

1 **S1 Supplementary Information text: Full description of the data**

2 **analysis**

3 In this supplementary information, we provide a full description of the different steps of our
4 data analysis. This includes the arguments for the choice of a particular approach as well as the
5 sensitivity of the output of each approach to its input parameters. Investigating the sensitivity of a
6 method increases our understanding of the relationship between input and output variables.
7 Furthermore, it provides information on the robustness of the approach.

8 In the following, we consider the four main parts of our analyses:

- 9 1. Normalization of expression values and classification of cell populations
- 10 2. Determining cell neighbours with the Delaunay Cell Graph (DCG)
- 11 3. Correlations of expression levels of neighbouring cells
- 12 4. Rule-based simulations of population composition in ICM of early blastocysts

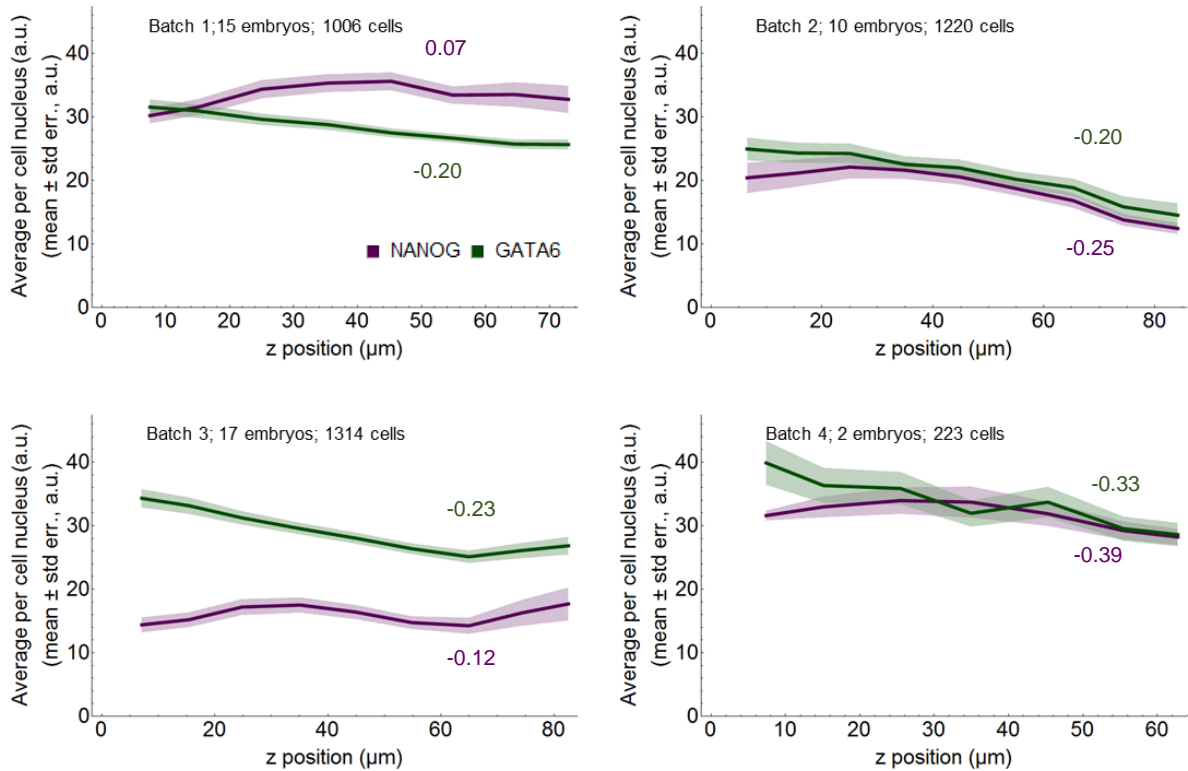
13

14 **1. Normalization of expression values and classification of cell populations**

15 The imaging data for the embryos was generated in four batches corresponding to different
16 imaging sessions and/or stainings. The mounting of the embryos for imaging resulted in a slight
17 squeezing along the z-axis of the image and hence extension along x and y (Fig S1, Step 3(i)). We
18 checked for fluorescence intensity decay along the z-axis for each batch. As this decay was minimal
19 due to the mounting of the embryos, intensity adjustment along z was not performed (Fig 1).

20 We assumed that the embryos that do not have fully segregated epiblast and primitive
21 endoderm should be spherical (early and mid blastocysts). Based on this assumption, we calculated
22 the deviation from sphericity for each of these embryos and rescaled the coordinates of the cell nuclei
23 to obtain spherical embryos. Embryos with segregated epiblast and primitive endoderm have hatched
24 from the zona and are elongated (late blastocysts). To rescale the coordinates of these late stage

25 embryos, we calculated for each batch the median rescaling factors for x, y and z of the early and mid
 26 blastocysts and applied these to the late blastocysts.
 27



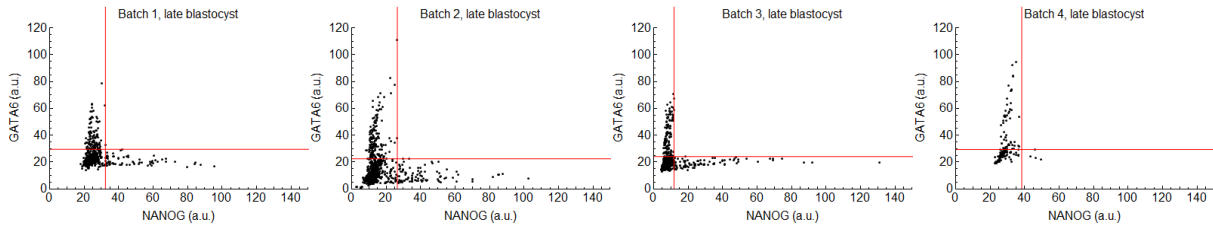
28 **Fig 1: Fluorescence intensity distribution along the z-axis.** Mean level of NANOG (purple) or GATA6 (green) (y-
 29 axis) fluorescence intensity in each cell (ICM and TE) versus its z position within the imaged z-stack in each of the
 30 four imaged embryo batches. The z position data are binned in 10 µm intervals. The shaded regions display the
 31 standard error of the mean. Batch, embryo and total cell numbers are indicated. Coloured numbers indicate the
 32 Spearman correlation values between NANOG (purple) and GATA6 (green) levels. Note that all values show a
 33 very weak or weak correlation indicating no evident decay of fluorescence intensity in deeper z positions.

34

35 Plotting the mean GATA6 expression levels versus the mean NANOG expression levels for all
 36 nuclei in the four imaging batches, we observed a shift in the data related to the batch number (Fig S1,
 37 Step 2). To align the data obtained from the four independent sessions, we established thresholds for
 38 NANOG and GATA6 expression for each batch, based on the data distribution in late stage embryos,
 39 where Epiblast (Epi) and Primitive Endoderm (PrE) are completely separated and no double positive
 40 (DP) cells occur. The thresholds were manually adjusted. The criterion was to determine the minimal

41 NANOG and GATA6 value, respectively, such that there are no double positive cells in late blastocysts
42 (see Fig 3).

43



44

45 **Fig 3: Population thresholds.** Raw data for NANOG and GATA6 expression in single cells in arbitrary units (a.u.)
46 in late embryos for the four batches (black) and the manually set thresholds to determine the four populations
47 (red).

48

49 Based on the thresholds, we linearly shifted the data of all batches and all stages, such that all
50 thresholds fall on top of each other. Since the range of the data does not vary much between batches,
51 we consider such a linear transformation most appropriate. This changes the absolute intensity levels
52 for each embryo but it does not change the relative intensity values in an embryo, which is the value
53 that is relevant for our analysis. Based on the thresholds for GATA6 and NANOG, all cells were classified
54 as double negative (DN: N- and G-), NANOG+/GATA6- (N+G-), NANOG-/GATA6+ (N-G+) and double
55 positive (DP: N+, G6+). We applied the same method to the *Nanog* mutant data set to align the
56 thresholds obtained from the data obtained in the five imaging sessions.

57 We also tested the k-means clustering used in [1] to determine the thresholds for our WT
58 embryo data set as well as for the *Nanog* mutant data sets. Unfortunately, for the mutant data set, the
59 clustering approach gave unreasonable results, including a large proportion of DN cells. Therefore, we
60 decided to use the manually adjusted approach that works for both cases.

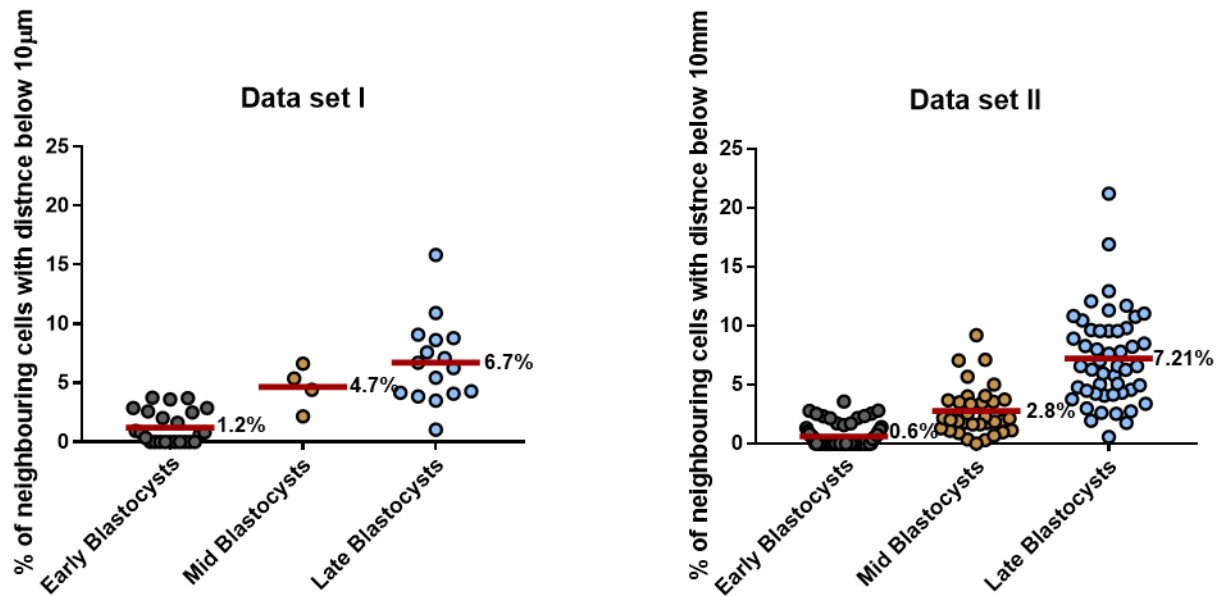
61 For the [1] data set, the imaging was performed in small dishes that didn't require the
62 mounting of the embryos, hence a rescaling was not required. Instead, the data set was corrected for
63 the decrease in intensity along z. Furthermore, Saiz et al. employed a k-means clustering for the
64 population assignment of their data. We took the corrected data set and population assignment from

65 [1] to perform our neighbourhood analyses. We noticed that there were some oversaturated nuclei
66 images and hence excluded all NANOG and GATA6 levels from the distribution that were two standard
67 deviations away from the respective mean. The remaining analysis was analogous to our data.

68

69 **2. Determining cell neighbours with the Delaunay Cell Graph (DCG)**

70 We recently proposed two approaches to model the cell neighbourhood [2]: the Proximity Cell
71 Graph (PCG), which provides a purely distance-based description of the cell neighbourhood and the
72 Delaunay Cell Graph (DCG), in which neighbourhood is determined by the Delaunay triangulation. The
73 Delaunay triangulation and its dual, the Voronoi tessellation, are routinely used to approximate the
74 nearest neighbours of a cell [2–4]. The Delaunay cell graph (DCG) is given by $DCG(V, E)$ where V is the
75 vertex set and E is the edge set of the graph. An edge $(u, w) \in E$ exists between two vertices $u \in V$
76 and $w \in V$ if the corresponding points are connected by a line in the Delaunay triangulation and the
77 Euclidean distance between u and w is less than a given threshold, which we chose as $30 \mu\text{m}$ (three
78 times the average diameter of a cell nucleus). To validate that the distance between the centroids of
79 two neighbouring cells is at least $10 \mu\text{m}$, we calculated this distance between all neighbouring cells in
80 the ICM (and their TE neighbours) for all embryos in data set I and II (Fig 3). These values fall within
81 the reported segmentation errors obtained with MINS [5], increasing in later embryos.



82

83 **Fig 3: Percentage of cells with a distance below 10 μm in data set I and II.** Each dot represents the percentage
 84 of distances of a cell to all its neighbours that fall below 10 μm in one embryo. The horizontal red line represents
 85 the average percentage within each developmental stage (numerical value is also shown).

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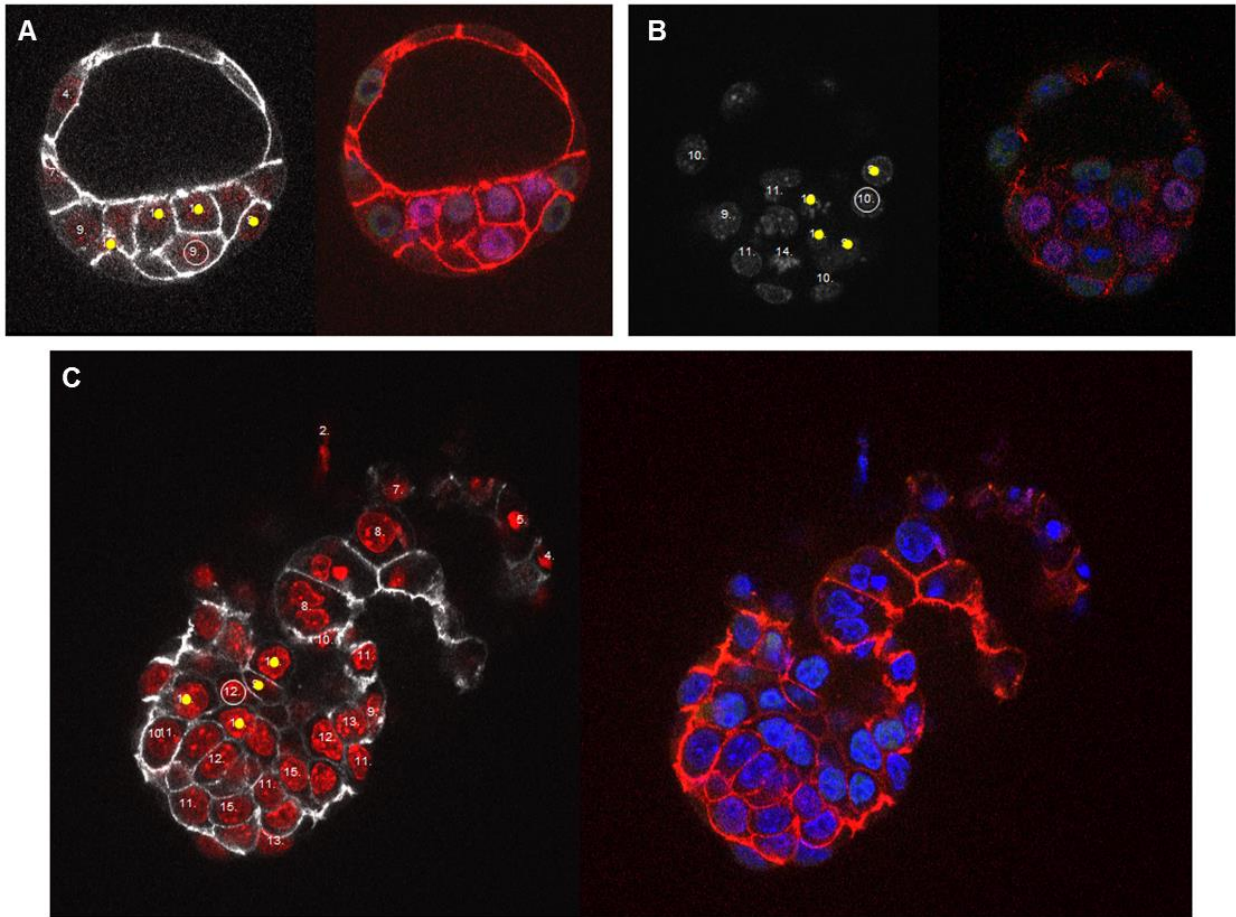
87 In a preliminary study to decide whether to use the Proximity Cell Graph (PCG) and/or the
 88 Delaunay Cell Graph (DCG) in mouse embryos, we generated a number of artificial shapes (ball, oblate
 89 spheroid, prolate spheroid, cuboid and box) and analysed the number of edges versus the number of
 90 vertices. As expected, we found that the number of edges in the PCG increases unreasonably with
 91 increasing number of vertices [2]. Furthermore, by definition, the PCG is completely dependent on the
 92 cut off length. PCG approximation was used in a recent study on a model for early cell lineage
 93 specification in mouse embryos with neighbour type simulations [6]. The authors assume in their
 94 simulations that the cells are non-overlapping spheres with a certain radius and a cut off length 1.2
 95 times the sum of the radii of the two cells. This is essentially if the spheres touch or almost touch. For
 96 a tissue with polygonal cells of different sizes like the ones found in mouse embryos, it is not trivial to
 97 determine an appropriate cut off length to obtain the nearest neighbours. The DCG is less sensitive to
 98 the cut off length and for cells in the centre of the embryo like in the ICM, the cut off length is irrelevant
 99 unless it is unreasonably small. Therefore, we decided to analyse the embryo data using the DCG.

100 We employed the DCG on the pre-processed nuclei centre of mass. For a given cell (vertex in
 101 the cell graph), the neighbouring cells are represented by the vertices that are connected through
 102 edges. In all our analyses, the set of neighbouring cells consists of all ICM cells and the TE cells that are
 103 neighbours to at least one ICM cell (Fig S1, Step4).

104 To evaluate the neighbour assignment of the DCG in the mouse embryos, we compared the
 105 results for the ICM cells of four early, three mid and two late embryos to a manual assignment included
 106 in our data set (Fig 4, and see Sup. Videos 1-3). For the manual assignment, we considered cells as
 107 neighbours if they are touching, identified by the membrane staining. The manual assignment only
 108 provides an indication. Judging the three-dimensional neighbourhood of the cells from slices of two-
 109 dimensional images is very difficult and gets even more challenging as the cell density and the
 110 irregularity of the cellular geometry increase with stage. We find that the accuracy of DCG compared
 111 to the manual assignment is 91 % (early), 82% (mid) and 83% (late) (see Table 1). We also found that
 112 0 (early), 3 (mid) and 13 (late) cells were not detected as neighbours by the automatic assignment
 113 compared to the manual assignment due to errors in the segmentation method used (MINS). Hence,
 114 if the cells were segmented correctly, the DCG did not miss a neighbourhood relationship. We conclude
 115 that for all stages, the DCG provides a robust description of the local cell neighbourhood in the ICM
 116 and a satisfactory approximation of which cells are touching.

117 **Table 1: Comparison of DCG neighbours to manual assignment of touching cells**

	Early (n=4)	Mid (n=3)	Late (n=2)
ICM cells	50	67	79
DCG neighbours	543	751	1031
Manual neighbours (touching)	495	617	851
Accuracy: Manual/DCG neighbours	0.91	0.82	0.83



118

119 **Fig 4: z Sections of early (A), mid (B) and late (C) embryos comparing DGC neighbour assignment and**
 120 **fluorescent immunostaining.** The left panels show membrane and/or nuclear staining. The yellow dots indicate
 121 DGC calculated neighbouring cells of the cell with an encircled number, that number indicates its number of
 122 neighbours; numbers in other cells indicate the number of neighbouring cells of that cell. The right panels show
 123 the original confocal images of the embryos shown, stained for NANOG (magenta), GATA6 (green), DAPI (blue)
 124 and β -catenin (membrane, red). Note that the embryos are upside down and not all the neighbours of the
 125 indicated cell are located in the same z section. See Sup. Videos 1-3 for the complete z-stack.

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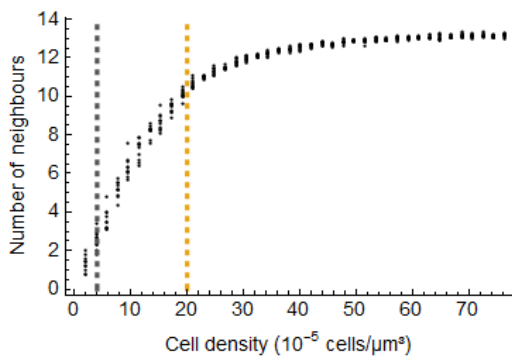
127 Sensitivity of the DCG

128 We investigated the sensitivity of the number of neighbours provided by the DCG with respect
 129 to cell density. We considered a ball of radius $50\ \mu\text{m}$ and randomly filled it with non-overlapping
 130 spheres of radius $5\ \mu\text{m}$ to represent the cells. For these simulated cells, we generated the DCG. The
 131 procedure was repeated ten times for cell numbers ranging from 10 to 400 in steps of 10, resulting in

132 cell densities ranging from $1.9 \times 10^{-5} \text{ cells}/\mu\text{m}^3$ to $76.43 \times 10^{-5} \text{ cells}/\mu\text{m}^3$. For comparison, manual
133 inspection of the ICM cells resulted in a cell density of $4 \times 10^{-5} \text{ cells}/\mu\text{m}^3$ in early embryos and
134 $20 \times 10^{-5} \text{ cells}/\mu\text{m}^3$ in mid embryos.

135 For the simulated DCGs, we find that for increasing cell density the average number of
136 neighbours increases and plateaus at around 13 neighbours (Fig 5).

137



138

139 **Fig 5: The mean number of neighbours derived from the DCG plateaus for high cell densities.** Each dot
140 represents the mean number of neighbours of one simulated DCG. The vertical lines indicate the manually
141 obtained cell densities in ICM of early (grey) and mid (yellow) blastocysts.

142

143 3. Correlations of expression levels of neighbouring cells

144 To relate the expression levels of a given cell to the expression levels of all its neighbours (both
145 TE and ICM), we calculated Spearman's correlation coefficient of the expression levels of a cell and the
146 median expression levels of its neighbours. We chose to use median level in the neighbours in
147 combination with Spearman's correlation coefficient as we reasoned that this measurement was the
148 variable, which made the least assumptions about the type of signals that might be regulating the
149 observed correlations. Furthermore, the median provides a more robust measure than the sum of all
150 signals as the median goes up slower and is also less sensitive to outliers than the sum. Spearman's
151 correlation coefficient does not require normally distributed data.

152 To determine whether the obtained correlations are statistically significant, we performed a
153 bootstrap resampling of the correlation coefficients of our data and compared the result with

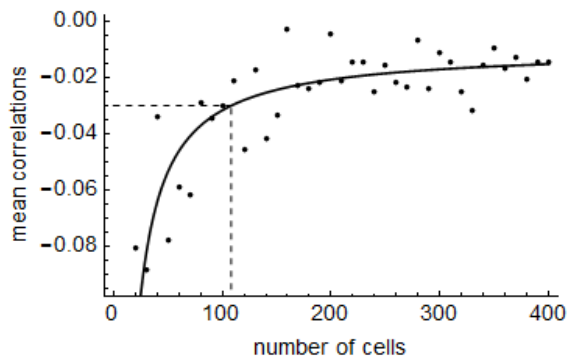
154 correlation coefficients of a null model. For the bootstrapping, we resampled the experimental data to
155 create 100 different data sets.

156

157 Sensitivity of the correlation analysis:

158 Spearman's rank correlation coefficient is the Pearson correlation coefficient after the two
159 variables have been separately transformed to ranks while retaining their pairing [7]. The value of the
160 correlation coefficient is affected by a number of factors, in particular the sample size [8]. Therefore,
161 we explored the sensitivity of the correlation value to the number of cells analysed. We know that for
162 a random distribution, the correlation value is zero. To test whether this analysis might be affected by
163 the topological properties of small DCG given the specific constraints on cell number, we used 100
164 artificially generated DCGs. These artificial DCGs consisted of cell numbers 10 to 400 in steps of 10 and
165 randomly assigned expression levels to each cell based on the uniform distribution over [0,1]. For each
166 DCG, we then calculated the correlation value and determined the mean correlation value for DCGs
167 with the same cell number. We find that if the number of cells analysed increases, the mean correlation
168 coefficient approaches zero (Fig 6). Hence, if the number of cells is large enough, the correlation
169 analysis is consistent.

170 Next, we investigated how the number of cells in the analysis is linked to the deviation of the mean
171 correlation from zero. Fitting the function $f(x) = -\frac{a}{x} - b$ resulted in $a=2.19$ and $b=0.0098$. Based on
172 $f(x)$, we estimated that on average, we need at least 108 cells in the analysis to obtain at most 3%
173 deviation (Fig 6). Less cells will lead to more noise in the correlation analysis, while more cells will
174 increase the precision. We chose 3 % as the threshold, since this is the point where the functions levels
175 off.



176

177 **Fig 6: More than 108 analysed cells results in an average deviation of less than 3%.** Mean correlation
 178 coefficients for 100 artificially generated DCGs of 10 to 400 cells in steps of 10 with expression levels drawn from
 179 the uniform distribution over [0,1] (dots). The continuous line indicates the fitted curve $f(x) = -\frac{2.19}{x} - 0.0098$
 180 and the intersection of $f(x)$. The 3% threshold is marked by the dashed line.

181

182 The ICM has 20 ± 1 cells in early, 24 ± 1 cells in mid, and 45 ± 4 cells in late embryos. Due to
 183 these small numbers, analysing the correlations individually in each embryo does not provide reliable
 184 results. Hence, we pooled the data for all cells, expecting a reliable result if the number of pooled cells
 185 is at least 108.

186

187 Null model for correlations:

188 The correlation analysis for the experimental data results in non-zero values. To test whether
 189 these results might be affected by specific constraints on NANOG/GATA6 distributions, we investigated
 190 whether the correlation values are significantly different from those of a null model. For the null model,
 191 we assumed the embryo geometry is given by the experimental data, hence we used the measured
 192 coordinates of the cells. The expression levels of the TE cells were also based on the experimental data.
 193 To assess the effect of NANOG/GATA6 distribution, we generated several different models using
 194 different assignment rules for the NANOG and GATA6 values of the ICM cells:

195 • Random model 1: The NANOG and GATA6 values of the ICM cells are randomly drawn from
 196 the uniform distribution over [0,1].

197 • Random model 2: The values of the ICM of each embryo are shuffled randomly.

198 • Random model 3: We generate the distributions for NANOG and GATA6 from all ICM cells of
199 all embryos at all stages. The values of an ICM cell are randomly drawn from these distributions.

200 • Random model 4: We generate the distributions for NANOG and GATA6 from all ICM cells of
201 all embryos of a given stage. This results in six distributions one for each stage for NANOG and GATA6,
202 respectively. For a cell in the ICM of a given embryo, the values for NANOG and GATA6 are randomly
203 drawn from the corresponding distribution depending on the stage of the embryo.

204 • Random model 5: The values of the ICM cells of all embryos in each stage are randomly
205 shuffled.

206

207 We generated each model for all the embryos in our data set, pooled all the cells in the ICM
208 from one stage and calculated the correlations of these cells with their neighbours both for NANOG
209 (Table 2) and GATA6 (Table 3). This procedure was repeated 100 times. We expect very low correlation
210 values for the random models.

211 **Table 2: Correlation values for different random assignments of NANOG expression (mean \pm standard**
212 **deviation)**

Model	Early	Mid	Late
Random model 1	-0.0006 \pm 0.04	0.15 \pm 0.01	0.25 \pm 0.003
Random model 2	0.2 \pm 0.04	0.04 \pm 0.08	0.3 \pm 0.05
Random model 3	-0.005 \pm 0.05	-0.02 \pm 0.1	-0.004 \pm 0.04
Random model 4	-0.009 \pm 0.04	-0.02 \pm 0.1	-0.02 \pm 0.04
Random model 5	0.003 \pm 0.06	0.002 \pm 0.1	-0.01 \pm 0.04

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219 **Table 3: Correlation values for different random assignments of GATA6 expression (mean \pm standard deviation)**

Model	Early	Mid	Late
Random model 1 (identical to above)	-0.0006 \pm 0.04	0.14 \pm 0.01	0.25 \pm 0.003
Random model 2	0.6 \pm 0.01	0.4 \pm 0.07	0.4 \pm 0.04
Random model 3	-0.005 \pm 0.05	0.0003 \pm 0.1	-0.0001 \pm 0.04
Random model 4	-0.001 \pm 0.05	-0.02 \pm 0.1	0.002 \pm 0.04
Random model 5	-0.004 \pm 0.05	0.004 \pm 0.1	0.006 \pm 0.04

220

221 We find that Random model 2 exhibits larger correlation values than the other models. This
 222 indicates that reshuffling the values of the ICM cell in each embryo individually does not introduce a
 223 sufficient randomization, due to the small number of cells in the ICM.

224 All the other models show similar results with values close to zero as expected from a random
 225 model. For all subsequent analyses shown in the main text, we used the method of Random model 3
 226 to calculate the null models for the neighbour correlations, rather than models 1, 4 or 5. The main
 227 reasons for this are that Random model 3 relies on the original data (unlike Random model 1) and its
 228 calculation is more straightforward, because we only need to consider two distributions for the data
 229 (one for NANOG and one for GATA6) rather than six as for Random models 4 and 5.

230 The correlation values for Random model 3 for the different experimental conditions are
 231 summarised in Tables 4 and 5.

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238 **Table 4: Correlation values for Random model 3 for wild-type and NANOG mutant analyses (mean \pm standard**
 239 **deviation)**

Experimental condition	Correlations		
	Early	Mid	Late
Our data (NANOG cell, NANOG neighbours)	-0.005 \pm 0.05	-0.02 \pm 0.1	0.004 \pm 0.04
Our data (GATA6 cell, GATA6 neighbours)	-0.005 \pm 0.05	0.0003 \pm 0.1	-0.0001 \pm 0.04
Our data (NANOG cell, GATA6 neighbours)	-0.003 \pm 0.04	-0.005 \pm 0.1	0.006 \pm 0.04
Our data (GATA6 cell, NANOG neighbours)	-0.002 \pm 0.05	-0.02 \pm 0.1	-0.0004 \pm 0.04
Saiz data (NANOG cell, NANOG neighbours)	-0.0005 \pm 0.03	0.001 \pm 0.04	-0.0008 \pm 0.03
Saiz data (GATA6 cell, GATA6 neighbours)	-0.002 \pm 0.03	-0.008 \pm 0.03	0.0001 \pm 0.03
Saiz data (NANOG cell, GATA6 neighbours)	-0.004 \pm 0.03	-0.002 \pm 0.04	-0.0006 \pm 0.03
Saiz data (GATA6 cell, NANOG neighbours)	-0.004 \pm 0.03	-0.0009 \pm 0.03	-0.003 \pm 0.03
NANOG mutant analysis, WT and heterozygotes (GATA6 cell, GATA6 neighbours)	-0.0008 \pm 0.04	-0.02 \pm 0.07	0.2 \pm 0.03
NANOG mutant analysis, mutants (GATA6 cell, GATA6 neighbours)	-0.003 \pm 0.08	-0.03 \pm 0.09	-0.1 \pm 0.04

240

241

242 **Table 5: Correlation values for Random model 3 for treated embryos (mean \pm standard deviation)**

Experimental condition	Correlation (no staging)
Treatment analysis, control (NANOG cell, NANOG neighbours)	-0.003 \pm 0.03
Treatment analysis, control (GATA6 cell, GATA6 neighbours)	-0.001 \pm 0.04
Treatment analysis, PD03 (NANOG cell, NANOG neighbours)	-0.003 \pm 0.04
Treatment analysis, PD03 (GATA6 cell, GATA6 neighbours)	-0.005 \pm 0.04

243

244 **4. Rule-based simulations of population composition in ICM of early blastocysts**

245 To generate the simulations of the four populations, we used the 64 early embryo data sets from
 246 Saiz et al. For each ICM cell, we determined the simulated cell population type based on two rules and
 247 kept the cell centroid and neighbours as obtained from the experimental data. We included the TE
 248 cells that are neighbouring at least one ICM cell with their features obtained from the experimental
 249 data. To obtain the population type for an ICM cell, we assigned it N+ or N- and G6+ or G6- expression
 250 according to these two rules:

251 1) G6+ cells are clustered; the clustering is achieved by randomly setting the percentage of being
 252 G6+ to 85 % and the rest to G6- ($p_{GATA6} = 0.85$);

253 2) cells with nine or close to nine neighbours are N+ up to 82 % ($p_{NANOG} = 0.82$), the rest N-.

254 The values for p_{GATA6} and p_{NANOG} are obtained from the experimental data and are the proportion of
 255 ICM cells positive for GATA6 or NANOG expression, respectively. Hence, p_{GATA6} is the proportion of
 256 DP and N-G+ cells and p_{NANOG} is the proportion of DP and N+G- cells. Combining this information for
 257 each cell, we determined its simulated population type.

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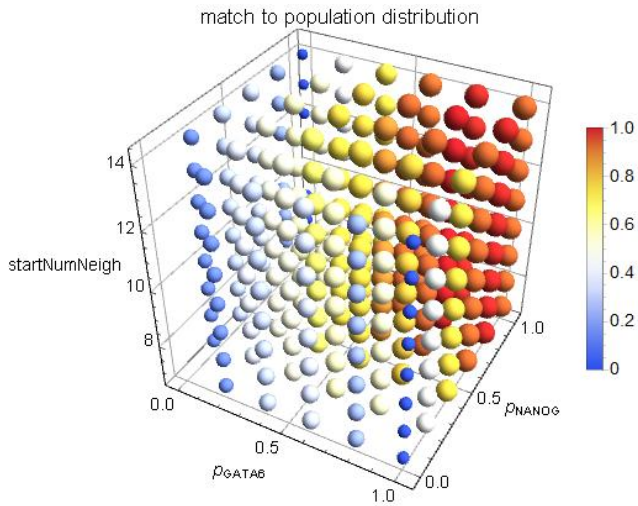
260 Sensitivity of the four populations model:

261 The four populations model relies on three parameters:

- 262 1. p_{GATA6} , the proportion of GATA6 positive cells, i.e DP and N-G+ cells
- 263 2. p_{NANOG} , the proportion of NANOG positive cells, i.e DP and N+G- cells
- 264 3. startNumNeigh, the number of neighbours at which we start assigning NANOG positive fate
- 265 to the cells

266 We analysed the sensitivity of the model to the values of these three parameters. We varied p_{NANOG}
267 and p_{GATA6} between 0 and 1 in steps of 0.2 and startNumNeigh between 7 and 14 in steps of 1. For
268 each parameter value combination, we performed 100 simulations. For each embryo, we calculated
269 the mean distribution of populations of the 100 simulations. The mean population distributions are
270 then summed up to obtain the total overall population distribution. This simulated total population
271 distribution is then compared to the total population distribution from the experimental data. To
272 assess the goodness of fit, we employed the mean squared error $MSE = Mean((popDist_{Sim} -$
273 $popDist_{Exp})^2)$, where $popDist_{Sim}$ is the population distribution of the simulations and $popDist_{Exp}$
274 the population distribution obtained from the experiments. For a better visualisation, we rescale the
275 MSE and obtain the simulation match $1 - \frac{MSE - Min(MSE)}{Max(MSE) - Min(MSE)}$. Hence, a simulation match of 0
276 corresponds to the parameter values with the worst match and a simulation match of 1 to the best
277 match (Fig 7)

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279

280 **Fig 7: Higher values of p_{NANOG} and p_{GATA6} provide a better match of the simulations to the experimental data.**

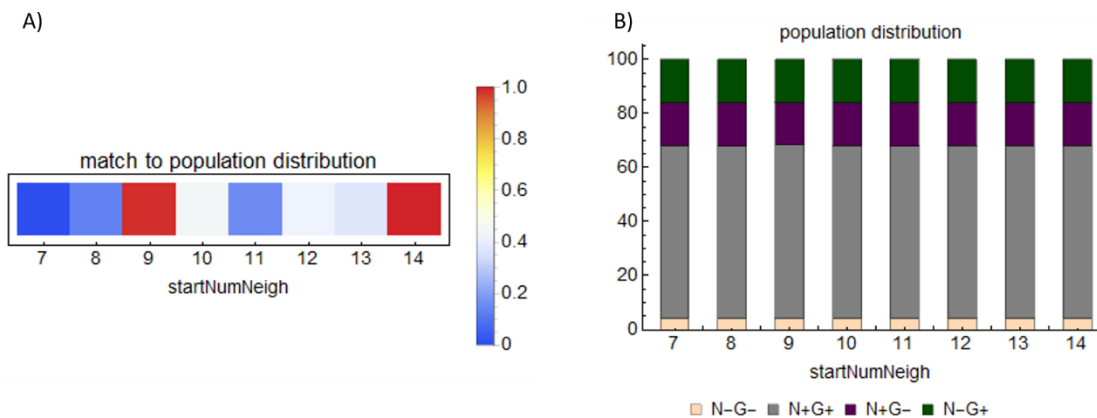
281 Simulation match to experimental data from early embryos (normalized to [0,1]) for the four populations model,
 282 varying p_{NANOG} and p_{GATA6} between 0 and 1 and startNumNeigh between 7 and 14.

283

284 Varying startNumNeigh independently showed the best match for 14, followed by 9 (Fig 8A).

285 Plotting the population distributions however showed that the differences between the simulations
 286 are negligible (Fig 8B).

287

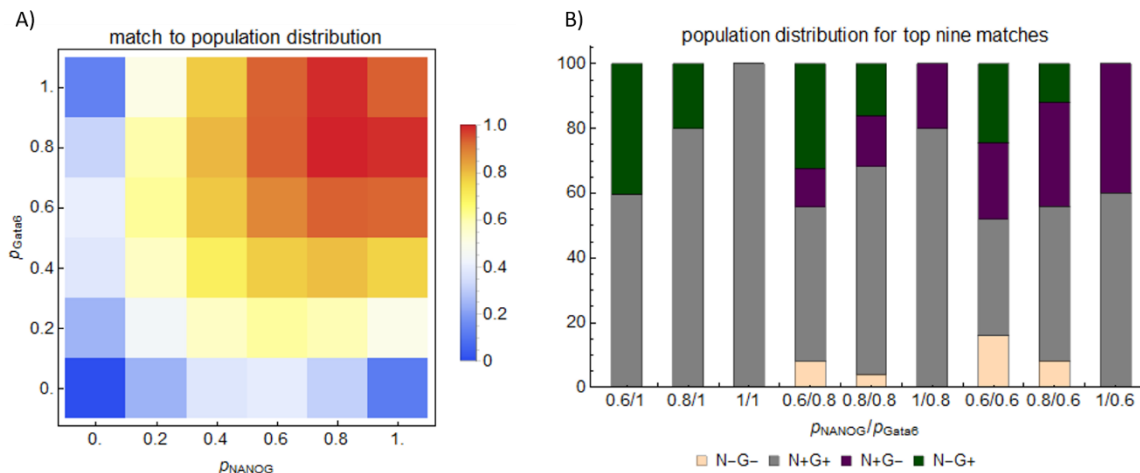


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289 **Fig 8: The four populations model is robust with respect to the parameter startNumNeigh.** Simulation match
 290 to experimental data from early embryos (normalized to [0,1]) (A) and population distributions (B) for the four
 291 populations model for $p_{NANOG} = 0.8$ and $p_{GATA6} = 0.8$ and startNumNeigh varying between 7 and 14.

292

293 Varying p_{NANOG} and p_{GATA6} shows that for values between 0.6 and 1 for both parameters, we
 294 obtain a reasonable fit, with the best fit for $p_{NANOG} = 0.8$ and $p_{GATA6} = 0.8$ (Fig 9A). Plotting the
 295 population distribution for the simulations of these nine parameter combinations, shows that
 296 increasing the values for p_{NANOG} or p_{GATA6} changes the composition of the populations in the
 297 simulated ICMs (Fig 9B). If p_{NANOG} or p_{GATA6} is one, only up to two populations arise. For values below
 298 one for p_{NANOG} and p_{GATA6} , the four populations arise and become more evenly distributed the
 299 smaller the values are.



300
 301 **Fig 9: The values of p_{NANOG} and p_{GATA6} determine the population distributions in the simulated ICMs.**
 302 Simulation match to experimental data from early embryos (normalized to [0,1]) (A) and population distributions
 303 for the top nine matches (B) for the four populations model for $startNumNeigh = 9$ and p_{NANOG} and p_{GATA6}
 304 varying between 0 and 1.

305

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