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## Measurement of the Decay $\Xi^0 \to \Lambda \gamma$ with Entangled $\Xi^0 \overline{\Xi}^0$ Pairs

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In this Letter, a systematic study of the weak radiative hyperon decay  $\Xi^0 \to \Lambda \gamma$  at an electronpositron collider using entangled  $\Xi^0 \bar{\Xi}^0$  pair events is presented. The absolute branching fraction for this decay has been measured for the first time, and is  $(1.347 \pm 0.066_{\text{stat.}} \pm 0.054_{\text{syst.}}) \times 10^{-3}$ . The decay asymmetry parameter, which characterizes the effect of parity violation in the decay, is determined to be  $-0.741 \pm 0.062_{\text{stat.}} \pm 0.019_{\text{syst.}}$ . The obtained results are consistent with the world average values within the uncertainties, offering valuable insights into the underlying mechanism governing the weak radiative hyperon decays. The charge conjugation parity (*CP*) symmetries of branching fraction and decay asymmetry parameter in the decay are also studied. No statistically significant violation of charge conjugation parity symmetry is observed.

The ground-state hyperons have played a crucial role in the understanding of weak interactions. However,

numerous unanswered questions persist regarding the weak decay mechanisms and the role of hyperons in nonperturbative quantum chromodynamics (QCD) [1, 2]. Specifically, weak radiative hyperon decays (WRHDs) provide valuable insights into the nature of nonleptonic weak interactions [3]. In general, the radiative decays of a spin- $\frac{1}{2}$  hyperon consist of a parity conserving (Pwave) and a parity violating (S-wave) amplitude. The decay asymmetry parameter  $\alpha_{\gamma}$ , determined by the phase difference between S- and P-waves, can be measured from the asymmetric decay angle distribution of the final state baryon and presents a longstanding puzzle in WRHDs [4]. Although decay asymmetries of  $\Sigma^+ \to p\gamma$ and  $\Xi^- \to \Sigma^- \gamma$  decays are expected to be zero under SU(3) symmetry, experiments have measured non-zero values for these [5, 6]. Various phenomenological models have been proposed to explain the experimental results [7–11], however, none of them provide a unified description of all WRHDs. In particular, the insufficiency of short-distance contributions (e.g. W-exchange processes [12]) to the large decay asymmetries indicates a substantial contribution from non-perturbative QCD effects. To make further progress towards solving this puzzle, new and more precise measurements of any WRHD are desired [13, 14].

It is widely believed in the scientific community that the violation of the combined charge conjugation and parity symmetries (CP) is essential for elucidating the matter-antimatter asymmetry in the universe [15]. The current observed CP asymmetries [16] and the predictions of the standard model (SM) through the introduction of a single weak phase in the Cabibbo-Kobayashi-Maskawa matrix [2] are insufficient in explaining the observed matter-antimatter asymmetry. This has led to a surge in studies of CP violation beyond weak hadronic decays and beyond the SM. Weak radiative decays of s quark [17], c quark [18] and b quark [19] are sensitive to new physics beyond the SM [20] and may exhibit over 10% CP asymmetry in some models [19, 21]. The situation is less clear for baryons compared to mesons due to the complexity of their systems [22]. Experimentally, though weak radiative decays of heavy mesons have been studied thoroughly [23], measurements in the baryon sector are very limited [24, 25]. Due to complex non-perturbative QCD effects, CP asymmetries in WRHDs, which involve an s quark, are more complicated for theory predictions than in  $\Lambda_c$ ,  $\Lambda_b$ , and other heavy baryons. Nevertheless, they are experimentally attractive because of the larger branching fractions (BFs) at the level of  $\mathcal{O}(10^{-3})$ .

The decay  $\Xi^0 \to \Lambda \gamma$  is a fundamental process for the study of WRHDs. The current experimental results on hyperon nonleptonic decays and magnetic moments provide a reliable prediction on the P-wave amplitude of  $\Xi^0 \to \Lambda \gamma$  [26]. Therefore, its  $\alpha_{\gamma}$  serves as a crucial value to confirm the sources of the S-wave amplitude in WRHDs. On the other hand, a chiral perturbation theory (ChPT) for baryons can be constructed with only a few input parameters [13]. In baryon ChPT, a low energy constant  $C_{\rho}$  describes the direct photon emission contribution to the real part of the S-wave amplitude at tree level. To date,  $C_{\rho}$  can only be determined through the processes  $\Xi^0 \to \Lambda \gamma$  and  $\Xi^0 \to \Sigma^0 \gamma$ . Therefore, robust and precise experimental results are urgently needed for improving the theory. Although studies of  $\Xi^0 \to \Lambda \gamma$  have been performed with ever-increasing statistics at fixed target experiments [6, 27–29], all the measured BFs have been reported as relative values to the BF of  $\Xi^0 \to \Lambda \pi^0$ . Furthermore, the systematic uncertainty is dominating the precision of BF and  $\alpha_{\gamma}$  measurements.

The observation of hyperon transverse polarization in the decays  $J/\psi \to B\bar{B}$   $(B = \Lambda, \Sigma^{\pm,0}, \Xi^{-,0})$  at BESIII has opened a new territory to study the character of hyperon decays [30–32]. The unique spin entanglement information present in hyperon pairs enhances the statistical sensitivity to  $\alpha_{\gamma}$  compared to fixed target experiments [29] by several times with the same sample sizes [33]. Additionally, the application of the double-tag (DT) method [34] enables the measurement of absolute BFs with lower systematic uncertainty. These advantages have been validated in the studies of the decays  $\Lambda \to n\gamma$  [35] and  $\Sigma^+ \to p\gamma$  [25] at BESIII, where significant deviations of BFs from the world average values [36] have been observed.

In this Letter, using the  $J/\psi \to \Xi^0(\to \Lambda \gamma) \bar{\Xi}^0(\to \bar{\Lambda} \pi^0)$ decay based on  $(10\,087 \pm 44) \times 10^6 J/\psi$  events [37] collected at BESIII, we report measurements of the absolute BF and the decay asymmetry parameter of  $\Xi^0 \to \Lambda \gamma$ , as well as a potential *CP* asymmetry in the decay. Throughout this Letter, charge conjugation (c.c.) is always implied and  $\Lambda$  is reconstructed using its decay  $\Lambda \to p\pi^-$ , unless explicitly noted otherwise.

A detailed description of the design and performance of the BESIII detector can be found in Ref. [38], while the simulation and analysis software framework for BESIII is described in Refs. [39]. A double-tag method [34] is employed for event selection. To search for the decay  $\Xi^0 \rightarrow \Lambda \gamma$ , events of  $J/\psi \rightarrow \Xi^0 \bar{\Xi}^0$  are tagged by reconstructing a  $\bar{\Xi}^0$  signal (named 'single-tag (ST)' events) using its dominant decay channel  $\bar{\Xi}^0 \rightarrow \Lambda \pi^0$ . Subsequently, the signal  $\Xi^0 \rightarrow \Lambda \gamma$  is searched for in the system recoiling against the ST  $\bar{\Xi}^0$  (named 'DT'). The absolute BF is calculated by BF( $\Xi^0 \rightarrow \Lambda \gamma$ ) =  $\frac{N_{\rm DT}^{\rm obs} \varepsilon_{\rm DT}}{N_{\rm ST}^{\rm obs} \varepsilon_{\rm DT}} \frac{1}{{\rm BF}_{\Lambda \rightarrow p\pi^-}}$ , where  $N_{\rm ST(DT)}^{\rm obs}$  and  $\varepsilon_{\rm ST(DT)}$  are the ST (DT) yields and the corresponding detection efficiencies, and BF<sub> $\Lambda \rightarrow p\pi^-$ </sub> is the BF of  $\Lambda \rightarrow p\pi^-$ .

A general formula for the differential cross sections of the signal  $J/\psi \rightarrow \Xi^0(\rightarrow \Lambda\gamma)\bar{\Xi}^0(\rightarrow \bar{\Lambda}\pi^0)$ and the dominant background  $J/\psi \rightarrow \Xi^0\bar{\Xi}^0 \rightarrow \Lambda\pi^0 + \bar{\Lambda}\pi^0$  contains the nine measurable angles  $\xi = (\theta_{\Xi^0}, \theta_{\Lambda}, \theta_p, \theta_p, \theta_{\bar{\Lambda}}, \theta_{\bar{p}}, \theta_{\bar{p}})$  [40] (as illustrated in the supplemental material [41]), where  $\theta_{\Xi^0}$  is the polar angle of  $\Xi^0$  in the  $J/\psi$  rest frame,  $\theta_{\Lambda}$  ( $\theta_{\bar{\Lambda}}$ ) and  $\phi_{\Lambda}$  ( $\phi_{\bar{\Lambda}}$ ) are the polar and azimuthal angles of  $\Lambda$  ( $\bar{\Lambda}$ ) with respect to the  $\Xi^0$  ( $\bar{\Xi}^0$ ) helicity frame, and  $\theta_p$  ( $\theta_{\bar{p}}$ ) and  $\phi_p$  ( $\phi_{\bar{p}}$ ) are the polar and azimuthal angles of p ( $\bar{p}$ ) with respect to the  $\Lambda$  ( $\bar{\Lambda}$ ) helicity frame, respectively. With the above defined helicity angles, the differential cross section can be constructed under the helicity formalism:  $d\sigma \propto W(\xi) d\xi$ , where

$$\mathcal{W} = \sum_{\mu,\bar{\nu}=0}^{3} \sum_{\mu'=0}^{3} \sum_{\bar{\nu}'=0}^{3} C_{\mu\bar{\nu}} a_{\mu\mu'}^{\Xi^{0}} a_{\mu'0}^{\Lambda} a_{\bar{\nu}\bar{\nu}'}^{\bar{\Xi}^{0}} a_{\bar{\nu}'0}^{\bar{\Lambda}}.$$
 (1)

Here, *C* represents the polarization and spin correlation matrix of  $\Xi^0 \bar{\Xi}^0$ , and *a* are the decay matrices of the hyperons (i.e.  $\Xi^0$ ,  $\bar{\Xi}^0$ ,  $\Lambda$  and  $\bar{\Lambda}$ ), which depend on the decay products [41, 42]. The parameters for the matrices include  $\alpha_{\psi}$  and  $\Delta \Phi_{\psi}$  for  $J/\psi \to \Xi^0 \bar{\Xi}^0$ ,  $\alpha_0$  ( $\bar{\alpha}_0$ ) and  $\Delta \phi_0$ ( $\Delta \bar{\phi}_0$ ) for  $\Xi^0 \to \Lambda \pi^0$  ( $\bar{\Xi}^0 \to \bar{\Lambda} \pi^0$ ),  $\alpha_{\gamma}$  ( $\bar{\alpha}_{\gamma}$ ) for  $\Xi^0 \to \Lambda \gamma$ ( $\bar{\Xi}^0 \to \bar{\Lambda} \gamma$ ), and  $\alpha_{\Lambda}$  ( $\bar{\alpha}_{\Lambda}$ ) for  $\Lambda \to p\pi^-$  ( $\bar{\Lambda} \to \bar{p}\pi^+$ ).

A Monte Carlo (MC) simulated sample of generic  $J/\psi$ decays is used to study the potential background. The signal MC samples for ST signal  $e^+e^- \to J/\psi \to \Xi^0(\to$ anything) $\bar{\Xi}^0(\to \bar{\Lambda}\pi^0)$ , DT signal  $J/\psi \to \Xi^0(\to \Lambda\gamma)\bar{\Xi}^0(\to$  $\bar{\Lambda}\pi^0$ ) and the dominant background  $J/\psi \rightarrow \Xi^0 \bar{\Xi}^0 \rightarrow$  $\Lambda \pi^0 + \bar{\Lambda} \pi^0$  are generated with the amplitude according to Eq. (1). The input decay parameters for the simulation are fixed to those of the latest measurement from BE-SIII [32], except for  $\alpha_{\gamma}$  and  $\bar{\alpha}_{\gamma}$  which are determined in this analysis. The slight difference in reconstruction efficiencies between the signal MC samples and data is corrected with control samples [25]. Specifically, the selection efficiency for protons is studied with the control sample  $J/\psi \to p\bar{p}\pi^+\pi^-$ , the one for  $\pi^-$  and  $\Lambda$  reconstruction with the control sample  $J/\psi \to \Xi^-(\to \Lambda \pi^-)\bar{\Xi}^+(\to \bar{\Lambda}\pi^+)$ , the one for  $\pi^0$  with the control sample  $J/\psi \to \Xi^0(\to$  $\Lambda \pi^0 \bar{\Xi}^0 (\to \bar{\Lambda} \pi^0)$ , and the one for photon with the control sample  $J/\psi \to \gamma \mu^+ \mu^-$ . The correction coefficients are extracted as a function of the particle momentum and polar angle, and the efficiency corrected signal MC sample will be used to evaluate the efficiency and measure  $\alpha_{\gamma}$ .

Charged tracks and photon candidates are detected in the main drift chamber (MDC) and electromagnetic calorimeter (EMC), and are selected individually, with the same requirements as in Ref. [32]. Particle identification (PID) is applied to select (anti-)proton candidates [32] while charged tracks other than proton candidates are regarded as pions. The  $\bar{\Lambda}$  candidate is reconstructed with  $\bar{p}\pi^+$  combinations, which are constrained to originate from a common vertex and are required to have an invariant mass with  $|M_{\bar{p}\pi^+} - M_{\bar{\Lambda}}| < 6 \text{ MeV}/c^2$ , where  $M_{\bar{\Lambda}}$  is the nominal  $\bar{\Lambda}$  mass [36]. The  $\pi^0$  candidates are reconstructed with pairs of photons whose invariant mass is within the interval 115 MeV/ $c^2 < M_{\gamma\gamma} <$ 150 MeV/ $c^2$ , and the momenta are updated by a kinematic fit constraining  $m_{\gamma\gamma}$  to the nominal  $\pi^0$  mass [36].

The ST  $\overline{\Xi}^0$  candidate is reconstructed with the  $\overline{\Lambda}\pi^0$ combination whose invariant mass  $(M_{\bar{\Lambda}\pi^0} - M_{\bar{p}\pi^+} + M_{\bar{\Lambda}})$ is closest to the nominal  $\Xi^0$  mass  $(M_{\Xi^0})$  from PDG [36], and is required to fall in  $\left|M_{\bar{\Lambda}\pi^0}-M_{\bar{p}\pi^+}+M_{\bar{\Lambda}}-M_{\Xi^0}\right|<$  $12 \,\mathrm{MeV}/c^2$ . The ST yield is extracted by performing a binned maximum likelihood fit on the distribution of the recoiling mass, defined as  $M_{\rm rec}$  =  $\sqrt{(E_{\rm cms} - E_{\bar{p}\pi^+} - E_{\pi^0})^2/c^4 - (\mathbf{p}_{\bar{p}\pi^+} + \mathbf{p}_{\pi^0})^2/c^2},$  where  $E_{\rm cms}$  is the center-of-mass energy,  $E_{\bar{p}\pi^+}$  ( $\mathbf{p}_{\bar{p}\pi^+}$ ) and  $E_{\pi^0}$  $(\mathbf{p}_{\pi^0})$  are the energies (momenta) of  $\overline{\Lambda}$  and  $\pi^0$  in the  $J/\psi$ rest frame, respectively. The model for fitting is constructed as follows. First, a signal sample, whose  $\pi^0$  is matched in the MC truth by requiring the angle between the generated and reconstructed  $\pi^0$  directions less than  $20^{\circ}$ , is obtained. Then, the signal is described with the  $M_{\rm rec}$  distribution of this signal sample. The backgrounds of  $J/\psi \to \pi^0 \Lambda \bar{\Sigma}^0 + \text{c.c.}, J/\psi \to \Sigma^{0*} \bar{\Sigma}^{0*}$ , and the combinatorial background of the signal are all described by the shapes of the corresponding MC simulated samples. Other backgrounds are described with a third-order polynomial function. To compensate the resolution difference between data and MC simulation, the signal shape is convolved with a Gaussian function. The fit curves are shown in the supplemental material [41]. The ST yields and the detection efficiencies evaluated with the corresponding signal MC samples are summarized in Table I.

The signal  $\Xi^0 \to \Lambda \gamma$  is selected with the remaining charged and neutral tracks recoiling against the ST  $\overline{\Xi}^0$ candidates. Events with at least one  $\Lambda \to p\pi^-$  candidate and one photon are selected for further DT analysis. A five-constraint (5C) kinematic fit is performed under the hypothesis  $J/\psi \to \Lambda \overline{\Lambda} \pi^0 \gamma$ , imposing overall energymomentum conservation and requiring the  $\pi^0$  candidate to have its nominal mass [36]. The  $\chi^2$  of the 5C kinematic fit ( $\chi^2_{5C}$ ) is required to be less than 40. In case of multiple candidate combinations in one event, only the one with the minimum  $\chi^2_{5C}$  is kept.

After the above selection, MC studies [43] indicate that the dominant sources of background events are the processes  $J/\psi \to \Xi^0(\to \Lambda \pi^0) \bar{\Xi}^0(\to \bar{\Lambda} \pi^0)$  and  $J/\psi \to \Sigma^0(\Sigma^{0*}) + X$ , from here on referred to as BKG-I and BKG-II, respectively, where X denotes any possible particle. In particular, the decays  $J/\psi \to \pi^0 \Lambda \bar{\Sigma}^0$ +c.c. and  $J/\psi \to \Sigma^{0*} \bar{\Sigma}^{0*}$  account for a large proportion of BKG-II.

The momentum of  $\Lambda$  in the rest frame of  $\Xi^0$   $(p_\Lambda)$ , which is well separated between the signal and BKG-I, will be used to determine the signal yield. It should be noted that  $\Sigma^{0(*)}$  in BKG-II are of short lifetime, and the daughter particles of  $\Lambda$  and  $\bar{\Lambda}$  originate from the same vertex point. Therefore, a powerful discrimination of signal from BKG-II requires [25] the distance L between the event primary vertex and the intersection point of  $\Lambda$  and  $\bar{\Lambda}$  momentum vector to satisfy  $L/\sigma_L > 2$ , where  $\sigma_L$  is the resolution of L [44]. This requirement rejects 90% of BKG-II events with a signal loss of less than 20%. The BKG-II events are further suppressed by the requirement of  $|M_{\gamma\bar{\Lambda}} - M_{\bar{\Sigma}^0}| > 12 \,\mathrm{MeV}/c^2$ , where  $M_{\gamma\bar{\Lambda}}$  is the invariant mass of  $\gamma$  from the signal side and  $\bar{\Lambda}$  from the ST side, and  $M_{\bar{\Sigma}^0}$  is the nominal  $\bar{\Sigma}^0$  mass [36].



FIG. 1. Distribution of (a)  $p_{\Lambda}$  for  $\Xi^0 \to \Lambda \gamma$  and (b)  $p_{\bar{\Lambda}}$  for  $\bar{\Xi}^0 \to \bar{\Lambda} \gamma$ . The black dots with error bars are data, the red solid curves are the fit results and the orange dashed, cyan dashed and magenta dashed curves are the signal,  $\Xi^0 \to \Lambda \pi^0$ , and other background shapes, respectively. The inserted figures are the zoomed-in views of the signal region.

Unbinned extended maximum likelihood fits are performed on the  $p_{\Lambda}$  distributions, shown in Fig. 1, to determine the DT yields. In the fit, the shapes of the signal channel  $\Xi^0 \to \Lambda \gamma$  and of the background channel  $\Xi^0 \to \Lambda \pi^0$  are described with the corresponding MC simulated shapes convolved with Gaussian functions, individually, and the remaining background is described with a first-order polynomial function. The fits are performed individually for the processes  $\Xi^0 \to \Lambda \gamma$  and  $\bar{\Xi}^0 \to \bar{\Lambda} \gamma$ , as shown in Fig. 1. A simultaneous fit between the two c.c. channels is also carried out by assuming the same BF between  $\Xi^0 \to \Lambda \gamma$  and  $\bar{\Xi}^0 \to \bar{\Lambda} \gamma$ . As summarized in Table I, the results are well consistent with each other.

The decay asymmetry parameter is measured for the  $\Xi^0 \to \Lambda \gamma$  and  $\bar{\Xi}^0 \to \bar{\Lambda} \gamma$  decay channels, which after applying 0.17 GeV/ $c < p_{\Lambda}(p_{\bar{\Lambda}}) < 0.19$  GeV/c include 371 and 391 events, respectively, with a signal purity of ~ 77%. The joint likelihood function ( $\mathcal{L}$ ) is constructed according to Eq. (1), which incorporates the set of observables  $\xi$  and a set of characterized decay parameters  $H = (\alpha_{\psi}, \Delta \Phi_{\psi}, \alpha_{\gamma}, \bar{\alpha}_0, \Delta \bar{\phi}_0, \alpha_{\Lambda}, \alpha_{\bar{\Lambda}})$ . The effect of the detection efficiency on  $\mathcal{L}$  is evaluated by the normalization factor  $\mathcal{N}$ , and is calculated with the efficiency corrected signal MC sample by using the importance sampling method [45]. The target function for the fit is  $S = -\ln \mathcal{L} + \ln \mathcal{L}_{\rm bkg}$ , where the contributions of background  $\mathcal{L}_{\rm bkg}$  are estimated with the corresponding MC samples, including  $J/\psi \to \Xi^0(\to \Lambda \pi^0)\bar{\Xi}^0(\to \bar{\Lambda}\pi^0)$ ,  $J/\psi \to \pi^0\Lambda\bar{\Sigma}^0+\text{c.c.}$  and  $J/\psi \to \Sigma^{0*}\bar{\Sigma}^{0*}$  MC samples. The background likelihoods are normalized to the fitted yields of the corresponding components in the data sample. The fits are performed for the  $\Xi^0 \to \Lambda \gamma$  and  $\bar{\Xi}^0 \to \bar{\Lambda}\gamma$  decays individually. Furthermore, a simultaneous fit, assuming the same magnitude but opposite sign for the decay asymmetry parameters between the c.c. channels, is also performed. All fit results are shown in Table I. The effect of the decay asymmetry is visualized via three moments, each of which is calculated for m = 8 intervals in  $\cos \theta_{\Xi^0}$ :

$$M_{1}(\cos\theta_{\Xi^{0}}^{k}) = \frac{m}{N} \sum_{i=1}^{N_{k}} \sin\theta_{\Lambda}^{i} \sin\theta_{\Lambda}^{i} \cos\phi_{\Lambda}^{i} \cos\phi_{\Lambda}^{i},$$
  

$$M_{2}(\cos\theta_{\Xi^{0}}^{k}) = \frac{m}{N} \sum_{i=1}^{N_{k}} \sin\theta_{\Lambda}^{i} \sin\phi_{\Lambda}^{i},$$
  

$$M_{3}(\cos\theta_{\Xi^{0}}^{k}) = \frac{m}{N} \sum_{i=1}^{N_{k}} \cos\theta_{p}^{i},$$
  
(2)

where N is the total number of events,  $\cos \theta_{\Xi^0}^k$  is the kth interval of  $\cos \theta_{\Xi^0}$  and  $N_k$  is the number of events in the interval. Fig. 2 shows the comparison of moments between data and MC projections. The total  $\chi^2$ , by averaging the  $\chi^2$  of the three moment distributions, are determined for  $\Xi^0 \to \Lambda \gamma$  and  $\bar{\Xi}^0 \to \bar{\Lambda} \gamma$ , respectively. The total  $\chi^2$  per degree of freedom are 10.5/8 and 10.6/8 by comparing data to phase space MC sample, and 7.5/8 and 7.2/8 by comparing data to the fit results. The fit results are more consistent with data on the moment distributions.



FIG. 2. Moment distributions of (a)  $M_1$ , (b)  $M_2$  and (c)  $M_3$ for the  $\Xi^0 \to \Lambda \gamma$  decay, and (d), (e), and (f) for the  $\bar{\Xi}^0 \to \bar{\Lambda} \gamma$ decay. The phase space MC events are represented by the red solid lines, the signal MC events by the blue dashed lines and the data by the black dots with error bars.

The statistical uncertainties of BFs and  $\alpha_{\gamma}$  are determined using the error covariance matrix of the fit results [46], and the total systematic uncertainties of BFs and  $\alpha_{\gamma}$  are studied individually. The total systematic uncertainties are summed in quadrature and are shown in Table I for the individual and c.c. combined results.

The systematic uncertainties of proton tracking and PID (0.5%), pion tracking (2.3%),  $\Lambda$  reconstruction (0.9%), and photon detection (0.4%) for the BF measurements are obtained as the statistical uncertainties of the efficiency correction coefficients. The uncertainties associated with the above sources for the  $\alpha_{\gamma}$  measurement (0.001 in total) are estimated by calculating  $\mathcal{N}$ from the signal MC sample without efficiency correction. The uncertainties associated with the  $\chi^2_{5C}$ ,  $L/\sigma_L$  and  $m_{\gamma\bar{\Lambda}}$  requirements are estimated by applying the identical or similar requirements on the control sample of  $J/\psi \to \Xi^0 (\to \Lambda \pi^0) \bar{\Xi}^0 (\to \bar{\Lambda} \pi^0)$ , and are determined to be 0.5% (0.001), 1.3% (0.001), 0.2% (0.001) for the BF  $(\alpha_{\gamma})$  measurement. Uncertainties from the input decay parameters [32] and  $\alpha_{\gamma}$  are estimated by varying the input parameters within their uncertainties in the signal MC generation and in the  $\alpha_{\gamma}$  fit, yielding the uncertainties 0.6 % for BF and 0.002 for  $\alpha_{\gamma}$ .

The uncertainties of ST (1.7%) and DT (1.8%) yields are estimated with alternative fit scenarios, including the fit range, bin width, signal and background shapes. The uncertainties associated with the fit on  $\alpha_{\gamma}$  are evaluated by changing the background yields within uncertainties and replacing the MC evaluated background likelihood value with that estimated with the sideband events (i.e. events satisfing 0.075 <  $p_{\Lambda}$  < 0.110 GeV/*c* and 0.204 <  $p_{\Lambda}$  < 0.216 GeV/*c*), which are determined to be 0.010 and 0.012, respectively. The total uncertainties are determined to be 4.9% (5.2%) for the BF of  $\Xi^0 \rightarrow \Lambda\gamma$ ( $\bar{\Xi}^0 \rightarrow \bar{\Lambda}\gamma$ ), and 4.6% for the c.c. combined BF result by averaging the uncorrelated uncertainties. The total uncertainties of  $\alpha_{\gamma}$  are 0.016 (0.044) for  $\Xi^0 \rightarrow \Lambda\gamma$ ( $\bar{\Xi}^0 \rightarrow \bar{\Lambda}\gamma$ ), and 0.019 for the combined result.

Based on the above results, two independent CP asymmetry observables are constructed,

$$\Delta_{CP} = \frac{BF_{+} - BF_{-}}{BF_{+} + BF_{-}} = -0.033 \pm 0.049_{\text{stat.}} \pm 0.031_{\text{syst.}},$$
$$A_{CP} = \frac{\alpha_{\gamma} + \bar{\alpha}_{\gamma}}{\alpha_{\gamma} - \bar{\alpha}_{\gamma}} = -0.120 \pm 0.084_{\text{stat.}} \pm 0.029_{\text{syst.}},$$
(2)

(3) where BF<sub>+</sub> (BF<sub>-</sub>) denotes the BF of  $\Xi^0 \to \Lambda \gamma$  ( $\bar{\Xi}^0 \to \bar{\Lambda} \gamma$ ), and the systematic uncertainties of  $\Delta_{CP}$  and  $A_{CP}$ only include the uncorrelated uncertainties. The results are consistent with zero within uncertainties.

In summary, we have performed a study of the weak radiative hyperon decay  $\Xi^0 \to \Lambda \gamma$  using  $\Xi^0 \bar{\Xi}^0$  pairs produced in  $(10\,087 \pm 44) \times 10^6 J/\psi$  events collected with the BESIII detector. Benefiting from the spin entanglement between  $\Xi^0$  and  $\bar{\Xi}^0$  from  $J/\psi$  decays, the absolute BF and decay asymmetry parameter  $\alpha_{\gamma}$  are measured with high precision. The absolute BF of this decay is

TABLE I. Individual and c.c. combined BFs and  $\alpha_{\gamma}$  measurement results of  $\Xi^0 \to \Lambda \gamma$  and  $\bar{\Xi}^0 \to \bar{\Lambda} \gamma$ . The first uncertainties are statistical and the second ones are systematic, if present.

| Channels                     | $\Xi^0 \to \Lambda \gamma$   | $\bar{\Xi}^0 \to \bar{\Lambda}\gamma$ |
|------------------------------|------------------------------|---------------------------------------|
| $N_{\rm ST}^{\rm obs}$       | $1400541{\pm}1989$           | $1611216{\pm}2111$                    |
| $\varepsilon_{\rm ST}(\%)$   | $17.61 {\pm} 0.01$           | $19.77 \pm 0.01$                      |
| $N_{\rm DT}^{\rm obs}$       | $308 \pm 21$                 | $330 \pm 25$                          |
| $\varepsilon_{\rm DT}$ (%)   | $4.49 {\pm} 0.02$            | $4.92 \pm 0.02$                       |
| Individual BF $(10^{-3})$    | $1.348 \pm 0.090 \pm 0.054$  | $1.326 \pm 0.098 \pm 0.066$           |
| Combined BF $(10^{-3})$      | $1.347 \pm 0.066 \pm 0.054$  |                                       |
| Individual $\alpha_{\gamma}$ | $-0.652 \pm 0.092 \pm 0.016$ | $0.830 \pm 0.080 \pm 0.044$           |
| Combined $\alpha_{\gamma}$   | $-0.741 \pm 0.062 \pm 0.019$ |                                       |

 $(1.347\pm0.066_{\text{stat.}}\pm0.054_{\text{syst.}})\times10^{-3}$ , and its decay asymmetry parameter  $\alpha_{\gamma}$  is  $-0.741\pm0.062_{\text{stat.}}\pm0.019_{\text{syst.}}$ . This work represents the first study of this decay at an electron-positron collider. The obtained results for



FIG. 3. Distribution of  $\alpha_{\gamma}$  versus BF of the  $\Xi^0 \to \Lambda \gamma$  decay. The black star denotes the results measured by this work and the blue contours correspond to the 68%/95% confidencelevel of the results. The red diamond represents the PDG values [36] of the BF and  $\alpha_{\gamma}$ . Other symbols in blue or cyan stand for the results predicted by the vector meson dominance model (VMD) [47], pole model (PM I refers to Ref. [7] and PM II refers to Ref. [9]), nonrelativistic constituent quark model (NRCQM) [10], broken SU(3) model (BSU(3)) [48] and a ChPT theory [49]. The BF result of ChPT theory [49] is scaled down by a factor of 10 to fit within the figure.

BF and  $\alpha_{\gamma}$  are consistent with the world average values [36] within  $1.6\sigma$  and  $0.6\sigma$ , respectively, but are inconsistent with various theoretical predictions. The results presented in this Letter serve as a fair confirmation of previous measurements [36] and highlight the need to improve the unified weak radiative hyperon decays theories [13, 26, 48]. This Letter also reports the first search for *CP* asymmetry in the decay  $\Xi^0 \to \Lambda \gamma$ . No evidence for *CP* violation is found, but its potential to study *CP* asymmetry in an electron-positron collider is exhibited and is expected to be further tested at the proposed Super Tau-Charm Facilities with data samples larger by two orders of magnitude [50, 51].

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- E. Goudzovski *et al.*, Rept. Prog. Phys. **86**, 016201 (2023).
- [2] I. I. Bigi, G. Ricciardi, and M. Pallavicini, New Era for CP Asymmetries (World Scientific, 2021).
- [3] R. E. Behrends, Phys. Rev. **111**, 1691 (1958).
- [4] Y. Hara, Phys. Rev. Lett. **12**, 378 (1964).
- [5] M. Bazin, H. Blumenfeld, and U. Nauenberg, Phys. Rev. Lett. 14, 154 (1965); M. Kobayashi, J. Haba, T. Homma, H. Kawai, K. Miyake, T. S. Nakamura, N. Sasao, and Y. Sugimoto, Phys. Rev. Lett. 59, 868 (1987); S. Teige et al., Phys. Rev. Lett. 63, 2717 (1989); M. Foucher et al. (E761 Collaboration), Phys. Rev. Lett. 68, 3004 (1992); T. Dubbs et al., Phys. Rev. Lett. 72, 808 (1994); A. Alavi Harati et al. (KTeV Collaboration), Phys. Rev. Lett. 86, 3239 (2001).
- [6] C. James et al., Phys. Rev. Lett. 64, 843 (1990).
- [7] M. B. Gavela, A. L. Yaouanc, L. Oliver, O. Pène, J. C. Raynal, and T. N. Pham, Phys. Lett. B 101, 417 (1981).

- [8] Y. I. Kogan and M. A. Shifman, Sov. J. Nucl. Phys. 38, 628 (1983).
- [9] G. Nardulli, Phys. Lett. B **190**, 187 (1987).
- [10] P. Y. Niu, J. M. Richard, Q. Wang, and Q. Zhao, Chin. Phys. C 45, 013101 (2020).
- [11] I. I. Balitsky, V. M. Braun, and A. V. Kolesnichenko, Nucl. Phys. B **312**, 509 (1989); D. Chang, arXiv:hepph/0011163 (2000); E. N. Dubovik, V. S. Zamiralov, S. N. Lepshokov, and A. E. Shkolnikov, Phys. At. Nucl. **71**, 136 (2008); P. Zenczykowski, Acta Phys. Polon. B **51**, 2111 (2020).
- [12] R. C. Verma and A. Sharma, J. Phys. G 12, 1329 (1986).
- [13] R. X. Shi, S. Y. Li, J. X. Lu, and L. S. Geng, Sci. Bull. 67, 2298 (2022).
- [14] R. X. Shi and L. S. Geng, Sci. Bull. 68, 779 (2023).
- [15] A. D. Sakharov, Pisma Zh. Eksp. Teor. Fiz. 5, 32 (1967).
- [16] J. H. Christenson, J. W. Cronin, V. L. Fitch, and R. Turlay, Phys. Rev. Lett. 13, 138 (1964); B. Aubert et al. (BaBar Collaboration), Phys. Rev. Lett. 87, 091801 (2001); K. Abe et al. (Belle Collaboration), Phys. Rev. Lett. 87, 091802 (2001); R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 122, 211803 (2019).
- [17] G. Costa and P. K. Kabir, Phys. Rev. Lett. 18, 429 (1967); G. Ecker, A. Pich, and E. de Rafael, Nucl. Phys. B 303, 665 (1988); H. Y. Cheng, Phys. Lett. B 315, 170 (1993); Phys. Rev. D 49, 3771 (1994).
- [18] N. Adolph, J. Brod, and G. Hiller, Eur. Phys. J. C 81, 45 (2021);
   S. de Boer and G. Hiller, JHEP 08, 091 (2017).
- [19] D. Atwood, M. Gronau, and A. Soni, Phys. Rev. Lett. **79**, 185 (1997); J. M. Soares, Nucl. Phys. B **367**, 575 (1991); M. Beneke, T. Feldmann, and D. Seidel, Eur. Phys. J. C **41**, 173 (2005); M. Matsumori, A. I. Sanda, and Y. Y. Keum, Phys. Rev. D **72**, 014013 (2005); P. Ball, G. W. Jones, and R. Zwicky, Phys. Rev. D **75**, 054004 (2007).
- [20] C. Delaunay, J. F. Kamenik, G. Perez, and L. Randall, JHEP 01, 027 (2013); J. Lyon and R. Zwicky, Phys. Rev. D 106, 053001 (2022); A. Paul and D. M. Straub, JHEP 04, 027 (2017); A. Biswas, S. Mandal, and N. Sinha, Int. J. Mod. Phys. A 33, 1850194 (2018).
- [21] G. Isidori and J. F. Kamenik, Phys. Rev. Lett. 109, 171801 (2012);
   G. Bhattacharyya, D. Chang, C. H. Chou, and W. Y. Keung, Phys. Lett. B 493, 113 (2000).
- [22] X. L. Chen, C. S. Gao, and X. Q. Li, Phys. Rev. D 51, 2271 (1995); S. S. Nair, E. Perotti, and S. Leupold, Phys. Lett. B 788, 535 (2019); G. Hiller and A. Kagan, Phys. Rev. D 65, 074038 (2002); N. Adolph and G. Hiller, Phys. Rev. D 105, 116001 (2022).
- [23] E. J. Ramberg *et al.* (E731 Collaboration), Phys. Rev. Lett. **70**, 2529 (1993); J. P. Lees *et al.* (BaBar Collaboration), Phys. Rev. Lett. **109**, 191801 (2012); T. Saito *et al.* (Belle Collaboration), Phys. Rev. D **91**, 052004 (2015); A. Abdesselam *et al.* (Belle Collaboration), Phys. Rev. Lett. **118**, 051801 (2017); T. Horiguchi *et al.* (Belle Collaboration), Phys. Rev. Lett. **119**, 191802 (2017).
- [24] R. Aaij *et al.* (LHCb Collaboration), Phys. Rev. D 105, L051104 (2022).
- [25] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. Lett. **130**, 211901 (2023).
- [26] J. Lach and P. Zenczykowski, Int. J. Mod. Phys. A 10, 3817 (1995).
- [27] V. Fanti *et al.* (NA48 Collaboration), Eur. Phys. J. C 12, 69 (2000).
- [28] A. Lai et al. (NA48 Collaboration), Phys. Lett. B 584,

251 (2004).

- [29] J. R. Batley et al., Phys. Lett. B 693, 241 (2010).
- [30] M. Ablikim *et al.* (BESIII Collaboration), Nature Phys. 15, 631 (2019); Phys. Rev. Lett. 126, 092002 (2021); Phys. Rev. Lett. 125, 052004 (2020); JHEP 11, 226 (2021); Nature 606, 64 (2022); M. Ablikim *et al.* (BE-SIII), (2024), arXiv:2406.06118 [hep-ex].
- [31] M. Ablikim *et al.* (BESIII Collaboration), arXiv:2309.14667 [hep-ex].
- [32] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. D 108, L031106 (2023).
- [33] P. C. Hong, R. G. Ping, T. Luo, X. R. Zhou, and H. Li, Chin. Phys. C 47, 093103 (2023).
- [34] R. M. Baltrusaitis *et al.* (MARK III Collaboration), Phys. Rev. Lett. **56**, 2140 (1986).
- [35] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. Lett. **129**, 212002 (2022).
- [36] R. L. Workman *et al.* (Particle Data Group), PTEP 2022, 083C01 (2022).
- [37] M. Ablikim *et al.* (BESIII Collaboration), Chin. Phys. C 46, 074001 (2022).
- [38] M. Ablikim et al. (BESIII Collaboration), Nucl. Instrum. Meth. A 614, 345 (2010).

- [39] W. Li *et al.*, Proc. Int. Conf. Comput. High Energy and Nucl. Phys , 225 (2006); D. M. Asner *et al.*, Int. J. Mod. Phys. A **24S1**, 499 (2009); J. Zhang *et al.*, Radiat. Detect. Technol. Methods **2**, 1 (2018).
- [40] E. Perotti, G. Fäldt, A. Kupsc, S. Leupold, and J. J. Song, Phys. Rev. D 99, 056008 (2019).
- [41] See Supplemental Material at URL to be inserted by publisher for additional details.
- [42] V. Batozskaya, A. Kupsc, N. Salone, and J. Wiechnik, Phys. Rev. D 108, 016011 (2023).
- [43] X. Zhou, S. Du, G. Li, and C. Shen, Comput. Phys. Commun. 258, 107540 (2021).
- [44] M. Xu et al., Chin. Phys. C 34, 92 (2010).
- [45] T. Kloek and H. K. van Dijk, Econometrica 46, 1 (1978).
   [46] F. James and M. Roos, Comput. Phys. Commun. 10, 343
- [40] F. James and M. Roos, Comput. Phys. Commun. 10, 343 (1975).
- [47] P. Zenczykowski, Phys. Rev. D 44, 1485 (1991).
- [48] P. Zenczykowski, Phys. Rev. D 73, 076005 (2006).
- [49] B. Borasoy and B. R. Holstein, Phys. Rev. D 59, 054019 (1999).
- [50] A. E. Bondar *et al.* (Charm-Tau Factory Collaboration), Phys. Atom. Nucl. **76**, 1072 (2013).
- [51] M. Achasov et al., Front. Phys. 19, 14701 (2024).