2.9	16.2 ± 3.1	16.6 ± 2.6
2.6	3.1	24.3 ± 3.5	21.8±2.8	16.3 ± 3.0	16.5 ± 2.5
3.0	3.1	23.9 ± 3.5	21.4 ± 2.8	16.3 ± 3.0	16.3 ± 2.5

Table A.7: (continued)

3.35	3.1	23.6 ± 3.5	21.0 ± 2.8	16.3 ± 3.0	16.2 ± 2.5
5.55	5.1	Z3.0±3.3	21.0±2.0	10.5 ± 5.0	10.2_2.5

A.9 Efficiency Figures

Figure A.16 Overview of calculated electron efficiencies at $\sqrt{s_{NN}}$ = 19.6 GeV (left column) & 27 GeV (right column). For a detailed description see Figure 3.4.

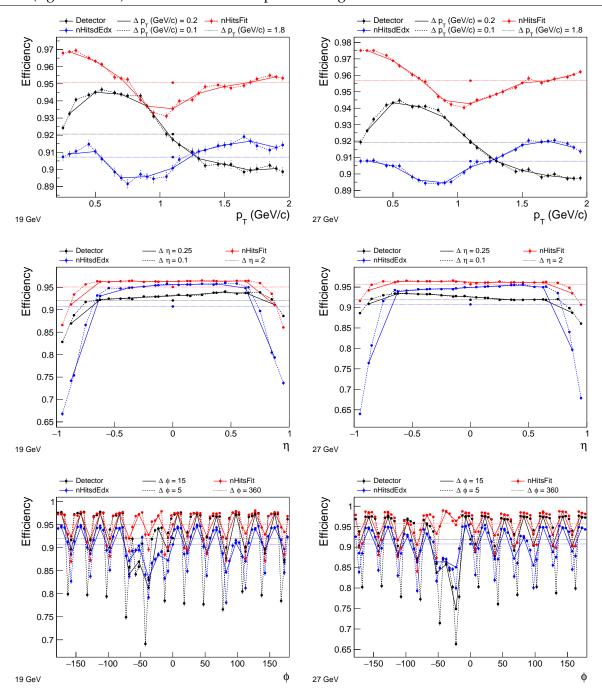


Figure A.17 Overview of calculated positron efficiencies at $\sqrt{s_{NN}}$ = 19.6 GeV (left column) & 27 GeV (right column). For a detailed description see Figure 3.4.

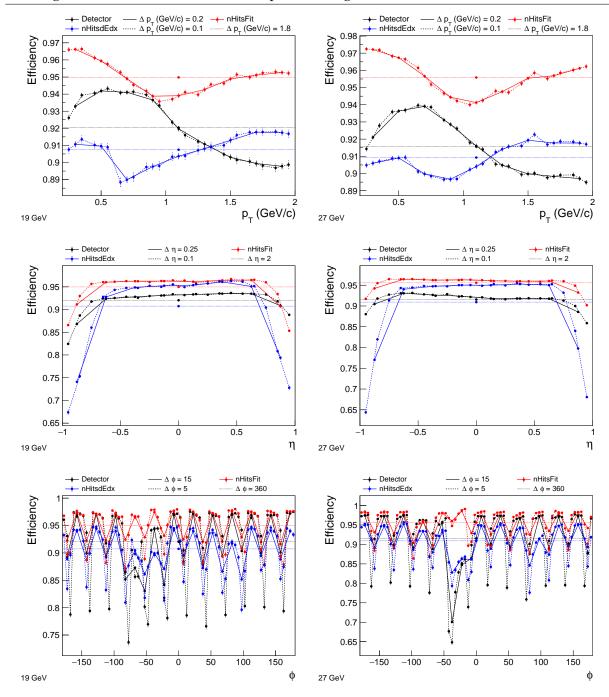
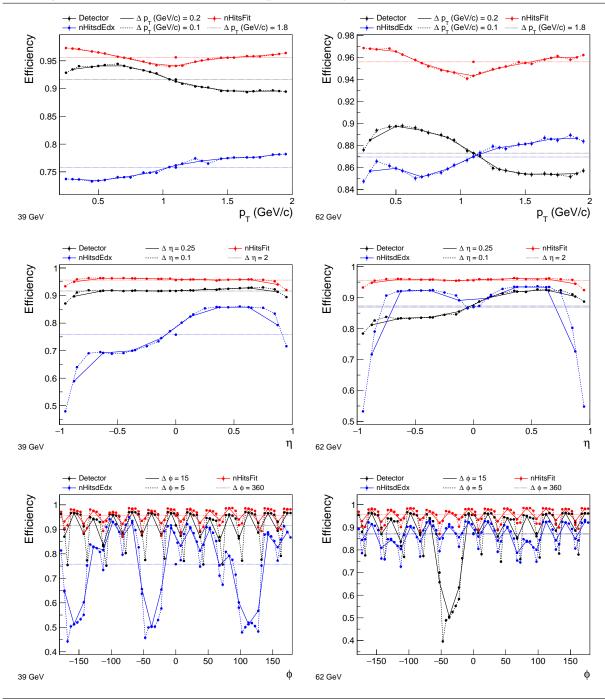


Figure A.18 Overview of calculated positron efficiencies at $\sqrt{s_{NN}}$ = 39 GeV (left column) & 62.4 GeV (right column). For a detailed description see Figure 3.4.



Appendix B

Software

B.1 StV0TofCorrection: Examples

1. Kaon from $\Omega^- \to \Lambda K^-$ (one step case)

```
// init once
StV0TofCorrection *v0tofcorr;
v0tofcorr = new StV0TofCorrection();
// event vertex
StThreeVectorD v0;
// --- for each omega candidate -----
// kaon helix
StPhysicalHelixD hel;
// original kaon TOF
Float_t Tof;
// corrected beta set to original
Float_t bCorr = BetaOrig;
// decay vertex of omega
StThreeVectorD v_om;
// kaon TOF hit
StThreeVectorD vtof;
// 4-mom vectors of omega
StLorentzVector t_om;
// kaon momentum
Float_t mom;
// correct beta if TOF hit exists
if ( tofhit ) {
 v0tofcorr->setVectors3D(v0)(v_om)(vtof);
  v0tofcorr->setMotherTracks(t_om);
  // using default cut on m2(K-)
  if (v0tofcorr->correctBeta(hel,Tof,bCorr,mom,1)) {
   // fill ntuple, histos etc.
  v0tofcorr->clearContainers();
```

2. Proton from $\Omega^- \to \Lambda K^- \to p\pi^- K^-$ (two step case)

```
// init once
StV0TofCorrection *v0tofcorr;
v0tofcorr = new StV0TofCorrection();
// event vertex
StThreeVectorD v0;
// --- for each omega candidate ------
// proton helix
```

```
StPhysicalHelixD helix;
// original proton TOF
Float_t Tof;
// corrected beta set to original
Float_t BetaCorr = BetaOrig;
// decay vertices of omega & lambda (ordering!)
StThreeVectorD v_om, v_lam;
// proton TOF hit
StThreeVectorD vtof;
// 4-mom vectors of omega & lambda (ordering!)
StLorentzVector t_om, t_lam;
// correct beta if TOF hit exists
if ( tofhit ) {
  v0tofcorr->setVectors3D(v0)(v_om)(v_lam)(vtof);
  v0tofcorr->setMotherTracks(t_om)(t_lam);
  v0tofcorr->correctBeta(helix, Tof, BetaCorr);
  v0tofcorr->clearContainers();
// calc new proton mass m2 by using BetaCorr
Float_t Mass2Corr = p*p*(1./(BetaCorr*BetaCorr)-1.);
// cut on new proton mass
if ( Mass2Corr > ... && Mass2Corr < ... ) {</pre>
 // fill ntuple, histos etc.
```

B.2 StBadRdos Database Files

database/dbfiles/database 11GeV 2010

```
11148001 3 17.01 23.02 23.08

11151010 4 11.10 17.01 23.02 23.08

11151028 3 17.01 23.02 23.08

11151040 4 17.01 21.11 23.02 23.08

11151080 5 01.07 17.01 21.11 23.02 23.08

11152053 6 01.07 07.05 17.01 21.11 23.02 23.08

11153012 7 01.07 01.09 07.05 17.01 21.11 23.02 23.08

11156032 8 01.07 01.09 07.05 09.03 17.01 21.11 23.02 23.08

11158011 9 01.07 01.09 07.05 09.03 11.01 17.01 21.11 23.02 23.08
```

database/dbfiles/database_19GeV_2011

```
12112008 3 01.06 19.06 19.07

12112060 4 01.06 19.01 19.06 19.07

12119001 5 01.06 05.11 19.01 19.06 19.07

12119008 6 01.06 03.07 05.11 19.01 19.06 19.07

12119049 4 01.06 19.01 19.06 19.07
```

database/dbfiles/database 200GeV 2010

```
11002120 1 23.08

11003094 2 23.07 23.08

11003101 4 23.07 23.08 23.09 23.10

11004007 5 23.02 23.07 23.08 23.09 23.10

11004040 2 23.02 23.08

11011017 3 09.05 23.02 23.08

11014041 2 23.02 23.08

11021015 8 19.07 19.08 19.09 19.10 19.11 19.12 23.02 23.08

11021034 3 19.09 23.02 23.08
```

```
11028018 2 23.02 23.08

11028114 3 23.01 23.02 23.08

11041021 4 17.01 23.01 23.02 23.08

11044005 3 17.01 23.02 23.08
```

database/dbfiles/database_200GeV_2011

database/dbfiles/database_27GeV_2011

```
12172013 6 01.06 03.07 03.08 05.09 19.06 19.07
12174055 12 01.06 03.07 03.08 05.01 05.02 05.03 05.04 05.05 05.06 05.09 ←
19.06 19.07
12174056 6 01.06 03.07 03.08 05.09 19.06 19.07
```

database/dbfiles/database_39GeV_2010

```
11099002 3 17.01 23.02 23.08
11101092 4 15.12 17.01 23.02 23.08
11102073 5 15.12 17.01 17.05 23.02 23.08
11103025 6 05.09 15.12 17.01 17.05 23.02 23.08
11105011 3 17.01 23.02 23.08
11105018 4 15.12 17.01 23.02 23.08
11105037 5 01.04 15.12 17.01 23.02 23.08
11106008 6 01.04 03.09 15.12 17.01 23.02 23.08
11106024 7 01.04 03.09 05.09 15.12 17.01 23.02 23.08
11106039 8 01.04 01.12 03.09 05.09 15.12 17.01 23.02 23.08
11108019 9 01.04 01.12 03.09 05.09 09.07 15.12 17.01 23.02 23.08
11108029 10 01.04 01.12 03.09 05.09 09.07 13.12 15.12 17.01 23.02 23.08
11108050 9 01.04 01.12 05.09 09.07 13.12 15.12 17.01 23.02 23.08
11108075 8 01.04 01.12 05.09 13.12 15.12 17.01 23.02 23.08
11109019 9 01.04 01.12 03.09 05.09 13.12 15.12 17.01 23.02 23.08
11109088 12 01.04 01.07 01.12 03.03 03.09 05.09 13.12 15.12 17.01 19.09
   23.02 23.08
11109114 11 01.04 01.12 03.03 03.09 05.09 13.12 15.12 17.01 19.09 23.02
   23.08
11110025 10 01.04 01.12 03.09 05.09 13.12 15.12 17.01 19.09 23.02 23.08
```

database/dbfiles/database_62GeV_2010

```
11078018 3 17.01 23.02 23.08

11092009 4 15.12 17.01 23.02 23.08

11092095 5 01.04 15.12 17.01 23.02 23.08

11094007 8 01.04 03.03 03.09 05.09 15.12 17.01 23.02 23.08

11095022 3 17.01 23.02 23.08
```

database/dbfiles/database_7GeV_2010

```
11114040 4 17.01 19.09 23.02 23.08
11114055 5 03.06 17.01 19.09 23.02 23.08
11116017 4 17.01 19.09 23.02 23.08
11117024 5 03.06 17.01 19.09 23.02 23.08
11118036 6 03.06 09.07 17.01 19.09 23.02 23.08
11119043 7 03.06 05.05 09.07 17.01 19.09 23.02 23.08
11121054 8 03.03 03.06 05.05 09.07 17.01 19.09 23.02 23.08
11122037 9 03.03 03.06 05.05 09.07 11.07 17.01 19.09 23.02 23.08
11122111 10 01.12 03.03 03.06 05.05 09.07 11.07 17.01 19.09 23.02 23.08
11125066 4 01.12 17.01 23.02 23.08
11130034 5 01.12 17.01 17.05 23.02 23.08
11133060 6 01.07 01.12 17.01 17.05 23.02 23.08
11134053 5 01.07 01.12 17.01 23.02 23.08
11136090 6 01.07 01.12 17.01 19.06 23.02 23.08
11136157 10 01.07 01.12 13.09 13.10 13.11 13.12 17.01 19.06 23.02 23.08
11137107 11 01.07 01.12 07.05 13.09 13.10 13.11 13.12 17.01 19.06 23.02
   23.08
11138036 12 01.12 09.10 13.09 13.10 13.11 13.12 17.01 17.05 19.06 23.02 \leftrightarrow
   23.08 23.09
11139051 4 01.12 17.01 23.02 23.08
11146054 3 17.01 23.02 23.08
```

B.3 STAR CVS to git Migration

configureHttpProxy.sh

```
#!/bin/bash
cfgfile=$HOME/gerrit_review/etc/gerrit.config
git config --file $cfgfile auth.type HTTP
git config --file $cfgfile --unset auth.httpHeader
git config --file $cfgfile gerrit.canonicalWebUrl http://gerrit4star.the- \( \to \)
huck.com/
git config --file $cfgfile httpd.listenUrl proxy-http://127.0.0.1:8081/
$HOME/gerrit_review/bin/gerrit.sh start
```

configureCGit.sh

```
#!/bin/bash
cfgfile=$HOME/gerrit_review/etc/gerrit.config
cgipath=/home/patrick/public/cgit4star.the-huck.com/public/cgit.cgi
git config --file $cfgfile gitweb.cgi $cgipath
git config --file $cfgfile gitweb.url http://cgit4star.the-huck.com/
git config --file $cfgfile gitweb.type cgit
$HOME/gerrit_review/bin/gerrit.sh restart
```

convertStarCVS.sh

```
#!/bin/bash
#set -xv
```

```
# variables
#-----
workdir="/star/institutions/lbl/huck/star cvs2git"
qitdir="$workdir/bare"
if [ ! -d $gitdir ]; then mkdir -v $gitdir; fi
cvs2svndir="$workdir/cvs2svn-2.4.0"
optfile="$workdir/git4star/my.cvs2git.options"
tmpopt="$workdir/tmp.cvs2git.options"
splitup="StRoot StarVMC StDb StarDb asps kumacs pams QtRoot"
skip="scripts online Cons conf root root3 group cgi CVSROOT"
skip=$skip" OnlTools root5 .backup offline obsolete Dsv HISTORY"
list='find $CVSROOT -noleaf -maxdepth 1 -type d ! -name repository'
#-----
#-----
StrIsInArr() {
 for i in $2; do
  if [[ "$1" == *"$i"* ]]; then return 0; fi
 done
 return 1
printRepo() {
 echo "current repo: $1"
 }
runCvs2Git() {
 sed "s:STARCVS-REPO:$1:" $optfile >> $tmpopt
 cd $cvs2svndir
 cvs2git --options=$tmpopt
 rm $tmpopt
}
genGitRepo() {
 rm -rfv $1; mkdir -pv $1; cd $1
 git init --bare
 tmpdir=$cvs2svndir/cvs2svn-tmp
 cat $tmpdir/git-blob.dat $tmpdir/git-dump.dat | git fast-import
 rm -rfv $tmpdir
 python $cvs2svndir/contrib/git-move-refs.py
 git gc --prune=now
convertRepo() {
 repo=$1
 printRepo $repo
 runCvs2Git $repo
 repodir=$2
 repobase='basename $repo'
 repocat=$repodir
```

```
if [ ! -z "$repodir"]; then repodir=$repodir"-"; fi
 reponame=$repodir$repobase.git
 outdir="$gitdir/$reponame"
 echo $outdir
 genGitRepo $outdir
 cfgfile="$outdir/config"
 echo "[gitweb]" >> $cfgfile
 echo "
        owner = STAR" >> $cfgfile
description = $repodir$repobase" >> $cfgfile
 echo "
 echo "
              category = $repocat" >> $cfgfile
#-----
# loop repos
# ($(top, sub) repo have to hold absolute urls to afs)
for toprepo in $list; do
 if StrIsInArr $toprepo "$skip"; then continue; fi # skip dirs
 if StrIsInArr $toprepo "$splitup"; then # descent into dir
   toprepobase='basename $toprepo'
   sublist='find toprepo -noleaf -maxdepth 1 -type d ! -name <math>\leftarrow
       $toprepobase '
   for subrepo in $sublist; do # loop sub-repositories
     convertRepo $subrepo $toprepobase
 else # convert top-repository
   convertRepo $toprepo
 fi
done
```

createGerritProjects.sh

```
#!/bin/bash
workdir="/star/institutions/lbl/huck/star_cvs2git"
gitdir="$workdir/bare"
tmpCloneDir="$workdir/tmp"
mkdir $tmpCloneDir
for dir in 'ls $workdir/bare'; do
 cd $workdir
 proj=${dir%.git}
  # create, git clone and push project
 ssh gerrit4star gerrit create-project --name $proj
  git clone $gitdir/$proj.git $tmpCloneDir/$proj
 cd $tmpCloneDir/$proj
 git push ssh://gerrit4star/$proj *:*
  # set require sign-off and change-id
  ssh gerrit4star gerrit set-project $proj --so --id
done
rm -rf $tmpCloneDir
```

writeManifest.sh

```
#!/bin/bash
workdir="/star/institutions/lbl/huck/star_cvs2git"
gitdir="$workdir/bare"
manifest=default.xml
echo '<?xml version="1.0" encoding="UTF-8"?>' > $manifest
echo '<manifest>' >> $manifest
echo ' <remote name="gerrit4star"' >> $manifest
echo ' fetch="ssh://gerrit4star"' >> $manifest
echo ' review="http://gerrit4star.the-huck.com" />' >> $manifest
echo ' <default revision="refs/heads/master"' >> $manifest
         remote="gerrit4star"' >> $manifest
echo '
          sync-j="4" />' >> $manifest
for repo in 'ls $gitdir'; do
 path='echo ${repo%.git} | sed 's:-:/:''
  echo '
           fert name="'${repo%.git}'" path="'${path}'"/>' >> ←
     $manifest
done
echo '</manifest>' >> $manifest
```

B.4 Screenshots of Gerrit and CGit for STAR



Figure B.2 gerrit4star change view

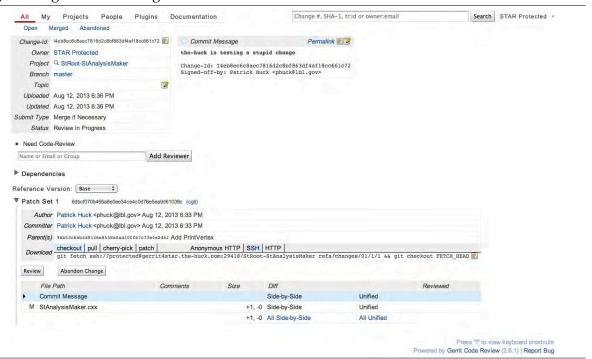
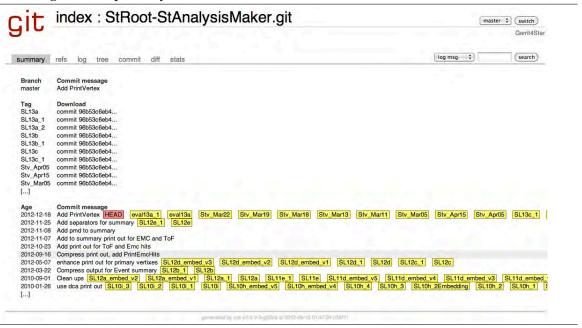


Figure B.3 cgit4star repository view



B.5 ckon - Typical Directory Structure

```
StRoot/
ElectronPid/
BetaPanels.cxx
BetaPanels.h
PureSampleAnalysis.cxx
PureSampleAnalysis.h
SigmaElFitsMaker.cxx
SigmaElFitsMaker.h
```

```
SigmaElFitsPlotter.cxx
    SigmaElFitsPlotter.h
    SigmaElFitsUtils.cxx
    SigmaElFitsUtils.h
    programs/
        README
       beta3sig.cc
       dedxCut.cc
       nsigparamsGP.cc
       pureSamp.cc
St.BadRdosDb/
   StBadRdosDb.cxx
    StBadRdosDb.h
    database/
       dbfiles
       genAll.sh
       genBadRdosDb.pl
   macros/
       testStBadRdosDb.C
YamlCfgReader/
    YamlCfgReader.cxx
    YamlCfgReader.h
    config.yml
```

B.6 ccsgp: Installation and Implementation

NOTE

This is a reprint of the online documentation in the version at the time of this thesis. Refer to the public auto-generated version at http://ccsgp-get-started.readthedocs.org/en/latest/.

ccsgp_get_started requires gnuplot, git, virtualenv and optionally hdf5. Install these dependencies via:

```
sudo port install gnuplot git-core py27-virtualenv [hdf5] # MacPorts
sudo apt-get install gnuplot git python-virtualenv [libhdf5-dev] # Debian
```

hdf5 is optional but if you'd like to save your image data to HDF5, you'll have to install it. Next, clone the <code>ccsgp_get_started</code> git repository, init the virtualenv, activate it and install all requirements:

Every time you start in a new terminal you have to activate the correct python environment by sourcing <code>env/bin/activate</code> again or instead use <code>env/bin/python</code> directly! The h5py package is currently omitted from the requirements. If you want to use it, uncomment the h5py requirement in "requirements.txt" and rerun <code>pip install -r requirements.txt</code>. If you intend to run the examples, clone the test data repository (somewhere outside of <code>ccsgp_get_started repository</code>) and <code>symlink pyanaDir</code> to the <code>ccsgp_get_started_data</code> directory:

```
git clone http://gitlab.the-huck.com/github/ccsgp_get_started_data.git
cd ccsgp_get_started/
ln -s <path/to/ccsgp_get_started_data> pyanaDir
```

pyana.aux.utils.checkSymLink checks for the pyanaDir symbolic link and the code won't run without it. Hence you need to generate a symlink called pyanaDir either to ccs gp_get_started_data or your own input/output directory (preferably separated from the code repository). Pull in public STAR dielectron data into a new branch to use gp_xfac and gp_panel:

```
cd <path/to/ccsgp_get_started_data>
git remote add dielec_public \
   http://gitlab.the-huck.com/star/dielectron_data_public.git
git checkout -b star_dielec
git pull dielec_public master
```

If you are part of the STAR collaboration you can also pull in the protected STAR dielectron data to include it in <code>gp_panel</code>:

```
git remote add dielec_protect \
   http://cgit.the-huck.com/dielectron_data_protected
git pull -Xtheirs dielec_protect master # STAR protected creds
```

The examples are based on a dataset of World Bank Indicators. See the "genExDat.sh" script in the same directory on how I extracted the data into the correct format for ccsgp. To generate all example plots based on ccsgp_get_started_data you can run: python -m pyana. Alternatively, you can run a specific module, for instance, and this way plot specific country initials:

```
python -m pyana.examples.gp_datdir [--log] <initial> <topN>
```

Use pdfnup to put multiple plots on one page. To start on your own read the documentation below or the source code and use one of the examples as a template.

pyana.examples.gp_datdir.gp_datdir(initial, topN)

example for plotting from a text file via numpy.loadtxt

Procedure

- prepare input/output directories
- load the data into an OrderedDict() [adjust axes units]
- sort countries from highest to lowest population
- select the <topN> most populated countries
- call ccsgp.make_plot with data from previous step
- See python -m pyana.examples.gp_datdir -h for help

Parameters

- **initial** (*str*) country initial
- topN (int) number of most populated countries to plot

Variables

- inDir—input directory according to package structure and initial
- outDir output directory according to package structure
- data Ordered Dict with datasets to plot as separate keys
- file data input file for specific country, format: [x y] OR [x y dx dy]
- **country** country, filename stem of input file

- file_url absolute url to input file
- nSets number of datasets

pyana.examples.gp_lcltpt.gp_lcltpt()

example plot to display linecolors, linetypes and pointtypes

pyana.examples.gp_xfac.gp_xfac()

example using QM12 enhancement factors

Procedure

- uses gpcalls kwarg to reset xtics
- numpy.loadtxt needs reshaping for input files with only one datapoint
- according poster presentations see QM12 and NSD review

Variables

- **key**—translates filename into legend/key label
- shift—slightly shift selected data points

pyana.examples.gp_panel.gp_panel(version, skip)

example for a panel plot using QM12 data (see gp_xfac)

Parameters

version (*str*) — plot version / input subdir name

pyana.examples.gp_stack.gp_stack(version, energies, inclMed, inclFits)

example for a plot w/ stacked graphs using QM12 data (see gp_panel)

Procedure

- omit keys from the legend
- manually add legend entries
- automatically plot arrows for error bars larger than data point value

Parameters

version (*str*) — plot version / input subdir name

pyana.examples.gp_rdiff.gp_rdiff(vers, nomed, noxe, diffRel, divdNdy)

example for ratio or difference plots using QM12 data (see gp_panel)

Procedure

- uses uncertainties package for easier error propagation and rebinning
- statistical error for medium = 0
- statistical error for cocktail ~ 0
- statistical error bar on data stays the same for diff
- implement ratio
- adjust statistical error on data for ratio
- adjust name and ylabel for ratio

Parameters

- **vers** (*str*) plot version
- **nomed** (*bool*) don't plot medium
- **noxe** (*bool*) don't plot x-errors
- **diffRel** (bool) plot ratio
- **divdNdy** (*bool*) divide by dNdy

pyana.examples.gp_ptspec.gp_ptspec()

another example for a 2D-panel plot (see gp_panel)

pyana.ccsgp.ccsgp.make_plot(data, properties, titles, **kwargs)

main function to generate a 1D plot

Procedure

- each dataset is represented by a numpy array consisting of data points in the format "[x, y, dx, dy1, dy2]", dy1 = statistical error, dy2 = systematic uncertainty
- for symbol numbers to use in labels see http://bit.ly/1erBgIk
- lines format: <x/y>=<value>: <gnuplot options>, horizontal = (along) x, vertical = (along) y
- labels format: label text: [x, y, abs.placement true/false]
- arrows format: [<x0>, <y0>], [<x1>, <y1>], <qnuplot props>

Parameters

- data (list) datasets
- **properties** (*list*) gnuplot property strings for each dataset (lc, lw, pt ...)
- **titles** (*list*) legend/key titles for each dataset
- **name** (*str*) basename of output files
- **title** (*str*) image title
- **debug** (*bool*) flag to switch to debug/verbose mode
- **key** (*list*) legend/key options to be applied on top of default_key
- **xlabel** (*str*) label for x-axis
- **ylabel** (*str*) label for y-axis
- **xr** (*list*) x-axis range
- **yr** (*list*) y-axis range
- **xlog** (*bool*) make x-axis logarithmic
- ylog (bool) make y-axis logarithmic
- **lines** (*dict*) vertical and horizontal lines
- **arrows** (*list*) arrows
- **labels** (*dict*) labels
- **Imargin** (*float*) defines left margin size (relative to screen)
- bmargin (*float*) defines bottom margin size
- rmargin (float) defines right margin size
- **tmargin** (*float*) defines top margin size
- **arrow_offset** (*float*) offset from data point for special error bars (see gp_panel)
- **arrow_length** (*float*) length of arrow from data point towards zero for special error bars (see gp_panel)
- arrow_bar (float) width of vertical bar at end of special error bars (see gp_panel)
- **gpcalls** (*list*) execute arbitrary gnuplot set commands

Returns

MyPlot

pyana.ccsgp.ccsgp.repeat_plot(plt, name, **kwargs)

repeat a plot with different properties (kwargs see make_plot)

Parameters

• **plt** (*MyPlot*) — plot to repeat

• name (str) — basename of new output file(s)

Returns

plt

pyana.ccsgp.ccsgp.make_panel(dpt_dict, **kwargs)

make a panel plot

Parameters

- name/title/debug are global options used once to initialize the multiplot
- x,yr/x,ylog/lines/labels/gpcalls are applied on each subplot
- same for "r,l,b,tmargin" where "r,lmargin" will be reset to allow for merged yaxes
- **key/ylabel** are only plotted in first subplot
- xlabel is centered over entire panel
- layout <cols>x<rows>, defaults to horizontal panel if omitted
- key_subplot_id sets the desired subplot to put the key in
- **dpt_dict** (*dict*)—OrderedDict with subplot titles as keys and lists of make_p lot "data/properties/titles" as values:

```
OrderedDict('subplot-title': [data, properties, titles], ...)
```

MyPlot Base Class

MyPlot is the base class of cosgp for basic gnuplot setup (bars, grid, title, key, terminal, multiplot) also providing utility functions for general plotting.

Parameters

- **title** (*str*) image title
- **name** (*str*) basename used for output files
- **debug** (*bool*) debug flag for verbose gnuplot output

Variables

- name basename for output files
- **epsname** basename + .*eps*
- **gp**—Gnuplot.Gnuplot instance
- **nPanels** number of panels in a multiplot
- **nVertLines** number of vertical lines
- nLabels number of labels
- nArrows number of arrows
- axisLog flags for logarithmic axes
- axisRange axis range for respective axis (set in setAxisRange)

_ascii()

write ascii file(s) w/ data contained in plot

_clamp(val, minimum=0, maximum=255)

convenience function to clamp number into min..max range

_colorscale(hexstr, scalefactor=1.4)

Scales a hex string by "scalefactor". Returns scaled hex string.

Notes

• taken from T. Burgess [291]

- To darken the color, use a float value between 0 and 1.
- To brighten the color, use a float value greater than 1.

Examples

```
>>> colorscale("#DF3C3C", .5)
#6F1E1E
>>> colorscale("#52D24F", 1.6)
#83FF7E
>>> colorscale("#4F75D2", 1)
#4F75D2
```

_convert()

convert eps/ps original into pdf, png and jpg format

_get_style_mod_prop(prop)

get style and modified property string

_hardcopy()

generate eps, convert to other formats and write data to hdf5

_hdf5()

write data contained in plot to HDF5 file

Notes

- easy numpy import \rightarrow (savetxt) \rightarrow gnuplot
- export to ROOT objects
- h5py howto (see http://www.h5py.org/docs/intro/quick.html)

Raises

ImportError

_plot_errs(data)

determine whether to plot primary errors separately and plot errorbars if data has more than two columns which are not all zero

Parameters

```
data (numpy.array) — one dataset
```

Variables

error_sums — sum of x and y errors

Returns

True or False

_plot_syserrs(data)

determine whether to plot secondary errors

Parameters

data (numpy.array) — one dataset

Returns

True or False

_prettify(str)

prettify string, remove special symbols

_setter(list)

convenience function to set a list of gnuplot options

Parameters

list (*list*) — list of strings given to gnuplot's set command

_sum_errs(data, i)

convenience function to calculate sum of i-th column

_using(data, prop=None)

determine string with columns to use

Parameters

- data (numpy.array) one dataset
- **prop** (*str*) property string of a dataset

Returns

1:2:3, 1:2:4 or 1:2:3:4

_with_errs(data, prop)

generate special property string for primary errors

Notes

- currently error bars are drawn in black
- use same linewidth as for points
- TODO: give user the option to draw error bars in lighter color according to the respective data points

Parameters

- data (numpy.array) one dataset
- **prop** (*str*) property string of a dataset

Returns

property string for primary errors

_with_main(prop)

get the correct property string for main data

_with_syserrs(prop)

generate special property string for secondary errors

Notes

- draw box in lighter color than point/line color
- does not support integer line colors, only hex

Parameters

prop (*str*) — property string of a dataset

Returns

property string for secondary errors

addHorizontalLine(y, opts)

draw horizontal line

Parameters

- y (*float*) y-position
- **opts** (*str*) line draw options

initData(data, properties, titles, subplot_title=None)

initialize the data

Notes

• all lists given as parameters must have the same length.

- each data set is drawn twice to allow for different colors for the errorbars
- error bars use the same linewidth as data points and line color black
- use *boxwidth 0.03 absolute* in gp_calls to set the width of the uncertainty boxes
- use alternative gnuplot style if "properties" contains a style specification in the form "with <style>" and if the style is in ccsgp.config.supported_styles (style specification has to be at the beginning of the property string!)

Parameters

- data (list of numpy arrays) data points w/ format [x, y, dx, dy] for each dataset
- **properties** (*list of str*) plot properties for each dataset (pt/lw/ps/lc...)
- titles (list of strings) key/legend titles for each dataset
- **subplot_title** (*str*) subplot title for panel plot case

Variables

- dataSets zipped titles and data for hdf5/ascii output and setAxisRange
- data list of Gnuplot. Data including extra data sets for error plotting

plot (hardcopy=True)

plot and generate output files

prepare_plot (margins=True, **kwargs)

prepare for plotting (calls all members of MyPlot)

setArrow(p0, p1, prop)

draw an arrow into the figure

Parameters

- p0 (list) start point [x, y]
- **p1** (*list*) end point [x, y]
- **prop** (*str*) gnuplot property string for the arrow

setAxisLabel(label, axis=x)

set label for specified axis

Parameters

- **label** (*str*) label
- axis (str) axis which to label

setAxisLog(log, axis=x)

set logarithmic scale for specified axis

Parameters

- **log** (*bool*) whether to set logarithmic
- **axis** (*str*) axis which to set logarithmic

setAxisLogs(**kwargs)

set axes logarithmic if requested

setAxisRange(rng, axis=x)

set range for specified axis

Notes

- automatically determines axis range to include all data points if range is not given.
- logscale and secondary errors taken into account
- y-axis range determined for points within given x-axis range

Parameters

- rng (*list*) lower and upper range limits
- axis (str) axis to which to apply range

setErrorArrows(**kwargs)

reset properties of arrows used to plot special errors

setKeyOptions(key_opts)

set key options

Parameters

key_opts (*list*) — strings for key/legend options

setLabel(label, pos, abs_place=False)

draw a label into the figure

Parameters

- **label** (*str*) label
- pos(list)—x,y position
- **abs_place** (*bool*) absolute or relative placement

setMargins(**kwargs)

set the margins

Notes

- keys other than l(b,t,r)margin are ignored
- if margin not given leave to gnuplot

setVerticalLine(x, opts)

draw a vertical line

Parameters

- x (float) position on x-axis
- **opts** (*str*) line draw options

Configuration Variables

var default_key

default options for legend/key

var basic_setup

bars, grid, terminal and default_key

var default_margins

default margins to define plot area

var xPanProps

xscale, xsize, xoffset for panel plots

var default_colors

provides a reasonable color selection (see palette)

pyana.ccsgp.utils.getOpts(i)

convience function for easy access to gnuplot property string

pyana.ccsgp.utils.zip_flat(a, b, c=None, d=None)

zips 2-4 lists and flattens the result

```
pyana.examples.utils.checkSymLink()
    check for symbolic link to input directory
pyana.examples.utils.enumzipEdges(eArr)
    zip and enumerate edges into pairs of lower and upper limits
pyana.examples.utils.getCocktailSum(e0, e1, eCocktail, uCocktail)
    get the cocktail sum for a given data bin range
pyana.examples.utils.getEdges(npArr)
    get numpy.array of bin edges
pyana.examples.utils.getErrorComponent(result, tag)
    get total error contribution for component with specific tag (stat/syst)
pyana.examples.utils.getMaskIndices(mask)
    get lower and upper index of mask
pyana.examples.utils.getUArray(npArr)
    uncertainty array multiplied by binwidth (col2 = dx)
pyana.examples.utils.getWorkDirs()
    get input/output dirs (same input/output layout as for package)
```

B.7 wp-pdf

Upgrade Constant in wp-config.php

```
// forces the filesystem method: "direct", "ssh", "ftpext", or " \leftrightarrow
   ftpsockets"
define('FS_METHOD', 'direct');
// absolute path to root installation directory
define('FTP_BASE', '/home/patrick/public/asciidoc.the-huck.com/public/' \leftrightarrow
   );
// absolute path to "wp-content" directory
define('FTP_CONTENT_DIR', '/home/patrick/public/asciidoc.the-huck.com/ ←
   public/wp-content/');
// absolute path to "wp-plugins" directory
\tt define('FTP\_PLUGIN\_DIR', '/home/patrick/public/asciidoc.the-huck.com/ \leftarrow \\
   public/wp-content/plugins/');
// absolute path to your SSH public key
define('FTP_PUBKEY', '/home/patrick/.ssh/<your-key>.pub');
// absolute path to your SSH private key
define('FTP_PRIVKEY', '/home/patrick/.ssh/<your-key>');
// either your FTP or SSH username
define('FTP_USER', '<username>');
// hostname:port combo for your SSH/FTP server
define('FTP_HOST', 'the-huck.com');
```

PHP Widget for Pagination

```
next page: <?php echo next_page_not_post('%title','expand','sort_column= \( \to \)
    menu_order'); ?><br>
previous page: <?php echo previous_page_not_post(' %title','expand',' \( \to \)
    sort_column=menu_order'); ?>
```

Makefile

```
# pdf document name
DOCOUT=asciidoc
# your initials
INITIALS=PH
# filelist (needs to be in order!)
# put paths to all asciidoc source files in
# filelist.txt or list them here directly
# you can submit single files via the *.txt target
# use SIMSTR=-n to simulate submission
FILELIST=$(shell cat filelist.txt)
# symbolic links
# this list is checked in the 'check' target
# and requirement for successfull compilation
# remove 'images' if no images included
# (or adjust to image include in source file)
LINKLIST = #images
###################################
# NO CHANGES REQUIRED BELOW #
###################################
# variables
DOCINFO=docinfo.xml
DOCINFOREV=$ (DOCOUT) -$ (DOCINFO)
TAGLIST=$(shell git tag -l | tr '\n' '')
# shell commands
SIMSTR=
BPCMD=blogpost.py $(SIMSTR) -p post
SEDCMD=sed -e '/^:blogpost/d' -e 's:\/\/=:=:'
# phony takes target always as out-of-date
.PHONY: all pdf hp docinfo check clean
# default target if none specified
all: pdf hp latex
# define directive for single revision entry
# argument: tagname
define REVCMD
echo '<revision>' >> $(DOCINFOREV)
echo ' <revnumber>'$(1)'</revnumber>' >> $(DOCINFOREV)
echo ' <date>'(shell git log -1 $(1) --format=%ad --date=short)'</date <math>\leftarrow
   >' >> $(DOCINFOREV)
echo ' <authorinitials>$(INITIALS)</authorinitials>' >> $(DOCINFOREV)
echo ' <revremark>'(shell git log -1 $(1) --format=B)'</revremark>'>> \leftarrow
    $ (DOCINFOREV)
echo '</revision>' >> $(DOCINFOREV)
endef
# define A2X command
# argument: format (pdf/tex), asciidoc file, outdir
# -a docinfo = include $(DOCOUT)-docinfo.xml
```

```
define A2XCMD
a2x - vv - a  latexmath -a  docinfo -L - D  $(3) -f  $(1) $(2)
# check whether required symbolic links exist
# abort otherwise
define TESTDEF
\$(if \$(wildcard \$(1)),\$$(info symlink \$(1) ok),\$$(error symlink \$(1) \leftrightarrow
   NOT found))
endef
check:
        $(foreach link, $(LINKLIST), $(eval $(call TESTDEF,$(link))))
# generate $(DOCOUT)-docinfo.xml
docinfo:
        cp $(DOCINFO) $(DOCINFOREV)
        $(foreach tag, $(TAGLIST), $(call REVCMD,$(tag)))
        echo '</revhistory>' >> $(DOCINFOREV)
# generate pdf
pdf: docinfo check
        cp preamb.txt $(DOCOUT).txt
        @$(foreach file, $(FILELIST), $(SEDCMD) $(file) >> $(DOCOUT).txt; \leftarrow
        $(call A2XCMD,pdf,$(DOCOUT).txt,.)
# generate page-by-page tex files for inclusion in latex document
latex: check
        mkdir tex && ln -s images tex/images
        @$(foreach file, $(FILELIST), $(call A2XCMD,tex,$(file),tex); )
# push all asciidocs to wordpress
hp: check
        @$(foreach file, $(FILELIST), $(BPCMD) $(file); )
# push a single asciidoc to wordpress
FORCE:
%.txt: FORCE
        $(BPCMD) $*.txt
# clean up
clean:
        @if [ -e $(DOCOUT).txt ]; then rm -v $(DOCOUT).txt; fi
        @if [ -e $(DOCOUT).pdf ]; then rm -v $(DOCOUT).pdf; fi
        @if [ -e $(DOCINFOREV) ]; then rm -v $(DOCINFOREV); fi
        @if [ -d tex ]; then rm -rfv tex; fi
```