EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

ALICE luminosity determination for Pb–Pb collisions at $\sqrt{s_{\mathrm{NN}}}$ = 5.02 TeV

ALICE Collaboration

Abstract

Luminosity determination within the ALICE experiment is based on the measurement, in van der Meer scans, of the cross sections for visible processes involving one or more detectors (visible cross sections). In 2015 and 2018, the Large Hadron Collider provided Pb–Pb collisions at a centre-of-mass energy per nucleon pair of $\sqrt{s_{\mathrm{NN}}}$ = 5.02 TeV. Two visible cross sections, associated with particle detection in the Zero Degree Calorimeter (ZDC) and in the V0 detector, were measured in a van der Meer scan. This article describes the experimental set-up and the analysis procedure, and presents the measurement results. The analysis involves a comprehensive study of beam-related effects and an improved fitting procedure, compared to previous ALICE studies, for the extraction of the visible cross section. The resulting uncertainty of both the ZDC-based and the V0-based luminosity measurement for the full sample is 2.5%. The inelastic cross section for hadronic interactions in Pb–Pb collisions at $\sqrt{s_{\mathrm{NN}}}$ = 5.02 TeV, obtained by efficiency correction of the V0-based visible cross section, was measured to be 7.67 ± 0.25 b, in agreement with predictions using the Glauber model.

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1 Introduction

Cross section measurements at colliders require precise luminosity determination. The rate R of a process can be expressed as

$$R = L\sigma, \tag{1}$$

where L is the luminosity and σ is the process cross section.

In a bunched circular collider, such as the Large Hadron Collider [1] (LHC), the particles circulate in packets (bunches) of finite length, defined by the radio-frequency structure of the accelerator. For two contra-rotating bunches colliding with a null crossing angle, the luminosity can be expressed as

$$L = v_{\mathrm{rev}}N_1 N_2 \int f_1(x,y)f_2(x,y)\mathrm{d}x\mathrm{d}y, \tag{2}$$

where v_{rev} is the accelerator revolution frequency, N_1 and N_2 are the bunch intensities, defined as the number of particles in a bunch, f_1 and f_2 are the probability density distributions of particles in the transverse (x,y) plane for the two bunches (where x is the horizontal direction and y is the vertical direction), assumed to be independent of the longitudinal coordinate z. A detailed discussion of the concept and definition of luminosity can be found in [2].

Assuming factorisation of the density distributions in the two transverse directions, such that

$$f_1(x,y) = f_{1x}(x)f_{1y}(y), \quad f_2(x,y) = f_{2x}(x)f_{2y}(y), \tag{3}$$

one can write

$$L = \frac{v_{\mathrm{rev}}N_1 N_2}{h_x h_y}, \tag{4}$$

where

$$h_x = \frac{1}{\int f_{1x}(x)f_{2x}(x)\mathrm{d}x} \quad \text{and} \quad h_y = \frac{1}{\int f_{1y}(y)f_{2y}(y)\mathrm{d}y} \tag{5}$$

are the effective widths of the beam overlap region.

The van der Meer (vdM) scan [3] is the most common technique employed for luminosity determination at colliders, see, e.g. [4] for a review, and [5–12] for measurements performed at the LHC. In vdM scans, the two beams are moved in the transverse plane, in discrete steps. The rate $R_{\mathrm{vis}}(\Delta x, \Delta y)$ of a reference (visible) process is measured as a function of the transverse beam separations $(\Delta x, \Delta y)$, defined as the distance between the centroids of the beam bunches. The x and y scans are usually performed separately, the beams being head-on (i.e. colliding with zero separation) in the non-scanned direction. In this case, the effective widths h_{x0} and h_{y0} for head-on collisions can be determined as

$$h_{x0} = \frac{\int R_{\mathrm{vis}}(\Delta x,0)\mathrm{d}\Delta x}{R_{\mathrm{vis}}(0,0)}, \quad h_{y0} = \frac{\int R_{\mathrm{vis}}(0,\Delta y)\mathrm{d}\Delta y}{R_{\mathrm{vis}}(0,0)} \tag{6}$$

(see [3] for a derivation).

When the beams collide with a non-zero crossing angle, Eqs. 2 and 5 need to be modified [2], but it can be shown [13] that the vdM scan technique still allows a precise luminosity determination, and, in particular, that Eqs. 4 and 6 still hold.

The main output of vdM scans is a measurement of the cross section σ_{vis} of the visible process, which can be determined as

$$\sigma_{\mathrm{vis}} = \frac{R_{\mathrm{vis}}(0,0)\, h_{x0} h_{y0}}{v_{\mathrm{rev}}N_1 N_2} \tag{7}$$

and used for the measurement of luminosity during physics data-taking:

$$L = \frac{R_{\mathrm{vis}}}{\sigma_{\mathrm{vis}}}. \tag{8}$$

The standard vdM scans are typically coupled with a length-scale calibration scan, whose aim is to determine the global conversion factor from the nominal beam displacement to the actual one. In these scans, the two beams are kept at constant separation and moved in consecutive steps in the same direction, and the position of the interaction vertex is measured, using the tracking detectors, as a function of the nominal beam position.

The vdM formalism assumes complete factorisation of the beam profiles in the two transverse directions, such that the beam overlap region is fully described by the product $h_x h_y$. Previous studies performed by ALICE [12, 14–18] and other LHC experiments [6–8, 10, 19] have shown that the actual LHC bunch shapes can violate the factorisation assumption. The size of the effect was found to vary from scan to scan and demanded corrections ranging from the per mil to the percent level. Non-factorisation effects can be studied and quantified by measuring the luminous region parameters, via the distribution of interaction vertices, as a function of the beam separation.

During Run 2, the LHC provided, in 2015 and 2018, lead–lead (Pb–Pb) collisions at a centre-of-mass energy per nucleon pair $\sqrt{s_{\text{NN}}}$ = 5.02 TeV. For collisions of lead ions, the visible cross section σ_{vis} seen by a detector (or set of detectors) with a given trigger condition has, in general, two components, one electromagnetic and one hadronic: $\sigma_{\text{vis}} = \varepsilon_{\text{EM}} \sigma_{\text{EM}} + \varepsilon_{\text{had}} \sigma_{\text{had}}$, where σ_{EM} and σ_{had} are the electromagnetic and hadronic inelastic cross sections and ε_{EM} and ε_{had} are the fractions of electromagnetic and hadronic inelastic events that satisfy the trigger condition.

The ALICE luminosity determination for the Run 2 Pb–Pb data samples is based on a vdM scan session that took place on November 29, 2018, during the LHC fill [1] labelled with the number 7483. The visible cross sections for two independent reference processes were measured in this scan session, and used for the indirect luminosity determination of the 2015 and 2018 samples, according to Eq. 8. Note that this procedure does not require a knowledge of ε_{had} or ε_{EM}.

This document is organised as follows. Section 2 describes the detectors used for the measurement, along with the relevant machine parameters and the procedure adopted for the scan. Section 3 summarises the analysis procedure and presents the results and uncertainties for the visible cross section and luminosity measurement, and for the inelastic hadronic cross section for Pb–Pb collisions at $\sqrt{s_{\text{NN}}}$ = 5.02 TeV. The hadronic cross section was determined by combining one of the measured visible cross sections and a data-driven estimate of the corresponding hadronic efficiency ε_{had}. Finally, Sec. 4 presents a brief summary of the work.

2   Experimental set-up

In the vdM scan, the cross section was measured for two reference processes, one triggered upon by the Zero Degree Calorimeter (ZDC), the other by the V0 detector. A detailed description of these detectors is given in [20], and their performance is discussed in [21, 22]. The ZDC system features two neutron calorimeters (ZNA, ZNC), located on opposite sides of the ALICE interaction point (IP2), each one at a distance of 112.5 m along the beam axis from IP2, covering the pseudorapidity (η) range $|\eta| > 8.8$. It is completed by two proton calorimeters and two electromagnetic calorimeters, not used for this measurement. The V0 detector consists of two hodoscopes, with 32 scintillator tiles each, located on opposite sides of the interaction region, at distances of 340 cm (V0A) and 90 cm (V0C) along the beam axis from IP2, covering the pseudorapidity ranges $2.8 < \eta < 5.1$ and $-3.7 < \eta < -1.7$, respectively. Note that the LHC beam 1 (2) travels clockwise (anticlockwise) from side A (C) to side C (A).

The ZDC-based visible cross section is defined by a trigger condition, called ZED in the following, which requires a signal in at least one of the two neutron calorimeters, corresponding to an energy

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[1]A fill is a time interval with continued presence of beam in the accelerator; it starts with the injection and ends with the beam dump.

deposition larger than ~ 1 TeV. Such a threshold is about three standard deviations below the expected signal from a 2.51 TeV neutron. Neutrons are emitted from the fragmentation/evaporation of Pb ions in electromagnetic dissociation events with (single- or double-side) neutron emission, or in hadronic events [23–27]. The trigger condition for the V0-based visible cross section, called V0M in the following, requires the sum of the signal amplitudes from all the V0 scintillators to be above a chosen threshold; during the 2018 Pb–Pb data taking, the threshold was such that the $\sim 50\%$ most central hadronic events were selected, and all electromagnetic events were rejected due to their relatively low particle multiplicity in the V0 acceptance.

The analysis procedure uses, for the length-scale calibration and non-factorisation corrections, the parameters of the luminous region measured via the distribution of interaction vertices, determined with the ALICE Inner Tracking System [28] (ITS).

During the vdM scan session, each Pb beam consisted of 648 bunches, and 619 bunch pairs were colliding at IP2. The minimum spacing between two consecutive bunches in each beam was 100 ns. The β^* value [2] at IP2 was 0.5 m. The nominal half vertical crossing angle of the two beams at IP2 was about -60 μrad, the minus sign indicating that the two beams exited the crossing region with negative y coordinate with respect to the beam axis [3]. The current in the ALICE solenoid (dipole) was 30 kA (6 kA), corresponding to a field strength of 0.5 T (0.7 T).

Two pairs of horizontal and vertical scans were performed, to obtain two statistically independent cross section measurements per bunch pair. In each horizontal (vertical) scan, the nominal beam separation Δx (Δy) was varied in 25 equal steps [4] from -97.3 μm to $+97.3$ μm. A separation of 100 μm corresponds to about six times the root mean square of the transverse beam profile. During each step, the beams were maintained in position for 28 s, and the ZED and V0M trigger counts were integrated in 14 time bins of 2 s each. The counts were measured separately for each colliding bunch pair. In order to provide additional input for non-factorisation studies, two diagonal scans were performed, where the beam separation was varied simultaneously in the two transverse directions. Finally, a set of length-scale calibration scans was performed.

The bunch intensities were of the order of $(7-10) \times 10^7$ Pb ions per bunch. The bunch-intensity measurement was provided by the LHC instrumentation [29]: a direct current transformer (DCCT), measuring the total beam intensity, and a fast beam current transformer (fBCT), measuring the relative bunch intensities. For the relative bunch intensities, data from a second device, the ATLAS beam pick-up system (BPTX [30]) was also used. The accelerator orbit is nominally divided in 3564 slots of 25 ns each. Given the radio-frequency configuration of the LHC, each slot is divided in ten buckets of 2.5 ns each. In nominally filled slots, the so-called main bunch is captured in the central bucket of the slot. Following the convention established in [31], the charge circulating outside of the nominally filled slots is referred to as ghost charge; the charge circulating within a nominally filled slot but not captured in the central bucket is referred to as satellite charge. The ghost and satellite charges do not contribute to the luminosity at the nominal interaction point. Hence, they must be subtracted from the total beam intensity. A measurement of the ghost-charge fraction was provided independently by the LHCb collaboration, via the rate of beam–gas collisions [5] occurring in nominally empty bunch slots, as described in [10], and by the LHC Longitudinal Density Monitor (LDM), which measures synchrotron radiation photons emitted by the beams [32]. The LDM also provides a measurement of the satellite-charge fraction. For the vdM

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[2]The $\beta(z)$ function describes the single-particle motion and determines the variation of the beam envelope as a function of the coordinate along the beam orbit (z). The transverse size of the beam at a given position along the beam trajectory is proportional to the square root of β. The notation β^* denotes the value of the β function at the interaction point.

[3]ALICE uses a Cartesian system whose origin is at the LHC Interaction Point 2 (IP2). The z axis is parallel to the mean beam direction at IP2 and points along the LHC Beam 2 (i.e. LHC anticlockwise). The y axis points upwards while the x axis is perpendicular to the y and z axes, forming a right-handed orthogonal system.

[4]See Appendix A for details

[5]A definition of beam–gas collision is provided in Section 3.

scan under analysis, the measured ghost-charge fraction was about 4% (3%) for beam 1 (beam 2) and the bunch-averaged satellite-charge fraction was about 3% for both beams, resulting in a total correction to the bunch intensity product (hence to the cross section) of about 13%. Satellite bunches in a beam may interact with main bunches in the other beam. These events must be identified and subtracted from the measured visible process rates, as will be described in Section 3.

3 Analysis and results

3.1 Visible cross section determination

In previous studies dedicated to the luminosity determination in pp [14–17], p–Pb [12, 18], and Pb–Pb [21] collisions in the ALICE experiment, the trigger rates were measured as a function of the beam separation and corrected for background and pile-up effects. A χ^2-based fit of the scan curves (separately for the x and y scans) yielded a measurement of $R(0,0)$, h_{x0}, and h_{y0}, which could be inserted directly into Eq. 7 to determine σ_{vis}. In comparison, e.g. to the studies performed for pp collisions, the present analysis deals with a collision rate per colliding bunch pair lower by about one order of magnitude for ZED and three orders of magnitude for V0M. This demands a different approach, designed to obtain a better treatment of statistical uncertainties at very small numbers of trigger counts. For each colliding bunch pair, the number of triggered events t_i and the number of sampled LHC orbits n_i during time bin i are used as inputs for a binomial likelihood fit:

$$\ln \mathscr{L} = \sum_i \left[t_i \ln P_i + (n_i - t_i) \ln (1 - P_i) \right] \tag{9}$$

where P_i is the probability of having a trigger in a bunch crossing, related to the mean number of triggers per bunch crossing μ_i by Poissonian statistics, $P_i = 1 - e^{-\mu_i}$. The quantity μ_i is modelled by the fit function, according to the relations

$$\mu_i = \frac{R_{\text{vis}}(\Delta x_i, \Delta y_i)}{\nu_{\text{rev}}} + p_{\text{s},i} + \tilde{p}_1 N_{1,i} + \tilde{p}_2 N_{2,i} + p_0 \tag{10}$$

and

$$R_{\text{vis}}(\Delta x_i, \Delta y_i) = \nu_{\text{rev}} N_{1,i} N_{2,i} \frac{\sigma_{\text{vis}}}{h_{x0} h_{y0}} f(\Delta x_i) g(\Delta y_i), \tag{11}$$

where: $N_{1,i}$ and $N_{2,i}$ are the intensities of the two colliding bunches; Δx_i and Δy_i are the beam separations, corrected for beam–beam deflection [33, 34] and orbit drifts [35, 36], f and g parametrise the luminosity dependence on Δx_i and Δy_i, respectively; h_{x0} and h_{y0} are the integrals of f and g, respectively, divided by their peak values, consistently with Eq. 6; $p_{\text{s},i}$ is the separation-dependent probability that the trigger is fired by a collision between one of the two colliding bunches and a satellite bunch in the other beam, or by the collision of two satellites; $\tilde{p}_1$ ($\tilde{p}_2$) is the probability that the trigger is fired by a collision of a bunch of beam 1 (beam 2) with residual gas in the beam pipe (beam–gas collision), normalised by the bunch intensity; p_0 is the probability that the trigger is fired in the absence of beams (detector noise).

The functions $f(\Delta x)$ and $g(\Delta y)$ were chosen to have a Gaussian core with mean value and standard deviation as the only free parameters, the normalisation being constrained by Eq. 7. In order to improve the description of data at large separation, the Gaussian function is modified at absolute separations larger than a certain threshold. For each scan step beyond the threshold, an independent offset is added to Δx_i or Δy_i in the definition of the fitting function, so that there is one additional fit parameter for each of these steps. The threshold is chosen, independently for each colliding bunch pair, as the minimum value allowing one to obtain $\chi^2/ndf \sim 1$; depending on the considered colliding bunch pair and scan, it is located 1.3–2.5 standard deviations away from the peak, and the total number of parameters needed to

describe the tails varies between 7 and 13. The function is constrained to be symmetric around the peak by using the same tail parameter for scan steps at opposite nominal separation. A formal definition of the fitting functions $f(\Delta x)$ and $g(\Delta y)$ is provided in Appendix A.

The parameters p_0, $\tilde{p}_1$ and $\tilde{p}_2$ were estimated by means of an independent fit to the trigger rates in non-colliding and empty bunch slots. Empty bunch slots located immediately after colliding bunch slots were excluded from the fit, because such bunch slots are affected by background from late spurious pulses (after-pulses) and would provide an overestimated measurement of the detector noise. Owing to the minimum spacing of 100 ns between colliding bunches, the contribution from a previous collision to the trigger counts in colliding bunch slots was found to be negligible for both ZED and V0M signals. Because of the large ZDC distance from IP2, the background induced on ZNA (ZNC) by beam–gas collisions of a bunch of beam 1 (2) happening upstream of the calorimeter results in a signal that is 31 bunch slots ($\sim$ 750 ns) earlier with respect to nominal beam–beam collisions of that bunch. During the vdM scan, the distribution of Pb-ion bunches along the LHC orbit was such that this background contribution shows up only in nominally empty bunch slots, with no effect on the colliding slots. Therefore, for the ZED analysis, this subset of the empty bunch slots was excluded from the background fit.

The separation-dependent contribution from main–satellite collisions $p_{\mathrm{s},i}$ was evaluated via the signal arrival-time spectra in ZNA and ZNC. The procedure is different for ZED and V0M due to the different selectivity of the two trigger classes. All events triggered by V0M are hadronic and have signals in both ZNA and ZNC. The two-dimensional distribution of arrival times in the two calorimeters for these events is shown in the left panel of Fig. 1. The satellite events are tagged by means of a square cut around the main–main collision peak position, located at (0, 0). Conversely, the ZED trigger has a large contribution from electromagnetic events with single-side neutron emission, so that most of the events have a signal only in one calorimeter. For this sub-sample of ZED-triggered events the estimation of the satellite contamination is based on the one-dimensional arrival time distributions in each of the ZNs, and the fraction of satellite collisions is obtained via a fit of the time distribution to a sum of Gaussian functions, with peak positions fixed to the values expected from the LHC radio-frequency structure (right panel of Fig. 1). The signal from a neutron emitted in a main–satellite collision has the same arrival time as that from a main–main collision if the neutron is emitted by an ion in the main bunch, while it is early or late if the neutron is emitted by an ion in the satellite bunch. Therefore, only half of the neutrons emitted in single-side events from main–satellite collisions are identified as such. Hence, a correction factor of two was applied to the satellite-collision fractions obtained from the single-side neutron event sample.

Due to the dead time of the ZDC detector electronics, the timing information could only be recorded for a fraction of the triggered events. The size of the sample available for the analysis of time spectra does not allow for a statistically significant determination of satellite-collision fractions for each bunch pair and separation step. Therefore, one can only estimate a bunch-averaged satellite contribution. In order to improve the accuracy of the satellite estimation, the fit procedure is therefore extended with a joint likelihood maximisation, based on both timing and trigger data, at each time bin. Let S_i be the number of events identified as main–satellite collisions in T_i recorded events (and t_i the number of trigger counts in n_i sampled orbits, as defined above), the joint binomial likelihood can be written as

$$\ln \mathscr{L}_i = t_i \ln P_i + (n_i - t_i) \ln (1 - P_i) + S_i \ln \left(\frac{p_{\mathrm{s},i}}{P_i} \right) + (T_i - S_i) \ln \left(\frac{P_i - p_{\mathrm{s},i}}{P_i} \right). \tag{12}$$

The maximisation procedure determines the most probable value for $p_{\mathrm{s},i}$ for the measured values of n_i, t_i, T_i and S_i and the current expected P_i. The $p_{\mathrm{s},i}$ value obtained is then fed into the global likelihood according to Eqs. 9 and 10.

In summary, the free parameters of the global likelihood fit for a given colliding bunch pair are the visible cross section, the mean values and standard deviations of the Gaussian cores of the $f(\Delta x)$ and
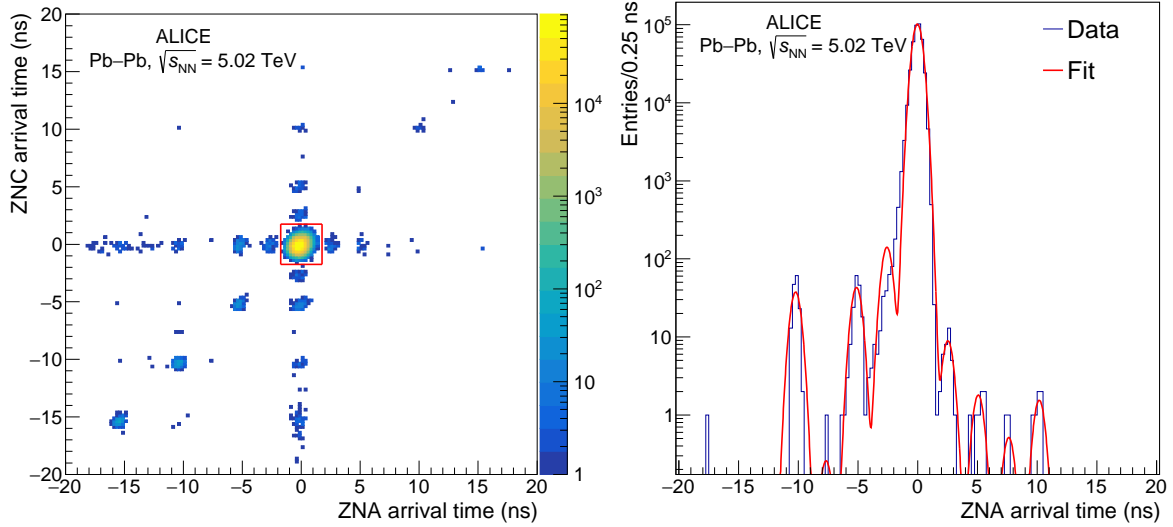
Figure 1: (Colour online) Left: correlation between the arrival times, relative to main–main collisions, of signals in ZNA and ZNC for events triggered by V0M. The square box depicts the satellite-collision rejection cut discussed in the text. Events outside the box are from main–satellite collisions (horizontal and vertical bands) and from satellite–satellite collisions (diagonal band). Right: distribution of the arrival time, relative to main-main collisions, in one of the two neutron calorimeters for ZED-triggered single-side neutron events. The superimposed curve shows a fit with a sum of Gaussian distributions. Both figures are for head-on collisions ($\Delta x = \Delta y = 0$).

$g(\Delta y)$ functions, and 7 to 13 tail parameters for each of the two functions.

As an example, in Fig. 2 the measured trigger probability per bunch crossing as a function of time during the vdM scan is shown for one pair of colliding bunches, together with the expectation from the fit. The values of χ^2/ndf are typically close to unity. As a remark, χ^2/ndf values as large as ~ 2 are obtained if a pure Gaussian function is used, without introducing any tail parameter.

The ZED and V0M analyses provide largely independent estimates of the effective beam widths h_{x0} and h_{y0}, via the fitted parameters of $f(\Delta x)$ and $g(\Delta y)$. The $h_{x0}h_{y0}$ products obtained in the ZED and in the V0M analysis are consistent within 0.13%, which provides an indication that detector-dependent effects such as background and pile-up are under control.

Three length-scale calibration scans were performed for each direction, with different displacement step size, in order to test for a possible dependence on such a parameter. The horizontal (vertical) calibration factor is the slope parameter of a linear fit to the measured horizontal (vertical) vertex displacement versus the nominal one, as illustrated in Fig. 3. The vertex position was determined using tracks reconstructed in the ITS. The resulting (multiplicative) correction factor to the fitted σ_{vis} is the product of the horizontal and vertical calibration factors, and was found to be 0.964±0.010. The uncertainty has a statistical (0.5%) and a systematic contribution. The latter accounts for deviations from the linear trend in the individual fits (0.3%), for the dependence of the results on the displacement step size (0.4%), and for the dependence of the results on the track and event selection criteria used in the vertex determination procedure (0.7%).

The impact of non-factorisation effects was evaluated by simultaneously fitting the rates and the luminous-region parameters (positions, sizes, transverse tilt) during both the standard and the diagonal scans with a three-dimensional non-factorisable double-Gaussian model [7, 14, 37, 38], and computing the bias on the head-on luminosity with respect to a factorisable model. The resulting (multiplicative) correction factor to the fitted σ_{vis} is 1.011±0.011, where, conservatively, an uncertainty as large as the correction is
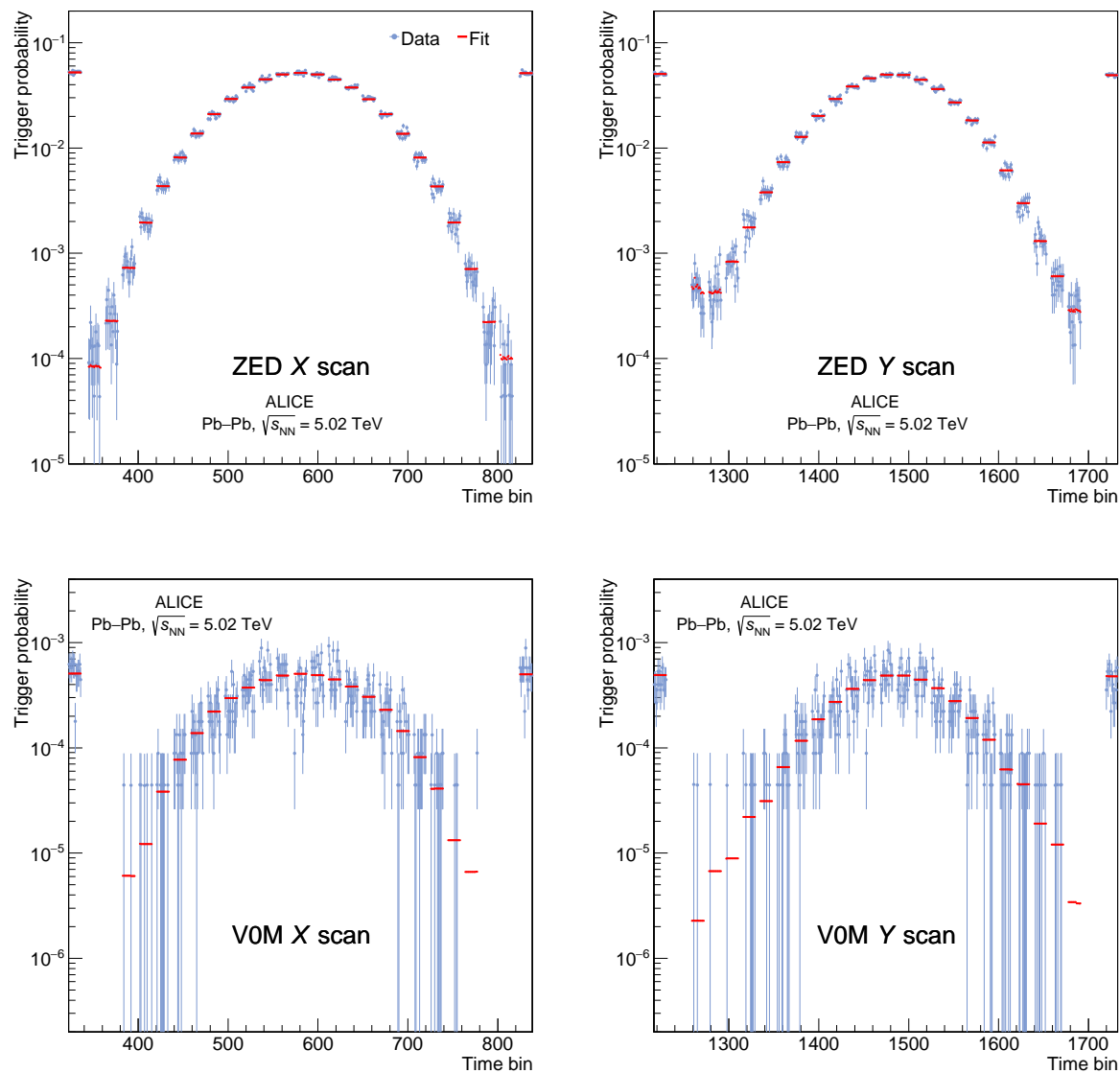
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Figure 2: (Colour online) ZED (top) and V0M (bottom) trigger probabilities per bunch crossing for a typical colliding bunch pair, as a function of time, during the first horizontal and vertical vdM scan. Each time bin corresponds to an acquisition window of ~ 2 s. The uncertainties are statistical only. The fit expectation values are also shown, as lines, in each time bin. Time bins during which the beams are being displaced, not considered in the analysis, are not shown.
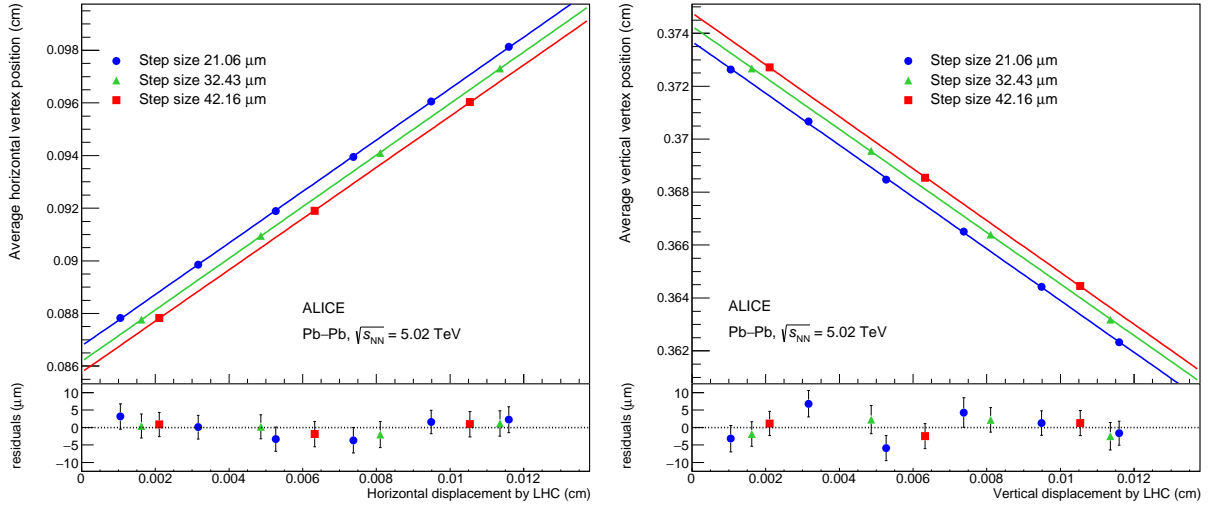
Figure 3: (Colour online) Nominal versus measured displacements in the horizontal (left) and vertical (right) length-scale calibration scans, obtained from events with reconstructed-track multiplicity ranging from 260 to 500. Data are represented by symbols, while a linear fit is represented by the solid lines. The uncertainties are smaller than the symbol sizes. The fit residuals are shown in the lower panel. The blue (green, red) lines and solid circles (triangles, squares) correspond to a nominal displacement step size of 21.06 μm (32.43 μm, 42.16 μm).

assigned, to account for the non-accurate description of some of the luminous-region parameters by the model.

The ZED and V0M cross sections measured for all colliding bunch pairs and scans are shown as a function of the product of bunch intensities $N_1 N_2$ in Fig. 4. For both luminometers and scans, no significant dependence of σ_{vis} on $N_1 N_2$ is observed. However, non-statistical fluctuations of the cross section are present, particularly visible for ZED, which has better statistical precision. In order to take these into account, a systematic uncertainty of 0.1% is assigned, computed as $\sqrt{\chi^2/ndf - 1}$ times the statistical uncertainty of the average cross section [39], where χ^2/ndf is obtained from the constant-value fits to the bunch-by-bunch cross sections shown in Fig. 4. The observed fluctuations are likely related to the significant bunch-by-bunch variation of the satellite-charge fraction (on the order of 50% root mean square, as measured by the LDM). A major contribution to the bunch-by-bunch spread of σ_{vis} was found to originate from pairs with large satellite-charge fraction. A bunch-by-bunch correction for satellite-charge was not performed in this analysis, due to a limited knowledge of the sensitivity of fBCT (or BPTX) to charge in satellite buckets. Instead, the bunch-averaged satellite charge was used as an overall correction to the total beam current measured by DCCT, assuming satellite charge does not contribute to the fBCT signal.

The bunch-averaged cross sections measured in the two scans agree within 1%, which is considered as an additional systematic uncertainty. The measured visible cross sections, obtained by averaging the results from the two scans, are $\sigma_{ZED} = 420.58 \pm 0.03$ (stat.) b and $\sigma_{V0M} = 3.933 \pm 0.003$ (stat.) b.

The combined impact of the subtraction of background from beam–gas collisions, electronic noise, and satellite collisions on the final cross section is about 1.5% for ZED and 1% for V0M, largely dominated by satellite collisions. The main source of uncertainty of the satellite-collision background estimation is the usage of bunch-integrated timing data in the evaluation of the satellite collision fractions, with a (potentially limited) sensitivity to bunch-by-bunch variations provided by the joint likelihood minimisation of Eq. 12. An alternative method was tested, where the satellite-collision probability $p_{s,i}$ for a given bunch pair is evaluated as the bunch-integrated satellite-collision fraction S_i/T_i measured with the
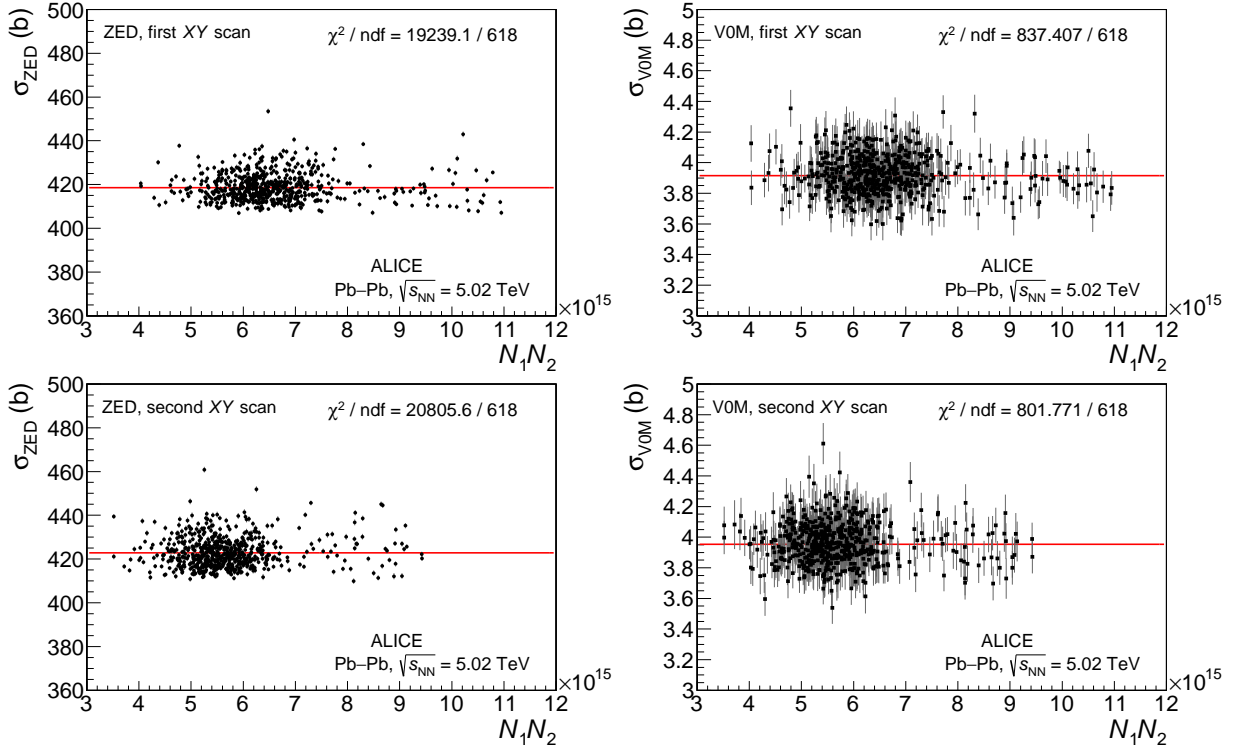
Figure 4: (Colour online) Measured ZED (left) and V0M (right) visible cross sections as a function of the product of the ion bunch intensities, for the first (top) and second vdM scan (bottom). Uncertainties are statistical only. The solid line represents a fit to a constant value.

ZDC timing, scaled by the ratio between the satellite charge fraction for that bunch pair and the bunch-averaged satellite-charge fraction, both measured by the LDM. The systematic uncertainty is estimated as the maximum difference, across scans and luminometers, between the visible cross sections obtained with the standard and alternative method, and amounts to 1.2%. The systematic uncertainty on the subtraction of background from beam–gas and electronic noise is estimated by setting the parameters p_0, $\tilde{p}_1$ and $\tilde{p}_2$ to zero in the likelihood fit (see Eq. 9 and 10). This corresponds to the extreme assumption that all counts in nominally non-colliding bunch slots originate from collisions involving ghost charge. The variation in visible cross section, retained as uncertainty, is 0.3% at most.

The uncertainty of the bunch intensity is 0.8%, from the quadratic sum of three components: 0.5%, from the uncertainty of the total beam current normalisation from the DCCT, evaluated as described in [40]; 0.2%, from the uncertainty of the relative bunch populations, evaluated as the difference between the fBCT- and BPTX-based results; and 0.6%, from the uncertainty of the ghost and satellite charge [10, 32], dominated by the difference between the LHCb and LDM measurements of the ghost-charge fraction. No additional uncertainty is assigned to the bunch-by-bunch spread of satellite charge, because about 95% of the bunches in each beam were colliding in IP2. Under these circumstances, the bunch-pair-averaged visible cross section is essentially driven by the total beam current measurement from DCCT (to which the sum of fBCT signals is normalised), and a non-perfect evaluation of the satellite charge in each bunch slot only leads to a bunch-by-bunch spread of the measured cross sections, with negligible or no bias to the final result, as was verified by making different assumptions for the fBCT sensitivity to satellites.

The measurement of the width of the beam-overlap region in a van der Meer scan can be perturbed by a variation of the bunch emittance during the scan itself. The variation rate of the effective beam widths was estimated with two different methods. The first uses the difference of the measured widths between the first and second scan, the second uses the time evolution of the rate at zero separation, corrected

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by the bunch intensity decay. The second method yields larger variation rates (by about 70%) than the first. The potential bias on the measured visible cross sections was estimated in a realistic simulation of the performed scans, assuming an exponential time dependence of the effective beam widths, using the slopes obtained with the second method. The resulting uncertainty is 0.5%.

Possible non-linearities in the steering magnet behaviour during the scan, e.g. due to hysteresis, were considered as a source of systematic uncertainty. A preliminary hysteresis model [41] developed for the LHC was used. The model provides, for each scan step and for both beams, an upper limit to the hysteresis-induced shift of the beam position with respect to its nominal value. For this fill, the maximum shift is about 0.5 μm. In order to estimate a possible bias on the cross section, the fit of Eq. 9 was performed with the separation at each step modified according to the predicted position shift of both beams. The change in average visible cross section is 0.2% for both luminometers and is retained as a systematic uncertainty.

The uncertainty of the orbit-drift correction was conservatively taken to be as large as the effect of the correction (0.15%). The uncertainty of the beam–beam deflection correction was evaluated by varying the input parameters to the deflection calculation within a reasonable range, as described in [14], and found to be less than 0.1%. The effect of distortions of the bunch shapes due to the mutual interaction between the two beams was also evaluated, within the framework outlined in [34], and found to be less than 0.1%.

The systematic uncertainty associated with the choice of the fitting strategy was evaluated: by varying the range of beam separations described by the Gaussian core (varying thereby the number of fit parameters used to describe the tails); by discarding the last scan step, where the satellite contribution is dominant; and by extracting the visible cross section from a simultaneous fit to all colliding bunch pairs, with common shape parameters, instead of averaging the results from individual fits. The resulting uncertainty is 0.4%.

The total systematic uncertainty of the visible cross section measurement, obtained as the quadratic sum of the contributions listed above, amounts to 2.4% for both ZED and V0M.

3.2   Hadronic inelastic cross section determination

As an additional output of the vdM scan analysis, the inelastic hadronic cross section σ_{had} was determined by correcting the visible cross section σ_{V0M} for the V0M trigger efficiency. The ALICE centrality determination framework [42, 43] assigns to each event a centrality value, based on the total signal amplitude in the V0 detector. The centrality is defined as the probability that a hadronic Pb–Pb collision results in an amplitude larger than the measured value. The centrality calibration for the 2018 sample was performed using a mimimum-bias trigger requiring a signal in each of V0A, V0C, ZNA and ZNC. Such a trigger is fully efficient for hadronic events and free from electromagnetic contamination for the $\sim 90\%$ most central events [44, 45]. In order to obtain the shape of the amplitude spectrum in the most peripheral events, the minimum-bias-triggered spectrum is fitted with a Monte Carlo implementation of the Glauber model [46], coupled with a two-component ancestor model for particle production; the fit is performed above a chosen amplitude threshold (anchor point, corresponding to a centrality of 90%), where no trigger bias is expected. The centrality distribution of V0M-triggered events, determined using the framework described above, is shown in Fig. 5. The distribution is uniform in the 0–50% centrality range, where the V0M trigger is fully efficient, then drops rapidly to zero in the range 50–52%. When the distribution is normalised such that its integral in 0–50% is 0.5, its total integral provides the V0M efficiency for hadronic interactions, ε_{had}. For the fill in which the vdM scan was performed, this procedure results in $\varepsilon_{had} = 0.513 \pm 0.012$. The quoted uncertainty is systematic and is obtained as the quadratic sum of two components. The first one, of 1.4%, was determined, similar to what was done in Ref. [44], by varying the centrality at the anchor point within $\pm 1\%$ (referring here to an absolute variation, i.e., from 89% to 91%). The second one, of 1.8%, was determined as the difference between the default efficiency

value and the one obtained by fitting the V0 amplitude spectrum with a different template, based on the T_RENTo model [47]. Finally, one has

$$\sigma_{had} = \frac{\sigma_{V0M}}{\varepsilon_{had}} = 7.67 \pm 0.25 \text{ b,}$$

where the quoted uncertainty is the combination of the statistical and systematic uncertainties of the visible cross section, of 2.4%, and of the trigger efficiency, of 2.3%. The measured cross section is in agreement with the prediction of (7.62 ± 0.15) b from Ref. [48], based on a Monte Carlo implementation of the Glauber model with a nuclear radius of ~ 6.7 fm, a nuclear skin depth for protons (neutrons) of ~ 0.45 fm (~ 0.56 fm), and an inelastic nucleon–nucleon cross section of ~ 67 mb.
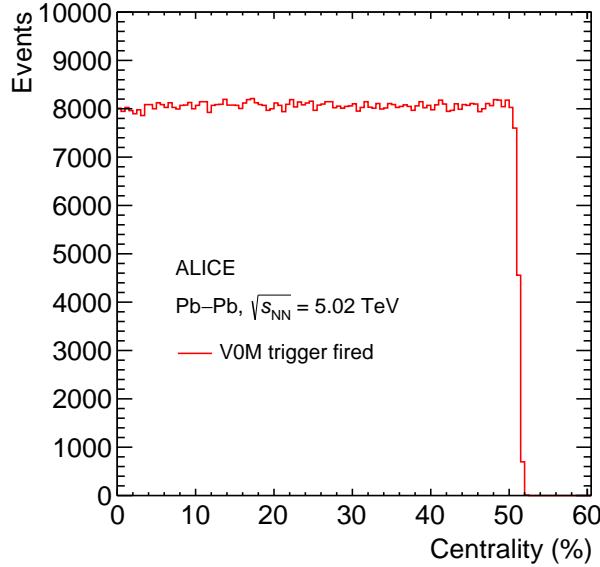

Figure 5: Centrality distribution of events satisfying the V0M trigger condition, for the LHC fill during which the vdM scan was performed.

3.3 Consistency and stability of the luminosity calibration

In order to test the stability and mutual consistency of the ZED and V0M calibrations, the luminosities measured with the two reference signals throughout the whole 2015 and 2018 data-taking periods were compared on a run-by-run basis. In the ALICE nomenclature, a run is a set of data collected within a start and a stop of the data acquisition, under stable detector and trigger configurations [6]. For each run, the trigger counts, integrated over colliding bunch slots, were corrected by subtracting the estimated beam–gas background, detector noise, and background from main–satellite collisions. As explained earlier, the beam–gas background was estimated by means of the counts in non-colliding bunch slots, rescaled by the relative fractions of beam intensities; the contribution from detector noise was estimated via the counts in empty slots; the background from main–satellite collisions was estimated using the ZDC timing data. For each run, the pile-up corrected ratio between the V0M- and ZED-based luminosities was computed from the corrected number of trigger counts N_{V0M} and N_{ZED} and from the total number of bunch crossings in the run N_{BC} as

$$\frac{L_{V0M}}{L_{ZED}} = \frac{\ln(1 - N_{V0M}/N_{BC})\sigma_{ZED}}{\ln(1 - N_{ZED}/N_{BC})\sigma_{V0M}}. \tag{13}$$

While the ZED trigger settings remained unchanged throughout the 2015 and 2018 data-taking periods, the threshold for the V0M trigger was different in 2015 and 2018. Furthermore, in 2018, the threshold

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[6]For the data-taking period under consideration, the duration of a run ranges from ~ 5 minutes to ~ 7 hours.
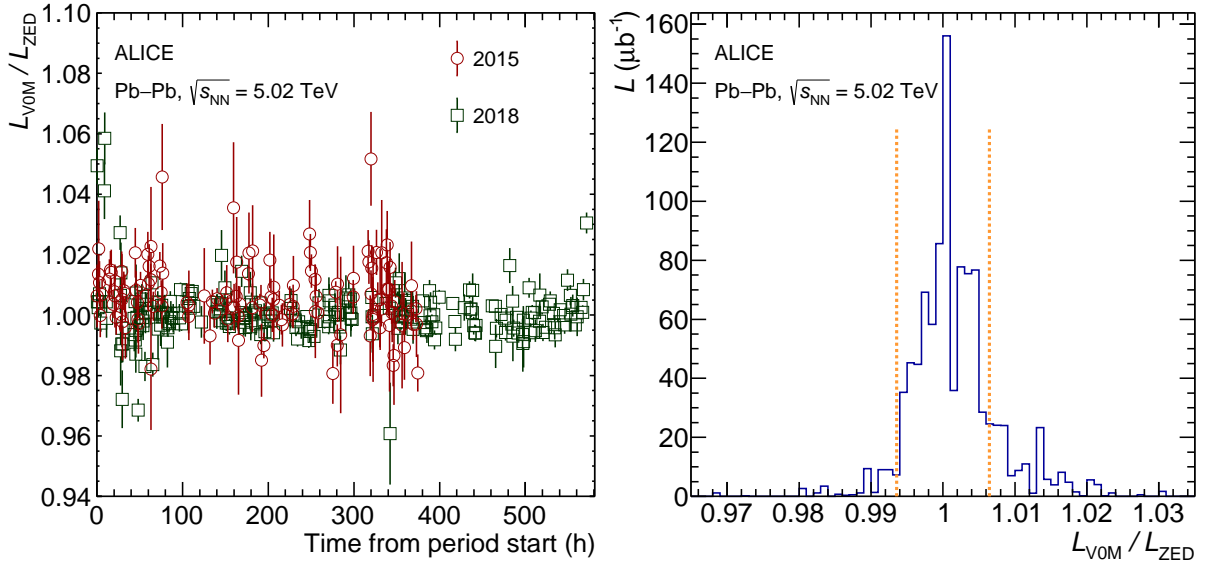
Figure 6: (Colour online) Left: ratio of V0M and ZED luminosities calculated according to Eq. 13 as a function of time with respect to the beginning of the data-taking periods for 2015 (circles) and 2018 (squares). The uncertainties are statistical. Right: distribution of the ratios for all runs (2015 and 2018), weighted with the run luminosity. The dashed vertical lines are located at $L_{V0M}/L_{ZED} = 1 \pm \alpha$, where $\alpha \sim 0.007$ is the mean quadratic difference from unity.

was slightly adjusted a few times during data-taking as the V0M-based centrality trigger was being tuned. For the data-taking periods with different threshold settings with respect to the vdM scan, the V0M trigger efficiency was re-determined with the procedure described earlier, and the V0M cross section re-scaled by the ratio of the measured efficiency to that measured in the fill containing the van der Meer scans.

The luminosity ratio as a function of time and the distribution of the ratio values over all runs, weighted with the run luminosity, is shown in Fig. 6. The mean quadratic difference of the ratio from unity is about 0.7% and is retained as a systematic uncertainty of the stability and mutual consistency of the luminosity calibration. When the analysis is restricted to the 2015 or 2018 sample, the mean quadratic difference from unity amounts to 1% or 0.5%, respectively.

3.4 Luminosity uncertainty

In Table 1 a summary of the different contributions to the uncertainty of the visible cross section and the luminosity measurement is presented. The luminosity uncertainty, obtained as the quadratic sum of the visible cross section uncertainty and of the stability and consistency uncertainty, amounts to 2.5% for both ZED and V0M. For the sake of comparison, the luminosity uncertainty obtained by ALICE for Pb–Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV (LHC Run 1) was of 5–6% [21].

4 Conclusions

In 2015 and 2018, the ALICE Collaboration took data with Pb–Pb collisions at a centre-of-mass energy $\sqrt{s_{NN}} = 5.02$ TeV. In order to provide a reference for the luminosity determination, vdM scans were performed and visible cross sections were measured for two processes, ZED (neutron emission in the acceptance of the neutron Zero Degree Calorimeters) and V0M (energy deposition in the V0 detector by events up to $\sim 50\%$ centrality). Each of the two detectors provides a measurement of the luminosity with a total uncertainty, for the full sample (2015 and 2018), of 2.5%. These uncertainties improve by about a factor of two with respect to those obtained by ALICE in previous studies dedicated to Pb–Pb

Table 1: Relative uncertainties of the measurement of visible cross sections and luminosity in Pb–Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV. The stability and consistency and the total luminosity uncertainties refer to the full Run 2 sample (2015 and 2018); uncertainties for the single periods are given in the text.

Source	Uncertainty (%) ZED | V0M
Statistical	0.008 | 0.08
$h_{x0}h_{y0}$ consistency (V0M vs ZED)	0.13
Length-scale calibration	1
Non-factorisation	1.1
Bunch-to-bunch consistency	0.1
Scan-to-scan consistency	1
Satellite collisions	1.2
Beam–gas and noise	0.3
Bunch intensity	0.8
Emittance variation	0.5
Magnetic non-linearities	0.2
Orbit drift	0.15
Beam–beam deflection and distortion	0.1
Fitting scheme	0.4
Total of visible cross section	2.4
Stability and consistency	0.7
Total of luminosity	2.5 | 2.5

collisions at $\sqrt{s_{NN}} = 2.76$ TeV. The inelastic cross section for hadronic interactions in Pb–Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV, obtained by trigger-efficiency correction of the V0M cross section, was measured to be 7.67 ± 0.25 b, in agreement with predictions from the Glauber model.

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A   Fitting function definition

The luminosity dependence on the horizontal separation is parametrised (see Eq. 11) with the fitting function $f(\Delta x)$.

With 25 scan steps, one can choose $-12 \leq j \leq +12$, so that the nominal separation at step j is given by

$$\Delta x_{\mathrm{nom},j} = \frac{j}{24}(\Delta x_{\mathrm{nom,max}} - \Delta x_{\mathrm{nom,min}}), \tag{A.1}$$

where $\Delta x_{\mathrm{nom,max}} = -\Delta x_{\mathrm{nom,min}} = 97.3\ \mu$m, and $j = 0$ denotes the (nominal) zero separation. As discussed in Section 3, the actual separation Δx_j is obtained by correcting the nominal separation $\Delta x_{\mathrm{nom},j}$ for the orbit drift and beam–beam deflection effects.

With the above convention, the fitting function is defined as

$$f(\Delta x_j) = e^{-\frac{(\Delta x_j - \mu + \delta_j)^2}{2\sigma^2}}, \tag{A.2}$$

with

$$\delta_j = \delta_{-j} \tag{A.3}$$

and

$$\delta_j = 0 \ \text{ for } \ |j| < j_0, \tag{A.4}$$

where $j_0 > 0$ is the threshold chosen for the transition between the Gaussian core and the tail (see Section 3 for details). The fit parameters in the function are the mean value μ, the standard deviation σ and the offsets δ_j (with $j_0 < j \leq 12$).

The definition of the function $g(\Delta y)$ used to parametrise the luminosity dependence on the vertical separation is identical, with independent offset parameters.

Depending on the considered colliding bunch pair, the fitting functions use $6 \leq j_0 \leq 9$.