

1 **Role of protonation states in stability of molecular dynamics**
2 **simulations of high-resolution membrane protein structures**

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23 **Abstract**

24 Classical molecular dynamics (MD) simulations provide unmatched spatial and time
25 resolution of protein structure and function. However, accuracy of MD simulations often
26 depends on the quality of force field parameters and the time scale of sampling. Another
27 limitation of conventional MD simulations is that the protonation states of titratable amino
28 acid residues remain fixed during simulations, even though protonation state changes
29 coupled to conformational dynamics are central to protein function. Due to the uncertainty
30 in selecting protonation states, classical MD simulations are sometimes performed with all
31 amino acids modeled in their standard charged states at pH 7. Here we performed and
32 analyzed classical MD simulations on high-resolution cryo-EM structures of two membrane
33 proteins that transfer protons by catalyzing protonation/deprotonation reactions. In
34 simulations performed with amino acids modeled in their standard protonation state the
35 structure diverges far from its starting conformation. In comparison, MD simulations
36 performed with pre-determined protonation states of amino acid residues reproduce the
37 structural conformation, protein hydration, and protein-water and protein-protein
38 interactions of the structure much better. The results suggest it is crucial to perform basic
39 protonation state calculations, especially on structures where protonation changes play an
40 important functional role, prior to launching any MD simulations. Furthermore, the combined
41 approach of protonation state prediction and MD simulations can provide valuable
42 information on the charge states of amino acids in the cryo-EM sample. Even though accurate
43 prediction of protonation states currently remains a challenge, we introduce an approach of
44 combining pKa prediction with cryo-EM density map analysis that helps in improving not only
45 the protonation state predictions, but also the atomic modeling of density data.

46

47 Keywords; molecular dynamics, protonation states, pKa calculations, cryo-electron
48 microscopy, electrostatics.

49 Introduction

50 Within the past decade, the resolution of single-particle cryo-EM structures has improved
51 dramatically, largely due to the improvements in direct electron detectors and processing
52 software ¹. The resolution of single-particle cryo-EM structures is now comparable to x-ray
53 crystallography and NMR structures, and the so-called “resolution revolution” has made it
54 possible to determine structures of many previously inaccessible complexes, particularly for
55 membrane proteins ². Many of these structures have a resolution below 2.5 Å, allowing
56 accurate modeling of protein conformations, including ordered water molecules, which has
57 significant implications in drug design ³ and is also central to our understanding of the
58 molecular mechanism of enzymes that catalyze proton transfer reactions ⁴.

59
60 Proton transfer can take place across a chain of water molecules via a Grotthuss-type
61 mechanism ⁵. However, proton transfer routes through proteins do not consist only of water
62 molecules but are often made up of hydrogen-bonded networks of polar and charged amino
63 acid residues. Besides titratable residues such as glutamic acid and lysine, which can donate
64 or accept protons, other residues that are part of these networks include asparagine and
65 glutamine, and serine, threonine, and tyrosine with hydroxyl groups in their sidechains. These
66 polar residues can not only assist in proton transfer reactions by stabilizing charged
67 intermediates but may also undergo protonation/deprotonation reactions in proteinaceous
68 environments ^{4, 6-8}. Moreover, titratable acidic and basic residues are well-known to act as
69 proton transfer elements and proton loading sites in several enzymes ^{4, 9, 10}. However, the
70 protonation states in protein structures are usually not explicitly modelled. Such information
71 can be obtained with neutron diffraction techniques, but only for relatively small proteins ¹¹.

72
73 The two main structure determination methods for protein complexes, x-ray crystallography
74 and cryo-EM, produce superficially similar results. However, they differ fundamentally in the
75 way atomic structures are imaged. X-rays are deflected by electrons and thus produce
76 electron density maps, but electrons are scattered by Coulomb potential, and they are thus
77 sensitive to charges. While positively charged ions just add extra density to an already positive
78 signal, negative charges, in particular O⁻, can give rise to negative electron scattering
79 amplitudes ¹²⁻¹⁴. As a result, negatively charged sidechains of glutamate and aspartate
80 residues are not visible in cryo-EM maps. Although the weak density of these sidechains has
81 sometimes been interpreted as a result of the radiation sensitivity of the carboxyl group ^{15, 16},
82 the former mechanism appears to have a larger contribution ^{14, 17-19}. The absence of sidechain
83 density hampers accurate model building. On the other hand, it makes it possible to
84 determine the charge state of acidic residues.

85
86 To complement cryo-EM structures, molecular dynamics (MD) simulations are often
87 performed ²⁰⁻³⁰. These help in studying the dynamics of the protein and the solvent, as well
88 as the binding and unbinding of lipids, ligands, and ions. The approach of combining structural
89 data with MD simulations is a powerful technique to understand protein structure and
90 function. The abundance of new structures gives plenty of opportunity to perform these
91 simulations routinely at various levels of computational approximations. However, one
92 limitation of conventional molecular dynamics is that covalent bonds are fixed throughout
93 the simulation, therefore the charge states of titratable residues (often selected as the
94 standard charge state that is Asp/Glu deprotonated, Lys/Arg protonated and His neutral)
95 remain unchanged. This results in a biased scenario, and biologically relevant conformational

96 states with alternative protonation states are not populated. Moreover, situations where
97 changes in protonation states can occur as a function of conformational dynamics (e.g.
98 membrane proteins catalyzing proton transfer) are also not captured. However, there are
99 various methods that can allow charge states of amino acids to change during MD
100 simulations, such as hybrid QM/MM MD, and constant pH MD, but these are generally
101 computationally costly³¹, although there have been recent improvements in the enhanced
102 scalability of constant pH MD³².

103

104 For many proteins, performing MD simulations by systematic altering of charge states of
105 individual titratable residues is unrealistic, due to the large number of such residues. Of
106 course, one can alter protonation states of selected conserved residues to study specific
107 questions, and this has indeed been performed to obtain valuable functional insights³³⁻³⁷.
108 However, due to the long-range nature of electrostatic interactions the protonation state of
109 one titratable residue affects another's by ca. 8 kcal/mol (with a separation of 10 Å at $\epsilon=4$)
110 and such aspects are often ignored when performing simulations.

111

112 Alternatively, one can calculate the pKa of all titratable residues in a protein for a given
113 conformational state (obtained from a cryo-EM experiment, for example) and perform MD
114 simulations in that fixed protonation state. There are several methods to perform pKa
115 calculations, many of which are based on continuum electrostatics approaches³⁸. However,
116 these require a significant amount of preprocessing and can display large variation in pKa
117 values due to subtle conformational changes. Alternatively, empirical methods, such as
118 Propka can be employed relatively easily, to give fast and sufficiently accurate predictions of
119 the pKa of all ionizable groups present in a protein, even if hundreds in number³⁹. Methods
120 like Propka⁴⁰, often give reasonable estimates for the pKa of buried titratable residues, in
121 particular if the sites are far from any redox active cofactors. Due to their rapid pKa
122 estimations, they can be used on thousands of simulation snapshots to obtain profiles of pKa
123 change as a function of conformational dynamics^{35, 41}. Similarly, Monte Carlo-based pKa
124 prediction methods have also been used to predict charged states of systems, either using
125 standalone PDB files or simulation snapshots⁴².

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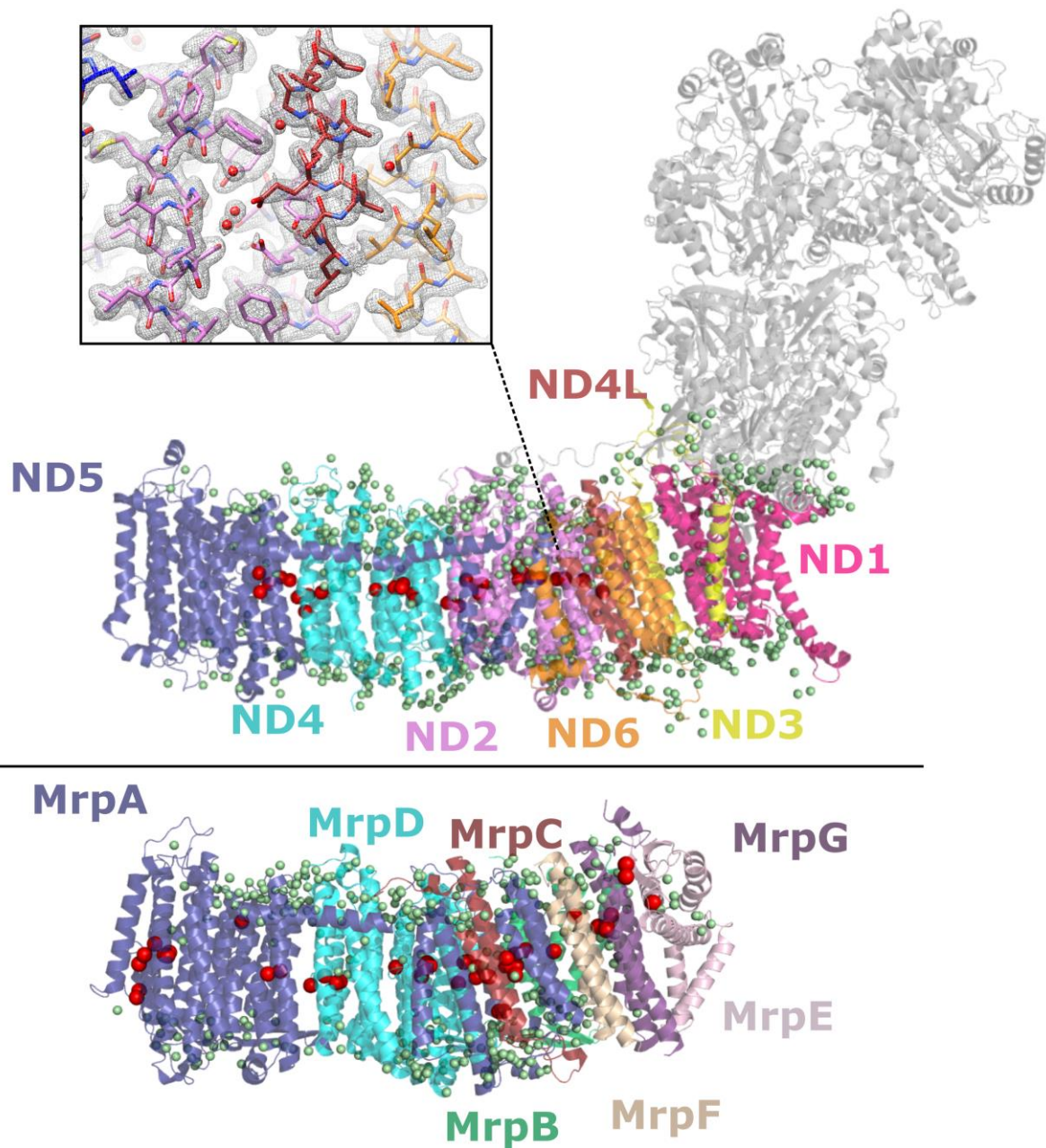
127 In this study, we present MD simulations on two high-resolution cryo-EM structures of
128 membrane proteins. The two structures are the respiratory complex I from *Yarrowia lipolytica*
129 (PDB 7O71, EMD-12742)⁴³ and the multiple resistance and pH adaptation (Mrp)
130 cation/proton antiporter from *Bacillus pseudofirmus* (PDB 7QRU, EMD-14124)⁴⁴. Both
131 proteins facilitate proton transfer reactions that involve amino acid residues and water
132 molecules, many of which have been resolved in the two structures. The role of protein
133 hydration, water dynamics as well as change in protonation state is central to the structure
134 and function of these proteins. By performing long time scale MD simulations in multiple
135 charge states of these proteins and extensively analyzing protein and solvent dynamics, we
136 show that both proteins deviate from the original cryo-EM conformation when simulated in
137 the standard protonation state of titratable amino acid residues, while MD simulations in pre-
138 defined protonation states stabilize the protein conformation much better. We propose that
139 the approach of protonation state prediction combined with MD simulations can give insights
140 into the charge state of residues in a cryo-EM structure. Furthermore, we find that the
141 prediction of protonation states of acidic residues agrees well with the charge state

142 assignment based on cryo-EM density maps, and that outliers can be identified with the
143 approach discussed here, leading to an improved modeling of cryo-EM density data.

144 **Results**

145 Two high-resolution membrane protein structures were chosen for this investigation. First,
146 the 2.1 Å resolution structure of complex I from *Y. lipolytica*, which is over 1 MDa in size, and
147 has more than 1600 structural water molecules resolved⁴³. Around 100 of these are in the
148 potential proton transfer pathways present in its membrane-bound subunits (Fig. 1). Second,
149 a structure from the evolutionarily related Na⁺/H⁺ Mrp antiporter⁴⁴ at a similar resolution of
150 2.2 Å. This protein is much smaller than complex I (ca. 213 kDa) and consists of membrane-
151 bound subunits only, without redox active cofactors. There are 360 water molecules resolved
152 in the structure of the Mrp antiporter, around 70 of them in the potential proton and sodium
153 transfer pathways (Fig. 1). The structure of complex I contains more than 1300 titratable
154 residues, while the Mrp structure has around 200. We performed MD simulations on both
155 complexes with all titratable sites either modeled in their standard states (S state) or based
156 on pKa calculations at pH 7 (P7 state). We find that in the P7 state, complex I has 68
157 neutralized titratable amino acids, out of which 25 are in the membrane core of the enzyme
158 (Fig. 1), while in the Mrp antiporter 13 residues are neutralized in the P7 state. Accordingly,
159 the charge reduces from +90/-94 to +83/-76 in the complex I membrane arm, and from +116/-
160 118 to +110/-112 in the Mrp upon neutralization of titratable sites as part of pKa calculations
161 (see Tables S1 and S2 for lists of residues neutralized in complex I and Mrp antiporter,
162 respectively).

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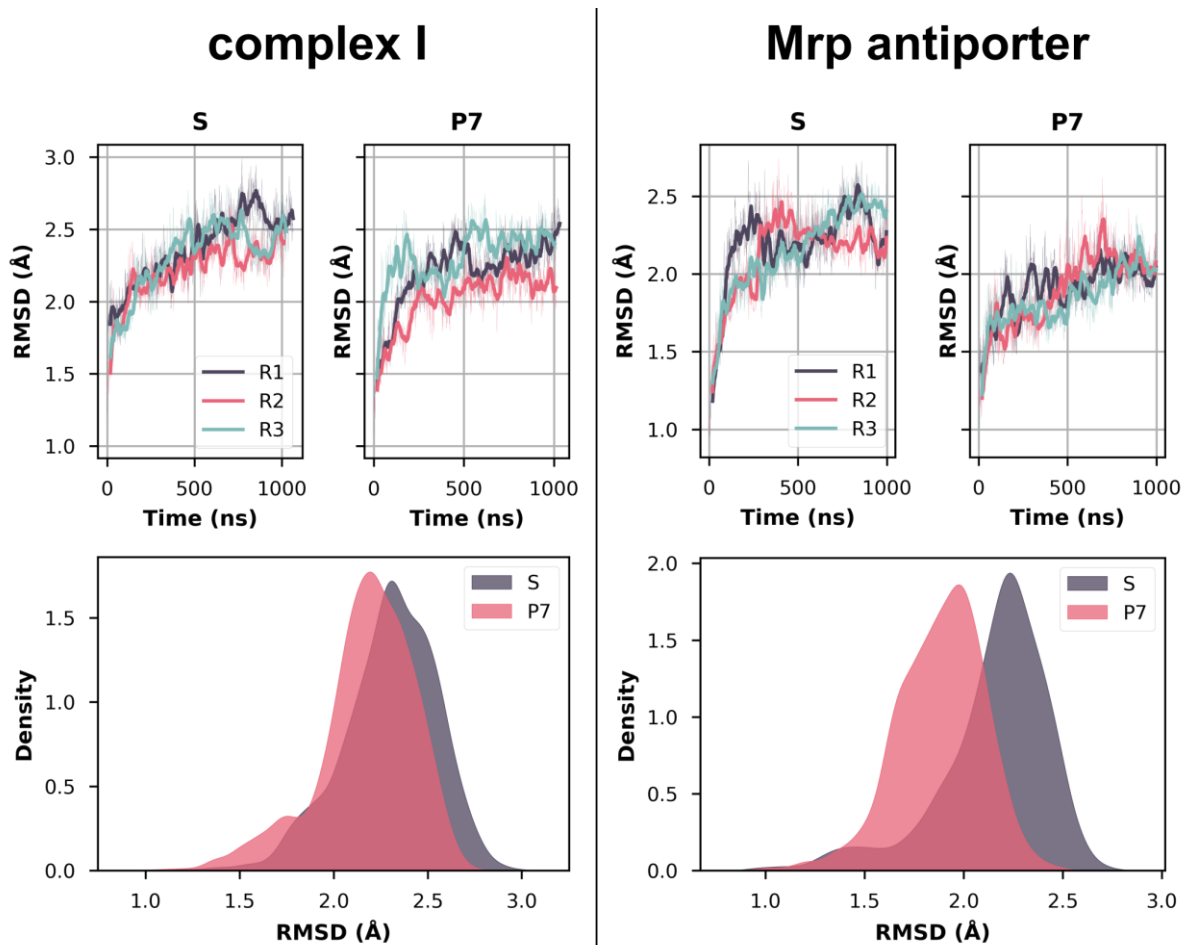


164
165 **Fig. 1** – Structure of the membrane domain of respiratory complex I (upper) and Mrp
166 antiporter (lower). The protein is shown in ribbon representation and colored by subunit. Only
167 core membrane-bound subunits are shown in color for complex I, with the hydrophilic core
168 subunits shown as gray. Structurally resolved water molecules are shown as small green
169 spheres, with those in the functionally relevant hydrophilic axes of complex I and Mrp
170 antiporter shown as larger red spheres. Proton translocation is suggested to take place
171 across this axis, which is a vital part of the mechanism for both proteins. The inset in the upper panel
172 shows a region of the complex I membrane arm within the high-resolution cryo-EM density
173 (grey mesh), including density for water molecules.

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178 Global mobility of proteins in P7 and S states

179 First, the overall global mobility of both systems was analyzed in the S and P7 states. Fig. 2
180 shows the time series as well as the distribution of the RMSD (root mean square deviation) of
181 the backbone atoms for the core membrane-bound subunits of complex I and Mrp antiporter
182 in the two simulation states. The P7 state systems with lower charge have overall lower RMSD
183 for both protein complexes, which means that the backbone atoms stay closer to the starting
184 conformation throughout the simulation. This notion is also true if a similar RMSD analysis is
185 performed on the C α backbone atoms and all protein atoms excluding hydrogens, even with
186 the inclusion of the hydrophilic domain of complex I (Fig. S1).
187



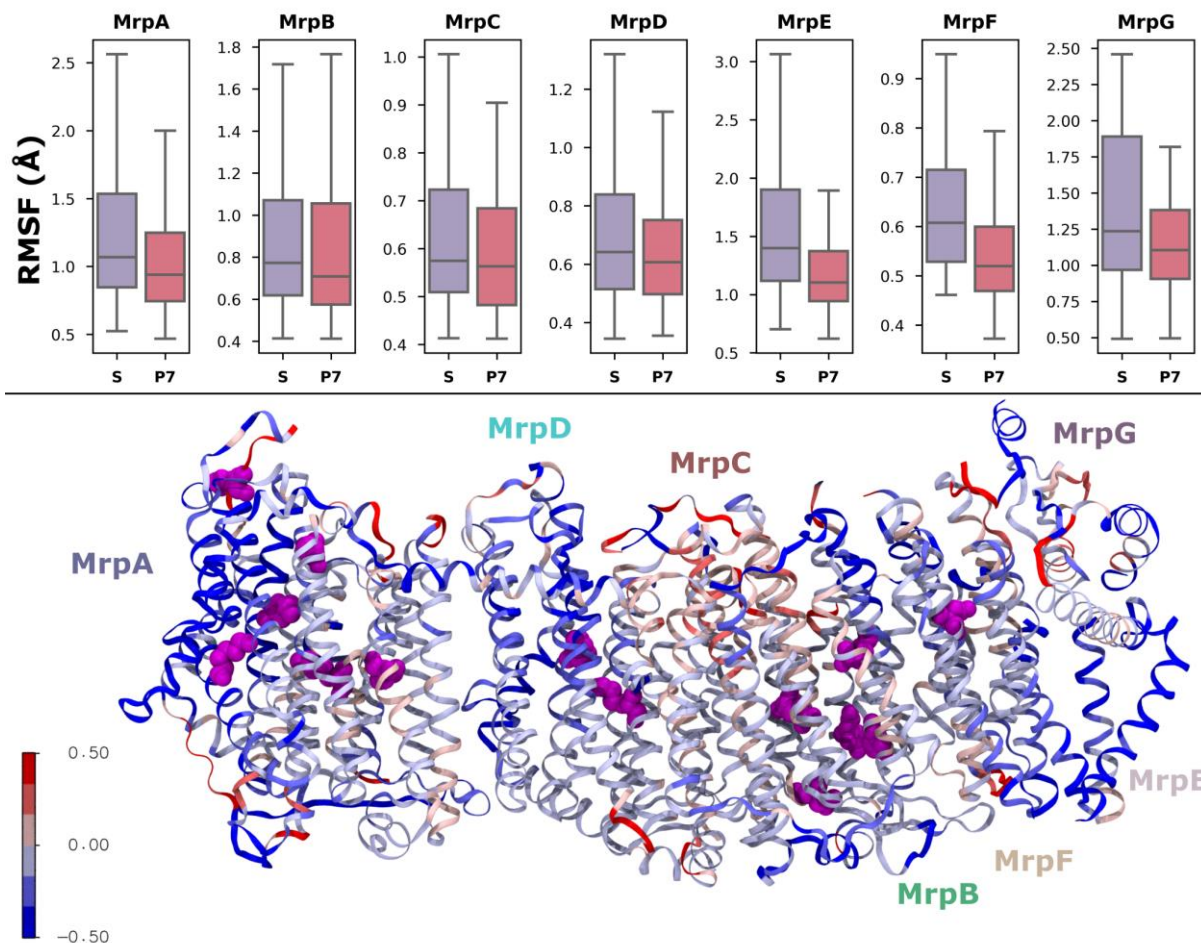
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190 **Fig. 2** – RMSD (root mean square deviation) of the backbone atoms over time for both
191 complex I (core membrane subunits, left panel) and Mrp antiporter (right panel) in S and P7
192 states. The upper plots show the RMSD as a time series, with each colored trace representing
193 a different simulation replica. The thick lines show the moving average of 20 ns, while the
194 thinner lines show the RMSD for every 1 ns. The bottom panels show the distribution of RMSD
195 values in the S and P7 states using a kernel density estimate (KDE) function with combined
196 data of all three replicas.

197

198 Similarly, the RMSF (root mean square fluctuation), which measures the average amount an
199 atom moves during the entire simulation, is also consistently found to be lower in the P7
200 states than in the S states. The boxplots in Fig. 3 show the RMSF of C α atoms in each individual
201 subunit of the Mrp antiporter. For all antiporter chains, lower RMSF values are observed in

202 the P7 state, indicating that there is an overall stability in the system as charges of titratable
203 sites are neutralized (based on pKa estimates). A similar trend was also observed in complex
204 I (Fig. S2). The spatial distribution of the RMSF data is shown in the lower panel of Fig. 3. MrpA
205 subunit (Figs. 1 and 3) has the largest number of titratable residues that undergo protonation
206 state changes to become neutralized and this has a clear impact in reducing the RMSF of the
207 subunit. Interestingly, the stability of the protein also increases in areas somewhat far from
208 the residues that change protonation states (magenta spheres), highlighting that the charge
209 change of just a few titratable residues can have conformational changes imparted both at
210 the local and the global level.



211
212 **Fig. 3** – (Top) RMSF (root mean square fluctuation) of α atoms in Mrp antiporter subunits,
213 calculated for all simulation data in S and P7 states. The box plots represent the distribution
214 of RMSF values for each subunit, in both states. The shaded box represents the interquartile
215 range, with the middle line showing the median. The upper and lower lines are the maximum
216 and minimum values respectively. (Bottom) The panel shows the protein structure colored
217 according to the extent of conformational change in the P7 state compared to the S state.
218 Red represents α RMSF increased in the P7 state and blue represents a decrease. The
219 magenta spheres show the positions of residues that undergo a protonation state change in
220 P7 simulations.

221
222 Overall, the key observation is that MD simulations performed in predefined protonation
223 states retain a structure closer to the cryo-EM conformation for both protein complexes
224 studied here. This in turn means that the simulated charge state is closer to the charge state

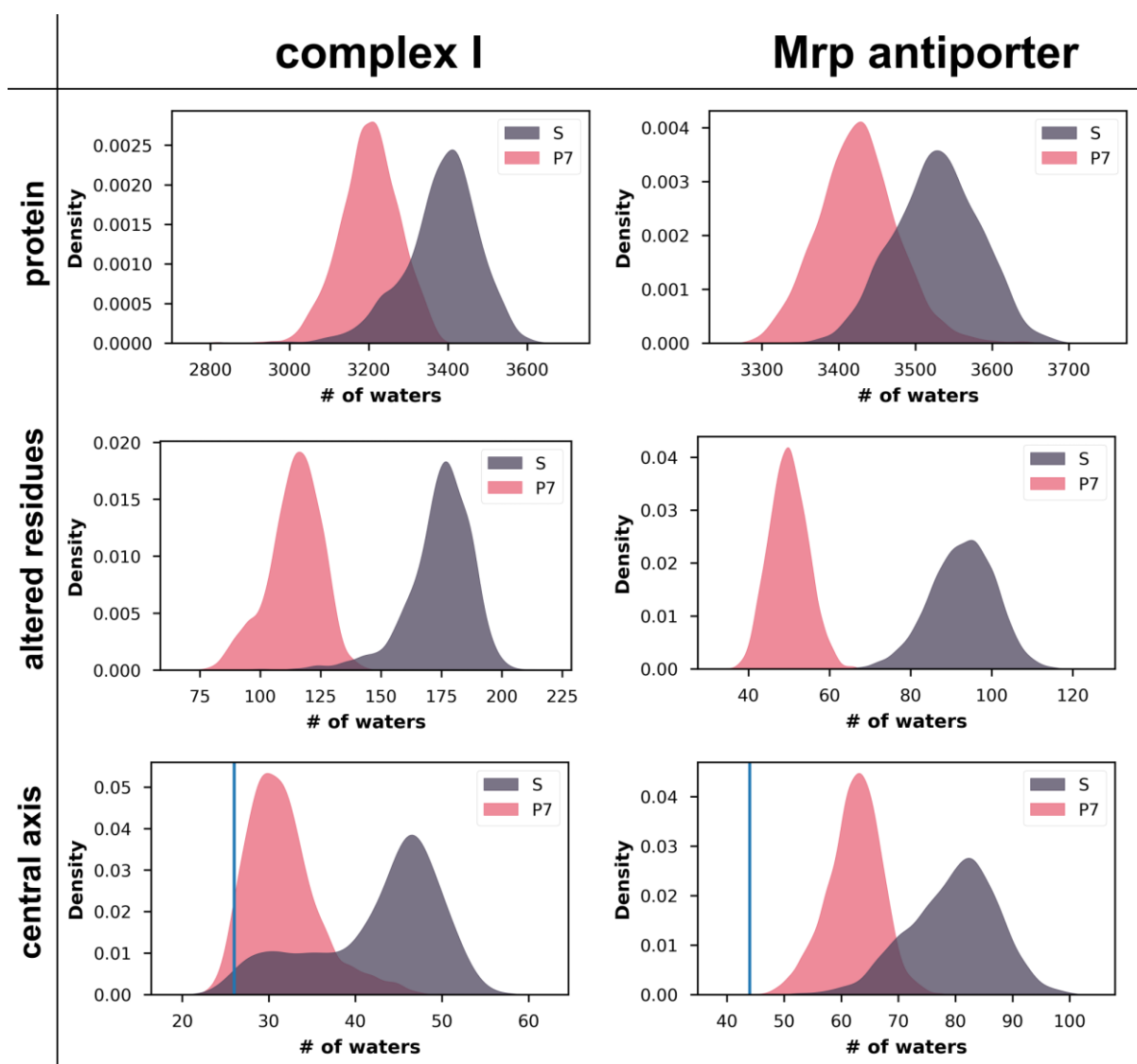
225 of the protein during cryo-EM sample preparation. To understand why P7 state simulations
226 show overall stability relative to the S state, we performed additional analyses.

227

228 **Water-protein interactions and protein hydration in P7 and S states**

229 In the high-resolution structures of complex I and Mrp antiporter, the positions of several
230 water molecules are resolved. We therefore next analyzed how water-protein interactions
231 and protein hydration are affected in the S and P7 simulation states. The contacts between
232 all water molecules and protein were clearly reduced in the P7 states compared with the S
233 states (Fig. 3, upper panels). The lower charge in P7 states (+83/-76 compared to +90/-94 in
234 S state of complex I and +110/-112 compared to +116/-118 in S state of Mrp antiporter)
235 prevents extensive hydration of the protein resulting in lower number of contacts between
236 water oxygens and protein. This is also reflected in the clear reduction of water contacts that
237 take place with the residues that change protonation state (Fig 3, middle panel).

238



239

240 **Fig. 3** – KDE plots for the number of water oxygen atoms in contact within 4 Å of protein
241 residues, with the left column showing data for complex I (core membrane subunits) and the
242 right for Mrp antiporter. Top panels show the number of waters in contact with all protein
243 atoms, middle panels show for protein residues that change protonation state in P7 state
244 simulations, and lower panels show the number of waters in contact with residues in the

245 functionally relevant horizontal axis (Fig. 1). Blue vertical lines in the lower panels indicate the
246 number of waters resolved in the cryo-EM structures that are in contact with the residues in
247 the central hydrophilic axis.

248

249 In both proteins, a hydrophilic axis runs through the central part of the membrane domain,
250 which is thought to be the structural basis for proton transfer reactions⁴³⁻⁴⁸. We next
251 evaluated the time evolution of internal water molecules in this hydrophilic axis for both
252 states in both proteins. We observed that the number of internal water molecules in the P7
253 state remains lower and closer to the water content observed in the structures, whereas in S
254 state runs, extensive hydration of the proteins is observed (Fig. 3, lower panel and Fig. S3).

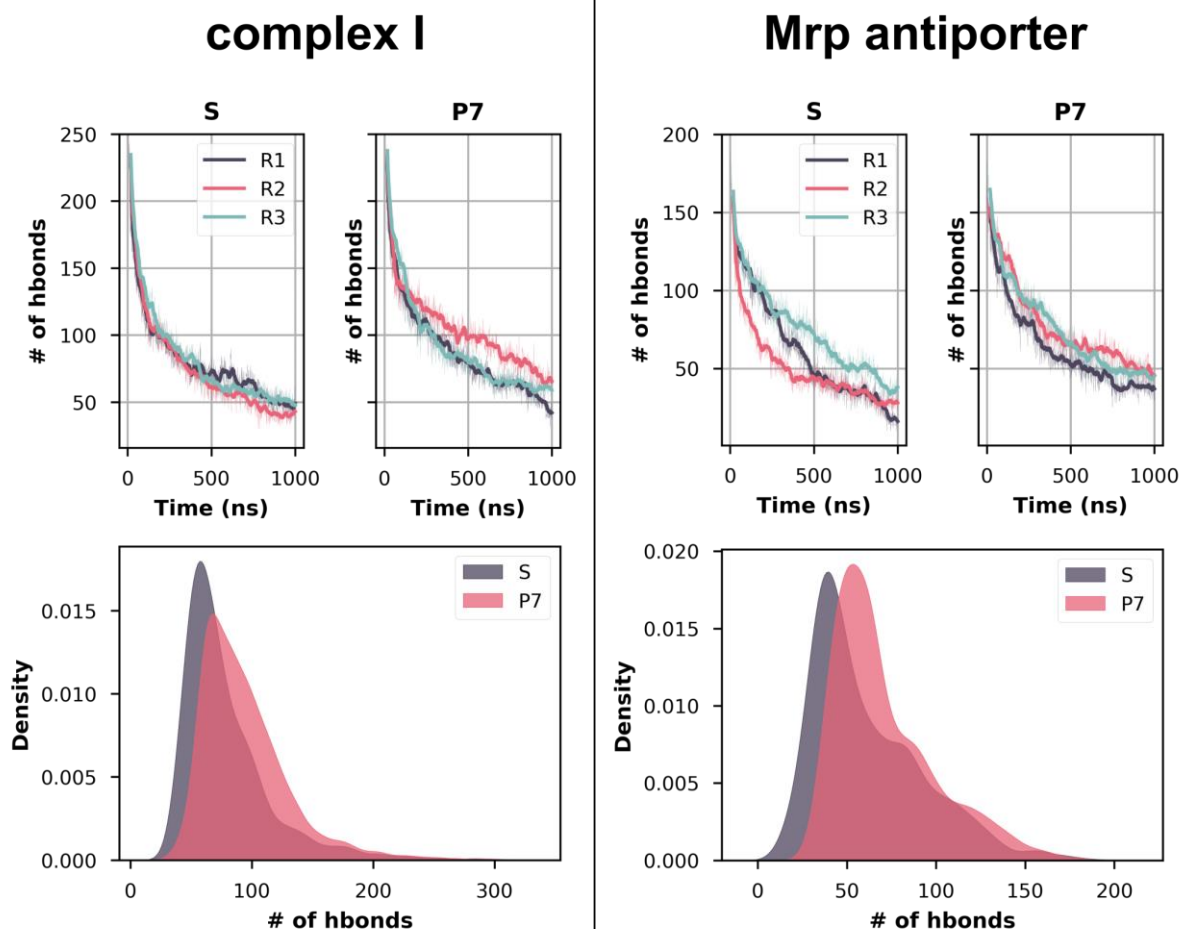
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256 Next, we analyzed the hydrogen bonding between the water molecules and the protein. The
257 time evolution of the hydrogen bonds between protein and structurally resolved water
258 molecules showed a more rapid decline in S states compared to the P7 states, with the latter
259 also displaying a slightly higher number of such interactions in long time scales (Fig. 4). This
260 indicates that although water exchange does take place in the P7 state, the exchange is less
261 rapid and a greater number of hydrogen bonds that existed in the initial structural state are
262 maintained for long time scales. The stable water-protein hydrogen bonds combined with
263 lower hydration in the P7 state also suggests a lower water exchange rate in these
264 simulations. The details of which protein-structural water hydrogen bonds are stabilized in
265 the Mrp antiporter is shown in Table S3, and notably the stabilization of these hydrogen bonds
266 is associated with a decrease in RMSF.

267

268 In Mrp antiporter, in the S state most structural waters loose hydrogen bonds with the protein
269 residues in the μs time scale, whereas in P7 state the loss is relatively slower and less
270 extensive in the given time scales (Fig. 4). Interestingly, the loss of hydrogen bonds is much
271 more drastic in complex I simulations, especially in the shorter time scales. To further probe
272 into the kinetics of loss of hydrogen bonding between the structural waters and protein, we
273 fitted the profiles (Fig. 4, upper panels) to exponential function (see methods) and obtained
274 the half-life of protein-water hydrogen bonds ($t_{1/2}$). The results show that on average in
275 complex I P7 state hydrogen bonds survive longer (average $t_{1/2} \sim 162$ ns) compared to S state
276 (average $t_{1/2} \sim 113$ ns). For relatively shorter time scales (ca. 500 ns), a more subtle but similar
277 effect was also observed for Mrp antiporter simulations (average $t_{1/2} \sim 135$ ns in S state
278 compared to ~ 145 ns in P7 state).

279



280
 281 **Fig 4** – Hydrogen bonds between protein and structural water molecules. (Top) The number
 282 of hydrogen bonds throughout the S and P7 simulation trajectories are shown as a time series.
 283 The different colors of traces represent different simulation replicas. (Bottom) The data from
 284 all trajectories is shown in the lower panels as a density. Only the core membrane subunits of
 285 complex I were considered for analysis. The hydrogen bonding distance was cut off at 3.5 Å
 286 and the angle at 150°.

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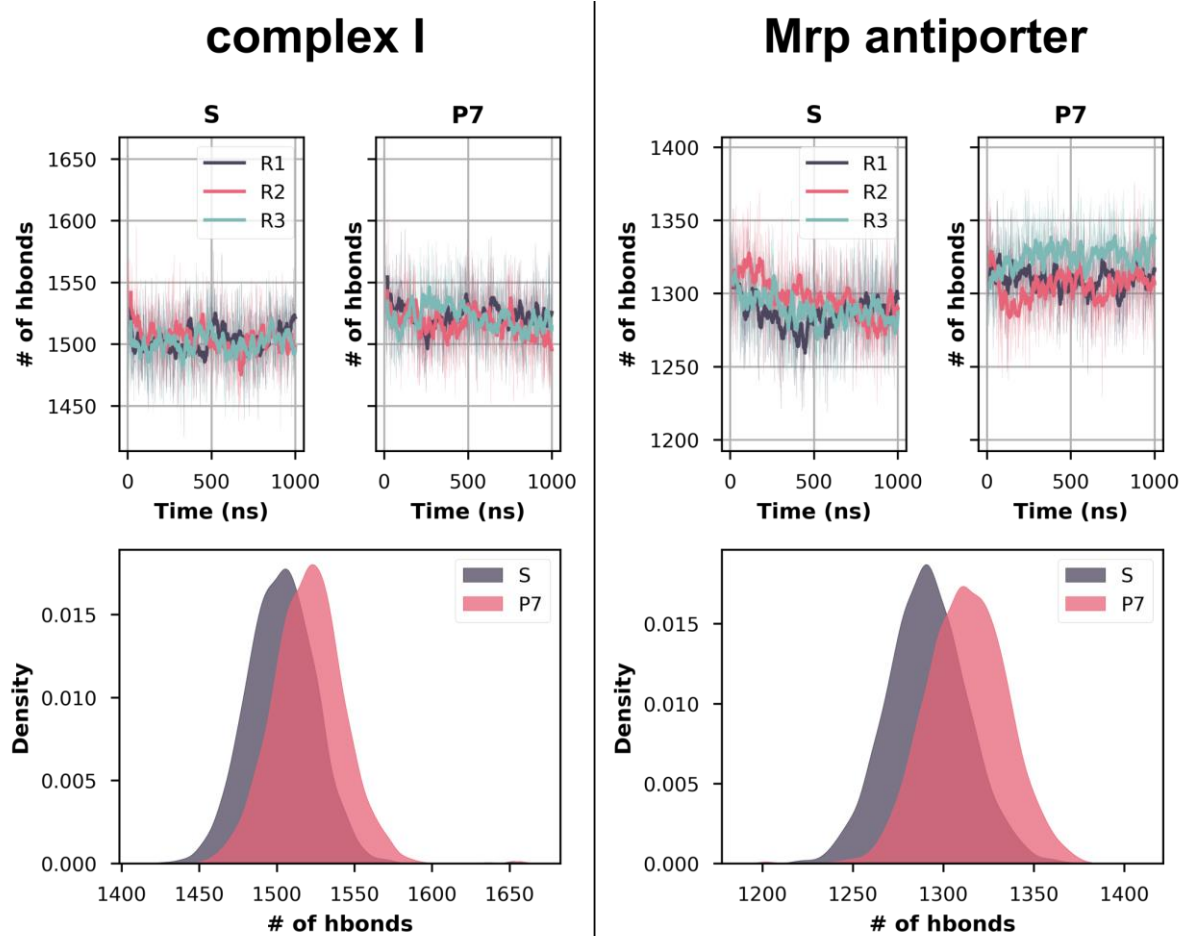
288 Protein-protein interactions

289 In addition to the protein-water hydrogen bonding interactions, protein-protein hydrogen
 290 bonds were also analyzed. The number of protein-protein sidechain hydrogen bonds are
 291 consistently found to be higher throughout the P7 state trajectories (Fig. 5). This implies that
 292 structural stability is higher in P7 states compared to the S states for both Mrp antiporter and
 293 complex I, as also observed in RMSD and RMSF analysis (see above). The lower number of
 294 protein-protein interactions is also in agreement with the higher level of hydration observed
 295 in the S state. In other words, enhanced water entry/exit in the protein causes protein-protein
 296 interactions to be perturbed, resulting in structural destabilization. Specific pairs of residues
 297 from the Mrp antiporter that showed a significant increase (>50 %) in hydrogen bonding are
 298 shown in Table S4. Interestingly, although only two of the residue pairs undergo changes in
 299 protonation state between S and P7 states, still several other pairs show enhancement in
 300 hydrogen bonding occupancy, pointing out that long-range effects can occur upon charge
 301 change.

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303

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305

306 **Fig. 5** – Number of hydrogen bonds between protein sidechains throughout the simulation
307 for complex I and Mrp antiporter. Top panels show the time evolution of all hydrogen bonds
308 for three different simulation replicas, with the hydrogen bonding distance cut off at 3.5 Å
309 and the angle at 150°. Bottom panels show the same data as KDE plots. In case of complex I,
310 only core subunits of the membrane arm are considered (see Fig. S4 for full protein).

311

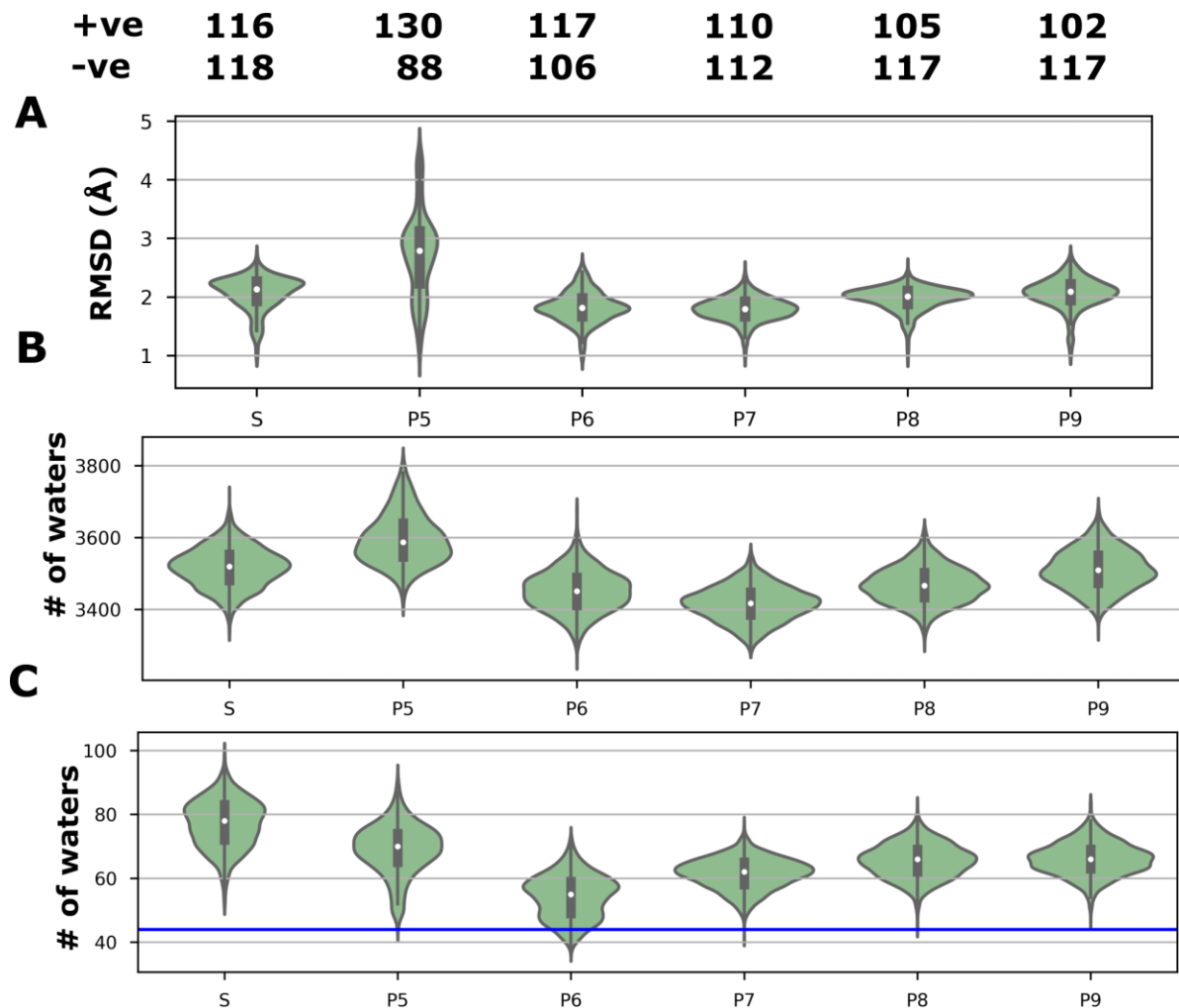
312 The above data on protein dynamics and hydration, as well as hydrogen bonding analysis in
313 two different charge states lead to the conclusion that higher protein fluctuations are caused
314 by extensive hydration, which in turn is caused by the highly charged state of the protein, as
315 in the S state. The correct (or near-to-correct) charge state of the protein is thus critical for
316 its structural stability. Hence, prior to launching long time scale MD simulations of high-
317 resolution membrane proteins, a proper charge analysis by means of pKa calculations is
318 recommended.

319

320 Simulations with different pH values

321 It is clear from the above analysis that the protein simulations that have charge states defined
322 by predetermined protonation states of titratable residues set at pH 7 are well-behaved and
323 are closer to the conformation obtained from cryo-EM. This is true for both global and local
324 mobility, as well as protein hydration. To further explore how altering protonation state
325 affects these characteristics, we performed a series of simulations of the Mrp antiporter
326 complex at 4 more pH values: 5, 6, 8, and 9. The RMSD of the protein (Fig. 6A) was lowest at
327 pH 6 and pH 7, with pH 5 showing the most instability. Similarly, both the number of water

328 molecules in contact with protein (Fig. 6B) and the number of water molecules in the central
 329 hydrophilic axis (Fig. 6C) was lowest for pH 6 and pH 7, with pH 5 deviating the most. At pH 5,
 330 many of the negatively charged residues become neutral, and positive residues stay positive.
 331 Importantly, many histidine residues become doubly protonated, which introduces excess
 332 positive charge in several regions of the protein. As a result, bulk water molecules enter the
 333 protein, causing instability in protein sidechains and loops, even more than in the S state.
 334
 335



336
 337 **Fig. 6** – Comparison of Mrp antiporter MD simulations with protonation states set at different
 338 pH values. Panel A shows the RMSD of backbone atoms, panel B shows the number of water
 339 molecules within 4 Å of all protein residues, and panel C shows the number of waters in
 340 the functionally relevant central axis (Fig. 1), with the blue line showing the number of waters in
 341 contact with protein observed in the cryo-EM structure. Data is shown as violin plots, where
 342 the shaded area is a KDE plot of all trajectory data and in the center is a box plot displaying
 343 the median (white dot with the black box indicating the interquartile range). The total number
 344 of positively and negatively charged residues at different pH are listed above panel A.
 345

346 **Charge state assignment based on cryo-EM density**

347 The above analysis highlights the importance of correct charge state description of protein,
 348 which is necessary for its stability during MD simulations. However, prediction of charge state
 349 by pKa calculations has its limitations. We thus attempted to deduce the protonation states

350 of amino acids from the high resolution cryo-EM data. Cryo-EM density maps can be used to
351 identify the charge states of acidic amino acid residues (glutamates and aspartates), because
352 neutral and negatively charged atoms have vastly different scattering amplitudes^{14, 17} and
353 thus different cryo-EM density profiles. By carefully analyzing the cryo-EM density in our high-
354 resolution maps, we obtained the charge states of selected glutamate and aspartate residues
355 and compared those to the pKa values obtained based on the modeled structure. We found
356 that there was an agreement between the charge state assignment based on the cryo-EM
357 maps (EMD-12742 for complex I and EMD-14124 for the Mrp antiporter) and the predicted
358 pKa based on the derived atomic models (PDBs 7O71 and 7QRU, respectively). However,
359 several acidic residues showed discrepancies; the pKa calculations predicted some
360 carboxylates to be charge neutral that were assigned to be anionic by the cryo-EM density
361 analysis (Table 1). A possible explanation for this discrepancy is that although the protein
362 model-based pKa predictions are largely correct (especially for buried residues), the positions
363 of the (invisible) sidechains of charged glutamates and aspartates were incorrectly modeled,
364 resulting in overestimated structure-based pKas. To fix this discrepancy between the two
365 estimates, the cryo-EM density map of respiratory complex I (EMD-12742) was revisited. We
366 remodeled the sidechains of selected residues that are predicted to be anionic based on
367 missing cryo-EM densities using Coot⁴⁹ and re-performed the pKa prediction on the new
368 model. A total of 7 glutamates and aspartates were remodeled one at a time (Table 1).
369

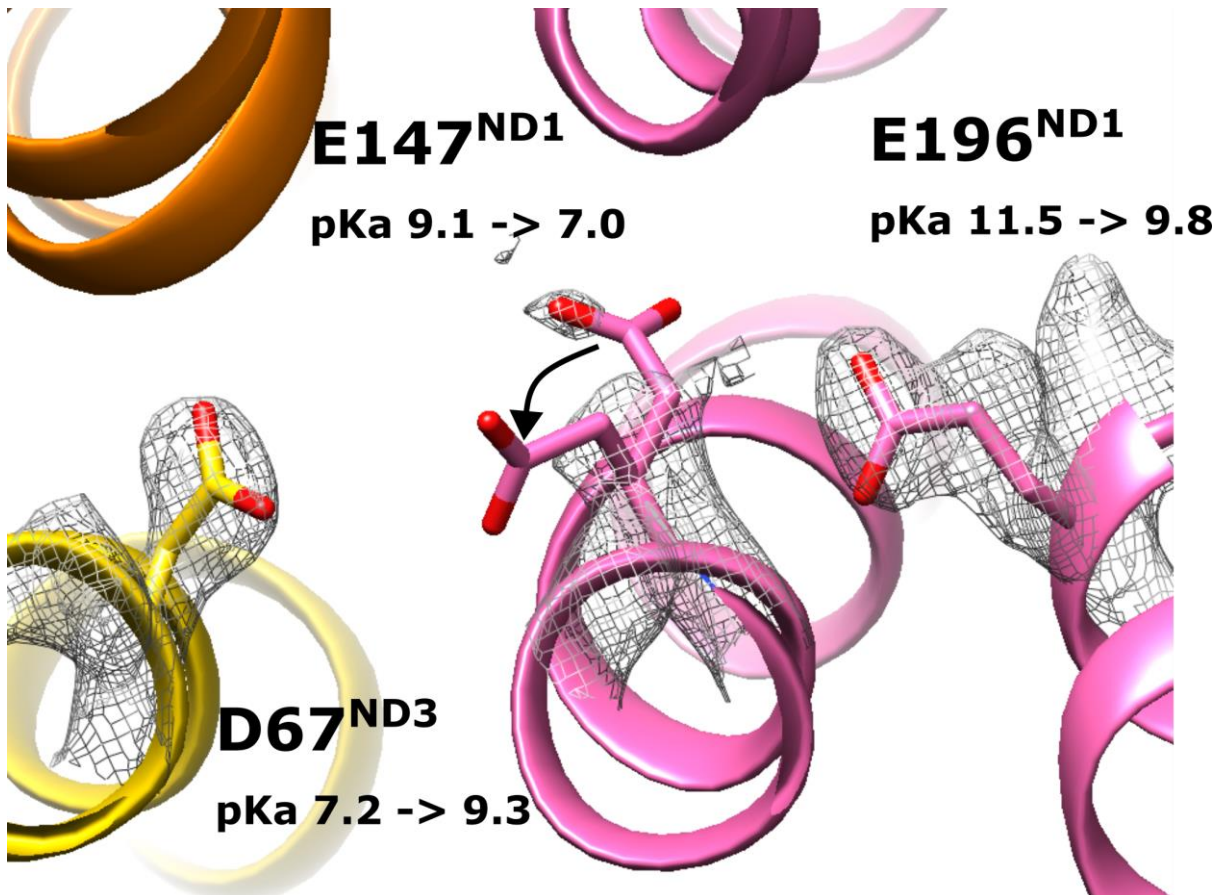
370 **Table 1** - Charge state of selected acidic amino acid residues in complex I from cryo-EM
371 density data (EMD 12742) and pKa calculations, based on PDB 7O71 coordinates or on a
372 remodeled carboxylate sidechain. All carboxylates were remodeled independently.

373 ^a D67^{ND3} was not remodeled, but instead the new pKa value is based on the structure with
374 E147^{ND1} remodeled.

	Density charge estimate	Original pKa	Remodeled pKa
E147 ^{ND1}	Charged	9.11	7.03
E206 ^{ND1}	Charged	8.85	6.37
E210 ^{ND1}	Charged	7.96	5.69
E231 ^{ND1}	Charged	7.44	6.56
D67 ^{ND3}	Neutral	7.18	9.34 ^a
E69 ^{ND3}	Charged	9.27	9.16
E30 ^{ND4L}	Charged	7.59	8.69
E66 ^{ND4L}	Charged	9.81	10.16

375
376 The residues E231^{ND1} and E147^{ND1} of the functionally relevant E-channel in complex I⁴³ were
377 both predicted to be neutral based on pKa calculations but charged based on density analysis.
378 When pKa calculations were performed on re-modeled sidechains, it led to a drop in their
379 sidechain pKa and stabilization of their deprotonated states in good agreement with cryo-EM
380 density-based assignment (Table 1). Interestingly, the remodeled sidechain conformation of
381 E147^{ND1} not only improved the pKa of the residue itself, but also that of residues in its
382 surroundings, e.g. D67^{ND3} (Fig. 7, Table 1). A similar improved agreement between pKa
383 prediction and cryo-EM-based charge state assignment was also observed for E206 and E210
384 from the ND1 subunit (Table 1), both of which are known to be central for protein function
385 ⁴³. However, pKa predictions of E30 and E66 from ND4L, as well as E69 from ND3 could not be

386 improved despite their remodeled sidechains. One potential reason for this could be that the
387 surroundings in two different conformations do not differ as drastically as in the other cases.
388 Furthermore, the approximate nature of pKa predictions is well known, and with no explicit
389 treatment of neighboring solvation can result in the overestimation of pKa values. All in all,
390 remodeling of several sidechains not only improved the charged state assignment, but also
391 improved the atomic modeling of cryo-EM density data (see discussion).
392



393
394 **Fig 7** - The remodeling of the sidechain of E147^{ND1} (indicated by black arrow) improved its pKa
395 as well as that of neighboring D67^{ND3}. The first value of pKa is based on the original
396 coordinates (PDB 7O71), while the second value is after remodeling the sidechain of E147^{ND1}.
397 The cryo-EM density of the three residues is shown as grey mesh.
398

399 Discussion

400 Protonation states of amino acids play a key role in protein structure stability and function.
401 However, it is extremely challenging to obtain an accurate estimate of the pKa of an amino
402 acid both by experiments and computations, and as a result in most cases, pKa values and
403 how they change during enzymatic action remains unknown. Because of this, MD simulations
404 are often performed by modeling amino acids in their fixed protonation states, including
405 standard charged states. Here we show that MD simulations of a membrane protein with all
406 amino acids modeled in their standard charged states results in lower stability of the protein
407 overall and drives the conformation of the protein far from its starting point that is the cryo-
408 EM conformation. Instead, if MD simulation is performed by fixing the charged states of
409 titratable amino acids based on pKa calculations, the conformational state remains closer to

410 the original structure. Our analysis of protein mobility and hydration, as well as residue-water
411 and residue-residue interactions supports this notion. Also, since the structural conformation
412 is retained in MD simulations performed after pKa calculations, we propose these more
413 closely match the charge states of amino acids that existed during the cryo-EM experiment.

414

415 Our results also indicate that the relationship between protein stability and hydration is
416 strong, and that reduced hydration leads to a more stable simulation system which can
417 maintain important interactions. When leaving all protonatable residues in their standard
418 charged states, hydration is considerably enhanced, resulting in important protein-protein
419 interactions being broken, thereby reducing stability.

420

421 The higher level of hydration observed in standard state simulations is primarily due to the
422 charged states of buried titratable amino acid residues. These charged amino acid residues in
423 the low protein dielectric interior create an unfavorable high-energy scenario due to poor
424 solvation. This establishes an electric field, pulling bulk water molecules into the protein and
425 enhancing solvation similar to the nanoscopic electroporation described earlier⁵⁰, see also³³.
426 We also note that protein hydration obtained from MD simulations performed in pre-defined
427 charge state is much closer to the structural hydration than that from the MD simulations
428 performed in standard state of the residues. Despite this, the hydration obtained from MD
429 simulations is in general higher than the hydration observed in the structure. The reason for
430 this discrepancy is in part due to the underestimation of protein hydration in the cryo-EM
431 maps, where only highly occupied and tightly bound water molecules can be observed.

432

433 By performing MD simulations in pre-determined charge state from pKa calculations, one not
434 only investigates the state that was captured during structure resolution, but also its time
435 evolution more accurately. This is particularly useful in situations where there are a
436 particularly large number of titratable residues present in the protein with possible functional
437 relevance, such as in photosynthetic and respiratory enzymes, as well as proteins that couple
438 translocation of ions or metabolites to proton transfer reactions. However, empirical pKa
439 calculations or more thorough continuum electrostatics based pKa estimations have limited
440 accuracy and site-site interaction energy terms can often dominate, leading to large scale pKa
441 shifts with subtle changes in structure. Thus, it is important to use an accurate input model,
442 based on high-resolution data where there is less uncertainty in sidechain placements. Below
443 ~2.5 Å resolution the correct rotamers of most sidechains can be confidently modeled, with
444 the key exception being negatively charged sidechains in cryo-EM maps, which have negative
445 atomic scattering factors^{13, 17, 18} and thus are usually invisible beyond the Cβ atoms. As
446 modeling and refinement programs do not take this into account, the sidechain orientation
447 of these residues is unreliable¹⁸. On the other hand, this fact makes it possible to deduce the
448 charge state of acidic residues from the cryo-EM density.

449

450 Here we propose a method that may assist to improve modeling of sidechains of acidic
451 residues. By performing fast empirical pKa calculations on the 3D model, pKas of all acidic
452 residues can be estimated. If the predicted pKa value suggests a neutral state of an acidic
453 residue that is expected to be anionic based on density analysis, this warrants remodeling of
454 the sidechain of the amino acid. If the remodeled sidechain conformation yields a lower pKa,
455 this is likely to be the more accurate conformation. By combining pKa calculations with
456 sidechain remodeling on selected acidic residues of complex I, we show here that this is

457 feasible. In our future work, we aim to automate this process and obtain more accurate
458 models of sidechains of acidic amino acid residues from the cryo-EM data.
459

460 **Methods**

461 We performed all-atom molecular dynamics simulations of complex I from *Yarrowia lipolytica*
462 (PDB: 7O71)⁴³ and Mrp antiporter from *Bacillus pseudofirmus* (PDB: 7QRU, altloc B)⁴⁴. Both
463 proteins were placed in a mixed lipid bilayer and solvated with TIP3P and NaCl. Gromacs
464 versions 2020 and 2021⁵¹ were used for minimization, equilibration, and production runs.
465 Full details of the molecular dynamics set ups can be found in previous work on complex I⁴³
466 and Mrp antiporter⁴⁴. The production runs were performed without any constraints in an NPT
467 ensemble, using Nosé–Hoover thermostat^{52, 53} at 310 K and Parrinello–Rahman barostat⁵⁴ at
468 1 atm. We employed the LINCS algorithm to achieve a 2 fs timestep⁵⁵, and the particle-mesh
469 Ewald method⁵⁶ with a cut-off of 12 Å to handle electrostatic interactions. The cut-off for van
470 der Waals interactions was 12 Å, with a switching distance of 10 Å. Table S5 lists the
471 simulations setups, and the S and P7 states for complex I and Mrp antiporter are extended
472 simulations from previous work. The P5, P6, P8, and P9 simulations of Mrp are new systems
473 constructed using the same protocol.

474

475 Estimates of pKa were performed using the Propka software package³⁹. The calculations were
476 performed on the PDB structures of both complex I and Mrp. Asp, Glu and His were
477 considered protonated (neutral) if their pKa was more than 7 in the P7 simulations, while Lys
478 was considered deprotonated if its pKa was less than 7. The same process was performed in
479 the P5, P6, P8, and P9 setups, with their respective pKa cutoffs changed. His was considered
480 with the δ -nitrogen protonated when neutral.

481

482 Exponential fit of hydrogen bond decay was calculated using the SciPy *curve_fit* function⁵⁷.
483 We used a mono-exponential of the form $y = me^{(-tx)} + b$, where m, t, and b were
484 parameters that could vary. The quality of the fit was determined using R², obtaining values
485 > 0.9. The half-life was calculated as $t_{1/2} = t \times \ln 2$.

486

487 The electron density analysis and remodeling of the resolved structures was done using
488 Coot⁴⁹. The change in the glutamic and aspartic acid conformations was achieved with the
489 rotamers function in Coot. The key requirement for the new position of the sidechain was a
490 substantial deviation from its previous position, as well as avoiding clashes with its
491 surroundings. Care was taken not to position the side chain in positive density.

492

493 Visualization, analysis, and figure preparation was performed using VMD, Pymol and UCSF
494 Chimera⁵⁸.

495

496

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