Hetero-crystal, a layer-building intermetallics: case studies of the 1144-phase TM-phosphides $AB(TM)_4P_4$ (TM=Fe, Ru, Co, Ni)

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The discovery of the 1144-phase, e.g. CaKFe₄As₄, creates opportunities to build novel intermetallics with alternative stacking of two parent compounds. Here we formalize the idea and introduce a concept, namely hetero-crystals (HC), to describe a unique class of bulk crystalline solids with such A-B stacking (including 1144-phases and beyond). HC generalizes hetero-structures from few-layer or thin-film semi-conductors to bulk intermetallics. We illustrate the HC concept with the example of 1144-phases. Theoretically, four families of phosphides $AB(TM)_4P_4$ (TM=Fe, Ru, Co, Ni) are investigated by first-principles calculations, wherein configurational, vibrational and electronic degrees of freedom are considered. It predicts a variety of stable 1144-phases (especially Ruand Fe-phosphides). Stability rules are found and structural/electronic properties are discussed. Experimentally, we synthesize high-purity CaKRu₄P₄ as a proof of principle example of such a HC. The synthetic method is simple and can be applied to other HC. Moreover, HC alludes to a new strategy to explore complex multi-component compounds, facilitated by a new phase diagram coordinated by collective descriptors.

1. INTRODUCTION

Breakthroughs in synthesis could evoke new material concepts. For example, graphene together with a variety of single-layer structures have substantiated and popularized the 2-D materials [1]. On the other hand, varying the attributes affiliated with existing conceptions could help discover new types of compounds. For example, the finding of high-entropy alloys (HEA) [2, 3] was motivated by the idea of tuning the number of alloy constituents and concentrations, which are two basic attributes based on present concepts of alloys. Such synthesis-conception duality is essential for material development, and the dual aspects are mutually inspiring. The recent discovery and study of $AeAFe_4As_4$ (A = alkali, Ae = alkalineearth) 1144-phase compounds [4–11] is such an example. Its synthesis implied creating quaternary compounds by judicious combinations of related ternary materials AFe_2As_2 and $AeFe_2As_2$; on the other hand, choosing and varying the cation attributes can yield broader intermetallic compounds, namely hetero-crystals (HC), as conceptualized in this work.

The 1144-phase (Fig. 1(a)) can be regarded as alternating cation layers in the 122-phase being replaced by hetero-cations [4]. Stoichiometrically, it is equivalent to 50% doping of $AeFe_2As_2$ by A (or A by Ae). However, the ordered substitution sets it apart from randomdoping alloys [12–14] and poses an intriguing conjecture: such ordered quaternary compounds might widely exist for the right combination of building blocks. Compared with 122-phases, 1144-phases feature distinct parameters (e.g., bonding angles, pnictogen heights) above and be-

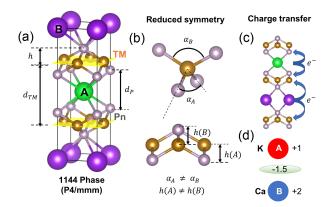


FIG. 1. (color online): (a) The crystal structure of the 1144phase. If A, B sites are occupied by the same cations, it becomes the 122-phase (b) Structure parameters with broken glide symmetry. (c) Charge transfer from cation-layers to TM-layers. (d) Schematic charge distribution of KCaRu₄P₄. The layers of K⁺ and Ca²⁺ take positive charges; each TMlayer takes -1.5e per unit cell. Pn stands for pnictogen and TM stands for transition metals

low the transition metal (TM) layer (Fig. 1(b)). Consequently, the *n*-glide plane across the Fe-layer disappears, and the space group is reduced from I4/mmm in 122phases, to P4/mmm in 1144-phases [8]. This fact might be relevant to the emergence of hedgehog spin textures [7], low-dimensional superconductivity (SC) [11], FM-SC coexistence [15], suppressed T_c with pressure [16], and disputed nematic behavior [7, 14, 17, 18]. Besides, the 1144 crystal surface has been suggested to be a platform for testing the Majorana zero modes [19, 20].

The 1144-phase is a representative of "ordered stacking" [21], instead of random substitution. A variety of HC can be designed and built by properly combining cation- and TM-layers. Compared with alloys, which mix elementary atoms into a solid solution (SS), HC use layers as basic units and pack them into certain ordered pattern. Since interesting phenomena (e.g., SC [7, 9, 11], magnetism [15]) usually arise from *d*-orbitals in TM-layers, the most revealing view of HC is that the TM-layer resides in between two hetero-cation layers (Fig. 1(a)). It is reminiscent of 2-D materials being sandwiched by the substrate and vacuum. Varying species of hetero-cations serves as attributes for HC to adjust chemical potentials and symmetry, just like choosing an underneath substrate and on-top dopants as the counterpart tuning for graphene [1, 22]. The pnictogen height h (Fig. 1(a)) exhibits considerable asymmetry on different sides with 5%-10% changes compared with 122-phases. The manipulation could be further enriched by the diverse candidates for substitution: Ru-Si [23], $VO_2[24]$ for TM-layers; and A, Ae, rare earth (RE) for cation layers [25].

The paper is organized as follows. Sec. 2 introduces the concept of HC. Sec. 3 explores the 1144-phase, a typical HC. Four families of phosphides $AB(TM)_4P_4$ (TM=Fe, Ru, Co, Ni) are chosen to be investigated. We discuss their formation conditions at zero and finite temperatures, accounting for the configurational, vibrational, and electronic degrees of freedom. A number of 1144-compounds (especially Ru- and Fe-based phosphides) are predicted to be stable. Other questions are also examined regarding the stability mechanism, electronic structures, and latent features of the 1144 crystals. Sec. 4 presents our work of synthesizing high-purity KCaRu₄P₄. Its structure is determined as a proof of principle example. In Sec. 5, we survey that HC are broadly existent, tuning-friendly, and of versatile physical properties, such as interplay of magnetism and superconductivity [26, 27], volume-collapsed phases [28–30], or heavy fermion behaviors [23]. It also presents an avenue for designing complex many-constituent intermetallic compounds beyond ternary alloys.

2. CONCEPT OF HETERO-CRYSTAL

We define HC via four aspects of features.

(i) They are bulk crystals, periodic along the z-axis, in contrast to low-dimensional or thin-film hetero-structures (like super-lattice [31] or tunneling junctions [32]).

(ii) They consist of two sub-systems: cation layers (usually metal elements) and skeleton layers (e.g., TM-pnictogen or TM-chalcogen layers). This not only specifies the architecture, but also affects HC's physical properties. For example, the two sub-systems differ in electronegativity and charge transfer between them (Fig. 1(c)(d)) leads to an ionic type of inter-layer bonding. The TM-layer motif (usually tetrahedron) causes particular hybridizations of d-orbitals that generate partially filled bands, promoting metallic properties and itinerant magnetism [26]. These features are evident distinctions from hetero-structures in the context of semiconductors [32].

(iii) They show an A-B stacking of alternating cation layers (the reason why "hetero" is assigned). As such, the concentration of A (or B) is fixed to 50% and disorder in cation layers is much suppressed. More importantly, the A-B stacking creates asymmetric up-and-down environments and distorts the TM-layer, which could be Fe-Pn, NiO₂ [33, 34], VO₂, and Mo_NO_{3N-1} (N =1, 2, 3...) [24]. The structural change associated with the symmetry breaking is huge compared to that by applying pressure. For instance, our calculation shows that the asymmetry for pnictogen height h (Fig. 1(b)) is up to 5%~10%. Thus it seems plausible that HC will behave distinctively from SS phases with identical stoichiometry.

(iv) HC are formed by combining two parent phases. For example, the 1144-phase can be synthesized by mixing two 122-compounds, as done in this work. In general, the parent phase refers to the phase that has the common skeleton layer as HC, but has mono-cations. It usually requires that the involved parent phases are stable on their own [25]. Condition (iv) suggests that seeking HC should begin with looking for stable parent phases (with occasional exceptions [25]). Hundreds of 122-phases have been synthesized [35], and the reservoir of parent compounds make forming the 1144-phase HC promising.

Besides the four definitions above, it is worth mentioning that although the 1144-phase is quaternary, it is effectively binary, as the main variables are the cations A and B. When the parent phases are mixed, entropy favors random mixing of A and B, forming a uniform SS phase; whereas if an ordered phase occurs, it must have been favored by enthalpy. Thus, the 1144-phase's emergence is closely linked to enthalpy battling with configuration entropy.

3. THEORETICAL RESULTS

3A. Stability of 1144-phase

The 1144-phase is presently limited to Fe-arsenides with cations from the alkali metal group (IA) or alkaline earth group (IIA) [25], and it is highly desirable to extend its chemical scope. Empirical rules for stable 1144phases have been recognized: a large cation-radius mismatch ΔR seems a favorable factor; besides, the lattice mismatch Δa is also relevant [4, 6]. The dependence of the two descriptors ΔR and Δa can be rationalized with the enthalpy change due to elastic deformations [8]. The mechanism is generic, so it applies to Ru-P 1144 systems and other TM-pnictides. On the other hand, descrip-

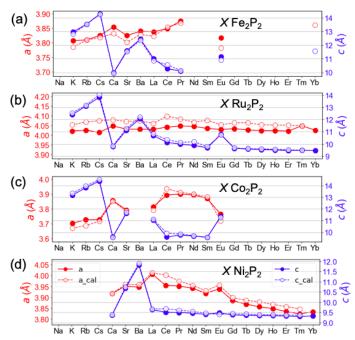


FIG. 2. (Color online): Lattice-parameters a (red) and c (blue) of the tetragonal unit of 122-phases. Filled and open points represent experimental and theoretical values. Missing points are unstable or not reported yet. Experimental results are cited from Springer Materials data base.

tors ΔR and Δa fail to encode charge information (i.e., valence states exhibited by the cation) [21], thus are incapable of treating situations with valence variation, e.g. when trivalent cations rare earth RE³⁺ are introduced. This implies additional descriptors are needed.

We start the search from the parent compounds of 122-phase pnictides, whose lattice parameters (experimental and calculated) are listed in Fig. 2(a)-(d). Notably, 122-phases are unstable with certain cations. The calculation is based on density functional theory (DFT) [36] with Perdew Burke Ernzerhof (PBE) exchangecorrelation functional, implemented by the Vienna ab initio simulation package (VASP). Both the unit cell and internal coordinates are fully relaxed. Calculation parameters are shown in the supplementary information (SI) [37]. The results of the calculated lattice parameters are close to the experimental values for most of systems with differences $\leq 1\%$. Except for Ce-contained 122 phases where lattice parameters are consistently overestimated, probably due to inherent issues of pseudo-potentials in treating variant valences of Ce.

The 1144-phase is achieved by mixing two 122-phases with common skeleton layers (Fig. 2). The reaction merely involves redistribution of cations, either ordered or random. Thus, the question becomes the competition between 1144-phase and 122-solution-phase (122(s)phase) [4, 8]. In general, the simplifying to two-phase competition is guaranteed by condition (iv) defined in Sec. 2, i.e., the existence of stable parent phases. This is indispensable, because having stable parent phases provides good starting points and allows the reaction to be studied in a simpler landscape.

At zero temperature, phase stability is dictated by the formation enthalpy $\Delta H = H_{122(s)} - H_{1144}$. The enthalpy of the ordered phase can be estimated from super-cell calculations within DFT. For the solution phase, however, calculation of enthalpy involves random configurations and we adopt the ideal solution approximation.

$$H_{122(s)} = x \cdot H_{122}^A + (1 - x) \cdot H_{122}^B, \tag{1}$$

where x is the concentration of cation A, and x = 1/2 in this case. The stable 1144-phases ($\Delta H > 5 \text{ meV/atom}$) are summarized in Fig. 3(a) (complete list seen in Sec. 2 of SI [37]) where ΔH is plotted against two descriptors:

$$\Delta a = -|a_{122}^A - a_{122}^B|,\tag{2}$$

$$\Delta c = |c_{122}^A - c_{122}^B| \tag{3}$$

with a and c denoting the lattice parameters of the tetragonal unit cell of parent 122-phases. A number of 1144-phases are found stable, especially for Fe- and Ruphosphides. The stable 1144-phases concentrate in a region of small $|\Delta a|$ and large $|\Delta c|$ (upper right corner of Fig. 3(a)), a tendency aligned with earlier findings [4, 8]. However, a closer inspection shows some discrepancies. For example, the two red hexagons (black arrow) deep in the upper-right corner (CsErRu₄P₄ and CsHoRu₄P₄) are not the most stable albeit they best satisfy the criteria. This implies additional descriptors, as discovered shortly.

At finite temperature, the phase stability is determined by the free energy:

$$\Delta G = G_{122(s)} - G_{1144}$$

= $\Delta H + \Delta E_0 - \Delta S_{conf}T - \Delta S_{vib}T - \Delta S_eT$, (4)

where E_0 is the zero-point vibration energy. S_{conf} , S_{vib} and S_e are configurational, vibrational and electronic entropies, respectively. The configuration entropy S_{conf} for the 1144-phase is zero. The S_{conf} of the 122(s)-phase (per unit cell) is estimated by [38]

$$S_{conf} = k_B (x \log x + (1 - x) \log(1 - x)), \qquad (5)$$

where x is defined in Eq. 1. In this case, S_{conf} is a constant 0.012 meV/(atom K). The electron entropy is estimated by

$$S_e = -k_B \int D(E)(f \cdot \log f + (1-f)\log(1-f)\cdot)dE, \quad (6)$$

where f is the Fermi distribution function and D(E) is the density of states, which are obtained from DFT calculations. Calculations of zero-point energy and vibration

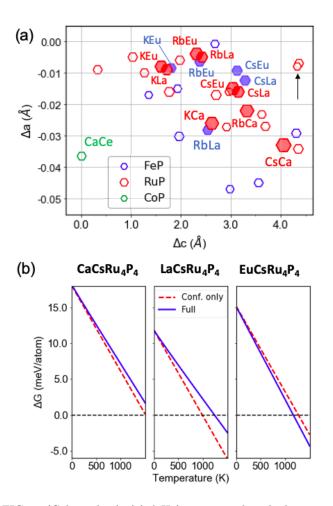


FIG. 3. (Color online): (a) ΔH (proportional to the hexagon size) plotted against two descriptors: $\Delta a = -|a_{122}^A - a_{122}^B|$, $\Delta c = |c_{122}^A - c_{122}^B|$, where *a* and *c* are lattice parameters of the two parent 122-phases $A(\text{TM})_2\text{P}_2$ and $B(\text{TM})_2\text{P}_2$. The most promising systems are highlighted with solid hexagons and the corresponding cations are denoted. (b) Temperature dependence of free energy $\Delta G = G_{122(s)} - G_{1144}$. ($\Delta G > 0$ 1144-phase is stable.) The dashed line only includes S_{conf} . The blue line further includes S_{vib} and S_e .

entropy S_{vib} are performed by the code *phonopy* within the harmonic approximation [39]. For the 122(s)-phase, S_{vib} and S_e are estimated with the average of two 122phases, similar to Eq. 1.

In Fig. 3(b) we plot ΔG as a function of temperature for three typical stable systems. At high temperature, the entropy will eventually bring the ordered 1144-phase into the 122(s)-phase. We define T^* as the temperature where $\Delta G=0$ and, below which, the 1144-phase is stable. Comparing the dashed (only includes S_{conf}) and solid curves in Fig. 3(b), we find that including S_{vib} and S_e modifies minimally the free energy, and thus conclude that the S_{conf} is the main contribution, which is consistent with previous findings [8]. As such, $\Delta H/S_{conf}$ may give a rough estimate of T^* . In Sec. 3 of [37] we provide ΔG calculations for more systems.

3B. General rules of phase stability

The stability of 1144-phases exhibits certain rules. As shown previously, descriptors Δc given by Eq. 3 (or atomic radius mismatch ΔR), and Δa given by Eq. 2, proved useful [4, 8]. They were first exemplified in Fearsenide 1144-systems and understood with an elastic model [8]. Next we will find a descriptor associated with the charge balance between cation layers and pnictogen (Pn) layers, which will subtly affect the 1144/122(s) stability.

The formation enthalpies ΔH of $ABFe_4As_4$ are plotted in Fig. 4(a), which shows that the stability gets enhanced from the lower-left to the upper-right in the graph. Thus, $ABFe_4As_4$ endorse the established rule [4, 8] that the 1144-phase is stabilized with large $|\Delta c|$ and small $|\Delta a|$. However, the rule seems inadequate for Ru-phosphides (Fig. 4(b)), as the stable and unstable systems remain unseparated. To elucidate the situation, we divide these data into subgroups by cation valence states, e.g., I + II(Fig. 4(c)) and II + III (Fig. 4(d)); then the rule manifests itself. Basically, the cation pair affects the stability: group I+II form a stable 1144-phase and II+III do not. Such distinction, obviously, relies on charge balance between the cation layer and TM-layer. In fact, charge balance is a generic factor, which also affects the 122-phases (Fig. 2(a)-(d)). For instance, mono-valence cations do not favor the 122-phase ANi_2P_2 (Fig. 2(d)). On the other hand, tri-valence cations never stabilize AFe_2As_2 (Fig. 2(a)). Note that the favorable charge balance for Ru-phosphides is alkali metal (AI) + alkaline earth (AII)(or AI+Eu), i.e., the effective valence state 1.5+, which is the same as in the Fe-arsenide [8, 25] systems, consistent with the anticipation of iso-valence substitution.

At the same time, the size effect still plays a role, as ΔH manifests a linear correlation with $(\Delta c)^2$ in each subgroup (insets of Fig. 4(c) and (d)). It suggests that the charge effect cooperates with the size effect, for which we formulate the formation enthalpy ΔH as two additive parts regarding the size and charge effects,

$$\Delta H = \Delta H_{size} + \Delta H_{charge} \tag{7}$$

The size part essentially accounts for the elastic energy and could be approximated as [8]

$$\Delta H_{size} = -\frac{1}{4}k_a(\Delta a)^2 + \frac{1}{2}k_c(\Delta c)^2 \tag{8}$$

The term ΔH_{charge} is a function of charge distribution $\rho(r)$, and the exact form could be exceedingly complex. However, it can be simplified in the 1144 scenario by noticing that there are limited choices of $\rho(r)$. Neglecting the minor distinctions due to the lattice constants, the charge distributions of, for instance, CaKRu₄P₄ and SrRbRu₄P₄ should be similar, both of which can be represented by the sketch of Fig. 1(c). Such resemblance

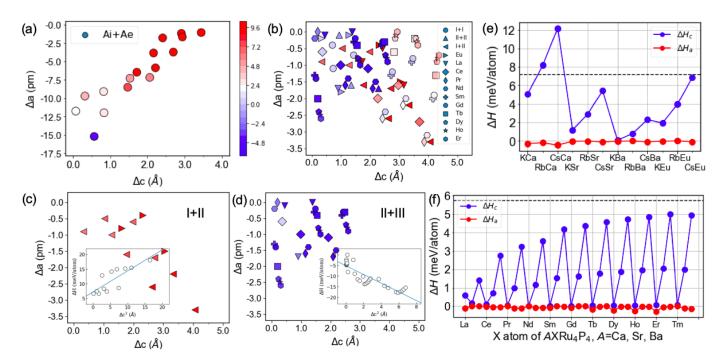


FIG. 4. (Color online): The formation enthalpy ΔH of (a) ABFe₄As₄ with A B being alkali metal (Ai) and Alkaline earth (Ae), (b) of ABRu₄P₄. Each spot represents a particular pair of A-B. Color scales represent ΔH , and red means stable 1144-phase (unit: meV/atom). I+II means alkali metal (AI) plus alkaline earth (AII); II+II means AII+AII; I+II means AI+AII. Eu, La, etc., mean the specific rare earth (RE) combined with another AI or AII. The ΔH of subgroups (c) I+II and (d) II+III. Other subgroups are shown in [37]. The shapes of points are consistent with the legend in (b). (e)(f) ΔH contribution from ΔH_a , ΔH_c and ΔH_0 . The dashed line represents the magnitude $|\Delta H_0|$. Note that ΔH_0 is positive for (e), but negative for (f). The *x*-axis (f) is arranged in an order of lanthanide contraction and ΔH_c is approximately quadratic in tendency.

helps classify 1144-phosphides into 13 groups, by the criterion that the in-group compounds should be composed of the same TM and cation valence (Sec. 5 of SI [37]). For example, BaRbFe₄P₄ belongs to the same group as $CaKFe_4P_4$; however, $BaRbRu_4P_4$ (for distinct TM) and $LaKFe_4P_4$ (distinct cation valence) do not. In each group, the $\rho(r)$ are considered identical. The limited options for $\rho(r)$ reduce the functional $\Delta H_{charge}[\rho(r)]$ to a function that takes 13 distinct values (Table I). Within each group, we assume the ΔH_{charge} being a constant ΔH_0 (positive means favorable for 1144). In all, there are three parameters pertaining to each group: k_a , k_c characterizing size effects in a-b plane and c-axis, respectively; and ΔH_0 characterizing the charge balance effects. These parameters can be evaluated by fitting ΔH obtained from first-principle calculations with Eq. 7 and Eq. 8. The results are tabulated in Table I.

All the groups are consistently yielding $|k_c| \ll |k_a|$, which is due to the common feature of 1144-phases: stronger in-plane bonding and weaker inter-layer bonding. Knowing k_a and k_c , one can straightforwardly evaluate the contributions by the *a*-*b* plane $\Delta H_a = -\frac{1}{4}k_a(\Delta a)^2$, and the *z*-axis $\Delta H_c = \frac{1}{2}k_c(\Delta c)^2$. Let us take Ru-phosphide based 1144 systems as an example. (Results for Fe-, Co-, and Ni-phosphides are found in SI [37].) Despite $|k_c| \ll |k_a|$, ΔH_c is substantially larger than ΔH_a

TABLE I. Force constants $k_a k_c$ and ΔH_{charge} for 13 different subgroups, obtained by fitting Eq. 7 and 8 to DFT results. Units for k and ΔH_0 are meV/(atom·Å²) and meV/atom.

Ru	k_a	k_c	ΔH_0	Co	k_a	k_c	ΔH_0
I+II	1675	1.48	7.17	I+II	2147	-0.69	-6.31
I+III	3395	-0.097	4.34	I+III	-1016	-1.68	-20.93
$_{\rm II+II}$	3816	-1.78	0.39	—			
$_{\rm II+III}$	-10206	-3.92	-5.74	$_{\rm II+III}$	-2632	-4.74	-1.81
Fe	k_a	k_c	ΔH_0	Ni	k_a	k_c	ΔH_0
I+II	4879	0.45	5.51	—			
I+III	4370	-0.24	6.34	—			
$_{\rm II+II}$	1869	-1.18	0.71	$_{\rm II+II}$	15177	-1.43	0.76
II+III	393	-2.44	-3.86	II+III	679	0.06	1.57

(Fig. 4(e) and (f)) due to the fact that $\Delta a \ll \Delta c$. Thus, Δc serves as the primary descriptor for Ru-phosphides; this rationalizes why solely Δc well accounts for the change of ΔH of Ru-phosphides as showed by insets of Fig. 4(c) and (d). (Mind that for general HC, the contribution of Δa is not always negligible, Sec. 4 of [37]).

As for the charge balance, the ΔH_0 of $ABRu_4P_4$ with I+II cations amounts to 7.17 meV/atom, comparable to the total $\Delta H \sim 10$ meV/atom of 1144-phases that have

been experimentally realized [8]. For II + III, ΔH_0 is negative, battling against the positive ΔH_c . However $|\Delta H_0|$ is overwhelmingly larger than ΔH_c . Thus, the instability for II+III is due to unfavorable charge balance, rather than size effects. Note that the iso-valence Fe and Ru, which are fitted independently, yield proximate ΔH_0 in counterparts I+II, II+II, etc. This justifies our approximation of neglecting lattice-parameter effects on $\rho(r)$. In contrast, the iso-valence replacement of Fe by Ru will drastically alter k_a and k_c . The distinct responses for size effects (k_a, k_c) and charge effects (ΔH_0) to TM-replacement is one latent feature of the 1144 phase, for which it is beneficial to separate ΔH in the two terms of Eq. 7. In addition, for the case II + II, 1144-phases share the same charge distribution as 122phases, for which ΔH is contributed solely by size effects and it yields $\Delta H_0 \sim 0$ as expected.

In short, the entangled contributions in ΔH are separated into size and charge effects, which are quantitatively evaluated. The significance hierarchy for Ruphosphide is $\Delta H_0 \simeq \Delta H_c \gg \Delta H_a$ (Fig. 4(e) and (f)). For broader HC, however, ΔH_0 , ΔH_c , and ΔH_a are comparable, neither of which could be safely neglected. On that account, $\Delta a \ \Delta c$ are incomplete, although they are useful descriptors to provide screening rules for stable 1144-phases. Complexity caused by charge effects still demands quantitative evaluation.

3C. Electronic structures

A fascinating observation about Fe-based SC is a phase diagram that involves various degrees of freedom and symmetries. [16, 26, 27] Understanding the interplay between spins, orbitals and lattices is at the heart of unraveling the origin of SC [40–42] and other intertwined orders [43, 44]. For instance, it is suggested that SC is mediated by magnetic fluctuations, which are intensified with a scenario of two-pocket Fermi surface (FS) [45, 46]. Thus, it is interesting to examine the FS and nesting vectors of 1144-phase Ru-phosphides and compare them with 122-phase or 1144-phase Fe-arsenide.

Generally speaking, the two-pocket features include: hole-pockets near Γ and electron-pockets near corner Min B.Z. (Fig. 5). The FS pocket is cylinder-like along k_z owing to the weakening band dispersion along the zaxis (Sec. 6 of SI [37]). That is, introducing heterocations impacts the FS similarly as reducing the dimension, although the periodicity along the z-axis remains intact. Thus, the FS could be characterized by $k_z=0$ plane (Fig. 5), and two-dimensional simplification for FS [47] seems plausible for the 1144-phase. On the other hand, the FS of LaRu₂P₂ strays away from the cylinder shape. This system exhibits isotropic superconductivity with $T_c \sim 4.1$ K, which could be understood with phonon mediation, evidenced by a consistent e-phonon coupling strength and large density of carriers at Fermi level. [48, 49]. The lack of magnetic moments for Ru [48] implies a different mechanism from its Fe-As counterparts. [12, 13].

The hole-pockets at Γ are smaller for CaCsRu₄P₄ (Fig. 5(a)) compared with its iso-valence peer $CaKFe_4As_4$ (Fig. 5(g)), and are even vanishing for $EuCsRu_4P_4$ (Fig. 5(c)). Seen from band structures of $EuCsRu_4P_4$, the bands originally at the Fermi level (FL) are suppressed $\sim 10 \text{ meV}$ below (Sec. 6 of SI [37]), probably subjective to tunability. A common feature for Fe-arsenide is that the hole-pocket is contributed by both d_{xz}/d_{yz} , and d_{xy} -orbitals, as seen in Fig. 5(g)(h), as well as in 1111-phases, 122-phases [45], and LaAFe₄As₄ [25]. In contrast, in the Ru-P 1144-phase, the d_{xy} disappears from the pockets at Γ (Fig. 5(a)-(c)). Notice that, in between the two pockets, there is another FS sheet contributed by d_{yz} , which is also seen in LaAFe₄As₄ [25], but absent for CaCsRu₄P₄. The distinction is mainly due to the so-called half-collapsed tetragonal phase (h-CT)[16], i.e., the pnictogen atoms in neighboring layers start to form p_z bonds [50] and push the bonding and anti-bonding states away from the FS.

In 1144-phases, *d*-electrons of Ru²⁺ occupy two spins equally, exhibiting zero magnetic moments, which suggests a ground state of diamagnetism or paramagnetism. In contrast, in Fe-asenide, Fe has a fraction of effective magnetic moments [7, 12, 45]. For instance, KCaFe₄As₄ bears~0.2 μ_B , and forms long range spin vortex ordering after Ni- or Co-doping [7]. Note that even paramagnetic phases might exhibit AFM magnetic fluctuations [51], which is a relic of long-range ordering. Thus, it is unclear whether the absence of long-range order might be changed with doping or other tunings. To shed light on this, we estimate the non-interacting electronic susceptibility [52, 53] (Fig. 5(d)-(f)).

$$\chi(\mathbf{q}) = -\frac{1}{V} \sum_{\mathbf{k},n,n'} \frac{f_n(\mathbf{k} + \mathbf{q}) - f_{n'}(\mathbf{k})}{\varepsilon_n - \varepsilon_{n'} + i\delta}$$
(9)

$$\times \langle \mathbf{k}, n | e^{-i\mathbf{q} \cdot \mathbf{r}} | \mathbf{k} + \mathbf{q}, n' \rangle \langle \mathbf{k} + \mathbf{q}, n' | e^{i\mathbf{q} \cdot \mathbf{r}} | \mathbf{k}, n \rangle.$$

The f_n and ε_n are Fermi distribution and nth band energies. The V is volume and $|\mathbf{k}, n\rangle$ stands for Bloch states. In our calculation, the transition matrix $\langle \mathbf{k} + \mathbf{q}, n' | e^{i\mathbf{q}\cdot\mathbf{r}} | \mathbf{k}, n \rangle$ is taken to be constant as an approximation.

The main nesting vector (black in Fig. 5(a)-(c)) varies with cation combinations. CaCsRu₄P₄ displays a commensurate (0, π) or (π , 0), reflecting the nesting between pockets at two neighboring M. LaCsRu₄P₄ shows a FS similar to CaKFe₄As₄ (Fig. 5(g)), and exhibits the same vector (π , π), due to the nesting between Γ and M. It has been found that below certain value of Pn-height the nesting vector (0, π) will change to (π , π) [54]. In our case, the Pn-height (the minimum) for CsCa is 1.13 Å and CsLa is 1.11 Å, which endorses the tendency found in

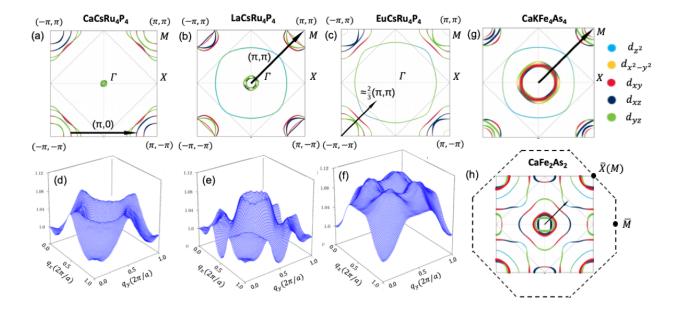


FIG. 5. (Color online) (a)-(c) FS in $k_z=0$ plane. Orbital contributions are distinguished by colors. The main nesting vector is denoted (the nesting vector is from origin to the highest peak of $\chi(q)$). (d)-(f) non-interacting electronic susceptibility $\chi(q)$. Note GGA+U is necessary for EuCs to remove f-orbitals from FL. (g)(f) FS of CaKFe₄As₄ and CaFe₂As₂. The B.Z. is based on the tetragonal cell (Fig. 1(a)) which contains 10 atoms. The dashed lines represent an alternative B.Z. based on primitive cell of 122-phases (containing 5 atoms) projected to $k_z = 0$ plane (octagon), where \bar{X} is equivalent to M point for 1144-phase.

the scenario of 11-phase [54]. In EuCsRu₄P₄, the pocket at Γ is absent, but has an additional FS sheet, for which $\chi(q)$ reach cusps at incommensurate positions $\frac{2}{3}(\pi,\pi)$ (Fig. 5(f)). In comparison, 122-phase Fe-arsenide, such as CaFe₂As₂ (Fig. 5(h)), exhibits a vector $\frac{1}{2}(\pi,\pi)$. Note that two choices of first B.Z. have been commonly used for 122-phases [26]: body-centered tetragonal (two formula units) and primitive. The latter one is more convenient to compare with the 1144-phase. The two choices are compared in Fig. 5(h).

3D. Crystal structures

The crystal parameters (e.g., pnictogen angles and lattice constants) are interesting to study [55–59]. We discuss them from three aspects. The first aspect regards two general rules about 1144-phases, namely *middlepoint rule* and *R-c rule*. The middle-point rule relates the lattice constants of the 1144-phase with those of its parent phases. That is, the *c*-lattice parameter of 1144phase $c_{1144} = \frac{1}{2}(c_{122}^A + c_{122}^B)$, where c_{122}^A and c_{122}^B are the *c*lattice parameters of the two 122-phases (Fig. 6(a)). For example, KCaRu₄P₄ is at the middle point of KRu₂P₂ and CaRu₂P₂. Remarkably, the rule generally applies to 1144-phases of phosphides and arsenides, and of various TM. However, the rule is only for the *c*-lattice parameters (Fig. 6(b)). This finding suggests that complexity in 1144-systems (probably also for general HC) could be segregated, i.e., the z-axis is the easy part and complexity mainly arises from the x-y plane. The other rule, R-crule, links crystal features with atomic information: the mismatch of the c-lattice parameters of two 122-phases $\Delta c = |c_{122}^A - c_{122}^B|$ is proportional to the mismatch of atomic radius $\Delta R = |R_A - R_B|$, where R_A and R_B are atomic radii of cation elements (metallic radius [60]). Noteworthy, a linear correlation is satisfactorily vielded by the fitting of various TMs (Fig. 6(c)) and cation combinations (inset of Fig. 6(c)); again, such a correlation does not hold for *a*-lattice parameters. The linearity could be partically rationalized by the intuitve picture of imagining the cation as a "hard ball". Since each unit cell contains two layers of cations, Δc should be linear with two times the diameter difference, i.e., $4 \cdot \Delta R$. However, the average slope is around $5 \Delta R$, somewhat deviating from the simple intuitive picture. The R-c rule is well verified by existing experimental data [4, 8] and a comparison is given in Sec. 8 of SI [37]. This reconciles the distinct descriptors used in previous studies [4, 8], i.e., ΔR and Δc turn out to be equivalent.

The second aspect concerns the strong asymmetry in structural parameters. Since the 1144-phase is the stacking of two 122-phases, we may wonder whether the TM-plane separation (inter-layer distance) in the 1144phase remains the same as in the 122-phase. We define $\Delta d = d_{TM}^{1144} - d_{TM}^{122}$ to describe its displacement direction and amplitude (Sec. 7c of SI [37]). For Ru-

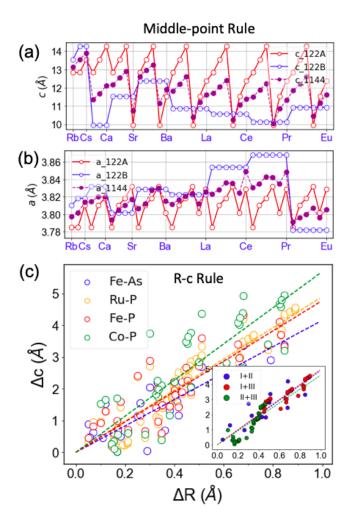


FIG. 6. (Color online) (a) The *c*-lattice parameters (calculation) for various 1144-phases (solid) and its parent phases (hollow). The solid spot is on the average of the two hollow spots. The full list of AB (from left to right): KRb, KCs, RbCs, KCa, RbCa, CsCa, KSr, RbSr, CsSr, CaSr, KBa, RbBa, CsBa, CaBa, SrBa, (K, Rb, Cs, Ca, Sr, Ba)Ln (Ln=La, Ce, Pr, Eu). For brevity, only B is listed on section boundaries. (b) The middle-point rule fails for *a*-lattice parameters, as considerable deviations are observed for CsCa, RbBa, CsBa, etc. (c) Linear fitting of Δc with ΔR . The slopes of different 1144-systems are quite close: $ABFe_4As_4$: 4.16, $ABRu_4P_4$: 4.90, $ABFe_4P_4$: 4.78, $ABCo_4P_4$: 5.69. The inset shows the fitting with grouping cation combinations, not distinguishing TM. The slopes are 4.91, 5.00, and 4.61 for I+II, I+III and II+III cations, respectively.

phosphides, the TM-planes tend to move toward the higher-valence cation and away from the lower-valence. For instance in CaKRu₄P₄, the separation between TM-layer and Ca²⁺ shrinks, while the separation between TM-layer and K⁺ increases. On the contrary, for Co, the TM-plane will displace toward the lower-valence side. Ni- and Fe-1144-phases display both tendencies. [37] Whichever direction it will move, the displacement magnitudes $|\Delta d/d_{122}| \sim 5\%$ -10% (Sec. 7 of [37]) are consid-

erably larger than the structural change that is achievable by applying pressure. Besides, pnictogen (Pn) heights and Pn-TM-Pn bonding angles also undergo large changes. The large change does not happen in solid solution phase, for each cation layer takes equal amounts of charge, unlike A, B are living separately in 1144-phases, which intensely breaks the glide symmetry and affects superconductivity. [55, 57, 58].

The third aspect is regarding derivative phases from HC, known as the half-collapsed phase (h-CT). In general, derivative phases can arise from particular architectures; for example, molecule folding emerges from longchain architectures. h-CT refers to an abrupt collapse of the lattice constant c at certain external pressure, first observed in KCaFe₄As₄ [28]. The collapse happens in two steps: the first-step in Ca-layers, the second in Klayers [30]; so h-CT refers to such a state where one layer collapses and the other does not. h-CT is peculiar for HC as it is determined by two general features: layerbuilding and distinct compressive capacities of heterocation layers [16, 29, 30]. h-CT is a consequence of A-B symmetry breaking, and also grants a method of tuning asymmetry, which leads to, for instance, suppression of SC [61]. Forming the collapsed phase is related to the energy valley of a double-minimum [62]. In the language of bonding, it requires the Pn-Pn bonding to be strengthened and Pn-TM bonding to be weakened. Therefore, there exists a critical distance d_P (defined in Fig. 1(a)), below which the collapsed phase will be formed. The critical d_P is found to be 2.8~3.0 Å for Fe-arsenide 1144phases, which is achievable with a moderate external pressure [29]. Noteworthy, Ru-phosphides 1144-systems exhibit smaller d_P and thereby may form h-CT with no or very little pressure, easier than Fe-arsenide. The critical d_P for phosphide is about 2.5 Å (Sec. 7e of [37]).

4. EXPERIMENTAL RESULTS

In this section we present our design and discovery of CaKRu₄P₄, a new example of a 1144-type compound and a proof of principle of our ability to identify and create new complex phases. CaKRu₄P₄ was chosen as a target phase based on the simultaneous large difference in the clattice parameter values and small difference in a-lattice parameter values exhibited by the KRu₂P₂ and CaRu₂P₂ ternary compounds. In addition, from a technical point of view, we had already mastered the simultaneous use of K and Ca as part of our efforts to grow $CaKFe_4As_4$. [6] We first synthesized KRu_2P_2 and $CaRu_2P_2$ as precursor compounds and then combined them to create the quaternary CaKRu₄P₄. We want to emphasize that this synthesis truly was based on designing the compound, based on our understanding of the requirements needed to stabilize the 1144 structure, and then implementing this design in our synthesis.

4A. Synthesis procedure

Polycrystalline CaKRu₄P₄ samples were growth by solid state reaction. CaRu₂P₂ and KRu₂P₂ polycrystalline samples were synthesized first as precursors which were prepared by putting lumps of potassium metal (Alfa Aesar 99.95% metals basis) or calcium metal pieces (Ames Laboratory, Materials Preparation Center (MPC) 99.9%), ruthenium powder (Alfa Aesar 99.95% metals basis) and lumps of red phosphorus (Alfa Aesar 99.999%) metals basis) into an alumina crucible that was arcwelded into a Ta tube and finally sealed into an amorphous silica ampoule. Because of the high vapor pressure of phosphorus, the temperature of furnace was ramped slowly, dwelling at 230°C and 500°C for 1 and 10 hours respectively, before being increased to 900°C and reacting for 96 hours. After cooling down to room temperature the initial reaction product was ground into powder and pressed into a pellet by tungsten carbide die press in argon filled glove-box. The pressed pellet was sealed in the manner described above and reacted at 900°C for another 96 hours. This process was repeated until phase pure KRu₂P₂ polycrystalline samples were synthesized. The similar process was repeated several times for CaRu₂P₂ until the phase was almost pure. Finally a pellet was pressed from a 1:1 molar ratio of CaRu₂P₂ and KRu₂P₂. This pellet was heated to 850°C and kept there for 95 hours after which the pellet was cooled to room temperature, ground, pressed and resealed. This procedure was repeated until the $CaKRu_4P_4$ phase (88% purity) was formed. Higher purity is thought to be possible with proper adjustment of precursors ratio before reaction.

4B. Structural analysis

Powder x-ray diffraction measurement were carried out on finely ground CaRu₂P₂ and KRu₂P₂ using a Rigaku MiniFlex II powder diffactometer with Cu K α radiation ($\lambda = 1.5406$ Å) with refinements done by GSAS.[63] The PXRD data of CaKRu₄P₄ was recorded at room temperature on a PANalytical X-Pert Pro Diffraction System with Co K α radiation ($\lambda = 1.78897$ Å). Powdered sample was evenly dispersed on a zero-background Si-holder with the aid of a small quantity of vacuum grease. Intensities were collected for the 2θ range from 15° to 110° in step sizes of 0.02° and dwell times of 300 s for each step. FullProf Suite program package was used for Rietveld refinement of the crystal structures [64].

The powder XRD pattern and Rietveld refinement for KRu_2P_2 , $CaRu_2P_2$ and $CaKRu_4P_4$ are shown in Fig. 7. X-ray refinement for $CaRu_2P_2$ and KRu_2P_2 are shown in Table II. The small difference in a-axis lattice parameters (4.044 versus 4.020 Å) and the large difference in c-lattice parameters (9.834 versus 12.371 Å) for $CaRu_2P_2$ and KRu_2P_2 respectively are clearly seen. For the $CaKRu_4P_4$

$\mathrm{CaRu}_2\mathrm{P}_2$	I4/mmm	a: 4.044(4)	c: 9.834(1)		
Atom(Mult)	x	y	z	Uiso	Occ.
Ca (2)	0	0	0	0.00361	1.0
Ru (4)	0	1/2	1/4	0.00357	1.0
P (4)	0	0	0.368(7)	0.00300	1.0
$\mathrm{KRu}_{2}\mathrm{P}_{2}$	I4/mmm	a: 4.020(2)	c: 12.371(8)		
Atom(Mult)	x	y	z	Uiso	Occ.
K (2)	0	0	0	0.00348	1.0
Ru (4)	0	1/2	1/4	0.00688	1.0
P (4)	0	0	0.347(0)	0.00437	1.0

TABLE III. X-ray data collection, refinement and residual parameters for the experimental sample including space group(SG), formula units/cell (Z) and refined lattice parameters for each of the constituent phase.

	$CaKRu_4P_4$	RuP	$CaRu_2P_2$
SG, Z	P4/mmm(123), 1	Pnma(62), 4	$I_{4}/mmm(139),2$
$a({A})$	4.048(1)	5.524(1)	4.050(1)
$b(\AA)$		3.158(1)	
c(A)	10.913(1)	6.128(1)	9.756(1)
$V(\AA^3)$	178.85(3)	106.95(2)	160.34(3)
Radiation		Co $K_a = 1.78901$	
2θ		$15 - 110^{\circ}$	
No. of data		5679	
Uniq. data	152	112	70
No. of Var.		31	
residuals	$R_B = 0.12$	$R_B = 0.22$	$R_B = 0.17$

sample, the X-ray data collection specifications, refined lattice parameters along with residual factors for all three phases are given in Table III, whereas the refined coordinates and isotropic displacement factors are presented for the main phase in Table IV. The clear appearance of peaks with h + k + l = odd in Fig. 7(c). is the qualitative indication that the CaKRu₄P₄ phase has formed

TABLE IV. Atomic Coordinates for $CaKRu_4P_4$, Isotropic Displacement Parameters (Å²), and Site Occupancies for the main phase

atom	position	Symm.	x	y	z	Biso	Occ.
Ca	1a	4/mmm	0	0	0	0.83(1)	1.0
Κ	1d	4/mmm	1/2	1/2	1/2	1.25(1)	1.0
Ru	4i	2mm	0	1/2	0.217(1)	1.22(1)	1.0
$\mathbf{P1}$	2g	4mm	0	0	0.340(1)	1.92(1)	1.0
P2	2h	4mm	1/2	1/2	0.107(1)	0.28(1)	1.0

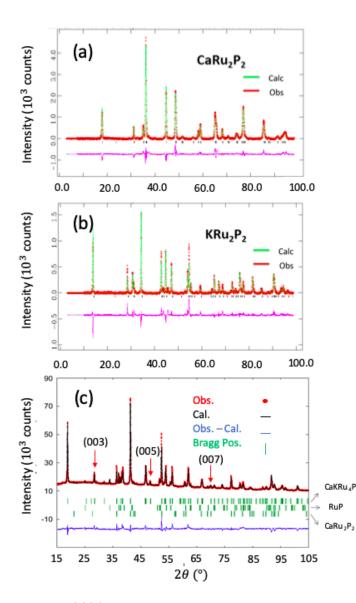


FIG. 7. (a)(b)Powder XRD pattern and Refinement of $CaRu_2P_2$ and KRu_2P_2 . (c) PXRD and Rietveld refinement results for the $CaKRu_4P_4$. (003), (005) and (007) peaks are indicated by the red arrows. The observed profile is indicated by red circles and the calculated profile by the solid line. Bragg peak positions are indicated by vertical tics, and the difference diffractogram is in blue.

[65].

For the CaKRu₄ P_4 refinement, first the zero-point shift and scale factor were refined. Next the lattice constants were refined, followed by the background parameters which involved a gradual increase of the polynomial used in the fit up to the sixth order. Consequently, the positional parameters are refined, beginning with the ruthenium atoms and followed by all phosphorus atoms. This is followed by refinement of the isotropic thermal parameters for all atoms at fixed 100% occupancies. Then the occupancy parameters are unfixed and refined together with thermal parameters. This step confirms 1:1:4:4 stoichiometry of the phase, as well as the Ca/K segregation to their separate unique sites, since minimal fluctuation (<1 %) of the occupancies is revealed at virtually same thermal parameters. Afterwards, profile-shape parameters are included with a peak-asymmetry correction for $2\theta < 40^{\circ}$. The final refinements with 31 parameters, including preferential alignment, and 5,679 data points were performed. Phase analysis of the data in Fig 7(c) gives ~ 88% of CaKRu₄P₄ estimated with ~10% CaRu₂P₂ and ~ 2% RuP after the final reaction. The existence of other phases may be due to air sensitive of KRu₂P₂. Some of the KRu₂P₂ may decompose to binary before react with CaRu₂P₂.

5. DISCUSSION

Here we discuss a few HCs beyond 1144-phases. The so-called 12442-phase (e.g., $K(Cs)Ca_2Fe_4As_4F_2$, [66, 67] $Pr_4Fe_2As_2TeO_4$ [68]) is obtained by stacking two 1111phases on either side of one 122-phase (Fig. 8(a)). Since Ln-O or Ca-F layers effectively serve as 1+ cations, it can be considered as alternative stacking of elemental cations Ca^{2+} and composite cations $(Ln-O)^+$ or $(Ca-F)^+$; the TM-layer is $(Fe-As)^{1.5-}$. Notice that the 12442-phase has a second stacking type (Fig. 8(b)), with Fe-As and La-O interchanging their roles. We may still think of it as 1111+122, but an alternative viewpoint is the Fe-As layer being sandwiched by two dislocated layers of 122phases. The latter viewpoint is more insightful because the Fe-As layer is the playground for SC and magnetism, while Ca or La-O altogether merely serve as electron donators. A particular stacking of the two could be achieved by selecting proper precursors [66, 68]. The 12442-phase implies that the cation could be a composite one, like $(Ln-O)^+$, expanding the pool for cations, as well as allowing extra tuning parameters: the stacking type (distinction of Fig. 8(a) and (b)). Other examples include the 22241-phase (Fig. 8(c)) [69], which contains alternative stacking of 1221-phases and 122-phases. Interestingly, it builds in oxide motifs, which are another big familiy of parent compounds. Recently, 112-phase nickelate SC attracted much attention [33, 34], which belong to the same structure family of cuprate SC[70] and is a limiting case $n \to \infty$ for the series of compounds $\operatorname{La}_{n+1}\operatorname{Ni}_n\operatorname{O}_{2n+1}$ [71]. In 112-phases, cations RE or IIA atoms are sandwiched by NiO₂ layers, a typical HC situation. We have seen many HC in Fe-SC and it is interesting to examine whether HC may exist in Ni- or Cu-based SC.

We shall emphasize that the crucial ingredient for HC is creating asymmetry on either side of a TM-layer, just the definition (iii) in Sec. 2. Note that (iii) does not exclude such situation as, for instance, AABAAB-stacking, because the double-layer AA could be viewed as a single combined layer and asymmetry still occurs at the

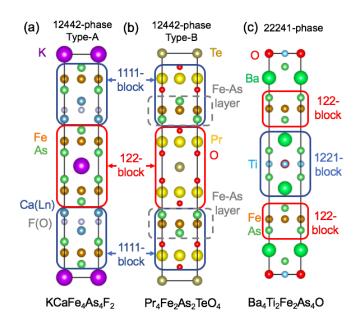


FIG. 8. (Color online) Examples of constructing heterocrystals. (a)(b) Two types of 12442-phase. Differences: type A: 4 layers of Fe-As and 2-layers of composite cation layers (Ca-F)⁺ per unit cell; type B: 2 layers of Fe-As and 4 layers of cation layers (Pr-O)⁺ (c) 22241-phase.

interface between AA and B. On the same account, it is acceptable for having a certain amount of stacking faults or disorder (e.g., the A-layer contains 10% B), as long as imperfections will not eliminate all the asymmetry. Conceptually, HC is not equated with disorder free; in fact, disorder could be introduced on purpose as seen in Ni- or Co-doped CaKFe₄As₄ [17]. But disorder precisely enters at TM-layers not cation layers and thus maintain the global symmetry breaking, which can be characterized by defining $\varepsilon = (d_{TM}(A) - d_{TM}(B))/\Delta d_0$ or $\varepsilon = (\alpha(A) - \alpha(B))/\Delta\alpha_0$, where Δd_0 and $\Delta\alpha_0$ are normalization factors. Then, HC ought to exist in a finite regime of ε , rather than on the single perfect point $\varepsilon = 1$. The virtue of being robust to imperfections has remained less noticed than the merits of suppressing disorder [4, 6, 8, 17]. Tolerance to imperfection helps lessen the conditions of growth.

HC alludes to a fundamental view of exploring complex alloys, as reflected by a new type of phase diagram (Fig. 9). A traditional phase diagram is coordinated by information of an individual atom (e.g., elemental species and concentrations) and becomes cumbersome when N > 3 (Fig. 9(a)). We introduce a different set of coordinates: Δc (or Δa) defined by Eq. 2, 3, and a tuple $\Omega = (n_A + n_B, |n_A - n_B|)$, where n_A, n_B are valence electron numbers for cations A B. For example, KCaRu₄P₄ has $n_A = 1(K)$, $n_B = 2(Ca)$, thus $\Omega = (3, 1)$. These coordinates rely on the whole collection of involved atoms, rather than each individual, thus referred to as "collec-

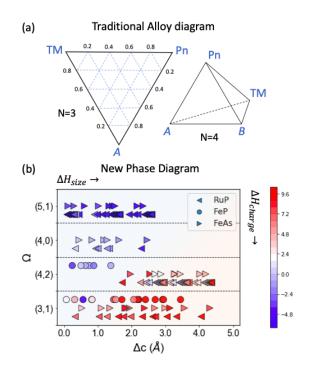


FIG. 9. (Color online) (a) Traditional phase diagram with N = 3 (triangle) and N = 4 (tetrahedron). The complexity of phase diagram will quickly increase with ingredient number N. Stable phases only sparsely distribute, leaving phase separation in most regions. [38] (b) Formation enthalpy of 1144-phases $ABRu_4P_4$, $ABFe_4P_4$, $ABFe_4As_4$ (color scales, meV/atom) vs collective descriptors as coordinates, with which the phase diagram could include compounds with flexible compositions and concentrations. It has a clear separation betwen the stable (red) and the unstable (blue) and is a generalization of phase diagram in [4].

tive". Kind of the idea of using transformed coordinates q to describe collective modes; meanwhile, the information remains unchanged, since Δc , Δa , Ω are ultimately from the individual information.

As such, one obtains a new phase diagram (Fig. 9(b)) of reduced dimensions, which can embody entries with flexible chemical ingredients, such as Fig. 9(b) that has included Fe-arsenide, Ru- and Fe-phosphide. Descriptors Δc , Ω do not depend on the number of constituents, thus complexity will not rely on the compounds being ternary, quaternary or beyond. In addition, the separating between stable and unstable HC is sharp, which reflects the fact that Δc and Ω have captured two universal factors for HC: size and charge effects. That is, x-axis Δc is in charge of ΔH_{size} and y-axis Ω in charge of ΔH_{charge} .

Traditional phase diagram is an efficient apparatus for SS that forms when entropy dictates. HC is an abnormality emerging out of the SS region, invoking new principles and methodology. The new paradigm changes the viewpoint about composite materials, which were based on combining multiple elementary atoms and tagged by

TABLE V. Formation enthalpy for stable 1144-systems. Units for Δa (Δc) and ΔH_0 are \mathring{A} and meV/atom, respectively

Ru-P	$ \Delta a $	$ \Delta_c $	ΔH	Fe-P	$ \Delta a $	$ \Delta c $	ΔH
KCa	0.026	2.623	14.98	KEu	0.009	1.806	8.14
RbCa	0.022	3.328	15.44	RbEu	0.007	2.380	8.68
CsCa	0.033	4.057	18.04	CsEu	0.009	3.130	8.87
KLa	0.009	1.721	10.04	KLa	0.030	1.966	7.58
RbLa	0.005	2.426	10.19	RbLa	0.028	2.540	8.50
CsLa	0.016	3.155	11.79	CsLa	0.012	3.290	9.40
KEu	0.008	1.611	12.90				
RbEu	0.004	2.316	14.19				
CsEu	0.015	3.045	15.17				

the number of species, such as binary, ternary. In contrast, HC is always viewed as a "binary" system that combines two building units; but these units could be composite objects. In other words, for complex alloys, it is beneficial (also necessary) to introduce intermediate structure units in between the elementary level and the final crystal. Just like we consider biological structures as aggregation of protein molecules rather than elementary atoms. For HC, parent phases or motifs play the role of the building units. Accordingly the attributes must be modified for HC: Δc , Δa are derived from parent phases, known as collector descriptors. The strategy for synthesizing will also be modified. A common procedure to discover new compounds is choosing a structure prototype and substituting certain atom with another of similar individual properties, like radius or electronegativity. HC shift the focus to studying the matching (or mismatch) of parent phases and motifs, which might lead to numerous hidden matter states.

6. SUMMARY

In summary, we introduce the concept of HC and address the following specific questions. What is HC? Are they broadly existing or not? What are the main features? What influences or insights will HC bring?

HC is inspired by simple intuition: make the random substitution in metallic alloys into an ordered A-B stacking; in other words, replace the layers in semiconductor hetero-structures by some metallic ingredients, such as TM-layers and cations. To make the idea precise, four definitions are given (Sec. 2): (i) bulk materials, (ii) cation layers plus TM-layers, (iii) A-B stacking and reduced symmetry, (iv) formed with two parent phases.

HC may exist broadly, as seen in Fig. 4, 9. By computational searching in phosphides of 1144-phase (TM=Fe, Ru, Co, Ni), we found a series of stable structures at ambient temperatures and pressures, particularly for Feand Ru-phosphides. The most promising ones are put in Table V for a quick survey. Our prediction is supported by synthesis of high-purity KCaRu₄P₄. The mechanism is the battling of enthalpy and configuration entropy. The enthalpy rises from size effects and charge balance, which could be characterized by two descriptors Δc and Ω (Fig. 9).

For crystal features, the TM-layers in HC commonly has strong distortion (5%~10%) compared with the parent phase. Besides, we suggest two universal latent rules: middle point rule $c_{1144} = \frac{1}{2}(c_{122}^A + c_{122}^B)$, and *R*-*c* rule $\Delta c \simeq 5.0 \cdot \Delta R$. For electronic features, HC commonly exhibit Fermi pockets, and weakening dispersion along the *z*-axis (Sec. 3C). Because HC have ions with *d*- and *f*orbitals, they often build compounds interesting for SC, magnetism, heavy Fermions, etc.

HC may upgrade our viewpoint about alloys, as HC are always viewed as "binary" systems that combine two parent phases; that is, the parent phase plays a role of a structure motif that bridges the atom and the crystal. Thus, It brings renewed interest of many known phases that can serve as the parent phase. Such insights also bring a new phase diagram that is coordinated by the so-called collective descriptors originating from parent phases. (Fig. 9).

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