Measurement of the absolute branching fraction of the three-body decay $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ and search for $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}, \Sigma^{0} K^{+} \pi^{0}$ and $\Lambda K^{+} \pi^{0}$
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The Cabbibo-favored decay $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ is studied for the first time using $6.1 \mathrm{fb}^{-1}$ of $e^{+} e^{-}$ collision data at center-of-mass energies between 4.600 and 4.840 GeV , collected with the BESIII detector at the BEPCII collider. With a double-tag method, the branching fraction of the threebody decay $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ is measured to be $(7.79 \pm 1.46 \pm 0.71) \times 10^{-3}$, where the first and second uncertainties are statistical and systematic, respectively. The branching fraction of the two-body decay $\Lambda_{c}^{+} \rightarrow \Xi(1530)^{0} K^{+}$is $(5.99 \pm 1.04 \pm 0.29) \times 10^{-3}$, which is consistent with the previous result of $(5.02 \pm 0.99 \pm 0.31) \times 10^{-3}$. In addition, the upper limit on the branching fraction of the doubly Cabbibo-suppressed decay $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}$ is $7.1 \times 10^{-4}$ at the $90 \%$ confidence level. The upper limits on the branching fractions of $\Lambda_{c}^{+} \rightarrow \Sigma^{0} K^{+} \pi^{0}$ and $\Lambda K^{+} \pi^{0}$ are also determined to be $1.8 \times 10^{-3}$ and $2.0 \times 10^{-3}$, respectively.

## I. INTRODUCTION

Hadronic decays of charmed baryons provide an ideal laboratory to understand the interplay of weak and strong interactions in the charm system [1-9], and the measured branching fractions of charmed baryons play an important role in constraining models of charmed hadronic decays [10, 11. However, no reliable phenomenological model of charmed baryon decays currently exists. The $\Lambda_{c}^{+}$baryon is the lightest charmed baryon, thus it is often a decay product in many charmed baryon decays. Hence, an investigation of the $\Lambda_{c}^{+}$decay is essential for understanding excited charmed baryons [12]. In charmed baryon decays, the non-factorizable contributions from W-exchange diagrams play an essential role.

In contrast, these effects are negligible in heavy meson decays [13]. Therefore, measurements of the absolute branching fractions of $\Lambda_{c}^{+}$decays are important to understanding the internal dynamics of charmed baryon decays [14.

In recent years, great progress has been made in the experimental study of the $\Lambda_{c}^{+}$baryon at the Belle [15], LHCb 16 and BESIII experiments [17-20. First, a breakthrough was achieved with the measurement of the absolute branching fraction of $\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}$[21, 22]. Next, BESIII directly measured the absolute branching fractions of twelve decay modes for the first time [21]. However, precise measurements for several Cabbibofavored (CF) decays of $\Lambda_{c}^{+}$are currently unavailable. Furthermore, a large number of the singly Cabbibosuppressed (SCS) decays and the doubly Cabbibo-


Fig. 1. The dominant Feynman diagram of the decay (a) $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ and (b) $n K^{+} \pi^{0}$.
suppressed (DCS) decays of $\Lambda_{c}^{+}$have not yet been studied. Based on the data sets at BESIII, measurements of the branching fractions of $\Lambda_{c}^{+}$decays of currently known decay modes could potentially reach a sensitivity of $10^{-4}$. In particular, the branching fraction of $\Lambda_{c}^{+} \rightarrow n \pi^{+}$was recently measured to be $(6.6 \pm 1.3) \times 10^{-4} \quad 17$. In addition, the data allows for a search of many rare $\Lambda_{c}^{+}$decays.

The three-body CF decay $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ is expected to have a large decay rate. Figure 1(a) presents a typical Feynman diagram of this decay. Some phenomenological models have predicted different branching fractions for the $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ decay, which are $(4.5 \pm 0.8) \times 10^{-2}[23]$ and $(3.2 \pm 0.6) \times 10^{-2}$ [24] by assuming $\mathrm{SU}(3)$ flavor symmetry and isospin asymmetry, respectively. Experimentally, there are only a few studies of $\Lambda_{c}^{+}$decays with a $\Xi^{0}$ baryon in the final state, and the three-body decay $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ has not yet been studied. Measurement of the branching fraction will help us further understand the underlying dynamics of $\Lambda_{c}^{+}$decays and distinguish among the different theoretical models [23].

The three-body DCS decay $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}$ is also of great interest, and phenomenological models of this decay mode have been proposed [23, 24]. $\mathrm{SU}(3)$ flavor symmetry predicts the branching fraction of $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}$ to be $(5.0 \pm 0.5) \times 10^{-5}$ [23]. Figure $1(\mathrm{~b})$ shows a typical Feynman diagram of $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}$. Experimental measurements of DCS decays of $\Lambda_{c}^{+}$are limited due to the suppressed branching fractions. Currently, the only study of a $\operatorname{DCS} \Lambda_{c}^{+}$decay is $\Lambda_{c}^{+} \rightarrow p K^{+} \pi^{-}$. The relative branching fraction $\mathcal{B}\left(\Lambda_{c}^{+} \rightarrow p K^{+} \pi^{-}\right) / \mathcal{B}\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}\right)$ is measured to be $(2.4 \pm 0.4) \times 10^{-3} \quad 25$.

In this paper, the three-body decays $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$, $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}, \Lambda_{c}^{+} \rightarrow \Sigma^{0} K^{+} \pi^{0}, \Lambda_{c}^{+} \rightarrow \Lambda K^{+} \pi^{0}$, and the two-body decay $\Lambda_{c}^{+} \rightarrow \Xi(1530)^{0} K^{+}$are studied experimentally with a double-tag (DT) method 26]. This analysis is performed using a data sample with an integrated luminosity of $6.1 \mathrm{fb}^{-1}$ collected at center-of-mass (CM) energies between 4.600 and 4.840 GeV , listed in Table 1, by the BESIII detector at the BEPCII collider. Throughout the text, the charge conjugate states are always implied.

Table 1. The CM energy and the integrated luminosity ( $\mathcal{L}_{\text {int }}$ ) for each energy point. The first and the second uncertainties are statistical and systematic, respectively.

| Dataset | CM energy $(\mathrm{MeV})$ | $\mathcal{L}_{\text {int }}\left(\mathrm{pb}^{-1}\right)$ |
| :---: | :---: | :---: |
| 4.600 | $4599.53 \pm 0.07 \pm 0.74$ | $586.90 \pm 0.10 \pm 3.90$ |
| 4.612 | $4611.84 \pm 0.12 \pm 0.28$ | $103.45 \pm 0.05 \pm 0.64$ |
| 4.620 | $4628.00 \pm 0.06 \pm 0.31$ | $519.93 \pm 0.11 \pm 3.22$ |
| 4.640 | $4640.67 \pm 0.06 \pm 0.36$ | $548.15 \pm 0.12 \pm 3.40$ |
| 4.660 | $4661.22 \pm 0.06 \pm 0.29$ | $527.55 \pm 0.12 \pm 3.27$ |
| 4.680 | $4681.84 \pm 0.08 \pm 0.29$ | $1664.34 \pm 0.21 \pm 10.32$ |
| 4.700 | $4698.57 \pm 0.10 \pm 0.32$ | $534.40 \pm 0.12 \pm 3.31$ |
| 4.740 | $4739.70 \pm 0.20 \pm 0.30$ | $164.27 \pm 0.07 \pm 0.87$ |
| 4.750 | $4750.05 \pm 0.12 \pm 0.29$ | $367.21 \pm 0.10 \pm 1.95$ |
| 4.780 | $4780.54 \pm 0.12 \pm 0.33$ | $512.78 \pm 0.12 \pm 2.72$ |
| 4.840 | $4843.07 \pm 0.20 \pm 0.31$ | $527.29 \pm 0.12 \pm 2.79$ |

## II. BESIII DETECTOR AND MONTE CARLO

The BESIII detector [29] records symmetric $e^{+} e^{-}$collisions provided by the BEPCII 30 storage ring, which operates in the CM energy range from 2.0 to 4.95 GeV , with a peak luminosity of $1.1 \times 10^{33} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}$ achieved at $\sqrt{s}=3.77 \mathrm{GeV}$ 31. The cylindrical core of the BESIII detector covers $93 \%$ of the full solid angle and consists of a helium-based multilayer drift chamber (MDC), a plastic scintillator time-of-flight system (TOF), and a CsI(Tl) electromagnetic calorimeter (EMC), which are all enclosed in a superconducting solenoidal magnet providing a 1.0 T magnetic field. The solenoid is supported by an octagonal flux-return yoke with resistive plate counter muon identification modules interleaved with steel 32 . The charged-particle momentum resolution at $1 \mathrm{GeV} / c$ is $0.5 \%$, and resolution of the ionization energy loss in the MDC $(\mathrm{d} E / \mathrm{d} x)$ is $6 \%$ for electrons from Bhabha scattering. The EMC measures photon energies with a resolution of $2.5 \%(5 \%)$ at 1 GeV in the barrel (end-cap) region. The time resolution in the TOF barrel region is 68 ps. The end-cap TOF system was upgraded in 2015 using multi-gap resistive plate chamber technology, providing a time resolution of 60 ps 33 .

Simulated samples produced with GEANT4-based 34 Monte Carlo software, which includes the geometric de-
scription 35, 36 of the BESIII detector and the detector response, are used to determine the detection efficiency and to estimate backgrounds. Exclusive simulation samples of $e^{+} e^{-} \rightarrow \Lambda_{c}^{+} \bar{\Lambda}_{c}^{-}$are produced with $\bar{\Lambda}_{c}^{-}$ decaying into ten specific tag modes and $\Lambda_{c}^{+}$decaying into $\Xi^{0} K^{+} \pi^{0}$ and $n K^{+} \pi^{0}$. The simulation includes the beam-energy spread and initial-state radiation (ISR) in the $e^{+} e^{-}$annihilations with the specific tag modes 37 modeled with the generator Kкмс [38, 39]. The signal events are modeled with a phase-space generator. The $e^{+} e^{-} \rightarrow \Lambda_{c}^{+} \bar{\Lambda}_{c}^{-}$line-shape implements the description from Ref. [18. The inclusive simulation sample, which consists of $\Lambda_{c}^{+} \bar{\Lambda}_{c}^{-}$events, $D_{(s)}$ production, ISR return to lower-mass $\psi$ states, and continuum processes $\left(e^{+} e^{-} \rightarrow\right.$ $u \bar{u}, d \bar{d}$ and $s \bar{s}$ ) is used to estimate the potential background. All the known decay modes of charmed hadrons and charmonia are modeled with evtgen 40, 41] using branching fractions either taken from the Particle Data Group 42, when available, or otherwise estimated with Lundcharm [43, 44]. Final state radiation from charged final state particles is incorporated using Рнотоs [45].

## III. METHODOLOGY

The $\bar{\Lambda}_{c}^{-}$baryons are fully reconstructed by their hadronic decays to $\bar{p} K^{+} \pi^{-}, \bar{p} K_{S}^{0}, \bar{p} K^{+} \pi^{-} \pi^{0}, \bar{p} K_{S}^{0} \pi^{0}$, $\bar{p} K_{S}^{0} \pi^{+} \pi^{-}, \quad \bar{\Lambda} \pi^{-}, \quad \bar{\Lambda} \pi^{-} \pi^{-} \pi^{+}, \quad \bar{\Lambda} \pi^{-} \pi^{0}, \quad \bar{\Sigma}^{0} \pi^{-} \quad$ and $\bar{\Sigma}^{-} \pi^{+} \pi^{-}$. These reconstructed decays are referred to as single-tag (ST) $\bar{\Lambda}_{c}^{-}$baryons, where the intermediate particles $K_{S}^{0}, \bar{\Lambda}, \bar{\Sigma}^{0}, \bar{\Sigma}^{-}$, and $\pi^{0}$ are reconstructed via $K_{S}^{0} \rightarrow \pi^{+} \pi^{-}, \bar{\Lambda} \rightarrow \bar{p} \pi^{+}, \bar{\Sigma}^{0} \rightarrow \gamma \bar{\Lambda}, \bar{\Sigma}^{-} \rightarrow \bar{p} \pi^{0}$ and $\pi^{0} \rightarrow \gamma \gamma$, respectively. From the remaining tracks and showers, the three-body decays $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ and $n K^{+} \pi^{0}$ are selected to form $\Lambda_{c}^{+}$candidates, which will be referred to as the recoiling system. Together with the $\bar{\Lambda}_{c}^{-}$candidates, these form a sample of DT events.

The branching fraction is expressed as:

$$
\begin{equation*}
\mathcal{B}=\frac{N_{\mathrm{sig}}}{\mathcal{B}_{\text {inter }} \cdot \Sigma_{i} N_{i}^{\mathrm{ST}} \cdot\left(\epsilon_{i}^{\mathrm{DT}} / \epsilon_{i}^{\mathrm{ST}}\right)}, \tag{1}
\end{equation*}
$$

where $N_{\text {sig }}$ is the signal yield of the DT candidates and $\mathcal{B}_{\text {inter }}$ is the product of branching fractions of intermediate $\Xi^{0}$ and $\pi^{0}$ decays on the signal side from the PDG 42]. $N_{i}^{\mathrm{ST}}$ denotes the yields of the ST candidates observed in data, and $\epsilon_{i}^{\mathrm{ST}}$ and $\epsilon_{i}^{\mathrm{DT}}$ are the ST and DT efficiencies, respectively.

## IV. EVENT SELECTION

The selection criteria in this analysis follow that of Ref. [17. Charged tracks are required to have a polar angle $(\theta)$ within $|\cos \theta|<0.93$, where $\theta$ is defined with respect to the $z$-axis, which is the symmetry axis of the MDC. Tracks, except for those from $K_{S}^{0}$ and $\bar{\Lambda}$ decays, are required to originate from an interaction region defined by $\left|V_{x y}\right|<1 \mathrm{~cm}$ and $\left|V_{z}\right|<10 \mathrm{~cm}$ (referred as a
tight track hereafter), where $\left|V_{x y}\right|$ and $\left|V_{z}\right|$ refer to the distances of closest approach of the reconstructed track to the interaction point (IP) in the $x y$ plane and the $z$ direction, respectively.

Particle identification (PID) for charged tracks combines measurements of the energy deposited in the MDC $(\mathrm{d} E / \mathrm{d} x)$ and the flight time in the TOF to form likelihoods $\mathcal{L}(h)(h=p, K, \pi)$ for each hadron $h$ hypothesis. Tracks are identified as protons when the proton hypothesis has the greatest likelihood $(\mathcal{L}(p)>\mathcal{L}(K)$ and $\mathcal{L}(p)>\mathcal{L}(\pi))$, while charged kaons and pions are identified by comparing the likelihoods for the kaon and pion hypotheses, $\mathcal{L}(K)>\mathcal{L}(\pi)$ and $\mathcal{L}(\pi)>\mathcal{L}(K)$, respectively.

The selection of tracks from $K_{S}^{0}$ and $\bar{\Lambda}$ is different from those of other tracks. Candidates of $K_{S}^{0}$ and $\bar{\Lambda}$ mesons are reconstructed from their decays to $\pi^{+} \pi^{-}$and $\bar{p} \pi^{+}$, respectively, where the charged tracks must satisfy $\left|V_{z}\right|<20 \mathrm{~cm}$ (referred as a loose track hereafter). The PID selection criteria are imposed on the antiproton candidate, while the charged pion is not subject to any PID requirement. A secondary vertex fit is performed for each $K_{S}^{0}$ or $\bar{\Lambda}$ candidate, and the momentum obtained from the fit is used in the subsequent analysis. The $K_{S}^{0}$ or $\bar{\Lambda}$ candidate is retained if the $\chi^{2}$ of the secondary vertex fit is less than 100. Furthermore, the decay vertex is required to be separated from the IP by a distance of at least twice the vertex resolution. For $K_{S}^{0}$ and $\bar{\Lambda}$, the invariant masses of $\pi^{+} \pi^{-}$and $\bar{p} \pi^{+}$pairs are required to be within $(0.487,0.511) \mathrm{GeV} / c^{2}$ and $(1.111,1.121) \mathrm{GeV} / c^{2}$, respectively. The $\pi^{+} \pi^{-}$and $\bar{p} \pi^{-}$invariant mass resolutions determined through simulations, are $2.9 \mathrm{MeV} / c^{2}$ and $1.2 \mathrm{MeV} / c^{2}$, respectively. Similarly, the $\bar{\Sigma}^{0}$ and $\bar{\Sigma}^{-}$ candidates are reconstructed from the $\gamma \bar{\Lambda}$ and $\bar{p} \pi^{0}$ final states with invariant masses within the ranges of (1.179, 1.203) $\mathrm{GeV} / c^{2}$ and $(1.176,1.200) \mathrm{GeV} / c^{2}$, respectively. The mass resolutions for $\bar{\Sigma}^{0}$ and $\bar{\Sigma}^{-}$are found, using simulation, to be $3.6 \mathrm{MeV} / c^{2}$ and $4.3 \mathrm{MeV} / c^{2}$, respectively.

Photon candidates are identified using showers in the EMC. The deposited energy of each shower must be more than 25 MeV in the barrel region $(|\cos \theta| \leq 0.80)$ or more than 50 MeV in the end-cap region $(0.86 \leq|\cos \theta| \leq$ $0.92)$. To suppress electronic noise and showers unrelated to the event, the difference between the EMC time and the event start time is required to be within $[0,700] \mathrm{ns}$.

A $\pi^{0}$ candidate is reconstructed with a photon pair, and their invariant mass is required to be within the range $(0.115,0.150) \mathrm{GeV} / c^{2}$. To improve the resolution, a kinematic fit is performed, where the diphoton invariant mass is constrained to the known $\pi^{0}$ mass [42], and the $\chi^{2}$ of the kinematic fit is required to be less than 200 . The momenta obtained from the kinematic fit are used in the subsequent analysis.

To distinguish the ST $\bar{\Lambda}_{c}^{-}$baryons from combinatorial backgrounds, the distributions of the energy difference $\Delta E$ are used, defined as

$$
\begin{equation*}
\Delta E \equiv E_{\bar{\Lambda}_{c}^{-}}-E_{\mathrm{beam}} \tag{2}
\end{equation*}
$$

where $E_{\text {beam }}$ is the beam energy, and $E_{\bar{\Lambda}_{c}^{-}}$is the total energy of the ST candidate, calculated in the $e^{+} e^{-}$rest frame. The signal events are expected to peak around zero in the $\Delta E$ distribution. If an event has multiple $\bar{\Lambda}_{c}^{-}$ candidates, the one with the smallest $|\Delta E|$ is retained, and the $\Delta E$ requirements are listed in Table 2 .

The beam-constrained mass $M_{\mathrm{BC}}$ of the selected ST candidates is defined as

$$
\begin{equation*}
M_{\mathrm{BC}} \equiv \sqrt{E_{\mathrm{beam}}^{2} / c^{4}-\left|\vec{p}_{\bar{\Lambda}_{c}^{-}}\right|^{2} / c^{2}} \tag{3}
\end{equation*}
$$

where $\vec{p}_{\bar{\Lambda}_{c}^{-}}$is the total momentum of the ST candidate and $M_{\mathrm{BC}}$ peaks at the $\bar{\Lambda}_{c}^{-}$mass. For each tag mode, the ST yield is determined by fitting the $M_{\mathrm{BC}}$ distribution. In the fit, the $\bar{\Lambda}_{c}^{-}$signal is described by the MC simulated shape convolved with a Gaussian function to compensate for the resolution difference between data and MC. The parameters of the Gaussian function are free in the fit and different for each energy and tag mode. The combinatorial background is described by an ARGUS function 46, with the end-point parameter fixed to the nominal beam energy. The fits to the $M_{\mathrm{BC}}$ distributions of the various tag modes for the 4.600-4.700 datasets are the same as Ref. 37. The fits to the $M_{\mathrm{BC}}$ distributions for the 4.740, 4.750, 4.780, and 4.840 datasets are shown in Fig. 2 . Candidates in the $M_{\mathrm{BC}}$ signal region, $(2.275,2.310) \mathrm{GeV} / c^{2}$, are kept for further analysis. The ST yields in data and the ST efficiencies for individual tags are listed in Table 2. The total ST yield, obtained by summing the ST yield of all tag modes and all energies, is found to be $N_{\mathrm{ST}}^{\mathrm{tot}}=130439 \pm 425$, where the uncertainty is statistical.

After the ST selection, we want to determine the number of $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ and $n K^{+} \pi^{0}$ candidates on the opposite side of the ST $\bar{\Lambda}_{c}^{-}$. The $K^{+}$and $\pi^{0}$ are reconstructed, as described above, from the remaining showers and tracks. Using total four-momentum conservation, the $\Xi^{0}$ signal is obtained from the distribution of recoil mass,

$$
\begin{align*}
M_{\text {recoil }}^{2}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)= & \left(E_{\text {beam }}-E_{K^{+}}-E_{\pi^{0}}\right)^{2} / c^{4} \\
& -\left|\rho \cdot \vec{p}_{0}-\vec{p}_{K^{+}}-\vec{p}_{\pi^{0}}\right|^{2} / c^{2} \tag{4}
\end{align*}
$$

where $E_{K^{+}}, E_{\pi^{0}}, \vec{p}_{K^{+}}$and $\vec{p}_{\pi^{0}}$ are the energies and momenta of $K^{+}$and $\pi^{0}$ candidates, respectively, $\rho=$ $\sqrt{E_{\text {beam }}^{2} / c^{2}-m_{\Lambda_{c}^{+}}^{2} c^{2}}$ is the magnitude of the $\Lambda_{c}^{+}$momentum, constrained by the beam energy, and $\vec{p}_{0}=$ $-\vec{p}_{\bar{\Lambda}_{c}^{-}} /\left|\vec{p}_{\bar{\Lambda}_{c}^{-}}\right|$is its direction. Similarly, the yield of the two-body decay $\Lambda_{c}^{+} \rightarrow \Xi(1530)^{0} K^{+}$is obtained using the recoil mass.

$$
\begin{equation*}
M_{\text {recoil }}^{2}\left(\Lambda_{c}^{\mathrm{ST}} K^{+}\right)=\left(E_{\text {beam }}-E_{K^{+}}\right)^{2} / c^{4}-\left|\rho \cdot \vec{p}_{0}-\vec{p}_{K^{+}}\right|^{2} / c^{2} \tag{5}
\end{equation*}
$$

The $\Xi^{0}$ predominant decay mode is $\Xi^{0} \rightarrow \Lambda \pi^{0}$ 42]. The $\Lambda$ baryon has two main decay modes, which are studied in this analysis: the neutral decay
mode $\Lambda \rightarrow n \pi^{0}$, which will be referred to as Cat1 , and the charged decay mode $\Lambda \rightarrow p \pi^{-}$, which will be referred to as Cat-2. The Cat-1 and Cat2 decays are shown schematically in Fig. 3. Four variables $\quad M_{\text {recoil }}^{\mathrm{Cat}-1}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right), \quad M_{\text {recoil }}^{\mathrm{Cat-2}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$, $M_{\text {recoil }}^{\mathrm{Cat}-1}\left(\Lambda_{c}^{\mathrm{ST}} K^{+}\right)$and $M_{\text {recoil }}^{\mathrm{Cat}-2}\left(\Lambda_{c}^{\mathrm{ST}} K^{+}\right)$are defined by Eqs. 4 and 5 . For Cat-1, a single tight track is reconstructed and identified as a $K^{+}$meson. In Cat-2, three charged tracks are reconstructed as a $K^{+}, p$, and $\pi^{-}$. The $K^{+}$is a tight track, while the other two are loose tracks from the $\Lambda \rightarrow p \pi^{-}$decay. The $p$ and $\pi^{-}$are constrained to originate from a common vertex to form the $\Lambda$ candidates by a vertex fit [47]. The invariant mass of the $\Lambda$ candidate is required to fall inside the range $(1.111,1.121) \mathrm{GeV} / c^{2}$.

The $\pi^{0}$ candidate is reconstructed via the process $\pi^{0} \rightarrow$ $\gamma \gamma$. If there are multiple $\pi^{0}$ candidates, the one with the minimum kinematic-fit $\chi^{2}$ is assumed to originate from the $\Lambda_{c}^{+}$baryon.

To suppress sources of background due to neutral hyperon decays from the decays $\Lambda_{c}^{+} \rightarrow \Lambda K^{+}, \Sigma^{0} K^{+}$ and $\Xi^{0} K^{+}$, the events falling inside the corresponding intervals of these three decays of the variable $M_{\text {recoil }}^{\mathrm{Cat-1}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+}\right)$are rejected. This requirement suppresses $95 \%$ of these backgrounds. Furthermore, electron mis-PID backgrounds are suppressed using PID and EMC information. To suppress contaminations from long-lived particles in the final state, any event with additional tracks, either loose or tight, is rejected. The DT efficiencies of each signal decay for Cat-1 and Cat-2 are summarized in Tables 3.7.

## V. BACKGROUND ANALYSIS

Potential sources of background are classified into two categories: those from $e^{+} e^{-} \rightarrow \Lambda_{c}^{+} \bar{\Lambda}_{c}^{-}$(denoted as $\Lambda_{c}^{+} \bar{\Lambda}_{c}^{-}$ background) and those directly originating from continuum hadron production in $e^{+} e^{-}$annihilation (denoted as $q \bar{q}$ background).

The $\Lambda_{c}^{+} \bar{\Lambda}_{c}^{-}$background is investigated for both categories with the $\Lambda_{c}^{+} \bar{\Lambda}_{c}^{-}$inclusive MC samples, after removing the signal processes. The $\Lambda_{c}^{+} \bar{\Lambda}_{c}^{-}$background distributions are the blue-shaded histograms in Figs. 4 and 5 , and they have been normalized to the same luminosity as data.

For the CAT-1 $q \bar{q}$ background, the data events in the $M_{\mathrm{BC}}$ sideband region, defined as $M_{\mathrm{BC}} \in(2.200,2.265)$ $\mathrm{GeV} / c^{2}$, are used. Since $\Lambda_{c}^{+} \bar{\Lambda}_{c}^{-}$background is present in the sideband region, it is estimated using inclusive simulation samples and subtracted from the total sideband yield to determine the $q \bar{q}$ background in the sideband. The $q \bar{q}$ background in the signal region is extrapolated from the yield in the sideband using information from the simulation. In Cat-2, the simulated $q \bar{q}$ samples are used.

Due to fake photons in the EMC, there exists a contamination from mismatched $\pi^{0}$ candidates (denoted as


Fig. 2. The $M_{\mathrm{BC}}$ distributions of ST channels of $\bar{\Lambda}_{c}^{-}$at (a) 4.740 GeV , (b) 4.750 GeV , (c) 4.780 GeV and (d) 4.840 GeV . The signal shape of the $\bar{\Lambda}_{c}^{-}$is described by the simulated shape convolved with a Gaussian resolution function, and the background is modeled with an ARGUS function. The points with error bars represent data. The (red) solid curves indicate the fit results and the (blue) dashed curves describe the background shapes. The vertical dashed lines show the $M_{B C}$ selection requirements.

Table 2. The $\Delta E$ requirements, the ST yields, and the ST detection efficiencies of each tag mode for the data samples between 4.740 and 4.840 GeV . The uncertainties of the ST yields are statistical only.

|  | 4.740 |  |  | 4.750 |  | 4.780 |  |  | 4.840 |  |
| :--- | :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| Tag mode | $\Delta E(\mathrm{MeV})$ | $N_{i}^{\mathrm{ST}}$ |  | $\epsilon_{i}^{\mathrm{ST}}(\%)$ | $N_{i}^{\mathrm{ST}}$ |  | $\epsilon_{i}^{\mathrm{ST}}(\%)$ | $N_{i}^{\mathrm{ST}}$ | $\epsilon_{i}^{\mathrm{ST}}(\%)$ |  |
| $\bar{p} K^{+} \pi^{-}$ | $(-34,20)$ | $1201 \pm 40$ | 48.4 | $2782 \pm 60$ | 48.1 | $3689 \pm 67$ | 47.1 | $2676 \pm 61$ | 43.8 |  |
| $\bar{p} K_{S}$ | $(-20,20)$ | $256 \pm 17$ | 48.5 | $525 \pm 24$ | 46.9 | $629 \pm 26$ | 44.2 | $475 \pm 23$ | 42.4 |  |
| $\bar{\Lambda} \pi^{-}$ | $(-20,20)$ | $144 \pm 12$ | 36.6 | $336 \pm 19$ | 37.0 | $383 \pm 21$ | 35.5 | $265 \pm 17$ | 32.8 |  |
| $\bar{p} K^{+} \pi^{-} \pi^{0}$ | $(-30,20)$ | $246 \pm 25$ | 17.8 | $607 \pm 40$ | 18.3 | $845 \pm 37$ | 17.3 | $583 \pm 39$ | 15.7 |  |
| $\bar{p} K_{S} \pi^{0}$ | $(-30,20)$ | $76 \pm 12$ | 18.7 | $212 \pm 20$ | 18.8 | $269 \pm 22$ | 18.3 | $185 \pm 20$ | 10.9 |  |
| $\bar{\Lambda} \pi^{-} \pi^{0}$ | $(-30,20)$ | $239 \pm 18$ | 18.1 | $529 \pm 30$ | 17.8 | $723 \pm 33$ | 18.0 | $513 \pm 28$ | 16.9 |  |
| $\bar{p} K_{S} \pi^{+} \pi^{-}$ | $(-20,20)$ | $89 \pm 13$ | 20.1 | $192 \pm 20$ | 19.3 | $292 \pm 24$ | 19.7 | $202 \pm 20$ | 17.6 |  |
| $\bar{\Lambda} \pi^{-} \pi^{+} \pi^{-}$ | $(-20,20)$ | $152 \pm 14$ | 13.6 | $326 \pm 21$ | 14.7 | $453 \pm 25$ | 17.5 | $348 \pm 22$ | 13.2 |  |
| $\bar{\Sigma}^{0} \pi^{-}$ | $(-20,20)$ | $58 \pm 8$ | 22.5 | $152 \pm 13$ | 22.0 | $196 \pm 15$ | 20.9 | $145 \pm 13$ | 20.5 |  |
| $\bar{\Sigma}^{-} \pi^{+} \pi^{-}$ | $(-30,20)$ | $136 \pm 16$ | 19.9 | $362 \pm 32$ | 19.6 | $500 \pm 32$ | 19.9 | $373 \pm 26$ | 17.5 |  |



Fig. 3. The schematic diagrams of the two analysis strategies, which are denoted (a) Cat-1 and (b) Cat-2 in the text.
$\pi^{0}$ mismatch). It has a wide shape and will not contribute to the narrow resonances in the distributions of $M_{\text {recoil }}^{\mathrm{Cat}-1}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ and $M_{\text {recoil }}^{\mathrm{Cat}-2}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$. The $\pi^{0}$ mismatch background is estimated using simulation samples. Events containing showers where the angular separation between the true and reconstructed $\pi^{0}$ directions is greater than $20^{\circ}$ are considered $\pi^{0}$ mismatch background, and the background is normalized according to the branching fractions of $\Lambda_{c}^{+} \rightarrow \Xi(1530)^{0} K^{+}$and $\Lambda_{c}^{+} \rightarrow$ $\Xi^{0} K^{+} \pi^{0}$ in the distributions of $M_{\text {recoil }}^{\text {Cat-1 }}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ and $M_{\text {recoil }}^{\mathrm{Cat-2}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$.

## VI. BRANCHING FRACTION MEASUREMENT

For the two-body decay $\Lambda_{c}^{+} \rightarrow \Xi(1530)^{0} K^{+}$, a simultaneous fit is performed by combining the Cat1 and Cat-2 distributions of $M_{\text {recoil }}^{\mathrm{Cat}-1}\left(\Lambda_{c}^{\mathrm{ST}} K^{+}\right)$and $M_{\text {recoil }}^{\mathrm{Cat}-2}\left(\Lambda_{c}^{\mathrm{ST}} K^{+}\right)$. The signal shapes are modeled with
the simulation shapes convolved with a Gaussian function representing the resolution difference between data and simulation samples. The background shapes are described by third-order polynomial functions, and the background yields are floating. The fitted curves with distributions of $M_{\text {recoil }}^{\mathrm{Cat}-1}\left(\Lambda_{c}^{\mathrm{ST}} K^{+}\right)$and $M_{\text {recoil }}^{\mathrm{Cat}-2}\left(\Lambda_{c}^{\mathrm{ST}} K^{+}\right)$ are shown in Fig. 4 . The signal yields are $30 \pm 6$ and $20 \pm 5$ events for Cat-1 and Cat-2, respectively. The DT efficiencies in Cat-1 and Cat-2 are summarized in Table 3, From Eq. 1. the branching fraction is determined to be $(5.99 \pm 1.04) \times 10^{-3}$, where the uncertainty is statistical. It is consistent with the previous result 48. The significance, at $6.9 \sigma$, is determined by evaluating the difference in likelihood values between fits that include and exclude the signal component, while considering the change in the number of degrees of freedom.

For the three-body decay $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$, the simultaneous fit shares the same branching fraction and takes into account the different detection efficiencies

Table 3. The DT detection efficiency $(\%)$ of $\Lambda_{c}^{+} \rightarrow \Xi(1530)^{0} K^{+}$in Cat-1/Cat-2 for each tag mode and each energy point.

|  | 4.600 | 4.612 | 4.620 | 4.640 | 4.660 | 4.680 | 4.700 | 4.740 | 4.750 | 4.780 | 4.840 |
| :--- | ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $p K^{-} \pi^{+}$ | $20.3 / 8.3$ | $19.3 / 7.4$ | $19.0 / 6.7$ | $18.6 / 6.7$ | $18.1 / 6.5$ | $17.8 / 6.5$ | $17.4 / 6.5$ | $15.7 / 6.5$ | $15.4 / 6.4$ | $14.9 / 6.5$ | $13.8 / 6.1$ |
| $p K_{S}^{0}$ | $22.1 / 9.0$ | $20.4 / 7.6$ | $18.7 / 8.0$ | $18.9 / 8.1$ | $18.4 / 6.7$ | $17.4 / 8.2$ | $17.5 / 7.5$ | $17.3 / 7.1$ | $16.8 / 7.1$ | $17.0 / 6.6$ | $14.0 / 6.6$ |
| $\Lambda \pi^{+}$ | $16.9 / 7.9$ | $15.6 / 6.9$ | $14.5 / 6.2$ | $14.5 / 6.0$ | $13.3 / 6.1$ | $13.0 / 5.6$ | $13.6 / 4.9$ | $13.9 / 5.3$ | $13.4 / 5.4$ | $12.1 / 5.1$ | $12.1 / 4.6$ |
| $p K^{-} \pi^{+} \pi^{0}$ | $5.3 / 1.6$ | $4.8 / 1.4$ | $4.6 / 1.5$ | $4.5 / 1.3$ | $4.4 / 1.3$ | $4.3 / 1.3$ | $4.1 / 1.3$ | $3.6 / 1.4$ | $3.5 / 1.4$ | $3.5 / 1.5$ | $3.3 / 1.4$ |
| $p K_{S}^{0} \pi^{0}$ | $8.0 / 2.9$ | $7.1 / 2.3$ | $7.1 / 2.0$ | $6.8 / 2.1$ | $6.5 / 2.2$ | $6.6 / 2.5$ | $6.0 / 2.1$ | $5.6 / 2.1$ | $5.3 / 2.2$ | $5.1 / 2.1$ | $4.8 / 2.0$ |
| $\Lambda \pi^{+} \pi^{0}$ | $6.7 / 2.0$ | $6.0 / 1.7$ | $5.8 / 1.8$ | $5.7 / 1.8$ | $5.4 / 1.6$ | $5.2 / 1.7$ | $5.1 / 1.7$ | $4.5 / 1.8$ | $4.7 / 1.7$ | $4.4 / 1.7$ | $4.1 / 1.8$ |
| $p K_{S}^{0} \pi^{+} \pi^{-}$ | $9.0 / 2.9$ | $8.7 / 2.4$ | $8.1 / 2.0$ | $7.9 / 2.2$ | $7.9 / 2.2$ | $7.4 / 2.2$ | $7.4 / 2.6$ | $6.7 / 2.5$ | $7.0 / 2.7$ | $6.7 / 2.8$ | $6.1 / 2.5$ |
| $\Lambda \pi^{+} \pi^{+} \pi^{-}$ | $6.2 / 1.7$ | $5.7 / 1.3$ | $5.4 / 1.6$ | $5.3 / 1.3$ | $5.1 / 1.4$ | $5.3 / 1.4$ | $5.2 / 1.4$ | $4.7 / 1.6$ | $4.5 / 1.7$ | $4.2 / 1.6$ | $4.4 / 1.8$ |
| $\Sigma^{0} \pi^{+}$ | $8.8 / 3.7$ | $7.8 / 3.0$ | $7.8 / 2.4$ | $7.3 / 2.8$ | $6.4 / 2.4$ | $6.6 / 3.4$ | $6.9 / 2.6$ | $5.8 / 2.5$ | $6.0 / 2.3$ | $5.4 / 2.4$ | $5.0 / 2.3$ |
| $\Sigma^{+} \pi^{+} \pi^{-}$ | $3.2 / 2.5$ | $3.2 / 2.3$ | $3.0 / 2.3$ | $3.0 / 2.4$ | $2.6 / 2.0$ | $2.8 / 1.9$ | $2.7 / 2.2$ | $2.3 / 1.0$ | $2.4 / 1.0$ | $2.2 / 1.1$ | $2.0 / 0.8$ |

Table 4. The DT detection efficiency(\%) of $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ in Cat-1/Cat-2 for each tag mode and each energy point.

|  | 4.600 | 4.612 | 4.620 | 4.640 | 4.660 | 4.680 | 4.700 | 4.740 | 4.750 | 4.780 | 4.840 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $p K^{-} \pi^{+}$ | $7.7 / 3.3$ | $7.4 / 2.8$ | $7.3 / 2.8$ | $7.2 / 2.7$ | $7.0 / 2.6$ | $7.1 / 2.7$ | $6.8 / 2.8$ | $6.3 / 2.6$ | $6.3 / 2.8$ | $5.9 / 2.8$ | $5.7 / 2.4$ |
| $p K_{S}^{0}$ | $8.6 / 3.7$ | $8.5 / 3.2$ | $7.6 / 3.1$ | $7.7 / 2.8$ | $7.7 / 2.9$ | $7.7 / 3.2$ | $7.3 / 2.5$ | $6.5 / 3.3$ | $6.7 / 2.9$ | $6.6 / 3.2$ | $6.3 / 2.4$ |
| $\Lambda \pi^{+}$ | $6.3 / 2.4$ | $6.0 / 2.0$ | $6.1 / 2.2$ | $6.1 / 2.1$ | $5.1 / 2.1$ | $5.5 / 1.9$ | $5.9 / 2.4$ | $5.3 / 2.2$ | $5.5 / 2.3$ | $5.2 / 2.5$ | $4.7 / 2.1$ |
| $p K^{-} \pi^{+} \pi^{0}$ | $1.9 / 0.8$ | $2.0 / 0.7$ | $2.0 / 0.7$ | $1.9 / 0.6$ | $2.0 / 0.6$ | $1.8 / 0.7$ | $1.8 / 0.6$ | $1.5 / 0.6$ | $1.4 / 0.6$ | $1.5 / 0.6$ | $1.3 / 0.6$ |
| $p K_{S}^{0} \pi^{0}$ | $2.9 / 1.1$ | $2.5 / 1.1$ | $2.5 / 1.0$ | $2.3 / 1.0$ | $2.5 / 1.1$ | $2.6 / 0.9$ | $2.4 / 1.0$ | $2.1 / 0.7$ | $2.1 / 0.8$ | $2.0 / 0.9$ | $2.2 / 0.8$ |
| $\Lambda \pi^{+} \pi^{0}$ | $2.5 / 0.9$ | $2.2 / 0.8$ | $2.1 / 0.8$ | $2.1 / 0.8$ | $2.1 / 0.7$ | $2.0 / 0.8$ | $2.0 / 0.8$ | $1.8 / 0.7$ | $1.7 / 0.7$ | $1.9 / 0.8$ | $1.8 / 0.7$ |
| $p K_{S}^{0} \pi^{+} \pi^{-}$ | $3.2 / 1.4$ | $2.7 / 1.0$ | $3.0 / 1.0$ | $3.1 / 1.0$ | $2.6 / 1.1$ | $2.7 / 0.9$ | $3.0 / 1.1$ | $2.4 / 0.9$ | $2.8 / 1.0$ | $2.7 / 1.0$ | $2.5 / 1.1$ |
| $\Lambda \pi^{+} \pi^{+} \pi^{-}$ | $2.2 / 0.8$ | $2.0 / 0.6$ | $1.8 / 0.6$. | $2.0 / 0.6$ | $1.9 / 0.6$ | $1.9 / 0.6$ | $1.9 / 0.7$ | $1.8 / 0.7$ | $1.6 / 0.6$ | $1.6 / 0.6$ | $1.8 / 0.6$ |
| $\Sigma^{0} \pi^{+}$ | $3.2 / 1.3$ | $2.8 / 1.3$ | $2.9 / 1.1$ | $2.5 / 1.3$ | $2.8 / 1.3$ | $2.9 / 1.1$ | $2.5 / 1.0$ | $2.7 / 1.1$ | $2.4 / 1.2$ | $2.2 / 1.0$ | $2.2 / 1.0$ |
| $\Sigma^{+} \pi^{+} \pi^{-}$ | $1.3 / 0.7$ | $1.2 / 0.4$ | $1.1 / 0.4$. | $1.1 / 0.5$ | $1.1 / 0.4$ | $1.0 / 0.5$ | $1.0 / 0.4$ | $0.8 / 0.5$ | $0.8 / 0.4$ | $0.8 / 0.4$ | $0.9 / 0.3$ |

Table 5. The DT detection efficiency (\%) of $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}$ in Cat-1 for each tag mode and each energy point.

|  | 4.600 | 4.612 | 4.620 | 4.640 | 4.660 | 4.680 | 4.700 | 4.740 | 4.750 | 4.780 | 4.840 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $p K^{-} \pi^{+}$ | 13.4 | 12.9 | 12.2 | 12.0 | 11.7 | 11.4 | 11.2 | 10.4 | 10.2 | 9.9 | 9.2 |
| $p K_{S}^{0}$ | 14.3 | 13.8 | 13.3 | 12.9 | 12.1 | 12.5 | 11.5 | 11.2 | 11.6 | 11.1 | 9.9 |
| $\Lambda \pi^{+}$ | 11.3 | 10.6 | 9.7 | 10.0 | 9.3 | 9.4 | 9.5 | 9.3 | 8.2 | 7.9 | 8.1 |
| $p K^{-} \pi^{+} \pi^{0}$ | 3.7 | 3.6 | 3.5 | 3.3 | 3.3 | 3.2 | 3.2 | 2.7 | 2.7 | 2.8 | 2.5 |
| $p K_{S}^{0} \pi^{0}$ | 4.8 | 4.5 | 4.3 | 4.5 | 4.2 | 4.0 | 3.8 | 3.1 | 3.4 | 3.4 | 3.0 |
| $\Lambda \pi^{+} \pi^{0}$ | 4.2 | 4.0 | 3.6 | 3.7 | 3.5 | 3.4 | 3.4 | 3.2 | 3.1 | 3.0 | 2.7 |
| $p K_{S}^{0} \pi^{+} \pi^{-}$ | 5.8 | 5.2 | 4.8 | 4.9 | 4.6 | 4.5 | 4.8 | 4.3 | 3.8 | 4.3 | 4.2 |
| $\Lambda \pi^{+} \pi^{+} \pi^{-}$ | 3.9 | 3.3 | 3.5 | 3.2 | 3.4 | 3.4 | 2.9 | 2.7 | 2.8 | 2.7 | 2.8 |
| $\Sigma^{0} \pi^{+}$ | 6.7 | 5.8 | 6.2 | 5.5 | 5.2 | 5.5 | 6.0 | 4.3 | 5.0 | 4.0 | 4.1 |
| $\Sigma^{+} \pi^{+} \pi^{-}$ | 2.4 | 2.3 | 2.1 | 2.3 | 2.2 | 2.2 | 2.0 | 1.8 | 1.9 | 1.9 | 1.6 |

Table 6. The DT detection efficiency(\%) of $\Lambda_{c}^{+} \rightarrow \Sigma^{0} K^{+} \pi^{0}$ in Cat-1/Cat-2 for each tag mode and each energy point.

|  | 4.600 | 4.612 | 4.620 | 4.640 | 4.660 | 4.680 | 4.700 | 4.740 | 4.750 | 4.780 | 4.840 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $p K^{-} \pi^{+}$ | $10.2 / 5.7$ | $9.7 / 5.3$ | $9.0 / 4.9$ | $9.3 / 4.9$ | $9.2 / 4.9$ | $8.7 / 4.8$ | $8.6 / 4.7$ | $8.3 / 4.5$ | $8.1 / 4.6$ | $7.7 / 4.5$ | $7.5 / 4.2$ |
| $p K_{S}^{0}$ | $11.4 / 6.1$ | $10.0 / 5.5$ | $9.7 / 5.3$ | $9.9 / 5.6$ | $10.0 / 5.5$ | $9.0 / 5.0$ | $9.4 / 4.6$ | $8.8 / 5.5$ | $8.6 / 5.4$ | $8.5 / 4.9$ | $8.2 / 4.8$ |
| $\Lambda \pi^{+}$ | $8.5 / 4.8$ | $8.5 / 3.6$ | $7.3 / 3.9$ | $7.4 / 4.3$ | $7.7 / 3.9$ | $7.0 / 4.0$ | $6.8 / 3.3$ | $6.9 / 3.9$ | $6.9 / 4.2$ | $6.2 / 3.7$ | $6.0 / 3.5$ |
| $p K^{-} \pi^{+} \pi^{0}$ | $2.7 / 1.2$ | $2.4 / 1.1$ | $2.5 / 1.1$ | $2.4 / 1.1$ | $2.3 / 1.1$ | $2.2 / 0.9$ | $2.4 / 1.0$ | $2.0 / 0.9$ | $2.0 / 1.0$ | $1.9 / 1.0$ | $1.9 / 1.0$ |
| $p K_{S}^{0} \pi^{0}$ | $4.1 / 1.7$ | $3.3 / 2.0$ | $3.4 / 1.7$ | $3.2 / 1.8$ | $3.0 / 1.7$ | $3.4 / 1.6$ | $3.1 / 1.8$ | $3.3 / 1.5$ | $2.7 / 1.4$ | $2.7 / 1.7$ | $2.4 / 1.3$ |
| $\Lambda \pi^{+} \pi^{0}$ | $3.1 / 1.7$ | $2.9 / 1.3$ | $2.7 / 1.4$ | $2.8 / 1.4$ | $2.8 / 1.2$ | $2.8 / 1.3$ | $2.5 / 1.2$ | $2.3 / 1.3$ | $2.3 / 1.3$ | $2.4 / 1.2$ | $2.1 / 1.2$ |
| $p K_{S}^{0} \pi^{+} \pi^{-}$ | $4.5 / 2.1$ | $4.1 / 1.8$ | $3.6 / 1.9$ | $3.8 / 1.9$ | $3.8 / 1.5$ | $3.4 / 1.7$ | $3.8 / 1.7$ | $3.7 / 1.6$ | $3.0 / 1.5$ | $3.5 / 1.6$ | $3.4 / 1.8$ |
| $\Lambda \pi^{+} \pi^{+} \pi^{-}$ | $3.1 / 1.4$ | $2.6 / 1.2$ | $2.5 / 1.1$ | $2.7 / 1.2$ | $2.7 / 1.3$ | $2.5 / 1.1$ | $2.5 / 1.2$ | $2.2 / 1.1$ | $2.2 / 1.2$ | $2.2 / 1.2$ | $2.2 / 1.2$ |
| $\Sigma^{0} \pi^{+}$ | $4.4 / 2.1$ | $4.6 / 2.1$ | $3.7 / 2.2$ | $3.6 / 1.9$ | $3.9 / 1.6$ | $3.8 / 1.8$ | $3.6 / 1.9$ | $3.4 / 2.0$ | $3.5 / 1.7$ | $3.2 / 1.7$ | $3.1 / 1.7$ |
| $\Sigma^{+} \pi^{+} \pi^{-}$ | $1.8 / 1.0$ | $1.6 / 0.8$ | $1.5 / 0.8$ | $1.5 / 0.8$ | $1.5 / 0.8$ | $1.4 / 0.9$ | $1.6 / 0.7$ | $1.2 / 0.7$ | $1.2 / 0.7$ | $1.3 / 0.8$ | $1.2 / 0.8$ |

Table 7. The DT detection efficiency (\%) of $\Lambda_{c}^{+} \rightarrow \Lambda K^{+} \pi^{0}$ in Cat-1/Cat-2 for each tag mode and each energy point.

|  | 4.600 | 4.612 | 4.620 | 4.640 | 4.660 | 4.680 | 4.700 | 4.740 | 4.750 | 4.780 | 4.840 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| $p K^{-} \pi^{+}$ | $11.0 / 6.4$ | $10.5 / 6.0$ | $10.0 / 5.6$ | $10.0 / 5.4$ | $10.1 / 5.4$ | $9.9 / 5.5$ | $9.5 / 5.4$ | $8.7 / 5.0$ | $8.6 / 5.1$ | $8.2 / 5.0$ | $7.9 / 4.6$ |
| $p K_{S}^{0}$ | $11.9 / 7.2$ | $10.9 / 6.7$ | $10.9 / 6.2$ | $11.1 / 6.1$ | $10.5 / 6.0$ | $9.9 / 5.6$ | $9.6 / 5.6$ | $9.6 / 5.8$ | $9.4 / 5.9$ | $9.3 / 5.9$ | $8.5 / 5.3$ |
| $\Lambda \pi^{+}$ | $9.8 / 4.9$ | $9.0 / 4.8$ | $7.9 / 4.5$ | $8.6 / 5.0$ | $8.0 / 4.5$ | $7.1 / 4.6$ | $7.8 / 4.3$ | $7.6 / 4.3$ | $7.3 / 4.8$ | $8.2 / 4.3$ | $7.4 / 3.7$ |
| $p K^{-} \pi^{+} \pi^{0}$ | $3.0 / 1.4$ | $2.9 / 1.3$ | $2.8 / 1.3$ | $2.8 / 1.2$ | $2.6 / 1.2$ | $2.6 / 1.2$ | $2.7 / 1.1$ | $2.3 / 1.2$ | $2.2 / 1.2$ | $2.2 / 1.1$ | $2.1 / 1.1$ |
| $p K_{S}^{0} \pi^{0}$ | $4.6 / 2.3$ | $3.6 / 1.9$ | $3.9 / 1.7$ | $3.5 / 1.8$ | $3.2 / 1.8$ | $3.4 / 1.9$ | $3.5 / 1.5$ | $2.7 / 1.7$ | $3.2 / 1.6$ | $2.9 / 1.6$ | $2.5 / 1.6$ |
| $\Lambda \pi^{+} \pi^{0}$ | $3.5 / 1.9$ | $3.2 / 1.7$ | $3.1 / 1.6$ | $3.1 / 1.6$ | $3.1 / 1.5$ | $3.0 / 1.5$ | $2.7 / 1.5$ | $2.6 / 1.4$ | $2.4 / 1.3$ | $2.4 / 1.3$ | $2.3 / 1.3$ |
| $p K_{S}^{0} \pi^{+} \pi^{-}$ | $4.7 / 2.4$ | $4.1 / 2.1$ | $4.0 / 1.9$ | $4.4 / 1.9$ | $4.2 / 1.8$ | $3.8 / 2.0$ | $4.1 / 1.8$ | $3.8 / 2.0$ | $3.4 / 2.0$ | $4.1 / 2.1$ | $3.5 / 1.9$ |
| $\Lambda \pi^{+} \pi^{+} \pi^{-}$ | $3.0 / 1.7$ | $2.7 / 1.3$ | $2.7 / 1.4$ | $2.7 / 1.4$ | $2.7 / 1.3$ | $2.8 / 1.4$ | $2.9 / 1.4$ | $2.4 / 1.4$ | $2.8 / 1.3$ | $2.5 / 1.3$ | $2.3 / 1.4$ |
| $\Sigma^{0} \pi^{+}$ | $5.1 / 2.8$ | $4.5 / 2.4$ | $4.4 / 2.7$ | $4.6 / 2.4$ | $4.2 / 2.4$ | $4.4 / 2.1$ | $4.0 / 2.2$ | $3.8 / 2.6$ | $3.4 / 2.5$ | $3.3 / 2.2$ | $3.0 / 2.1$ |
| $\Sigma^{+} \pi^{+} \pi^{-}$ | $2.1 / 1.4$ | $1.9 / 1.1$ | $1.8 / 1.1$ | $1.6 / 1.0$ | $1.8 / 1.1$ | $1.6 / 1.0$ | $1.5 / 0.9$ | $1.6 / 0.8$ | $1.5 / 0.9$ | $1.3 / 0.8$ | $1.3 / 0.8$ |

of the individual processes. The fit projections of $M_{\text {recoil }}^{\mathrm{Cat}-1}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ and $M_{\text {recoil }}^{\mathrm{Cat}-2}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ are shown in Fig. 5 and the total signal yields of $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ are $57 \pm 9$ and $40 \pm 7$ events for Cat- 1 and Cat-2, respectively.

The DT efficiencies of Cat-1 and Cat-2 for $\Lambda_{c}^{+} \rightarrow$ $\Xi^{0} K^{+} \pi^{0}$ are summarized in Table 4. The simulation samples use a flat phase space model, but intermediate resonances could affect the momentum and angular distributions of the final state particles, which would affect DT efficiencies. Therefore, the simulation samples are reweighted to match data. The two variables, $M\left(K^{+} \pi^{0}\right)$ and $M_{\text {recoil }}\left(\Lambda_{c}^{\mathrm{ST}} \pi^{0}\right)$, are selected for the reweighting procedure using a $6 \times 6$ binning scheme with uniformly spaced bins. The overall efficiency is $3.44 \%$ before the procedure and $3.61 \%$ after.

Using the results of fits to $M_{\text {recoil }}^{\mathrm{Cat}-1}\left(\Lambda_{c}^{\mathrm{ST}} K^{+}\right)$and $M_{\text {recoil }}^{\mathrm{Cat-2}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+}\right)$and correcting for the differences in efficiency, the contributions to the three-body decays $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ are calculated. After subtracting them, the yields of the three-body decay $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ are $48 \pm 9$ and $31 \pm 7$ for Cat-1 and Cat-2, respectively. Using Eq. 1 and the corrected efficiency, the branching fraction is determined to be $(7.79 \pm 1.46) \times 10^{-3}$, where the uncertainty is statistical, and the statistical significance is $8.6 \sigma$.

For the three-body decays $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}, \Lambda_{c}^{+} \rightarrow$ $\Sigma^{0} K^{+} \pi^{0}$ and $\Lambda K^{+} \pi^{0}$, simultaneous fits are made to the $M_{\text {recoil }}^{\mathrm{Cat}-1}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ and $M_{\text {recoil }}^{\mathrm{Cat}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ distributions as shown in Figs. 6, 7 and 8. For the three-body decay $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}$, the signal yield is $10 \pm 6$ events and DT efficiencies in Cat-1 are summarized in Table 5. The upper limit on the branching fraction of this decay at the $90 \%$ confidence level is $\mathcal{B}\left(\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}\right)<7.1 \times 10^{-4}$. For the three-body decays $\Lambda_{c}^{+} \rightarrow \Sigma^{0} K^{+} \pi^{0}$ and $\Lambda K^{+} \pi^{0}$, the signal yields of $\Lambda_{c}^{+} \rightarrow \Sigma^{0} K^{+} \pi^{0}$ are $7 \pm 5$ and $6 \pm 4$ events for Cat-1 and Cat-2, respectively. The signal yields of $\Lambda_{c}^{+} \rightarrow \Lambda K^{+} \pi^{0}$ are $10 \pm 4$ and $10 \pm 4$ events for Cat-1 and Cat-2, respectively. The DT efficiencies in are summarized in Tables 6 and 7 and the upper limits are $\mathcal{B}\left(\Lambda_{c}^{+} \rightarrow \Sigma^{0} K^{+} \pi^{\sigma}\right)<1.8 \times 10^{-3}$ and $\mathcal{B}\left(\Lambda_{c}^{+} \rightarrow \Lambda K^{+} \pi^{0}\right)<2.0 \times 10^{-3}$, respectively. The black solid curves in Figs. 6(b), 7(c) and 8(c) show the resulting
likelihood distributions for these three decays.

## VII. SYSTEMATIC UNCERTAINTIES

The systematic uncertainties for the branching fraction measurements include those associated with the ST yields $\left(N_{i}^{\mathrm{ST}}\right)$, detection efficiencies of the ST $\bar{\Lambda}_{c}^{-}\left(\epsilon_{i}^{\mathrm{ST}}\right)$, detection efficiencies of the DT events $\left(\epsilon_{i}^{\mathrm{DT}}\right)$ and signal yield $\left(N_{\text {sig }}\right)$. Since Eq. 1 contains a ratio of ST and DT efficiencies, any systematic uncertainty on the tag side is canceled to first order. Each of them is evaluated relative to the measured branching fraction.

The numbers of charged tracks are required to be only one (Cat-1) or three (Cat-2) without any extra charged tracks. This difference between data and MC simulation for this selection is studied with control sample of $\Lambda_{c}^{+} \rightarrow$ $p K^{-} \pi^{+}$(the other $\bar{\Lambda}_{c}^{-}$goes to the 10 tag modes). The uncertainty on the requirement of the number of charged tracks is assigned to be $2.2 \%$, which is denoted as "No extra charged track" in Table 8 .

The tracking efficiencies for $K$ as a function of transverse momentum has been studied with the process $J / \psi \rightarrow K_{S}^{0} K^{+} \pi^{-} \rightarrow K \pi^{+} \pi^{-} \pi^{-}$. The efficiency differences between data and MC simulation are both $1 \%$ for $K^{+}$tracking and PID efficiencies, which are taken as the systematic uncertainties [49].

The uncertainties of the background and fits of the distributions of $M_{\text {recoil }}^{\mathrm{Cat-1}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ and $M_{\text {recoil }}^{\mathrm{Cat}-2}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ arise from the sideband range and background estimation. First, the uncertainty for the data sideband and $q \bar{q}$ background estimation is derived from the statistical uncertainty of the background estimate in the $M_{\mathrm{BC}}$ sideband region and the variation of the sideband range. Second, the background shape is changed from a polynomial function to an ARGUS function. The differences between the new and nominal results are taken as the systematic uncertainties.

The uncertainty due to the $\Lambda$ reconstruction efficiency, which is estimated by a weighted root-mean-square of the statistical uncertainties for different $(p, \cos \theta)$ intervals, is assigned to be $0.6 \%$ using a sample of $J / \psi \rightarrow \bar{p} K^{+} \Lambda$


Fig. 4. The fit projections of (a) $M_{\text {recoil }}^{\mathrm{Cat-1}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+}\right)$and (b) $M_{\text {recoil }}^{\mathrm{Cat-2}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+}\right)$distributions. The black points with error bars are data. The black line is the sum of all the components in the fit. The blue-shaded histograms are the $\Lambda_{c}^{+} \bar{\Lambda}_{c}^{-}$backgrounds. The green-shaded histograms are from the data sideband (in Cat-1) or hadron sample (in Cat-2).


Fig. 5. Fit projections of (a) $M_{\text {recoil }}^{\mathrm{Cat-1}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ and (b) $M_{\text {recoil }}^{\mathrm{Cat-2}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ distributions. The black points with error bars are data. The black line is the sum of all the components in the fit. The blue-shaded histograms are the $\Lambda_{c}^{+} \bar{\Lambda}_{c}^{-}$background. The green-shaded histograms are from the data sideband (in Cat-1) or hadron sample (in Cat-2). The purple line represents the signal shape of the three-body decay $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$. The dashed blue line represents the one-dimensional histogram PDF that describes the background distributions of $M_{\text {recoil }}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$, which are modeled with an ARGUS function.
decays 50].
The uncertainty due to the $\pi^{0}$ selection with the minimum kinematic-fit $\chi^{2}$ is studied with control sample of $\Lambda_{c}^{+} \rightarrow \Sigma^{+} \omega$ and $\Lambda_{c}^{+} \rightarrow \Sigma^{+} \pi^{0}$. The difference between data and MC simulation is assigned as $1 \%$.

The uncertainty due to the $\pi^{0}$ mismatch component in the fit is evaluated using simulation samples with an alternative $\pi^{0}$ matching approach, where the $\pi^{0}$ candidate closest to the true $\pi^{0}$ is chosen to be the reconstructed $\pi^{0}$ candidate. The fit is performed on the simulation samples, using both the nominal and alternative $\pi^{0}$ matching, and the difference in the fitted branching fraction
between them is taken as the systematic uncertainty.
The uncertainty in reweighting the $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ simulation samples is derived using different 2D variables and different choices of 2D binning, for instance 6 bins $\times 6$ bins to 7 bins $\times 7$ bins. The uncertainty is determined in a similar manner as the uncertainty from the background shape.

The total systematic uncertainty for the two strategies is obtained by taking the quadratic sum of the individual values. Some systematic uncertainties are the same between two strategies, e.g. tracking and PID of the charged kaon, so they are assumed to be fully correlated


Fig. 6. Fit projections on (a) $M_{\text {recoil }}^{\mathrm{Cat-1}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ distribution and (b) Likelihood distribution over the branching fractions of $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}$.


Fig. 7. Fit projections on (a) $M_{\text {recoil }}^{\mathrm{Cat-1}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$, (b) $M_{\text {recoil }}^{\mathrm{Cat-2}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ distributions and (c) Likelihood distributions over the branching fractions of $\Lambda_{c}^{+} \rightarrow \Sigma^{0} K^{+} \pi^{0}$. The black curve denotes the fit result with systematic uncertainty. The blue arrows show the results corresponding to $90 \%$ confidence level.


Fig. 8. Fit projections on (a) $M_{\text {recoil }}^{\mathrm{Cat-1}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$, (b) $M_{\text {recoil }}^{\mathrm{Cat-2}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ distributions and (c) Likelihood distributions over the branching fractions of $\Lambda_{c}^{+} \rightarrow \Lambda K^{+} \pi^{0}$.
in the combination. Other systematic uncertainties are independent between two strategies, e.g. $\Lambda$ reconstruction, background estimation in the fits on the distributions of $M_{\text {recoil }}^{\mathrm{Cat}-1}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$ and $M_{\text {recoil }}^{\mathrm{Cat-2}}\left(\Lambda_{c}^{\mathrm{ST}} K^{+} \pi^{0}\right)$, and they are treated without any correlation in the combination. The different systematic sources are listed in Table 8, where the two categories have been separated explicitly.

## VIII. SUMMARY

With $6.1 \mathrm{fb}^{-1}$ of $e^{+} e^{-}$collision data collected at eleven CM energy points between 4.600 and 4.840 GeV with the BESIII detector at BEPCII, the CF decays $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ and $\Lambda_{c}^{+} \rightarrow \Xi(1530)^{0} K^{+}$are observed with significances of $8.6 \sigma$ and $6.9 \sigma$, respectively. The branching fraction of $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ is measured to

Table 8. Systematic uncertainties.

| Sources | $\Lambda_{c}^{+} \rightarrow \Xi(1530)^{0} K^{+}$ |  | $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ |  | $\Lambda_{c}^{+} \rightarrow \Sigma^{0} K^{+} \pi^{0}$ |  | $\Lambda_{c}^{+} \rightarrow$ | $\Lambda K^{+} \pi^{0}$ | $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Cat-1 | Cat-2 | Cat-1 | Cat-2 | Cat-1 | Cat-2 | Cat-1 | Cat-2 | Cat-1 |
| No extra charged track |  |  |  |  | 2.2 |  |  |  |  |
| $K^{+}$tracking |  |  |  |  | 1.00 |  |  |  |  |
| $K^{+}$PID |  |  |  |  | 1.00 |  |  |  |  |
| $\pi^{0}$ reconstruction |  |  |  |  | 1.00 |  |  |  |  |
| ST yield |  |  |  |  | 0.40 |  |  |  |  |
| Statistics | 0.14 | 0.13 | 0.14 | 0.14 | 0.14 | 0.14 | 0.14 | 0.14 | 0.14 |
| Background PDF | 1.17 | 1.17 | 2.05 | 2.05 | 2.41 | 2.41 | 1.37 | 1.37 | 2.06 |
| $\Lambda$ reconstruction | - | 2.70 | - | 2.70 | - | 2.70 | - | 2.70 | - |
| $\pi^{0}$ selection | - | - | 1.00 | 1.00 | - | - | - | - | - |
| $\pi^{0}$ mismatch | 2.00 | - | 5.13 | - | - | - | - | - |  |
| Reweighting | - | - | 4.95 | 2.43 | - | - | - | - | - |
| Sum | 3.66 | 3.12 | 8.00 | 4.41 | 3.72 | 3.77 | 3.15 | 3.20 | 3.50 |

Table 9. The comparison between the measurement and theoretical predictions $\left(\times 10^{-3}\right)$.

|  | $\Lambda_{c}^{+} \rightarrow \Xi(1530)^{0} K^{+}$ | $\Lambda_{c}^{+} \rightarrow \Xi^{0} K^{+} \pi^{0}$ | $\Lambda_{c}^{+} \rightarrow \Sigma^{0} K^{+} \pi^{0}$ | $\Lambda_{c}^{+} \rightarrow \Lambda K^{+} \pi^{0}$ | $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| This measurement | $5.99 \pm 1.04 \pm 0.29$ | $7.79 \pm 1.46 \pm 0.71$ | $<1.8$ | $<2.0$ | $<0.71$ |
| K. K. Sharma et al. [23] | - | $45 \pm 8$ | $1.2 \pm 0.3$ | $4.5 \pm 0.8$ | $0.05 \pm 0.005$ |
| Jian-Yong Cen et al. [24] | - | $32 \pm 6$ | $0.7 \pm 0.2$ | $3.5 \pm 0.6$ | $0.05 \pm 0.006$ |
| $\mathcal{B}($ previous results) [48] | $5.02 \pm 0.99 \pm 0.31$ | - | - | - | - |

be $(7.79 \pm 1.46 \pm 0.71) \times 10^{-3}$, where the first and second uncertainties are statistical and systematic, respectively. It is smaller than the theoretical predictions $(4.5 \pm 0.8) \times 10^{-2}[23]$ and $3.2 \pm 0.6 \times 10^{-2}$ [24]. Comparisons of theory and experiment are shown in Table 9. The branching fraction of $\Lambda_{c}^{+} \rightarrow \Xi(1530)^{0} K^{+}$is $(5.99 \pm 1.04 \pm 0.29) \times 10^{-3}$, which is consistent with the previous result $(5.02 \pm 0.99 \pm 0.31) \times 10^{-3}$ 48].

The upper limits on the branching fractions at the $90 \%$ confidence level of the SCS or DCS decays $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}$, $\Sigma^{0} K^{+} \pi^{0}$ and $\Lambda K^{+} \pi^{0}$ are $7.1 \times 10^{-4}, 1.8 \times 10^{-3}$ and $2.0 \times 10^{-3}$, respectively. The upper limit of the branching fraction of $\Lambda_{c}^{+} \rightarrow \Lambda K^{+} \pi^{0}$ is incompatible with the theory predictions 23, 24. The upper limits of the branching fractions of $\Lambda_{c}^{+} \rightarrow \Sigma^{0} K^{+} \pi^{0}$ and $\Lambda_{c}^{+} \rightarrow n K^{+} \pi^{0}$ are consistent with the theoretical predictions [23, 24]. These results are essential for the understanding of the dynamics in the charmed baryon decays.

## IX. ACKNOWLEDGEMENT

The BESIII collaboration thanks the staff of BEPCII and the IHEP computing center for their strong support. This work is supported in part by National Key R\&D Program of China under Contracts Nos. 2020YFA0406400, 2020YFA0406300; National Natu-
ral Science Foundation of China (NSFC) under Contracts Nos. 11635010, 11735014, 11835012, 11935015, 11935016, 11935018, 11961141012, 12022510, 12025502, 12035009, 12035013, 12192260, 12192261, 12192262, 12192263, 12192264, 12192265, 12221005, 12225509, 12235017, 12005311; the Fundamental Research Funds for the Central Universities, Sun Yat-sen University, University of Science and Technology of China; 100 Talents Program of Sun Yat-sen University; the Chinese Academy of Sciences (CAS) Large-Scale Scientific Facility Program; Joint Large-Scale Scientific Facility Funds of the NSFC and CAS under Contract No. U1832207; the CAS Center for Excellence in Particle Physics (CCEPP); 100 Talents Program of CAS; The Institute of Nuclear and Particle Physics (INPAC) and Shanghai Key Laboratory for Particle Physics and Cosmology; ERC under Contract No. 758462; European Union's Horizon 2020 research and innovation programme under Marie Sklodowska-Curie grant agreement under Contract No. 894790; German Research Foundation DFG under Contracts Nos. 443159800, Collaborative Research Center CRC 1044, GRK 2149; Istituto Nazionale diFisica Nucleare, Italy; Ministry of Development of Turkey under Contract No. DPT2006K-120470; National Science and Technology fund; National Science Research and Innovation Fund (NSRF) via the Program Management Unit for Human Resources \& Institutional Development, Re-
search and Innovation under Contract No. B16F640076; Olle Engkvist Foundation under Contract No. 200-0605; STFC (United Kingdom); Suranaree University of Technology (SUT), Thailand Science Research and Innovation (TSRI), and National Science Research and Innovation

Fund (NSRF) under Contract No. 160355; The Royal Society, UK under Contracts Nos. DH140054, DH160214; The Swedish Research Council; U. S. Department of Energy under Contract No. DE-FG02-05ER41374.
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