Supporting Information for Non-random network connectivity comes in pairs

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SI1

Solving

$$\mu = px + (1 - p)y \tag{1}$$

for p gives

$$p = \frac{\mu - y}{x - y},\tag{2}$$

which, plugged into

$$\varrho = \frac{px^2 + (1-p)y^2}{\mu^2},\tag{3}$$

yields

$$\varrho = \frac{\left(\frac{\mu - y}{x - y}\right)x^2 + \left(1 - \frac{\mu - y}{x - y}\right)y^2}{\mu^2} \tag{4}$$

$$= \frac{\left(\frac{\mu - y}{x - y}\right)(x^2 - y^2) + y^2}{\mu^2} \tag{5}$$

$$=\frac{(\mu-y)(x+y)+y^2}{\mu^2}$$
 (6)

$$=\frac{x+y}{\mu} - \frac{xy}{\mu^2}. (7)$$

SI2

Solve

$$p = \frac{\mu - y}{x - y} \tag{8}$$

for y and since $x \ge \mu$,

$$y = \frac{\mu - px}{1 - p} \le \frac{\mu - p\mu}{1 - p} = \mu. \tag{9}$$

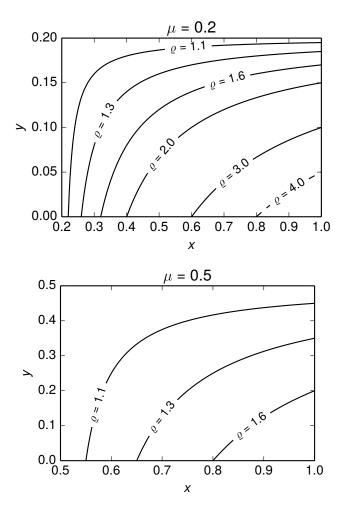


Figure S1: Relative overrepresentation ϱ of bidirectional connections in networks with a fraction of pairs connected with a high probability x and the rest of the pairs connected with a low probability y. **Top** Overall connection probability in the network $\mu=0.2$ **Bottom** $\mu=0.5$