A general principle of dendritic constancy – a neuron's size and shape invariant excitability

*Hermann Cuntz^{a,b}, Alexander D Bird^{a,b}, Marcel Beining^{a,b,c,d}, Marius Schneider^{a,b}, Laura Mediavilla^{a,b}, Felix Z Hoffmann^{a,b}, Thomas Deller^{c,1}, Peter Jedlicka^{b,c,e,1}

^{*a*} Ernst Strüngmann Institute (ESI) for Neuroscience in cooperation with the Max Planck Society, 60528 Frankfurt am Main, Germany

^b Frankfurt Institute for Advanced Studies, 60438 Frankfurt am Main, Germany

^{*c*} Institute of Clinical Neuroanatomy, Neuroscience Center, Goethe University, 60590 Frankfurt am Main, Germany

^d Max Planck Insitute for Brain Research, 60438 Frankfurt am Main, Germany

^{*e*} ICAR3R – Interdisciplinary Centre for 3Rs in Animal Research, Justus Liebig University Giessen, 35390 Giessen, Germany

¹ Joint senior authors

*cuntz@fias.uni-frankfurt.de

Keywords

Electrotonic analysis, Compartmental model, Morphological model, Excitability, Neuronal scaling, Passive normalisation, Cable theory

Dendritic constancy

In brief

We show that realistic neuron models essentially collapse to point neurons when stimulated by randomly distributed inputs instead of by single synapses or current injection in the soma.

Highlights

- A simple equation that predicts voltage in response to distributed synaptic inputs.
- Responses to distributed and clustered inputs are largely independent of dendritic length.
- Spike rates in various Hodgkin Huxley (HH) like or Leaky Integrate-and-Fire (LIF) models are largely independent of morphology.
- Precise spike timing (firing pattern) depends on dendritic morphology.
- NeuroMorpho.Org database-wide analysis of the relation between dendritic morphology and electrophysiology.
- Our equations set precise input-output relations in realistic dendrite models.

Dendritic constancy

1

18

Abstract

Reducing neuronal size results in less cell membrane and therefore lower input conductance. 2 Smaller neurons are thus more excitable as seen in their voltage responses to current injections з in the soma. However, the impact of a neuron's size and shape on its voltage responses to 4 synaptic activation in dendrites is much less understood. Here we use analytical cable theory 5 to predict voltage responses to distributed synaptic inputs and show that these are entirely 6 independent of dendritic length. For a given synaptic density, a neuron's response depends 7 only on the average dendritic diameter and its intrinsic conductivity. These results remain 8 true for the entire range of possible dendritic morphologies irrespective of any particular 9 arborisation complexity. Also, spiking models result in morphology invariant numbers of 10 action potentials that encode the percentage of active synapses. Interestingly, in contrast to 11 spike rate, spike times do depend on dendrite morphology. In summary, a neuron's excitability 12 in response to synaptic inputs is not affected by total dendrite length. It rather provides a 13 homeostatic input-output relation that specialised synapse distributions, local non-linearities 14 in the dendrites and synaptic plasticity can modulate. Our work reveals a new fundamental 15 principle of dendritic constancy that has consequences for the overall computation in neural 16 circuits. 17

Introduction

Because of their cell-type specific characteristic morphologies, dendritic trees have commonly 19 been assumed to be crucial for a neuron's intrinsic computations. It has been shown that 20 altering the morphology (Mainen and Sejnowski, 1996; Vetter et al., 2001) or the topology 21 (van Elburg and van Ooyen, 2010; van Ooyen et al., 2002) of neurons while keeping the 22 electrotonic features unchanged has a profound impact on the spiking behaviour of the cell. 23 On the other hand, the morphology of dendrites has been shown to be largely predicted 24 by connectivity rules (Cuntz et al., 2010) rather than by the specific computation that they 25 perform. Also, dendrites were shown to follow general principles that equalise passive (Bird 26 and Cuntz, 2016; Cuntz et al., 2007; Connelly et al., 2016; Jaffe and Carnevale, 1999) and active 27 (Häusser, 2001; Magee, 2000) signal propagation indicating that the blueprints of computation 28 for single neurons might be more stereotypical than previously assumed. In fact, principles of 29 conservative scaling that preserve electrotonic features have been proposed for a number of 30 cell types (Bakken and Stevens, 2011; Bekkers and Stevens, 1990; Cuntz et al., 2013). Similarly, 31

Dendritic constancy

Cuntz et al.

general morphological scaling laws, have been discovered for dendritic arbours of various
sizes (Cuntz et al., 2012; Snider et al., 2010; Teeter and Stevens, 2011). However, it remains
unclear how electrotonic and morphological scaling principles relate to one another and how
their interplay would affect well-known neuronal computations in dendrites (e.g. Branco et al., 2010; Gabbiani et al., 2002; Poirazi et al., 2003b,a; Single and Borst, 1998). Therefore, we
study here the dependence of input-output properties of dendrites on their size and shape.

One of the most eminent electrophysiological features of neurons that depend on dendritic 38 shape is the input conductance (Koch et al., 1990; Rall et al., 1967). Smaller cells with smaller 39 input conductances are more excitable for somatic current injections than larger cells because a 40 voltage threshold for spike initiation is reached with a lower input current in accordance with 41 Ohm's law (Chavlis et al., 2017; Šišková et al., 2014). This relation is true for somatic activation 42 of neurons and its size- and shape-dependence of voltage responses is well understood. 43 However, the corresponding effect of changes in input conductance on voltage responses to 44 distributed synaptic inputs have not been sufficiently studied. Rules identified for current 45 transfer within dendritic arbours (Bird and Cuntz, 2016; Cuntz et al., 2007; London et al., 46 1999; Rall and Rinzel, 1973; Rinzel and Rall, 1974) have allowed the prediction of responses 47 to individual or a few synaptic inputs (Magee, 2000; Williams and Stuart, 2003). Similar 48 rules should be applicable at the level of richer synaptic input but they have not yet been 49 identified. In this work, we specifically address the question how neuronal firing rate and 50 firing patterns are affected by dendritic size and shape in the case of multiple, distributed 51 synaptic inputs. We show that passive electrotonic principles generally render the synaptically 52 driven excitability of neurons invariable to length for the entire range of existing dendritic 53 trees. Since this dendritic constancy principle supports the stability of neuronal spiking, it 54 may complement other well-established synaptic and intrinsic mechanisms of firing rate 55 homeostasis (Turrigiano and Nelson, 2004). 56

Dendritic constancy



Fig 1. Analytical prediction indicates that responses to distributed synaptic inputs in a cable are independent of cable length.

A, Sketch illustrating the impact of a new branch on dendrite length and number of synapses. **B**, Input conductance G_{IN} of cables with constant diameters for a wide range of electrotonic lengths. G_{∞} , the input conductance of a semi-infinite cable and \hat{G}_{IN} , the collapsed total membrane conductance are indicated by dashed lines for reference. **C**, Mean steady-state voltage responses to distributed inputs as a function of electrotonic length. V_{∞} , the response to distributed synapses in the semi-infinite cable and \hat{V} , the linear extrapolation of the voltage response at the root and therefore the response in a collapsed cable are indicated by dashed lines. **D**, Bottom panel shows steady-state voltage responses at the proximal end to distributed current injections every μ m (straight line, **Equation 1**) and to synaptic inputs every μ m (dashed line, **Equation 1'**). Top panel shows the average current transfer versus the ratio of G_{IN} to \hat{G}_{IN} for the cables of varying lengths from **B**. Panels **B**—**D** were obtained from numerical simulations validating exactly the results of our analytical calculations.

Results

The idea behind this work comes from the simple reasoning that while larger neurons are in principle less excitable they also receive more synapses (**Figure 1A**). The higher input conductance and resulting decreased excitability might therefore compensate for the increase of effective current the neuron receives through its synaptic inputs. In contrast to most traditional theoretical studies on dendritic integration with their focus on somatic activation

Dendritic constancy

of the cell or activation with few synapses, we therefore focus here on the voltage responses to distributed synaptic inputs. In the following, we first study these relations analytically in the simple passive cable and subsequently move to passive and then active responses in dendritic trees with their full morphology. 66

Analytical calculations for passive cables predict length-invariant responses 67 to distributed synaptic inputs 68

Experimentally, the input conductance that predicts a neuron's excitability is most typically 69 obtained from somatic current injection with concurrent somatic voltage measurements 70 using Ohm's law to relate conductance, current and voltage. The corresponding analytical 71 calculations for a simple dendritic cable are readily available from classical cable theory 72 introduced to neuroscience by Wilfrid Rall. Considerations of current spread in a passive 73 cylinder allow one to predict the input conductance G_{IN} for any cable of electrotonic length L 74 measured in terms of $\lambda = \sqrt{\frac{G_{id}}{4G_m}}$, the electrotonic length constant, a distance unit over which 75 the voltage decays to about a third of the proximal voltage (Koch and Segev, 1999; Rushton, 76 1937). Here, the diameter is d_i , the specific axial conductance is G_i and the specific membrane 77 conductance is G_m . For short cables, G_{IN} increases nearly linearly with L as it approximates 78 the collapsed input conductance $\hat{G}_{IN} = G_m \pi d\lambda L$ of the cable, the total sum of the membrane 79 leak (Figure 1B). At the other extreme, G_{IN} at the proximal sealed end in a semi-infinite cable 80 is $G_{\infty} = G_m \pi d\lambda$, the total conductance of a λ length cylinder since $G_{IN} = G_{\infty}L$. For longer 81 cables of electrotonic length L, the input conductance at the proximal end G_{IN} approaches G_{∞} 82 asymptotically as $G_{IN} = G_{\infty} \tanh(L)$ (Figure 1B). More distal patches of membrane therefore 83 contribute less and less to the total proximal input conductance, setting with G_{∞} a lower 84 bound for the overall excitability of the cell. In all cases, increasing either the diameter d, the 85 specific axial conductance G_i or the specific membrane conductance G_m all increase the input 86 conductance as well as G_{∞} . 87

As mentioned earlier, apart from their larger input conductance, larger cells also receive more synaptic inputs if one considers constant synaptic density. In the case of very short cables, number of synapses since both scale linearly with L. Interestingly, however, the impact of synapses onto voltage at the proximal end diminishes with distance in the very same way as the impact of a distal patch of membrane on the proximal input conductance. The same space of the second secon

Dendritic constancy

reference values V_{∞} , the average proximal voltage in response to distributed synapses over the 94 dendritic length of a semi-infinite cable, and \hat{V} , the voltage response of these synapses when 95 they are collapsed to an isopotential piece of membrane, behave similarly to their respective 96 input conductance counterparts G_{∞} and G_{IN} (Figure 1C). It can be shown analytically (see 97 Methods, "Cable equation for responses to distributed inputs", Equations 3–7) that, along 98 the entire electrotonic length, input conductance and synaptic currents cancel one another 99 precisely. Correspondingly, the average current transfer throughout the cable, i.e. the fraction 100 of injected synaptic current that reaches the proximal cable end, is equal to the ratio of G_{IN} 101 to \hat{G}_{IN} , i.e. the fraction of overall conductance felt at the proximal cable end (**Figure 1D**, top 102 panel). 103

The voltage responses to distributed current injections I_{dist} per unit length are therefore equivalent to the total current injected over the entire metric length $l = \lambda L$ of the neuron into its collapsed membrane leak, i.e.

$$V_{dist} = \frac{I_{dist}l}{\hat{G}_{IN}} = \frac{I_{dist}}{G_m \pi d} \tag{1}$$

(**Figure 1D**, bottom panel, straight line). From this particular application of Ohm's law to 107 dendritic trees, the voltage response to distributed inputs is entirely independent of neuronal cable length while it depends only on the specific conductance per surface membrane G_m and 109 the diameter d of the cable as well as G_i , since I_{dist} is defined per unit electrotonic length. This is in stark contrast with voltage responses to proximal "somatic" current injections where 111 $V = \frac{I}{G_{\infty} \tanh(L)}$, and length impacts the excitability of a neuron by decreasing V dramatically 112 when increasing L. It is clear, however, that in a realistic setting, excitatory neuronal inputs 113 produce synaptic currents that are distributed over the dendritic tree rather than being somatic. 114 In fact, synaptic currents flow through synaptic conductances that further increase the overall 115 conductance per unit length assuming that synaptic densities are homogeneous and constant. 116 The corresponding voltage responses to distributed synaptic conductances are therefore 117 slightly lower than the ones from current injections. However, also these effects remain 118 independent of total cable length: 119

$$V_{syn} = \frac{I_{syn}}{G_m \pi d + G_{syn}} \tag{1'}$$

(Figure 1D, dashed line). In conclusion, our analytical calculations and numerical simulations reveal a new electrotonic principle of dendritic constancy ensuring an equal impact of 121

Dendritic constancy

Cuntz et al.

distributed synaptic inputs in a passive cable independent of its length.



Fig 2. Passive steady-state model responses to distributed synaptic inputs are independent of dendrite length, topology and diameter distribution.

Sample morphologies (left), their input conductances (middle panels) and responses to steady-state distributed inputs (rightmost panels) compared with the prediction from **Equation 1**. **A**, Blowfly Lobula Plate tangential cell (TC) dendrites (red, n = 55) with G_m of $500 \frac{\mu S}{cm^2}$; **B**, Dentate gyrus granule cells (GCs) of rat (light blue, n = 43) and mouse (dark blue, n = 8) with G_m of $26.3 \frac{\mu S}{cm^2}$ — differences in the species come from different average diameters in the two populations; **C**, Monkey cortical pyramidal cell (PC) dendrites (green, n = 69) with G_m of $38 \frac{\mu S}{cm^2}$. Each dot corresponds to one morphology; lighter dots are original morphologies without diameter normalisation. Large darker dots are results for morphologies with diameters normalised to the average of their respective population; small darker dots are individual predictions from **Equation 1** for each non-normalised morphology with its respective average diameter. Straight black lines show predictions from **Equation 1** using the average diameter of each population of morphologies and their respective G_m . The dashed lines show the collapsed input conductance \hat{G}_{IN} as it increases linearly with the total amount of cable.

Dendritic constancy

Passive responses encode percentage of active synaptic inputs in a manner that is largely independent of branching topology and dendrite length 124

Importantly, the principle of dendritic constancy found in the construction of the simple cable 125 with constant diameter can be generalised to branched and tapered neuronal morphologies. 126 We show this at the example of Lobula Plate tangential cells (TCs, n = 55) in the blowfly, ¹²⁷ dentate gyrus granule cells (GCs) in rat (n = 43) and mouse (n = 8) and cortical pyramidal cells (PCs, n = 69) in the monkey with their respective G_m under steady-state distributed 129 inputs (Figure 2). These three datasets were chosen to represent a very leaky large cell (TC), 130 a small and electrotonically compact cell (GC) and the most typical cortical cell (PC) from a 131 range of different species. Normalising the average diameters to the overall average diameter d of the respective datasets shows that the steady-state responses are independent of branching 133 patterns and diameter taper (compare larger dark dots with black lines in rightmost panels 134 in **Figure 2**). In addition, the individual voltage responses of each cell with their original 135 diameters were well predicted by Equation 1 (small dark dots in rightmost panels of Figure 2) 136 with normalised root mean square errors (nRMSE) of 1.3% for TCs, 0.9% for GCs, and 1.2%137 for PCs. 138

Our prediction also accounts for responses to a smaller proportion of activated synapses, i.e. a 139 lower synaptic density, with voltage responses linearly relating with the percentage of active 140 synapses. However, it is important to show what effect a specific, more clustered, distribution 141 of synapses would have on the overall responses in individual neurons. We therefore titrated 142 for any given percentage of active synapses the two most extreme distributions: We compare 143 voltage responses to the activation of a given proportion of the most distal (Figure 3, solid 144 lines) and, respectively, the most proximal (Figure 3, dashed lines) synapses. Even under such 145 clustering of active synapses, neurons seemed to be able to encode the percentage of active 146 synapses with their root voltages both in the steady-state (Figure 3, middle panels) and in 147 dynamic simulations (Figure 3, right panels) following Equation 1' that includes the synaptic 148 conductances present in these simulations. Importantly, passive somatic voltage responses 149 reflected the percentage of active synaptic inputs independently of morphological complexity 150 and dendrite length (compare Figure 3A with Figures 3B and C). 151

Dendritic constancy



Fig 3. Passive model voltage responses follow relative percentage of active synapses even when these are clustered.

Synapse distributions (left), steady-state responses to partial activation of synapses (middle) and responses to sample levels of (100%, 75%, 50%, 25% and 0%) in dynamic simulations (rightmost panels). **A**, **B**, and **C**, each single out one morphology (the one shown on the left) from the populations used in **Figure 2** (using the same colour scheme). Dashed coloured lines are the responses to the most proximal synapses while solid coloured lines show the responses to the activation of the most distal synapses. The space in between both responses is shaded. For example, the 25% line means that the 25% most proximal synapses were active (dashed lines) and in a second simulation the 25% most distal synapses were active (solid lines). Black dashed lines are predictions from **Equation 1'** that include the synaptic conductance. Scale bars show $100\mu m$.

Next, we tested whether the principle of dendritic constancy holds across diverse dendrite ¹⁵² branching patterns and sizes in a large number of different cell types. Indeed, our calculation ¹⁵³ for the steady-state voltage response to distributed inputs in the simple cable yielded good ¹⁵⁴ predictions for the wide range of real dendritic morphologies from the July 2016 version of ¹⁵⁵ the NeuroMorpho.Org database (Ascoli, 2006). We selected those datasets (223 datasets, 9, 841 ¹⁵⁶ reconstructions, **Table S1**) that contained dendritic morphologies with sufficient detail in ¹⁵⁷

Dendritic constancy

Cuntz et al.

all three dimensions and with reconstructed diameters (see Methods). Input conductances 158 and steady-state voltage responses to distributed inputs were calculated after normalising 159 the diameters to an average $1\mu m$ and for generic values of G_m of $50\frac{\mu S}{cm^2}$ that are typical for 160 cortical pyramidal cells (Figure 4A). We observed here that very large trees exhibited a trend 161 to smaller voltage responses. We found similar results in morphological models for dendritic 162 trees based on minimum spanning trees (Cuntz et al., 2007, 2010, 2012) covering a very large 163 range of possible complexities and overall sizes in synthetic dendrites (Figure S1). Also, 164 the dynamic responses to synaptic stimulation were well predicted for morphologies from 165 NeuroMorpho.Org using Equation 1' but very small trees showed strong fluctuations because 166 of the small number of synapses there (Figure 4B). Overall, the responses were faithful to our 167 prediction over a range of four orders of magnitude of dendritic length (nRMSE of 5.1% for 168 the steady state responses compared with **Equation 1**). 169

Dendritic constancy



Fig 4. NeuroMorpho.Org database-wide analysis reveals neuronal size and shape invariant passive model responses to distributed inputs.

A, Voltage responses to distributed inputs with G_m of $50 \frac{\mu S}{cm^2}$ in a large selection of all morphologies from NeuroMorpho.Org (223 datasets, 9, 841 reconstructions, **Table S1**) after normalisation of average diameters to $1\mu m$. Larger consistent subgroups are indicated by colours, representative morphology and label. Unlabelled smaller groups are different shades of grey in the background. The straight line indicates the analytical prediction from **Equation 1** for an unbranched cable. Input conductances G_{IN} (left bottom) and input resistances R_{IN} (right bottom) are indicated in the same colour code as in the top panel and compared to the case where the overall membrane was collapsed in \hat{G}_{IN} and \hat{R}_{IN} respectively (dashed lines). **B**, Passive dynamic responses and prediction from **Equation 1'** (dashed line) in the first morphology of each of the 223 datasets, similarly to the three morphologies in **Figure 3**, rightmost panels. Since small worm neurons (yellow) exhibited large fluctuations around the mean, this panel is shown at two different scales.

Spike frequency but not temporal sequence of spikes is independent of ¹⁷⁰ model dendrite shape and size in response to distributed synaptic inputs ¹⁷¹

So far, we have shown a fundamental aspect of passive normalisation of the neural response 172 to synaptic inputs that seems true for all dendritic morphologies. In the following, we 173 used a classical spiking model of cortical pyramidal cells (Mainen et al., 1995; Mainen and 174 Sejnowski, 1996) to test whether our principle of dendritic constancy translates to active 175 spiking neurons. When incorporated in diverse neuronal morphologies from different cell 176 types, this spiking mechanism was previously shown to exhibit strongly varying spiking 177 patterns for somatic current injections (Figure 5A, top row; similar analysis to the original 178 paper using the model #2488 from ModelDB however with normalised average diameters for 179 a better comparison with our predictions, see Methods) (Mainen and Sejnowski, 1996). To 180 quantify the spiking behaviour in four different cell types we plotted firing rates as a function 181 of injected current into the soma (f-I-curves, **Figure 5B**, top panel). As expected, the spiking 182 frequency increased with decreasing dendrite size rendering smaller cells more excitable. 183 We used interspike interval (ISI) distributions to characterise the temporal structure of the 184 spike trains (bursting vs. non-bursting) in the different morphologies (Figure 5B, bottom 185 panel, ISI distribution refers to single cell firing). L5 pyramidal cells exhibited bursts of three 186 spikes (as indicated by a larger proportion of short ISIs) and L3 pyramidal cells bursts of two spikes (as indicated by two equal peaks in the ISI distributions). Interestingly, when stimulated by distributed synaptic inputs instead of somatic current injections, the differences 189 in the temporal structure of the spiking (bursting vs. non-bursting) remained dependent on 190 the respective morphology with similar ISI distributions as well as coefficients of variation 191 (cv) (**Figure 5C**, bottom panel). However, the numbers of spikes were equalised and were 192 independent of dendritic tree size irrespective of the frequency of stimulation (Figure 5A, 193 bottom traces, and **Figure 5C**, top panel). The equalised passive voltage responses predicted 194 by our dendritic constancy (**Figure 5C**, rightmost panel, bottom traces, subthreshold) were 195 transformed into equal number of spikes in the active model (Figure 5C, rightmost panel, top 196 traces). Taken together, in response to distributed synaptic inputs, spike numbers (frequencies) 197 were independent of morphology while spike times (as reflected in the temporal structure 198 of the spiking in the form of bursting vs. non-bursting) remained affected by morphological 199 properties of dendrites in line with previous observations by Mainen and Sejnowski (1996) for 200 responses to somatic current injections. 201

Dendritic constancy





Simulations using the spiking mechanism by Mainen and Sejnowski (1996) in their four sample morphologies of L3 aspiny (dark orange), L3 pyramidal (green), L4 stellate (dark blue), and L5 pyramidal (pink) cells after normalising the diameters. **A**, Sample voltage traces for 0.25nA current injections into the soma (top, similar to Figure 1 in the original work; see Methods) and distributed synaptic inputs at 1Hz (bottom). **B**, Firing rate vs. current injection in the soma and **C**, responses to distributed synaptic inputs for the same four cases. Sample subthreshold (bottom, 0.25Hz) and suprathreshold (top, 1Hz; truncated spikes at dashed line) synaptic activation in the four morphologies are shown in the rightmost panels. Interspike interval (ISI) distributions are shown below the respective panels for 40sec simulations at indicated current injections and synaptic activation with corresponding coefficients of variation (cv). Note the two peaks in ISI distributions of L3 and L5 pyramidal cells indicative of their bursting. Colours indicate the different morphologies from **A** throughout the figure.

Dendritic constancy

Cuntz et al.

In order to verify that the results in the model by Mainen and Sejnowski were not model- 2012 specific, we performed similar simulations in two distinct well-established active models 203 of CA1 pyramidal cells by Jarsky et al. (2005) and Poirazi et al. (2003b). We integrated the 204 corresponding active ion channel models into the set of all good reconstructions of hippocam- 205 pal pyramidal cell morphologies (n = 105) from NeuroMorpho.Org after normalising their 206 diameters to $1\mu m$ (Figure 6A). The model by Jarsky et al. has previously been used to study 207 the separate effects of inputs from Schaffer collaterals (SC) and the perforant path (PP) (Jarsky 208 et al., 2005). This gave us the opportunity to compare our results for distributed inputs over 2009 the entire dendrite with results for inputs that were clustered in a more realistic manner 210 according to their anatomical (layer-specific) origin. In this case we compared stimulating 211 all synapses with 1Hz (Figure 6B, black dots) and, separately, only synapses impinging on $_{212}$ the basal dendrites (Figure 6B, red dots) or on the distal apical dendrite and tuft region 213 (Figure 6B, cyan dots). Remarkably, in all cases, the firing rates were independent of neuron 214 size. Again, the number of spikes was indicative of the percentage of active synapses scanned 215 in a similar manner to **Figure 3** (**Figure 6B**, rightmost panel). In particular, the corresponding 216 input-output functions were almost identical when measured in two different sample mor-217 phologies of radically different total dendritic length (Figure 6B, rightmost panel, compare 218 both sets of solid and dashed lines). 219

A second model of CA1 pyramidal cells by Poirazi et al. (2003b) has become archetypal for 220 compartmentalised computations in dendrites. Similarly to the model by Jarsky et al., we 221 incorporated the ion channel models by Poirazi et al. into the NeuroMorpho.Org collection 222 of hippocampal pyramidal cell morphologies and subjected the individual compartmental ²²³ models to various combinations of distributed synaptic inputs. The model by Poirazi et 224 al. produced large dendritic events that were distinct from the somatic action potentials 225 (**Figure 6C**, voltage traces red – dendrite vs black – somatic). Intriguingly, both numbers 226 of somatic spikes and large dendritic events were independent of total dendritic length 227 (Figure 6C, left lower and upper panels respectively). 228

Dendritic constancy



Fig 6. Dendritic constancy in two active models of hippocampal CA1 pyramidal neurons including dendritic spikes and clustered inputs.

A, All 105 morphologies of rat hippocampal pyramidal cells from NeuroMorpho.Org that passed our manual curation criteria (Colours are random). **B**, CA1 pyramidal cell model by Jarsky et al. (2005) with its responses to distributed synaptic inputs 500pS, 1Hz in the set of all 105 morphologies. Black dots show spiking responses to activation of all synapses while red (basal) and cyan (apical) show responses to activation of subregions of the dendrite as indicated in the sketch on the left. Rightmost panel shows spike output analysis for selective activation of a subset of all most proximal (dashed line) and most distal synapses (solid line). Since roughly 50% of synapses were active in both the basal and apical stimulations, corresponding values of the curve for proximal (red) and distal (cyan) synapses are highlighted in the rightmost panel as well as values for all synapses (black). The two sets of curves (two dashed, two solid lines, respectively) represent two morphologies of radically different size (10mm vs. 15mm of total dendritic length). See next page.

Dendritic constancy

Fig 6. (continued) The shaded area highlights the range of responses in clustered synapses for the morphology shown in the inset. **C**, CA1 pyramidal cell model by Poirazi et al. (2003b) driven by distributed synaptic inputs 500pS, 1Hz in the set of all selected 105 hippocampal pyramidal cell morphologies from NeuroMorpho.Org. Top row, Large dendritic events (red dots) were measured at the branch with highest y value respectively and detected after low pass filtering the local voltage signal there with a Gaussian filter with variance of 100ms (see dashed line). Bottom row, Somatic events (black dots) as measured directly from the somatic voltage, shown for one sample morphology. Rightmost panels show resulting frequency of somatic (black, bottom) and dendritic (red, top) events with one point each per morphology as a function of total dendritic length.

Spiking reset converts constant membrane voltage into constant spike rates 229

The results from the active compartmental models pose the question as to why the con- 230 stant voltages transform into constant numbers of spikes. Such a transformation could be 231 a consequence of each spike essentially shunting and resetting the entire neuron (Häusser, 232 2001) while erasing its voltage history. Under these assumptions, a leaky integrate-and-fire 233 (LIF) (Stein, 1965) mechanism coupled to the dendrite could help elucidate the constancy of 234 spike numbers. We chose to implement a LIF that resets the voltage throughout the entire 235 dendritic tree after passing a threshold voltage at the dendrite's root. Incorporating such a 236 spiking mechanism in the four cell types of Figure 2, yielded an output spiking frequency 237 that was indeed independent of dendritic length (Figure 7A) for any given synaptic input 238 frequency. In fact, the entire input-output (IO) curves were essentially independent of the 239 morphology (Figure 7B). We then derived an analytical solution for the transformation of 240 variable synaptic input activity into firing rate output (see Methods, Equations 10-22). In line 241 with our numerical LIF simulation results (Figure 7A, and B), the mean analytical voltage 242 response to stochastic inputs in a uniform cable was independent of length. The variance of 243 the subthreshold voltage response decayed to a constant for dendrites of total electrotonic 244 length greater than one. Our analytical predictions for the IO relationship (Brunel and Hakim, 245 1999) are 246

$$R^{-1} = \tau \int_0^\infty \frac{1}{z} e^{\frac{-z^2}{2}} \left(e^{z\frac{v_{th}-\mu_v}{\sigma_v}} - e^{z\frac{v_{re}-\mu_v}{\sigma_v}} \right) dz$$
(2)

with firing rates R for subthreshold voltage mean μ_v and standard deviation σ_v impinging ²⁴⁷ on a membrane with time constant τ , firing threshold v_{th} , and voltage reset v_{re} . R always ²⁴⁸ converges to constant values for cable lengths longer than the electronic length (see Methods, ²⁴⁹ **Equations 10–22, Figure 7B** bold black lines). Importantly, R is practically independent of ²⁵⁰ dendritic length, if the mean afferent drive is sufficiently strong and so the output firing rate ²⁵¹

Dendritic constancy

is less dependent on fluctuations (as seen in **Figure 7A**). In our case in **Figure 7B**, the specific 252 membrane conductance in the different cell types determined the slope of the IO curves with 253 a very sharp slope in the leaky blowfly TC that in reality produces spikelets and shallower 254 curves in the other cell types with lower conductivity through the membrane. Interestingly, 255 the percentage of active synapses was encoded in the number of spikes (**Figure 7C**) in analogy 256 to the voltages in **Figure 3** (compare with IO curves in **Figure 7B**). Again, this was true even 257 for clustered synapses (plots show most distal synapses as solid lines vs. most proximal 258 synapses as dashed lines). 259

Dendritic constancy



Fig 7. Spiking responses to distributed inputs in leaky integrate-and-fire (LIF) neurons with realistic dendritic morphologies as the source of leak indicate that voltage reset throughout the entire dendritic tree contributes to spike rate constancy.

LIF mechanism in its simplest form (without adding soma or axon, the LIF resets the voltage in the entire dendrite after spiking) introduced into the dendritic root of the cell types from **Figure 2** with the same colours and membrane properties. **A**, Top row, Sample spike trains for 10 different TC, 5 rat GC, 5 mouse GC and 10 monkey PC dendritic morphologies are shown underneath the corresponding morphologies. Bottom row, Firing rates are shown with error bars (standard deviation, invisible in GCs and PCs) for one selected input frequency for each cell type are shown as a function of length. **B**, Input-Output (IO, Frequency of synaptic activation vs. spiking frequency) plots for all available morphologies for TCs (left), mouse and rat GCs (middle) and monkey PCs (right). Respective cable calculations from **Equation 2** that are independent of length are shown as bold black lines. **C**, Responses to selective activation of the most proximal (dashed lines) and most distal (solid lines) synapses in the dendrite. The areas between these two extreme scenarios for clustered synapses are shaded.

Dendritic constancy

Cuntz et al.

Similarly, incorporating the LIF mechanism into the dendritic morphologies of the Neuro- 200 Morpho.Org database (with a uniform specific membrane conductance, see **Figure 4**) yielded 261 invariant IO curves over a very large range of morphologies. Only the IO curves from tiny 262 worm neurons (yellow) and very large spinal cord motoneurons (red) deviated from the re- 263 maining curves (Figure 8A, LIF model, compare also these results with analytical predictions 264 from Equation 2). In the same morphologies, we also showed spike number invariance using 265 an adaptive exponential LIF (AdExpLIF) (Brette and Gerstner, 2005) for two specific temporal 266 patterns of spikes typically seen in compartmental models, a bursting mode and spiking mode 267 with spike frequency adaptation (Figure 8B and C, AdExpLIF model). Overall, LIF based 268 spiking models were consistent with the dendritic constancy of passive voltage responses to 269 distributed synaptic inputs transforming into constant spike numbers that were independent 270 of dendritic length or shape. 271

Dendritic constancy





Adaptive exponential LIF (AdExpLIF) in NeuroMorpho.Org dendrites



Fig 8. NeuroMorpho.Org database-wide spiking responses to distributed inputs in leaky integrateand-fire (LIF) and adaptive exponential LIF (AdExpLIF) neurons are independent of dendritic size and shape.

Similar panels as in **Figure 7A and B** but for all morphologies from **Figure 4** with the respective membrane properties used there: Sample voltage traces in sample morphologies for all seven morphological categories (left panels), firing rates in response to a given input frequency (middle panels, input frequency is indicated), and IO curves (right panels). Colours as in **Figure 4** in increasing dendrite size: Yellow (worm neurons); orange (nitergic neurons); cyan (hippocampal granule cells); pink (retinal ganglion cells); blue (cortical pyramidal cells); green (hippocampal pyramidal cells); red (cat motoneurons). **A**, Regular leaky integrate-and-fire (LIF) spiking mechanism incorporated in all dendritic morphologies. Similarly to **Figure 7**, calculations from **Equation 2** are shown as a bold black line. **B**, Adaptive exponential LIF (AdExpLIF) that includes an additional channel for spike frequency adaptation and results in less regular spiking. **C**, Long time constant in the adaptation channel of the AdExpLIF for testing our dendritic constancy theory under extreme burst firing.

Dendritic constancy

Cuntz et al.

Discussion

272

In this work, we used analytical methods to demonstrate a general principle of dendritic 273 constancy regarding the voltage and spiking responses to distributed synaptic inputs. Synaptic 274 inputs effectively encounter an apparent input conductance in the soma (i.e. the transfer 275 conductance) corresponding to the collapsed membrane leak of the entire dendrite onto the 276 soma. As a consequence, more synaptic currents in larger cells are precisely compensated by 277 the additional dendritic leak. Our dendritic version of Ohm's law (Equation 1 and Equation 1' 278 as well as **Equation 2** for spikes with variable inputs) is independent of morphological 279 features and spiking mechanisms and predicts isoelectrotonic behaviour for anatomically 280 distinct dendritic trees shaped by species-specific scaling (Beining et al., 2017; Cuntz et al., 281 2013), developmental expansion (Mckay and Turner, 2005) or neurodegenerative shrinkage 282 (Platschek et al., 2016). Finally, our simulations in a classical model by Mainen and Sejnowski 283 (1996), as well as other established spiking models (Jarsky et al., 2005; Poirazi et al., 2003b) 284 and LIF models showed that synaptic stimulation in different dendritic trees leads to similar 285 responses in terms of firing rates but not patterns (spike times). This was true for uniformly 286 activated synapses but also to a large degree for clustered synapses, so much so, that the 287 somatic firing rate allowed for an approximate estimation of the percentage of active synapses 288 independent of their dendritic location. Taken together, our analytical and numerical results 289 imply that the principle of voltage and spike rate constancy is general since it holds in all ²⁹⁰ (branched and unbranched) dendritic arbours activated by distributed synaptic conductances. 291

Limitations for dendritic constancy

What are the assumptions and limitations of our computational analysis? First, dendritic ²⁹³ constancy will be affected by a number of dendritic features. The voltage responses do depend ²⁹⁴ on the specific membrane conductances and average dendritic diameters. While average ²⁹⁵ dendritic diameters do not seem to vary much in the NeuroMorpho.Org database (**Figure S2**), ²⁹⁶ G_m values are known to vary between cell types (Borst and Haag, 1996) (**Figures 2, 3 and 7**) ²⁹⁷ and also within cell types (e.g. Garden et al., 2008). In addition, the somatic membrane ²⁹⁸ leak affects the dendritic constancy results when somata are very large compared to the ²⁹⁹ overall dendritic membrane if their diameters are not normalised together with the dendrites ³⁰⁰ (i.e. if they do not scale with dendrite length) and if they do not receive synaptic inputs ³⁰¹ (**Figures S2 and S3**).

Dendritic constancy

Cuntz et al.

Second, in our analysis, we assumed uniform kinetics, conductances and reversal potentials 303 of synaptic inputs. In this respect, it would be interesting to further explore models with 304 variations in distance-dependent synaptic properties (Häusser, 2001; Magee and Cook, 2000) 305 as well as democratising effects on distal synapses (London and Segev, 2001; Rudolph and 306 Destexhe, 2003). Here, we show for a distance-dependent linear gradient of maximal synaptic 307 conductance (increasing with dendritic path length from the root) that dendritic constancy 308 is preserved in the hippocampal CA1 pyramidal cell model by Jarsky et al. and in the 309 NeuroMorpho.Org morphologies (Figures S4A and B). Furthermore, our analytical solutions 310 predict that dendritic constancy applies also to inhibitory synapses with negative reversal 311 potentials (same models, Figures S5A and B). However, the effects of layer-specific somatic 312 or dendritic inhibition, introducing local or distant shunts (Gidon and Segev, 2012) and their 313 interaction with active channels (see below) need to be studied in detail. 314

Third, it also remains unclear how dendritic non-linearities such as dendritic NMDA or calcium spikes would operate in the context of our dendritic constancy principle. Such non-linear computations would include dendritic integration features known to play a role depending on relative locations of synaptic inputs (Branco et al., 2010; Cuntz et al., 2003; Poirazi et al., 2003b; Polsky et al., 2004). Surprisingly, our active cortical and hippocampal models exhibited dendritic constancy (without requiring any specific tuning) of spike numbers and even in the numbers of dendritic active events in the model by Poirazi et al. (**Figures 6C**). However, many further aspects related to dendritic voltage-dependent channels remain to be explored. For instance, potassium channels and H-channels are capable of affecting local synaptic potentials as well as backpropagating spikes (Chen et al., 2006; Magee, 1999). It would be intriguing to test how these channels shape dendritic constancy for synchronous or asynchronous, clustered or distributed synaptic inputs.

Fourth, it remains to be determined how dendritic constancy might interact with recently described homeostatic plasticity of the axon initial segment (AIS) in the form of activitydependent changes in its location and length and in the distribution of its ion channels (Adachi det al., 2015; Kuba, 2012). Decreased or increased synaptic activity can induce homeostatic lengthening or shortening of the AIS with a compensatory increase or decrease in neuronal size (Evans et al., 2015; Kuba et al., 2010). However, the effect of AIS det all provide the or location on excitability is more complex and depends on neuronal size (Gulledge and Bravo, 2016). Therefore, further computational and experimental analyses are needed to 324

Dendritic constancy

better understand the link between the neuron's size and shape invariant excitability that we describe here and AIS plasticity. 336

Of particular interest is our observation that spike times rather than spike numbers remained 337 affected by morphological properties of dendrites in a similar manner to responses to somatic 338 current injections (Mainen and Sejnowski, 1996). Our simulations revealed that in the case of 339 synaptic stimulation, both dendritic constancy as well as variability in firing patterns were 340 maintained at the same time in active models of four different reconstructed cortical cell types. 341 Although two cortical cell models displayed regular firing and the other two bursting, all 342 of them generated similar firing rates. The somatic bursting behaviour has been previously 343 explained as a consequence of delayed dendritic depolarisations and subsequent return 344 currents from dendrites, arising due to two key factors: (1) moderate coupling resistance 345 between somatic and dendritic regions in combination with (2) separated distributions of 346 fast and slow active channels in soma and dendrites (Mainen and Sejnowski, 1996). Our 347 synaptically driven simulations confirmed and extended these analyses by showing that 348 the electrotonic mechanisms of dendritic constancy are able to normalise spike numbers in 349 cells with different dendritic sizes and shapes without disrupting the active burst generating 350 mechanisms. It is tempting to speculate that dendritic constancy could support homogeneous 351 spike-rate coding across different morphologies while at the same time allowing for cell- 352 type specific spike-time coding. In other words, dendritic constancy may facilitate neuronal 353 computations by maintaining stable firing rates while keeping variability of spike patterns 354 (Denève and Machens, 2016; Denève et al., 2017; Gjorgjieva et al., 2016). 355

Clinical relevance of dendritic constancy

The dendritic constancy principle could be of clinical relevance. Changes in dendritic size and ³⁵⁷ shape are hallmarks of many neurological disorders, including chronic stress (Conrad et al., ³⁵⁸ 2017), stroke (Brown et al., 2010; Qin et al., 2014) and neurodegeneration (Šišková et al., 2014; ³⁵⁹ Spires and Hyman, 2004). Whereas dendritic atrophy caused by direct damage to a neuron is ³⁶⁰ considered part of the disease process (Šišková et al., 2014), dendritic remodelling occurring ³⁶¹ in disconnected brain areas, i.e. network damage, is most likely homeostatic and restorative in ³⁶² nature. For example, the perforant pathway to the dentate gyrus degenerates in aged humans ³⁶³ and in Alzheimer´s disease (Leal and Yassa, 2013; Yassa et al., 2010). As a consequence, ³⁶⁴ the target neurons of this pathway – dentate granule cells – retract their dendrites. This ³⁶⁵

Dendritic constancy

dendritic retraction is caused by denervation and not by the disease itself (Einstein et al., ³⁶⁶ 1994). Experimental animal data have shown that such denervated and retracted granule cells ³⁶⁷ (Vuksic et al., 2011) eventually achieve synapse densities on their dendrites comparable to ³⁶⁸ pre-denervation levels (Steward et al., 1988). In that case, the input conductance as well as ³⁶⁹ the number of synapses with additional unit length would likely cancel each other out. The ³⁷⁰ dendritic tree has fine-tuned itself to achieve firing rate homeostasis (Platschek et al., 2016, ³⁷¹ 2017). We show here that this feature is not specific to dentate granule cells and that synaptic ³⁷² excitability of neurons is size-invariant for all dendritic trees due to a general electrotonic ³⁷³ principle. Thus, transneuronal dendritic remodelling appears to play a homeostatic role in ³⁷⁴ maintaining information throughput in a partially damaged network. ³⁷⁵

Practical consequences for computational modelling and input-output computation of neurons

Equations 1 and 1' allow for quantitative predictions of voltage responses to distributed 378 synaptic inputs. This can be helpful for tuning large-scale morphologically realistic com- 379 partmental models (e.g. Markram et al., 2015) because by setting synaptic conductances to 380 a specific value, it is possible to achieve a target voltage (and corresponding spike numbers 381 from **Equation 2**). Thus, dendritic constancy simplifies the estimation of a neuron's behaviour 382 within a network. For instance, for a given synaptic conductance, the frequency of synap- 383 tic activation required to reach a particular membrane voltage can be computed. From the perspective of network computations, the principle of dendritic constancy can be viewed 385 as a mechanism for preserving stable neuronal activity in the circuit (as done in **Figure 7**). 386 Intuitively, adding new synapses to a spiking network model would create more spikes. Even 387 one additional spike can dramatically alter network dynamics (London et al., 2010). However, 388 dendritic constancy is one possible mechanism to prevent this from happening, because the cell's number of output spikes depends on the relative number of active synapses and not on 390 their absolute number. This means that increasing the number of synapses while adjusting 391 the morphology accordingly would effectively not change the total number of spikes in the 392 network. 393

In summary, our principle of dendritic constancy serves as an equalising homeostatic mechanism on which dendritic non-linearities and synaptic plasticity can operate (London and Häusser, 2005; Turrigiano, 2017). It creates a passive backbone for the conservation of excitabil-396

Dendritic constancy

Cuntz et al.

ity converting a neuron to a reliable size- and synapse number-independent "summing point" ³⁹⁷ within the network (Segev and London, 2000) but at the same time, it allows for more complex ³⁹⁸ computations with active dendrites (Schmidt-Hieber and Nolan, 2017). Because dendritic constancy is based on basic electrotonic properties, it applies to all neurons receiving distributed ⁴⁰⁰ excitatory or inhibitory inputs. This simple and universal principle has previously been overlooked because most studies focused on neuronal firing activated by somatic current injections ⁴⁰¹ or by few synaptic inputs instead of distributed synaptic stimulation. Dendritic constancy ⁴⁰³ becomes apparent after leaving the "somatocentric" and embracing the "synaptocentric" view ⁴⁰⁴ of a neuron's input-output transformation. ⁴⁰⁵

Acknowledgments

We would like to thank S. Jagannath, S. Platschek and S. Rozada for performing preliminary analyses and A. Castro, F. Effenberger and M. Schölvinck for useful discussions and comments on the manuscript. The work was supported by BMBF (01GQ1406 – Bernstein Award 2013 to H.C.; OGEAM 031L0109B to T.D.), Deutsche Forschungsgemeinschaft (CRC 1080 to T.D.), University Medical Center Giessen and Marburg (UKGM; to P.J.), LOEWE CePTER – Center for Personalized Translational Epilepsy Research (to P.J. and T.D.) and F.Z.H. was supported by the International Max Planck Research School (IMPRS) for Neural Circuits in Frankfurt. The authors declare to have no competing financial interests.

Author contributions

H.C., A.D.B, M.B, M.S., L.M., F.Z.H., T.D. and P.J. conceived the study and wrote the paper. ⁴¹⁶ H.C., M.B., M.S., L.M. and F.Z.H. performed the numerical simulations and A.D.B. performed ⁴¹⁷ the analytical calculations. ⁴¹⁸

Materials and methods

Data and algorithm availability

All passive electrotonic and leaky integrate-and-fire (LIF) simulations were done in Matlab 421 (Mathworks Inc, 2015b, 2017b and 2018b) using our own open-source software package, 422

406

415

419

Dendritic constancy

Cuntz et al.

the TREES toolbox (Cuntz et al., 2010) (www.treestoolbox.org, Interim version). TREES 423 toolbox functions are marked in italic and end with a $_tree$ suffix throughout the Methods 424 section. Active compartmental model simulations were done in NEURON (Carnevale and 425 Hines, 2004) using our new software T2N to communicate with the TREES toolbox in Matlab 426 (Beining et al., 2017). All results were further analysed in Matlab. All dendritic morphologies 427 were downloaded from www.NeuroMorpho.Org (Ascoli, 2006) in July 2016. The active model 428 for the spiking mechanism by Mainen and Sejnowski (1996) for Figure 5 used model #2488 429 from ModelDB (Hines et al., 2004). The LIF and adaptive exponential leaky integrate-and-fire 430 (AdExpLIF) models (Brette and Gerstner, 2005) using realistic dendritic leak in **Figures 7 and 8** 431 were implemented in Matlab. All new functions (cgin_tree, LIF_tree, LIF_FR_tree, 432 AdExpLIF_tree) will be made available as part of the TREES toolbox on publication at www. 433 treestoolbox.org via Github. The code and data for all figures will be made available at 434 https://zenodo.org/ on publication. The code was tested on various operating systems. 435 Individual methods are detailed in the following but can best be appreciated in the actual 436 Matlab scripts. 437

Cable equation for responses to distributed inputs.

The voltage response at distance x along a closed cable of length l due to current of magnitude ⁴³⁹ I_{app} injected at the root (Rall, 1959, 1962) is ⁴⁴⁰

$$v(x) = v_0 \left[\frac{\cosh\left(\frac{l-x}{\lambda}\right)}{\cosh\left(\frac{l}{\lambda}\right)} \right],\tag{3}$$

where λ is the electrotonic length constant and v_0 is the voltage at the root:

$$v_0 = \frac{\coth\left(\frac{l}{\lambda}\right)}{G_{\infty}} I_{app}.$$
(4)

As transfer resistance is symmetric in dendrites (Koch and Segev, 1999; Rall et al., 1967; 442 Rushton, 1937) this also gives the voltage $v_x(0)$ at the root due to current injection at a distance 443 x 444

$$v_x(0) = \frac{I_{app}}{G_{\infty}} \left[\frac{\cosh\left(\frac{l-x}{\lambda}\right)}{\sinh\left(\frac{l}{\lambda}\right)} \right].$$
(5)

To find the total voltage V for currents injected along the entire cylinder, we require the 445

438

Dendritic constancy

integral over all synaptic sites

$$V = \frac{I_{app}}{G_{\infty} \sinh\left(\frac{l}{\lambda}\right)} \int_{0}^{l} \cosh\left(\frac{l-x}{\lambda}\right) dx.$$
 (6)

$$V = \frac{\lambda I_{app}}{G_{\infty}} = \frac{I_{app}}{G_m \pi d}.$$
(7)

Morphologies for passive electrotonic simulations.

Simple cables $(12.5\mu m - 12.5m m \text{ length in } 12.5\mu m \text{ steps})$ of constant $1\mu m$ diameter (Figures 1B- 448 **D**) or various dendritic morphologies (Figures 2–4) were resampled to constant $1\mu m$ internode 449 resolution (using *resample_tree*). Individual datasets used in combination with specific 450 membrane properties were from blowfly Lobula Plate tangential cells (TCs, n = 55) (Cuntz 451 et al., 2008) (Figures 2A and 3A, $G_m = 500 \frac{\mu S}{cm^2}$), rat (Rihn and Claiborne, 1990) (n = 43) 452 and mouse (Schmidt-Hieber et al., 2007) (n = 8) dentate gyrus granule cells (GCs, Fig- 453 ures 2B and 3B, $G_m = 26.3 \frac{\mu S}{cm^2}$) and monkey cortical pyramidal cells (Luebke et al., 2015; 454 Coskren et al., 2015) (PCs, n = 69, Figures 2C and 3C, $G_m = 38 \frac{\mu S}{cm^2}$). The three datasets were 455 also used in the context of leaky integrate-and-fire (LIF) spiking models in Figures 7. Dendrite 456 morphologies from the entire NeuroMorpho.Org database were used for Figures 4 and 8 457 by manual curation of all existing archives to select those with sufficient diameter profiles, 458 sufficient depth information in z, sufficiently high-quality reconstructions and no sudden 459 jumps in z (selection, 223 datasets, 9, 841 reconstructions, see **Table S1**). The selected archives $_{460}$ were sorted by cell types into the following categories in decreasing order of total cable 461 length: Spinal cord motoneurons (red), hippocampal pyramidal cells (green), neocortical 462 pyramidal cells (blue), retinal ganglion cells (pink), hippocampal granule cells (cyan), nitrergic 463 neurons (orange), *C. elegans* neurons (yellow), and other (different shades of grey per dataset). 464 These categories were chosen as representatives for the possible scales of dendrites rather 465 than because they corresponded to consistent cell types. All dendrite morphologies were 466 normalised to a given average diameter (to the average diameters in their specific archives for 467 **Figures 2 and 7** and to $1\mu m$ for **Figures 4 and 8**). 468

Passive steady-state measures for dendritic morphologies.

The collapsed input conductance was measured by summing up the leak conductance over 470 the entire membrane surface of the dendrite using the function *surf_tree*. The resulting 471

469

446

Dendritic constancy

485

calculation is made available in the new TREES toolbox function *cqin_tree*. Remaining 472 electrotonic features are all readily available from the electrotonic signature (*sse_tree*) as 473 introduced previously (Cuntz et al., 2010). Briefly, all membrane and axial conductances are 474 arranged according to the tree's adjacency matrix and the current transfer between all nodes is 475 obtained by taking the inverse of the resulting conductance matrix. Local input resistances are 476 then found on the diagonal of this electrotonic signature since current there is injected in the 477 same node as the voltage is measured. Voltage responses to distributed inputs are simply the 478 sum over the column or row of the electrotonic signature since the matrix is symmetric and 479 the system is linear. While this method simulates steady-state distributed current injections, 480 synaptic conductances associated with batteries according to their specific reversal potentials can be simulated instead (using the *syn_tree* function). The passive results were obtained in 482 their purest form in dendrites without the associated somata and axons. Only for Figures S3 483 was the effect of somata explored in detail (see below). 484

Passive dynamic responses to distributed synaptic conductances.

Synaptic inputs were simulated as a Poisson process inducing synaptic conductances at a 486 given frequency per synapse. The dynamics of the conductance trace was given by the 487 form $G_{syn} = G_{scale} \left(e^{-\frac{t}{\tau_1}} - e^{-\frac{t}{\tau_2}} \right)$ with a rise time constant of $\tau_2 = 0.5ms$ and a decay time 488 constant of $\tau_1 = 2.5ms$. G_{scale} was set using Equation 1 to ensure that the integral over time 489 of the synaptic conductance profile produced the same voltage as the steady state cases 490 (compare **Figure 2** rightmost panels with rightmost panels in **Figure 3**) at an input frequency 491 of 5Hz per synapse. Our novel TREES toolbox function LIF_tree was used without a 492 voltage threshold for spiking in the case of the passive dynamic responses. *LIF_tree* injects 493 distributed synapses into the conductance matrix that defines the dendritic tree in a timeresolved dynamic manner and produces local voltage responses throughout the dendrite. In 495 **Figures 3 and 4** the voltage time courses at the dendritic root were plotted for a subset of 496 morphologies (the ones shown in **Figure 3** and the first morphology in each of the 223 datasets 497 in **Figure 4**) for better clarity. 498

Effect of soma size on dendritic constancy — analytical treatment.

Consider an electrotonically compact soma of radius R attached to a dendritic cable of length l_{500} and radius r. The intrinsic properties are given by the specific conductance of the intracellular 501

Dendritic constancy

medium G_i and membrane conductance G_m . The soma has a leak conductance of $G_s(R) = 502$ $4\pi R^2 G_m$. The voltage along the cable due to a current injection of magnitude I_{app} at the soma 503 is given by 504

$$v(x) = \left[\frac{I_{app}}{G_{\infty}\left(1 + G_s(R)\tanh\left(\frac{l}{\lambda}\right)\right)}\right] \frac{\cosh\left(\frac{l-x}{\lambda}\right)}{\cosh\left(\frac{l}{\lambda}\right)}$$
(8)

for $\lambda = \sqrt{\frac{G_i d}{4G_m}}$, the electrotonic length constant of the cable, and $G_{\infty} = \frac{\pi G_i d^2}{4\lambda}$, the semi-infinite conductance. Note that this derivation relies on a self-consistent description of the root voltage v_0 due to the current flowing into the dendrite. Due to the symmetry of transfer resistance, this is also the voltage induced at the soma by current injection at a site x. Consider the total somatic response V_{Tot} to distributed synaptic currents:

$$V_{Tot} = \int_0^l v(x) dx;$$

$$V_{Tot} = \int_0^l \left[\frac{I_{app}}{G_{\infty} \left(1 + G_s(R) \tanh\left(\frac{l}{\lambda}\right) \right)} \right] \frac{\cosh\left(\frac{l-x}{\lambda}\right)}{\cosh\left(\frac{l}{\lambda}\right)} dx;$$
$$V_{Tot} = \frac{I_{app}}{\pi dG_m} \left[\frac{\tanh\left(\frac{l}{\lambda}\right)}{G_s(R) + \tanh\left(\frac{l}{\lambda}\right)} \right].$$
(9)

It can be seen that the term in brackets determines the deviation from dendritic constancy. ⁵¹⁰ A small value of $G_s(R)$ is key as tanh is bounded by one. **Figures S3** plots the relationship ⁵¹¹ between somatic radius R and dendritic constancy for different electrotonic lengths $\frac{l}{\lambda}$ and the ⁵¹² relationship between the electrotonic length $\frac{l}{\lambda}$ and dendritic constancy for somatic radii R. ⁵¹³

Spiking model by Mainen and Sejnowski.

We used our new tool T2N (Beining et al., 2017) to port the existing model for the spiking ⁵¹⁵ mechanism by Mainen and Sejnowski (1996) #2488 from ModelDB (Hines et al., 2004) to ⁵¹⁶ our TREES toolbox package in Matlab. In T2N, calculating spike frequency vs. current ⁵¹⁷ injections or vs. synaptic input frequencies using different dendritic morphologies becomes ⁵¹⁸ easy to implement. The required simulations are distributed automatically on the available ⁵¹⁹ computing cores and the entire toolset from the TREES toolbox becomes available to better ⁵²⁰ edit and analyse dendritic trees and the resulting simulation variables. The code is available ⁵²¹ but, briefly, the simulations ran 40*sec* with a time step of 0.05*ms* and a pre-run for 200*ms*. ⁵²²

Dendritic constancy

The initial voltage was set to -70mV, which was a close match for resting voltages for the 523 four different morphologies. The voltage was calculated every $50\mu m$ and a current injection 524 electrode was inserted into the root or synapse point processes into every node (separated 525 by $1\mu m$). Morphologies from the original model were translated into TREES toolbox and 526 resampled to $1\mu m$ internode distances. The dendritic diameters were normalised to $1\mu m$ and 527 soma with axon divided into axon hillock, initial segment, nodes of Ranvier and myelinated 528 segments were added as in the original model with the respective ion channel conductances. 529 Implicit spines were modelled according to the original model for the current injections 530 but even the L3 aspiny cell was implemented as spiny in all cases for better comparison. 531 Responses to distributed synaptic inputs were modelled with *Exp2Syn* point processes with 532 rise time constant of $\tau_2 = 0.2ms$ and decay time constant of $\tau_1 = 2.5ms$ driven by NetStim 533 point processes in artificial point neurons under Poisson process conditions (noise 1) and 534 following a given input frequency. The random seeds for the *NetStim* process were set to be 535 independent for different synapses. 536

CA1 pyramidal cell spiking models.

Electrotonic compartmentalisation and location dependent ion channel distributions allow for separate non-linear integration of inputs in different regions of dendrites. In order to check how these conditions affect our results, we studied two models of CA1 pyramidal cells that are known to produce dendritic spikes. The dendritic arborisation of pyramidal cells follows a laminar structure that generally reflects the different main excitatory afferents impinging on their dendrites from different brain regions. This distinctive structural organisation is also manifested in the way the electrotonic properties and active channels are distributed. Therefore, it was necessary to define how non-uniform channel distributions scale in the different morphologies.

Jarsky et al. 2005 model.

We ported the model by Jarsky et al. (2005) to T2N in a similar manner as with the model by Mainen and Sejnowski. This model includes four active conductances: a voltage-gated Na⁺ 549 conductance, a delayed rectifier K⁺ conductance, a proximal A-type K⁺ conductance, and a 550 distal A-type K⁺ conductance with a higher half-inactivation voltage. These conductances 551 were distributed as a function of path distance from the soma. The Na⁺ and the delayed 552

537

560

rectifier K⁺ conductance were modelled following a uniform distribution, the weak excitability version of the model by Jarsky. The A-type K⁺ current was modelled with the experimentally reported six-fold increase in conductance along the apical dendrites resulting in variable slopes of the linear increase between soma and tuft in different morphologies. The apical set dendrites were divided with borders along the apical trunk to contain 3.14% (proximal apical), 577 36.27% (medial apical), 68.90% (distal) and 100% (tuft) of the total apical length respectively. 558 These divisions occurred at path distances of around $100\mu m$, $300\mu m$ and $500\mu m$.

Poirazi et al. 2003 model.

The model by Poirazi et al. (2003b) was also ported to T2N, and similarly adapted to apply 561 to different pyramidal cell morphologies. The model consists of a wide variety of active and 562 passive membrane mechanisms (see the online supplement in Poirazi et al., 2003b), including 563 17 types of ion channels, most of them non-uniformly distributed along the somato-dendritic 564 axis. The apical trunk stems were divided according to laminar depth from soma to stratum 565 lacunosum-moleculare (> 68.90% from the total apical dendrite length, similarly as in the 566 model by Jarsky) and the ion channel distributions were rescaled accordingly. The apical 567 trunk dendrites that bifurcate within the stratum radiatum giving rise to two or more main 568 apical dendrites were also considered as the apical trunk region. Similarly to the original 569 Poirazi model, a peritrunk region was defined as the first $50\mu m$ in path length from every 570 oblique branch that extended away from the apical trunk. The remaining apical branches 571 were considered as the apical region with a further distinction of more distal dendrites, 572 located beyond a laminar depth away from the soma of $300\mu m$ (distal apical) and $350\mu m$ (tuft). 573 The passive parameters and channel densities were similar to the Poirazi model, except for 574 axial conductances being distributed uniformly and the leak reversal potential being fixed to 575 -70mV rendering slightly different resting potentials for each cell morphology. 576

Integrate-and-fire spiking model with passive dendrite leak.

Dynamic LIF spiking responses for all morphologies in **Figures 2–4** were obtained using the ⁵⁷⁸ LIF_tree function in a similar way as for passive dynamic responses (see above). In the case ⁵⁷⁹ of the LIF responses, synaptic conductances were set using **Equation 1'** to reach -60mV at ⁵⁸⁰ the dendrite root when activated at 1Hz. By then setting the voltage threshold of the LIF ⁵⁸¹ mechanism in the dendrite root to -60mV we ensured that spiking started around 1Hz input ⁵⁸²

Dendritic constancy

Cuntz et al.

frequency (**Figure 7B**). Spikes were generated throughout the dendrite when the threshold ⁵⁸³ was reached at the dendritic root, resetting the voltage everywhere to -70mV. Morphologies ⁵⁸⁴ from NeuroMorpho.Org were used in their pure dendritic form (without soma or axon) and ⁵⁸⁵ after normalising dendritic diameters for each population. ⁵⁸⁶

Adaptive exponential integrate-and-fire spiking model with passive den- 587 drite leak. 588

Since the simple LIF is generally not able to reproduce the variety of temporal firing patterns 589 that occur in real neurons we extended it by an adaptation current in combination with an 590 exponential activation term (Brette and Gerstner, 2005), while preserving passive parameters. 591 This also allowed us to test yet another spiking mechanism for our theory of dendritic 592 constancy. Instead of a fixed threshold for spike initiation, action potentials in the adaptive 593 exponential leaky integrate-and-fire (AdExpLIF) are generated through a positive, exponential 594 feedback in the voltage of the dendritic root V_{root} , given by the differential equation $\frac{dV_{root}}{dt}$ = 595 $\Delta_T \cdot e^{\left(\frac{V_{root} - V_T}{\Delta_T}\right)}$. By setting the slope factor to $\Delta_T = 2mV$ and the threshold to $V_T = -60mV$ 596 we made sure that spiking started around 1Hz input frequency similar to our LIF simulations. 597 The exponential activation term in the soma makes precise processing of fast fluctuating inputs 598 during synaptic bombardment possible (Fourcaud-Trocmé et al., 2003), as spike initiation is 599 not instantaneous in contrast to the LIF. The upswing of the potential beyond -60mV grows 600 rapidly to infinity, which is why the exact numerical threshold for a voltage reset has almost no influence on spike timing and was set to $V_{thres} = 10mV$ in all simulations. Altering the 602 parameters of spike initiation had no effects on the constancy of spike numbers with respect to 603 morphology (> 50mV). The adaptation current w acted as a negative feedback on the voltage 604 in each segment of the dendritic tree and was given by: 605

$$\tau \frac{dw}{dt} = a(w - E_L) - w. \tag{10}$$

Once the dendritic root reached V_{thres} , the voltage in each node was reset to $V_{reset} = -70mV$ 606 in the case of spike frequency adaptation. Increasing the reset voltage to -60mV induced 607 bursting. After a spike was triggered, the variable w was increased by an amount b in all 608 segments, which was b = -60fA in the adaptation and bursting neuron model. Depending on 609 b, the bursting neuron elicited several spikes in a short period of time until w counterbalanced 610 the exponential activation term, resulting in a longer ISI in between bursts. In case of the 611

Dendritic constancy

Cuntz et al.

bursting model, the time constant was set to 30ms. Increasing the time constant to $\tau = 100ms$ 612 in combination with a high value of *b* resulted in spike frequency adaptation. 613

Stochastic inputs: Subthreshold voltage moments.

Consider a sealed dendrite of physical length l with electrotonic length constant λ . The voltage time course at the proximal end due to a single brief injection of current of magnitude a at electrotonic position $0 \le x \le l$ is given by 617

$$\varepsilon(x,t) = \frac{a\lambda e^{-\frac{t}{\tau}}}{l} \left[\frac{1}{2} + \sum_{n=1}^{\infty} \cos\left(\frac{n\pi x}{l}\right) e^{-\left(\frac{n\pi\lambda}{l}\right)^2 \frac{t}{\tau}} \right].$$
 (11)

This is plotted in **Figure S6A** (dashed lines). Given that synapses are uniformly distributed over [0, l], the expected (ensemble) value of ε at a given time t, $\langle \varepsilon(t) \rangle$, is given by ⁶¹⁹

$$\langle \varepsilon(t) \rangle = \int_0^L \varepsilon(x,t) P[x] dx = \frac{a e^{-\frac{t}{\tau}}}{2L}$$
(12)

where we have written $L = \frac{l}{\lambda}$ for the electrotonic length. The voltage above rest at the soma, neglecting for the moment a threshold-rest mechanism, is given by a sum of independent synaptic inputs

$$v(t) = \sum_{\{x_i, t_i\}} \varepsilon \left(x_i, t - t_i\right) \chi_{[t_i, \infty)}(t)$$
(13)

where the times t_i are given by a Poisson process of rate $r_{\lambda}l$, the locations x_i are uniformly distributed along the dendrite, and $\chi_{[t_i,\infty)}(t)$ is the indicator function of the interval $[t_i,\infty)$.

The subthreshold steady-state mean voltage above rest $\langle v \rangle$ can be found by taking expectations 625

$$\langle v \rangle = r_{\lambda} L \int_0^\infty \frac{1}{L} \int_0^L \varepsilon(x, t) dx dt = \frac{a r_{\lambda} \tau}{2}$$
 (14)

This is independent of *L*. Similarly, the subthreshold variance in *v* can be written as

$$Var(v) = r_{\lambda}L \int_0^\infty \frac{1}{L} \int_0^L \varepsilon^2(x,t) dx dt = \frac{a^2 r_{\lambda}\tau}{8} \coth(L)$$
(15)

where the coth(L) term approaches 1 in the limit of large *L* (Figure S6B, dashed lines).

626

627

Dendritic constancy

Cuntz et al.

Stochastic inputs: Subthreshold voltage moments for synaptic currents.

The above calculations give the voltage impulse response at the soma. If a synapse has its own time course $\zeta(t)$ (with $\zeta(t) = 0$ for t < 0), then the somatic voltage above rest is given instead by 631

$$v(t) = \sum_{\{x_i, t_i\}} \zeta * \varepsilon \left(x_i, t - t_i \right) \chi_{[t_i, \infty)}(t)$$
(16)

where $\zeta * \varepsilon(x,t) = \int_0^t \zeta(\theta)\varepsilon(x,t-\theta) d\theta$ represents convolution in time. A typical synaptic filter ⁶³² is modelled as a difference of exponentials with timescales τ_f and τ_s such that ⁶³³

$$\zeta(t) = \frac{e^{-\frac{t}{\tau_f}} - e^{-\frac{t}{\tau_s}}}{\tau_f - \tau_s}$$
(17)

Note that each term in the series form of $\varepsilon(x, t)$ can be written as $c_n e^{-\frac{t}{\tau_n}}$ for some coefficient c_n and timescale τ_n as defined above (with c_n typically dependent on input location x). Then each such term convolves with $\zeta(t)$ to give 636

$$\frac{c_n \tau_n}{\tau_s - \tau_f} \left(e^{-\frac{t}{\tau_n}} \left(\frac{\tau_f}{\tau_f - \tau_n} - \frac{\tau_s}{\tau_s - \tau_n} \right) - \left(\frac{\tau_f e^{-\frac{t}{\tau_f}}}{\tau_f - \tau_n} - \frac{\tau_s e^{-\frac{t}{\tau_s}}}{\tau_s - \tau_n} \right) \right)$$
(18)

if τ_f , $\tau_s \neq \tau_n$. In the case that one of $\tau_f = \tau_n$ or $\tau_s = \tau_n$ (without loss of generality let $\tau_f = \tau_n$) 637 the form is instead 638

$$\frac{c_n}{\tau_s - \tau_n} \left(\left(\frac{\tau_s \tau_n}{\tau_s - \tau_n} \right) \left(e^{-\frac{t}{\tau_n}} - e^{-\frac{t}{\tau_s}} \right) - t e^{-\frac{t}{\tau_n}} \right)$$
(19)

with an additional synaptic filter alongside the dendritic filter given by **Equation 11**, the difference in somatic voltage responses to proximal and distal inputs is reduced even for synapses that are fast compared to the membrane time constant (**Figure S6A**).

The subthreshold mean is unchanged from the instantaneous case as $\int_0^{\infty} \zeta(\theta) d\theta = 1$, and the ⁶⁴² subthreshold variance can be computed by squaring the above terms, integrating *t* from 0 to ⁶⁴³ ∞ and *x* from 0 to *l*, and summing the infinite series. The result is cumbersome to write in ⁶⁴⁴ full, but can be plotted in **Figure S6B**. The variance is lower in the case of the synaptic filter ⁶⁴⁵ compared to instantaneous current injection. ⁶⁴⁶

Dendritic constancy

Cuntz et al.

Stochastic inputs: Subthreshold characteristic functions and firing rate approximation. 647

The firing rate can in principle be calculated exactly from the expected time for the stochastic ⁶⁴⁹ process (**Equation 13**) to first reach the firing threshold v_{th} from the voltage reset v_{re} . Given ⁶⁵⁰ a uniform initial voltage v_0 (which decays with timescale τ), the random variable $V_{\{T,v_0\}}$ ⁶⁵¹ describes the voltage T seconds later. The characteristic function $\phi_v(s, T, v_0) = \mathbb{E}\left[e^{-sV_{\{T,v_0\}}}\right]$ of ⁶⁵² $V_{\{T,v_0\}}$ is given by (Rice, 1944)

$$\phi_v(s, T, v_0) = exp\left[-rl\left(\int_0^T 1 - \mathbb{E}_x\left[e^{-s[\varepsilon(x,t)]}\right]dt\right) + v_0 e^{-\frac{T}{\tau}}\right]$$
(20)

where the expectation \mathbb{E}_x is over synaptic locations x. This can be inverted to give the probability distribution f_v of $V_{\{T,v_0\}}$. An additional integral transform over T, $\psi_v(\rho, v_0) = \frac{1}{655}$ $\mathbb{E}\left[e^{-\rho T}f_v\right]$, allows the moment generating function $M_{FP}(t)$ of the first-passage time density to be written as (Siegert, 1951)

$$M_{FP}(t) = \frac{\psi_v(-\rho, v_{re})}{\psi_v(-\rho, v_{th})}$$

$$\tag{21}$$

The mean first-passage time, and hence the output firing rate, could then be extracted from $\frac{dM_{FP}}{dt}|_{t=0}$.

In practice, the above procedure is numerically sensitive and the following approximation is robust to the high cumulative input rates typically seen across an entire dendritic tree. Taking the subthreshold voltage mean μ_v and standard deviation σ_v allows the firing rate R to be accurately approximated (Alijani and Richardson, 2011) using the equation from Brunel and Hakim (1999)

$$R^{-1} = \tau \int_0^\infty \frac{1}{z} e^{-\frac{z^2}{2}} \left(e^{zz_{th}} - e^{zz_{re}} \right) dz$$
(22)

where $z_{th} = \frac{v_{th} - \mu_v}{\sigma_v}$ and $z_{re} = \frac{v_{re} - \mu_v}{\sigma_v}$. This is plotted as a function of dendrite length in ⁶⁶⁵ Figure S6B and as a function of input firing rate in Figure S6C.

Combining the above equations, the output firing rate R can be written, in the case of instantaneous synapses, in terms of intrinsic quantities as

Dendritic constancy

677

$$R^{-1} = \frac{C}{G_m} \int_0^\infty \frac{1}{z} e^{-\frac{z^2}{2}} \left[e^{z\sqrt{\frac{2\lambda G_m}{rlC \coth \frac{1}{\lambda}}} \left(\frac{2\pi dG_m v_{th}}{I_{dist}} - \frac{rlC}{\lambda G_m}\right)} - e^{z\sqrt{\frac{2\lambda G_m}{rlC \coth \frac{1}{\lambda}}} \left(\frac{2\pi dG_m v_{re}}{I_{dist}} - \frac{rlC}{\lambda G_m}\right)} \right] dz$$
(23)

where, as before, *C* is the specific capacitance, G_m is the membrane conductivity, *l* is the dendrite length, *d* is the average diameter, $\lambda = \sqrt{\frac{G_i d}{4G_m}}$ is the electrotonic length, G_i is the axial conductivity, and I_{dist} is the current induced by a single synapse. Additionally, *r* is the rate of synaptic activation per μm , and v_{re} and v_{th} are the reset and threshold voltages respectively.

In the case of filtered synapses, there is not a compact form for R and **Equation 22** is used directly with the subthreshold mean and variance as derived above. The code to calculate R analytically can be found in the function LIF_FR_tree for synaptically filtered current injections.

References

- Adachi R, Yamada R, Kuba H (2015) Plasticity of the axonal trigger zone. *Neuroscien-* 678 *tist* 21:255–265.
- Alijani AK, Richardson MJE (2011) Rate response of neurons subject to fast or frozen noise: From stochastic and homogeneous to deterministic and heterogeneous populations. *Physical Review E* 84:011919.
- Ascoli GA (2006) Mobilizing the base of neuroscience data: the case of neuronal morphologies. 683 Nature Reviews Neuroscience 7:318–324. 684
- Bakken TE, Stevens CF (2011) Visual system scaling in teleost fish. *Journal of Comparative* 685 *Neurology* 153:142–153. 686
- Beining M, Mongiat LA, Schwarzacher SW, Cuntz H, Jedlicka P (2017) T2N as a new tool for robust electrophysiological modeling demonstrated for mature and adult-born dentate granule cells. *eLife* 6:e26517.
- Bekkers JM, Stevens CF (1990) Two different ways evolution makes neurons larger. *Progress* 690 *in Brain Research* 83:37–45. 691

Bird AD, Cuntz H (2016) Optimal current transfer in dendrites. <i>PLOS Computational Biology</i> 12:e1004897.	692 693
Borst A, Haag J (1996) The intrinsic electrophysiological characteristics of fly lobula plate tan- gential cells: I. Passive membrane properties. <i>Journal of Computational Neuroscience</i> 3:313–336.	694 695
Branco T, Clark BA, Häusser M (2010) Dendritic discrimination of temporal input sequences in cortical neurons. <i>Science</i> 329:1671–1675.	696 697
Brette R, Gerstner W (2005) Adaptive exponential integrate-and-fire model as an effective description of neuronal activity. <i>Journal of Neurophysiology</i> 94:3637–3642.	698 699
Brown CE, Boyd JD, Murphy TH (2010) Longitudinal in vivo imaging reveals balanced and branch-specific remodeling of mature cortical pyramidal dendritic arbors after stroke. <i>Journal of Cerebral Blood Flow and Metabolism</i> 30:783–791.	700 701 702
Brunel N, Hakim V (1999) Fast global oscillations in networks of integrate-and-fire neurons with low firing rates. <i>Neural Computation</i> 11:1621–1671.	703 704
Carnevale NT, Hines ML (2004) The NEURON Book. Cambridge University Press.	705
Chavlis S, Petrantonakis PC, Poirazi P (2017) Dendrites of dentate gyrus granule cells con- tribute to pattern separation by controlling sparsity. <i>Hippocampus</i> 27:89–110.	706 707
Chen X, Yuan LL, Zhao C, Birnbaum SG, Frick A, Jung WE, Schwarz TL, Sweatt JD, Johnston D (2006) Deletion of Kv4.2 gene eliminates dendritic A-type K+ current and enhances induction of long-term potentiation in hippocampal CA1 pyramidal neurons. <i>Journal of Neuroscience</i> 26:12143–12151.	708 709 710 711
Connelly WM, Crunelli V, Errington AC (2016) Passive synaptic normalization and input synchrony-dependent amplification of cortical feedback in thalamocortical neuron dendrites. <i>Journal of Neuroscience</i> 36:3735–3754.	712 713 714
Conrad CD, Ortiz JB, Judd JM (2017) Chronic stress and hippocampal dendritic complexity: Methodological and functional considerations. <i>Physiology & Behavior</i> 178:66–81.	715 716
Coskren PJ, Luebke JI, Kabaso D, Wearne SL, Yadav A, Rumbell T, Hof PR, Weaver CM (2015) Functional consequences of age-related morphologic changes to pyramidal neurons of the rhesus monkey prefrontal cortex. <i>Journal of Computational Neuroscience</i> 38:263–283.	717 718 719

Cuntz H, Forstner F, Borst A, Häusser M (2010) One rule to grow them all: a general theory of neuronal branching and its practical application. <i>PLoS Computational Biology</i> 6:e1000877.	720 721
Cuntz H, Forstner F, Haag J, Borst A (2008) The morphological identity of insect dendrites. <i>PLoS Computational Biology</i> 4:e1000251.	722 723
Cuntz H, Forstner F, Schnell B, Ammer G, Raghu SV, Borst A (2013) Preserving neural function under extreme scaling. <i>PLoS ONE</i> 8:e71540.	724 725
Cuntz H, Haag J, Borst A (2003) Neural image processing by dendritic networks. <i>PNAS</i> 100:11082–11085.	726 727
Cuntz H, Haag J, Forstner F, Segev I, Borst A (2007) Robust coding of flow-field parameters by axo-axonal gap junctions between fly visual interneurons. <i>PNAS</i> 104:10229–10233.	728 729
Cuntz H, Mathy A, Häusser M (2012) A scaling law derived from optimal dendritic wiring. <i>PNAS</i> 109:11014–11018.	730 731
Denève S, Alemi A, Bourdoukan R (2017) The brain as an efficient and robust adaptive learner. <i>Neuron</i> 94:969–977.	732 733
Denève S, Machens CK (2016) Efficient codes and balanced networks. <i>Nature Neuroscience</i> 19:375–382.	734 735
Einstein G, Buranosky R, Crain BJ (1994) Dendritic pathology of granule cells in Alzheimer's disease is unrelated to neuritic plaques. <i>Journal of Neuroscience</i> 14:5077–5088.	736 737
Evans MD, Dumitrescu AS, Kruijssen DL, Taylor SE, Grubb MS (2015) Rapid modulation of axon initial segment length influences repetitive spike firing. <i>Cell Reports</i> 13:1233–1245.	738 739
Fourcaud-Trocmé N, Hansel D, van Vreeswijk C, Brunel N (2003) How spike generation mechanisms determine the neuronal response to fluctuating inputs. <i>Journal of Neuroscience</i> 23:11628–11640.	740 741 742
Gabbiani F, Krapp HG, Koch C, Laurent G (2002) Multiplicative computation in a visual neuron sensitive to looming. <i>Nature</i> 420:320–324.	743 744
Garden DLF, Dodson PD, O'Donnell C, White MD, Nolan MF (2008) Tuning of Synaptic Integration in the Medial Entorhinal Cortex to the Organization of Grid Cell Firing Fields. <i>Neuron</i> 60:875–889.	745 746 747

Gidon A, Segev I (2012) Principles governing the operation of synaptic inhibition in dendrites. <i>Neuron</i> 75:330–341.	748 749
Gjorgjieva J, Drion G, Marder E (2016) Computational implications of biophysical diversity and multiple timescales in neurons and synapses for circuit performance. <i>Current Opinion in Neurobiology</i> 37:44–52.	750 751 752
Gulledge AT, Bravo JJ (2016) Neuron morphology influences axon initial segment plasticity. <i>eneuro</i> 3:ENEURO.0085–15.2016.	753 754
Häusser M (2001) Synaptic function: dendritic democracy. Current Biology 11:R10–12.	755
Hines ML, Morse T, Migliore M, Carnevale NT, Shepherd GM (2004) ModelDB: A database to support computational neuroscience. <i>Journal of Computational Neuroscience</i> 17:7–11.	756 757
Jaffe DB, Carnevale NT (1999) Passive normalization of synaptic integration influenced by dendritic architecture. <i>Journal of Neurophysiology</i> 82:3268–3285.	758 759
Jarsky T, Roxin A, Kath WL, Spruston N (2005) Conditional dendritic spike propagation following distal synaptic activation of hippocampal CA1 pyramidal neurons. <i>Nature Neuroscience</i> 8:1667–1676.	760 761 762
Koch C, Douglas RJ, Wehmeier U (1990) Visibility of synaptically induced conductance changes: theory and simulations of anatomically characterized cortical pyramidal cells. <i>Journal of Neuroscience</i> 10:1728–1744.	763 764 765
Koch C, Segev I (1999) Methods in neuronal modeling - from ions to networks MIT Press, Cambridge, MA.	766 767
Kuba H (2012) Structural tuning and plasticity of the axon initial segment in auditory neurons. <i>Journal of Physiology</i> 590:5571–5579.	768 769
Kuba H, Oichi Y, Ohmori H (2010) Presynaptic activity regulates Na+ channel distribution at the axon initial segment. <i>Nature</i> 465:1075–1078.	770 771
Leal SL, Yassa MA (2013) Perturbations of neural circuitry in aging, mild cognitive impairment, and Alzheimer's disease. <i>Ageing Research Reviews</i> 12:823–831.	772 773
London M, Häusser M (2005) Dendritic computation. Annual Review of Neuroscience 28:503–532.	774

Dendritic constancy

London M, Meunier C, Segev I (1999) Signal transfer in passive dendrites with nonuniform membrane conductance. <i>Journal of Neuroscience</i> 19:8219–8233.	775 776
London M, Roth A, Beeren L, Häusser M, Latham PE (2010) Sensitivity to perturbations in vivo implies high noise and suggests rate coding in cortex. <i>Nature</i> 466:123–127.	777 778
London M, Segev I (2001) Synaptic scaling in vitro and in vivo. <i>Nature Neuroscience</i> 4:853–855.	779
Luebke JI, Medalla M, Amatrudo JM, Weaver CM, Crimins JL, Hunt B, Hof PR, Peters A (2015) Age-related changes to layer 3 pyramidal cells in the rhesus monkey visual cortex. <i>Cerebral</i> <i>Cortex</i> 25:1454–1468.	780 781 782
Magee (1999) Dendritic Ih normalizes temporal summation in hippocampal CA1 neurons. <i>Nature Neuroscience</i> 2:508–514.	783 784
Magee JC (2000) Dendritic integration of excitatory synaptic input. <i>Nature Reviews Neuroscience</i> 1:181–190.	785 786
Magee JC, Cook EP (2000) Somatic EPSP amplitude is independent of synapse location in hippocampal pyramidal neurons. <i>Nature Neuroscience</i> 3:895–903.	787 788
Mainen ZF, Joerges J, Huguenard JR, Sejnowski TJ (1995) A model of spike initiation in neocortical pyramidal neurons. <i>Neuron</i> 15:1427–1439.	789 790
Mainen ZF, Sejnowski TJ (1996) Influence of dendritic structure on firing pattern in model neocortical neurons. <i>Nature</i> 382:363–366.	791 792
 Markram H, Muller E, Ramaswamy S, Reimann MW, Abdellah M, Sanchez CA, Ailamaki A, Alonso-Nanclares L, Antille N, Arsever S, Kahou GAA, Berger TK, Bilgili A, Buncic N, Chalimourda A, Chindemi G, Courcol JD, Delalondre F, Delattre V, Druckmann S, Dumusc R, Dynes J, Eilemann S, Gal E, Gevaert ME, Ghobril JP, Gidon A, Graham JW, Gupta A, Haenel V, Hay E, Heinis T, Hernando JB, Hines M, Kanari L, Keller D, Kenyon J, Khazen G, Kim Y, King JG, Kisvarday Z, Kumbhar P, Lasserre S, Le Bé JV, Magalhães BRC, Merchán-Pérez A, Meystre J, Morrice BR, Muller J, Muñoz-Céspedes A, Muralidhar S, Muthurasa K, Nachbaur D, Newton TH, Nolte M, Ovcharenko A, Palacios J, Pastor L, Perin R, Ranjan R, Riachi I, Rodríguez JR, Riquelme JL, Rössert C, Sfyrakis K, Shi Y, Shillcock JC, Silberberg G, Silva R, Tauheed F, Telefont M, Toledo-Rodriguez M, Tränkler T, Van Geit W, Díaz JV, Walker 	 793 794 795 796 797 798 799 800 801 802
<u> </u>	

Dendritic constancy

R, Wang Y, Zaninetta SM, DeFelipe J, Hill SL, Segev I, Schürmann F (2015) Reconstruction and simulation of neocortical microcircuitry. <i>Cell</i> 163:456–492.	803 804
Mckay BE, Turner RW (2005) Physiological and morphological development of the rat cerebellar Purkinje cell. <i>Journal of Physiology</i> 567:829–850.	805 806
Platschek S, Cuntz H, Deller T, Jedlicka P (2017) Lesion-induced dendritic remodeling as a new mechanism of homeostatic structural plasticity in the adult brain In <i>The Rewiring Brain</i> , Vol. 15, pp. 203–218. Elsevier.	807 808 809
Platschek S, Cuntz H, Vuksic M, Deller T, Jedlicka P (2016) A general homeostatic principle following lesion induced dendritic remodeling. <i>Acta Neuropathologica Communications</i> 4:19.	810 811
Poirazi P, Brannon T, Mel BW (2003a) Arithmetic of subthreshold synaptic summation in a model CA1 pyramidal cell. <i>Neuron</i> 37:977–987.	812 813
Poirazi P, Brannon T, Mel BW (2003b) Pyramidal neuron as two-layer neural network. <i>Neuron</i> 37:989–999.	814 815
Polsky A, Mel BW, Schiller J (2004) Computational subunits in thin dendrites of pyramidal cells. <i>Nature Neuroscience</i> 7:621–627.	816 817
Qin L, Jing D, Parauda S, Carmel J, Ratan RR, Lee FS, Cho S (2014) An adaptive role for BDNF Val66Met polymorphism in motor recovery in chronic stroke. <i>Journal of Neuroscience</i> 34:2493–2502.	818 819 820
Rall W (1959) Branching dendritic trees and motoneuron membrane resistivity. <i>Experimental Neurology</i> 527:491–527.	821 822
Rall W (1962) Theory of physiological properties of dendrites. <i>Annals of the New York Academy of Sciences</i> 96:1071–1092.	823 824
Rall W, Burke RE, Smith TG, Nelson PG, Frank K (1967) Dendritic location of synapses and possible mechanisms for the monosynaptic EPSP in motoneurons. <i>Journal of Neurophysiology</i> 30:1169–1193.	825 826 827
Rall W, Rinzel J (1973) Branch input resistance and steady attenuation for input to one branch of a dendritic neuron model. <i>Biophysical Journal</i> 13:648–687.	828 829
Rice SO (1944) Mathematical analysis of random noise. Bell Systems.	830

Dendritic constancy

Rihn LL, Claiborne BJ (1990) Dendritic growth and regression in rat dentate granule cells during late postnatal development. <i>Developmental Brain Research</i> 54:115–124.	831 832
Rinzel J, Rall W (1974) Transient response in a dendritic neuron model for current injected at one branch. <i>Biophysical journal</i> 14:759–790.	833 834
Rudolph M, Destexhe A (2003) A fast-conducting, stochastic integrative mode for neocortical neurons in vivo. <i>Journal of Neuroscience</i> 23:2466–2476.	835 836
Rushton WAH (1937) Initiation of the propagated disturbance. <i>Proceedings of the Royal Society B</i> 124:210–243.	837 838
Schmidt-Hieber C, Jonas P, Bischofberger J (2007) Subthreshold dendritic signal processing and coincidence detection in dentate gyrus granule cells. <i>Journal of Neuroscience</i> 27:8430–8441.	839 840
Schmidt-Hieber C, Nolan MF (2017) Synaptic integrative mechanisms for spatial cognition. <i>Nature Neuroscience</i> 20:1483–1492.	841 842
Segev I, London M (2000) Untangling dendrites with quantitative models. <i>Science</i> 290:744–750.	843
Siegert AJF (1951) On the First Passage Time Probability Problem. Physical Review 81:617–623.	844
Single S, Borst A (1998) Dendritic integration and its role in computing image velocity. <i>Science</i> 281:1848–1850.	845 846
Šišková Z, Justus D, Kaneko H, Friedrichs D, Henneberg N, Beutel T, Pitsch J, Schoch S, Becker A, von der Kammer H, Remy S (2014) Dendritic structural degeneration is func- tionally linked to cellular hyperexcitability in a mouse model of Alzheimer's disease. <i>Neu-</i> <i>ron</i> 84:1023–1033.	847 848 849 850
Snider J, Pillai A, Stevens CF (2010) A universal property of axonal and dendritic arbors. <i>Neuron</i> 66:45–56.	851 852
Spires TL, Hyman BT (2004) Neuronal structure is altered by amyloid plaques. <i>Reviews in the Neurosciences</i> 15:267–278.	853 854
Stein RB (1965) A theoretical analysis of neuronal variability. <i>Biophysical Journal</i> 5:173–194.	855
Steward O, Vinsant SL, Davis L (1988) The process of reinnervation in the dentate gyrus of adult rats: an ultrastructural study of changes in presynaptic terminals as a result of sprouting. <i>Journal of Comparative Neurology</i> 267:203–210.	856 857 858

Dendritic constancy

Teeter CM, Stevens CF (2011) A general principle of neural arbor branch density. <i>Current Biology</i> 21:2105–2108.	859 860
Turrigiano GG (2017) The dialectic of Hebb and homeostasis. <i>Philosophical transactions of the Royal Society of London. Series B, Biological sciences</i> 372:4–6.	861 862
Turrigiano GG, Nelson SB (2004) Homeostatic plasticity in the developing nervous system. <i>Nature Reviews Neuroscience</i> 5:97–107.	863 864
van Elburg RAJ, van Ooyen A (2010) Impact of dendritic size and dendritic topology on burst firing in pyramidal cells. <i>PLoS Computational Biology</i> 6:e1000781.	865 866
van Ooyen A, Duijnhouwer J, Remme MWH, van Pelt J (2002) The effect of dendritic topology on firing patterns in model neurons. <i>Network: Computation in Neural Systems</i> 13:311–325.	867 868
Vetter P, Roth A, Häusser M (2001) Propagation of action potentials in dendrites depends on dendritic morphology. <i>Journal of Neurophysiology</i> 85:926–937.	869 870
Vuksic M, Del Turco D, Vlachos A, Schuldt G, Müller CM, Schneider G, Deller T (2011) Unilat- eral entorhinal denervation leads to long-lasting dendritic alterations of mouse hippocampal granule cells. <i>Experimental Neurology</i> 230:176–185.	871 872 873
Williams SR, Stuart GJ (2003) Role of dendritic synapse location in the control of action potential output. <i>Trends in Neurosciences</i> 26:147–154.	874 875
Yassa MA, Muftuler LT, Stark CEL (2010) Ultrahigh-resolution microstructural diffusion tensor imaging reveals perforant path degradation in aged humans in vivo. <i>PNAS</i> 107:12687–12691.	876 877

Dendritic constancy

Cuntz et al.

Supporting information



Fig S1. Steady-state passive responses to distributed inputs in synthetic dendrites are independent of dendrite length and shape.

Similar analysis as in **Figure 4** but for 10,000 synthetic dendritic trees obtained using extended minimum spanning trees that reproduce many features of real dendrites (Cuntz et al., 2010). These cover a wide range of tree complexities as well as overall sizes (see Methods).



Fig S2. Distributions of diameters in somata and dendrites of the NeuroMorpho.Org database.

A, Distribution of soma radii in NeuroMorpho.Org. Not every cell had well-reconstructed somata explaining the tail of very small radii. High-quality soma reconstructions were not an inclusion criterion for this study that focuses on dendritic trees in the main text. **B**, Distribution of average dendrite diameters after resampling to $1\mu m$ internode distances to weigh each location in the dendritic tree homogeneously.

Dendritic constancy



Fig S3. Effect of soma size on dendritic constancy. See next page

Dendritic constancy

Fig S3. (continued) A, Analytical calculations of relative deviation from dendritic constancy (compared to 100%) as a function of somatic radius for different lengths of dendrite (top panel) and as a function of length for different somatic radii (bottom panels). Used cables had $1\mu m$ diameter, specific membrane conductance $G_m = 50 \frac{\mu S}{cm^2}$ and specific axial resistance of $Ri = 100\Omega cm$. **B**, Similar calculation for the NeuroMorpho.Org database as **Figure 4A** but with appended somata that do not receive synaptic inputs (see Methods for more details). Here, colours indicate the radius of the appended soma.

Dendritic constancy



Fig S4. Effect of inhomogeneous distance-dependent synapse weights on dendritic constancy.

In these plots, synapses were scaled from $0.8 \times$ to $1.2 \times$ in a linear relation with distance (path length) from soma. **A**, Analogous to **Figure 6B**, the model by Jarsky et al. (2005) with inhomogeneous synapse weights. **B**, Analogous to **Figure 8A**, the LIF model in NeuroMorpho.Org morphologies with inhomogeneous synapse weights.

Dendritic constancy

Cuntz et al.

Distributed excitation (80 %) and inhibition (20 %)



Fig S5. Effect of inhibitory synapses on dendritic constancy.

In these plots, 20% of all synapses were randomly selected to have a reversal potential of -80mV, which renders them inhibitory synapses. **A**, Analogous to **Figure 6B**, the model by Jarsky et al. (2005) with 20% inhibitory synapses. **B**, Analogous to **Figure 8A**, the LIF model in NeuroMorpho.Org morphologies with 20% inhibitory synapses.

Dendritic constancy

Cuntz et al.



Analytical calculations in the cable: Voltage to spike transformation

Fig S6. Transformation of voltage fluctuations into spikes.

A, Voltage response as a function of time at the proximal end of a sealed dendrite of electrotonic length 1 to an instantaneous (dashed lines) and synaptically filtered (double exponential $\tau_{rise} = 0.5ms$, $\tau_{decay} = 2.5ms$, solid lines) current injection with magnitude a = 1. Blue lines show responses at 0.2 and yellow lines at 0.8 electrotonic distance. The time constant of the membrane was $\tau = 20ms$. **B**, Top panel, subthreshold proximal voltage variance as a function of electrotonic length for different input rates per unit electrotonic length: 200, 300, 400, and 500Hz. a = 2.5 and $\tau = 20ms$. Bottom panel, firing rate as a function of electrotonic length: 200, 300, 400, and 500Hz. a = 2.5 and $\tau = 20ms$. Bottom panel, firing rate as a function of electrotonic length for different input rates per unit electrotonic length: 200, 300, 400, and <math>500Hz. a = 2.5 and $\tau = 20ms$. Bottom panel, firing rate as a function of electrotonic length for different input rates per unit electrotonic length: 200, 300, 400, and <math>500Hz. a = 2.5 and $\tau = 20ms$. As in **A**, dashed lines for instantaneous and solid lines for filtered current injections. **C**, Output firing rate as a function of afferent rate for dendrites of different electrotonic lengths: 0.1, 1, and 10, 000. a = 2.5 and $\tau = 20ms$. As in **A**, dashed lines for instantaneous and solid lines for filtered current injections.

Dendritic constancy

Cuntz et al.

Table S1. Selected datasets from NeuroMorpho.Org

Lab	Species	Region	Cell type
Acsady	rat	ventral thalamus	modulated
Alvarez	rat	spinal cord	motoneuron
Amaral	rat	hippocampus	pyramidal
Araujo	proechimys	hippocampus	pyramidal-like
Araujo	rat	hippocampus	pyramidal
Ascoli	mouse	spinal cord	motoneuron
Ascoli	rat	basal forebrain	choline acetyltransferase (ChAT)- positive
Ascoli	rat	basal forebrain	neuropeptide Y (NPY)-positive
Ascoli	rat	hippocampus	not reported
Avendano	rat	brainstem	Intersubnuclear neuron
Barrionuevo	rat	hippocampus	pyramidal
Bartos	mouse	hippocampus	basket
Bartos	mouse	hippocampus	dendritic targeting
Bartos	mouse	hippocampus	perisomatic targeting
Bianchi	chimpanzee	neocortex	pyramidal
Bikson	rat	neocortex	not reported
Bikson	rat	neocortex	pyramidal
Blackman	mouse	neocortex	basket
Blackman	mouse	neocortex	pyramidal
Brown	rat	neocortex	multipolar
Brown	rat	neocortex	neurogliaform
Brown	rat	neocortex	pyramidal
Brown	rat	neocortex	tripolar
Brumberg	mouse	neocortex	pyramidal
Burke	cat	spinal cord	motoneuron
Cameron	cat	spinal cord	motoneuron
Cameron	rat	brainstem	motoneuron
Cauli	rat	neocortex	neuropeptide Y (NPY)-positive
Cauli	rat	neocortex	bipolar
Cauli	rat	neocortex	pyramidal
Chalupa	mouse	retina	ganglion
Chmykhova	frog	spinal cord	motoneuron
Chmykhova	turtle	spinal cord	motoneuron
Cho	mouse	hippocampus	granule
Claiborne	rat	hippocampus	granule
Claiborne	rat	hippocampus	pyramidal
Collin	pouched lamprey	retina	ganglion
Cossart-Bernard	rat	hippocampus	oriens-lacunosum moleculare
Cossart-Bernard	rat	hippocampus	perforant pathway-associated
Cossart-Bernard	rat	hippocampus	perisomatic targeting
Cossart-Bernard	rat	hippocampus	Schaffer-collateral associated
Cossart-Bernard	rat	hippocampus	trilaminar

Dendritic constancy

Lab	Species	Region	Cell type
Cox	drosophila	peripheral nervous	multidendritic-dendritic ar-
	melanogaster	system	borization (DA)
De Koninck	rat	neocortex	pyramidal
Del Negro	mouse	myelencephalon	non-glutamatergic
Dendritica	guinea pig	cerebellum	Purkinje
Dendritica	rat	basal ganglia	dopaminergic
Dendritica	rat	cerebellum	Purkinje
Dendritica	rat	neocortex	pyramidal
Destexhe	cat	neocortex	pyramidal
Destexhe	rat	dorsal thalamus	thalamocortical
Dusart	mouse	cerebellum	Purkinje
Esclapez	rat	hippocampus	pyramidal
Feldmeyer	rat	neocortex	fast-spiking
Feldmeyer	rat	neocortex	horizontal
Feldmeyer	rat	neocortex	inverted
Feldmeyer	rat	neocortex	multipolar
Feldmeyer	rat	neocortex	pyramidal
Feldmeyer	rat	neocortex	tangential
Franca	rat	neocortex	nitrergic
Fukunaga	mouse	main olfactory bulb	mitral
Fukunaga	mouse	main olfactory bulb	tufted
Fyffe	cat	spinal cord	Ia inhibitory
Fyffe	cat	spinal cord	motoneuron
Fyffe	cat	spinal cord	Renshaw
Fyffe	cat	spinal cord	spinocerebellar
Garcia-Cairasco	rat	hippocampus	granule
Gonzalez-Burgos	monkey	neocortex	basket
Gonzalez-Burgos	monkey	neocortex	double bouquet
Gonzalez-Burgos	monkey	neocortex	neurogliaform
Gonzalez-Burgos	monkey	neocortex	pyramidal
Gonzalez-Burgos	mouse	neocortex	basket
Gonzalez-Burgos	mouse	neocortex	pyramidal
Groen	rat	hippocampus	pyramidal
Gulyas	rat	hippocampus	calbindin (CB)-positive
Gulyas	rat	hippocampus	cholecystokinin (CCK)-positive
Gulyas	rat	hippocampus	calretinin (CR)-positive
Gulyas	rat	hippocampus	pyramidal
Gulyas	rat	hippocampus	parvalbumin (PV)-positive
Hajos	mouse	hippocampus	Chandelier
Halnes	mouse	thalamus	GABAergic
Hay	rat	neocortex	pyramidal
Helmstaedter	rat	neocortex	not reported
Helmstaedter	rat	neocortex	pyramidal
Henckens	rat	amygdala	pyramidal
Henckens	rat	amygdala	stellate
Henckens	rat	hippocampus	pyramidal

Dendritic constancy

Lab	Species	Region	Cell type
Henckens	rat	neocortex	pyramidal
Henny	rat	basal ganglia	dopaminergic
Irintchev	rat	brainstem	motoneuron
Jacobs	bottlenose dolphin	neocortex	aspiny
Jacobs	bottlenose dolphin	neocortex	pyramidal-like
Jacobs	chimpanzee	cerebellum	basket
Jacobs	chimpanzee	cerebellum	Golgi
Jacobs	chimpanzee	cerebellum	granule
Jacobs	chimpanzee	cerebellum	Lugaro
Jacobs	chimpanzee	cerebellum	stellate
Jacobs	clouded leopard	cerebellum	basket
Jacobs	clouded leopard	cerebellum	granule
Jacobs	clouded leopard	cerebellum	Lugaro
Jacobs	clouded leopard	cerebellum	stellate
Jacobs	elephant	cerebellum	basket
Jacobs	elephant	cerebellum	Golgi
Jacobs	elephant	cerebellum	Lugaro
Jacobs	elephant	cerebellum	stellate
Jacobs	giraffe	cerebellum	basket
Jacobs	giraffe	cerebellum	Golgi
Jacobs	giraffe	cerebellum	granule
Jacobs	giraffe	cerebellum	Lugaro
Jacobs	giraffe	cerebellum	stellate
Jacobs	giraffe	neocortex	crab-like
Jacobs	giraffe	neocortex	neurogliaform
Jacobs	giraffe	neocortex	pyramidal
Jacobs	human	cerebellum	basket
Jacobs	human	cerebellum	Golgi
Jacobs	human	cerebellum	granule
Jacobs	human	cerebellum	Lugaro
Jacobs	human	cerebellum	stellate
Jacobs	human	neocortex	pyramidal
Jacobs	humpback whale	cerebellum	basket
Jacobs	humpback whale	cerebellum	Golgi
Jacobs	humpback whale	cerebellum	granule
Jacobs	humpback whale	cerebellum	Lugaro
Jacobs	humpback whale	cerebellum	stellate
Jacobs	humpback whale	neocortex	aspiny
Jacobs	humpback whale	neocortex	pyramidal-like
Jacobs	humpback whale	neocortex	sternzelle
Jacobs	manatee	cerebellum	basket
Jacobs	manatee	cerebellum	stellate
Jacobs	minke whale	neocortex	aspiny
Jacobs	minke whale	neocortex	pyramidal
Jacobs	minke whale	neocortex	pyramidal-like

Dendritic constancy

Lab	Species	Region	Cell type
Jacobs	Siberian tiger	cerebellum	basket
Jacobs	Siberian tiger	cerebellum	Golgi
Jacobs	Siberian tiger	cerebellum	granule
Jacobs	Siberian tiger	cerebellum	Lugaro
Jacobs	Siberian tiger	cerebellum	stellate
Jaeger	rat	basal ganglia	not reported
Jaeger	rat	cerebellum	glutamatergic
Jaffe	rat	hippocampus	not reported
Jaffe	rat	hippocampus	pyramidal
Johnson	domestic pig	hippocampus	granule
Johnston	rat	hippocampus	pyramidal
Jonas	rat	hippocampus	basket
Kim	mouse	hippocampus	pyramidal
Kisvarday	cat	neocortex	pyramidal
Kole	rat	hippocampus	pyramidal
Korngreen	rat	neocortex	pyramidal
Krieger	mouse	neocortex	pyramidal
Kubota	rat	neocortex	basket
Lai	mouse	basal ganglia	medium spiny
Lee	mouse	amygdala	pyramidal
Lee	mouse	hippocampus	granule
Lien	rat	hippocampus	dendritic targeting
Lien	rat	hippocampus	perisomatic targeting
Luebke	monkey	neocortex	pyramidal
Luzzati	guinea pig	basal ganglia	Neuroblast
Luzzati	mouse	basal ganglia	Neuroblast
Mailly	rat	basal ganglia	dopaminergic
Markram	rat	neocortex	basket
Markram	rat	neocortex	bipolar
Markram	rat	neocortex	bitufted
Markram	rat	neocortex	Chandelier
Markram	rat	neocortex	Descending
Markram	rat	neocortex	double bouquet
Markram	rat	neocortex	horizontal
Markram	rat	neocortex	Martinotti
Markram	rat	neocortex	neurogliaform
Markram	rat	neocortex	not reported
Markram	rat	neocortex	pyramidal
Markram	rat	neocortex	Small
Markram	rat	neocortex	stellate
Martone	mouse	cerebellum	Purkinje
Maxwell	cat	spinal cord	spinocerebellar
Meyer	rat	neocortex	pyramidal
Meyer	rat	neocortex	stellate
Miller	salamander	retina	ganglion

Dendritic constancy

Lab	Species	Region	Cell type
Mizrahi	mouse	main olfactory bulb	periglomerular
Mustaparta- Lofaldli	moth	antennal lobe	olfactory
Nolan	mouse	entorhinal cortex	stellate
Nusser	rat	main olfactory bulb	deep short axon
Nusser	rat	main olfactory bulb	external tufted cell (ETC)
OpenWorm	C. elegans	pharyngeal ner- vous system	motoneuron
OpenWorm	C. elegans	pharyngeal ner- vous system	pharyngeal
OpenWorm	C. elegans	somatic nervous system	amphid
OpenWorm	C. elegans	somatic nervous system	motoneuron
OpenWorm	C. elegans	somatic nervous system	not reported
OpenWorm	C. elegans	somatic nervous system	ring
OpenWorm	C. elegans	somatic nervous system	somatic
Poorthuis	mouse	neocortex	pyramidal
Poria	mouse	retina	ganglion
Povysheva	rat	neocortex	not reported
Rhode	cat	brainstem	vertical
Rose	cat	spinal cord	motoneuron
Santhakumar	rat	hippocampus	semilunar granule
Sjostrom	mouse	neocortex	basket
Sjostrom	mouse	neocortex	Martinotti
Sjostrom	mouse	neocortex	pyramidal
Smith	rat	ventral striatum	aspiny
Smith	rat	ventral striatum	medium spiny
Smith-Koizumi	rat	myelencephalon	inspiratory
Soltesz	mouse	hippocampus	pyramidal
Somogyi	rat	hippocampus	basket
Spruston	rat	hippocampus	not reported
Spruston	rat	hippocampus	pyramidal
Staiger	rat	neocortex	pyramidal
Staiger	rat	neocortex	stellate
Strettoi	mouse	retina	ganglion
Svoboda	rat	neocortex	pyramidal
Sztarker	locust	optic Lobe	somatic
Tepper	mouse	basal ganglia	tyrosine-hydroxylase-positive
Timofeev	cat	neocortex	pyramidal
Timofeev	cat	ventral thalamus	thalamocortical
Todd	rat	spinal cord	projection neuron
Turner	rat	hippocampus	dendritic targeting

Dendritic constancy

Lab	Species	Region	Cell type
Turner	rat	hippocampus	granule
Turner	rat	hippocampus	pyramidal
Turner	rat	hippocampus	total molecular layer projecting
Vervaeke	mouse	cerebellum	Golgi
Vuksic	mouse	hippocampus	granule
Wearne-Hof	monkey	neocortex	pyramidal
Wittner	guinea pig	hippocampus	pyramidal
Zaitsev	monkey	neocortex	pyramidal