

**JOHANN WOLFGANG GOETHE-UNIVERSITÄT  
FRANKFURT AM MAIN**

**FACHBEREICH WIRTSCHAFTSWISSENSCHAFTEN**

**Raimond Maurer / Shohreh Valiani**

**Hedging the Exchange Rate Risk in International  
Portfolio Diversification:  
Currency Forwards versus Currency Options**

**No. 109  
June 2003**



**WORKING PAPER SERIES: FINANCE & ACCOUNTING**

**Raimond Maurer / Shohreh Valiani**

**Hedging the Exchange Rate Risk in International Portfolio Diversification:  
Currency Forwards versus Currency Options**

**No. 109**

**June 2003**

**ISSN 1434-3401**

**WORKING PAPER SERIES FINANCE AND ACCOUNTING ARE INTENDED TO MAKE RESEARCH FINDINGS AVAILABLE TO OTHER RESEARCHERS IN PRELIMINARY FORM, TO ENCOURAGE DISCUSSION AND SUGGESTIONS FOR REVISION BEFORE FINAL PUBLICATION. OPINIONS ARE SOLELY THOSE OF THE AUTHORS.**

# Hedging the Exchange Rate Risk in International Portfolio Diversification: Currency Forwards versus Currency Options

by

Raimond Maurer and Shohreh Valiani

June 2003

*Raimond Maurer*

Professor for Investment, Portfolio Management and Pension Finance, School of Business and Economics, Goethe-University Frankfurt/M., 60054 Frankfurt, Germany  
e-mail: [RMaurer@wiwi.uni-frankfurt.de](mailto:RMaurer@wiwi.uni-frankfurt.de); web: [www.finance.uni-frankfurt.de](http://www.finance.uni-frankfurt.de)

*Shohreh Valiani* (corresponding author)

Graduate Program "Finance and Monetary Economics", School of Business and Economics, Goethe University, Frankfurt am Main, Mertonstr. 17-21, D-60054 Germany,  
email: [valiani@wiwi.uni-frankfurt.de](mailto:valiani@wiwi.uni-frankfurt.de); web: [www.finance.uni-frankfurt.de](http://www.finance.uni-frankfurt.de)

*Keywords: International Portfolio Diversification, Currency Hedging, FX Derivatives, Short-fall Risk*

JEL: F31, G11, G15

## **Abstract**

As past research suggest, currency exposure risk is a main source of overall risk of international diversified portfolios. Thus, controlling the currency risk is an important instrument for controlling and improving investment performance of international investments. This study examines the effectiveness of controlling the currency risk for international diversified mixed asset portfolios via different hedge tools. Several hedging strategies, using currency forwards and currency options, were evaluated and compared with each other. Therefore, the stock and bond markets of the, United Kingdom, Germany, Japan, Switzerland, and the U.S, in the time period of January 1985 till December 2002, are considered. This is done from the point of view of a German investor. Due to highly skewed return distributions of options, the application of the traditional mean-variance framework for portfolio optimization is doubtful when options are considered. To account for this problem, a mean-LPM model is employed. Currency trends are also taken into account to check for the general dependence of time trends of currency movements and the relative potential gains of risk controlling strategies.

# 1 Introduction

Since 1973, the exchange rates of major currencies have been permitted to float freely against one another. This, along with increases in the volume of the world trade, has escalated the foreign currency risk. Compared to investments in domestic assets, fluctuating exchange rates represent an additional risk factor for investors who want to diversify their portfolios internationally. Therefore, it is important to study whether hedging the exchange rate risk is worthwhile and to which extent.

To effectively manage the currency risk, a variety of approaches have been employed, such as currency swaps, multi-currency diversification, and hedging via forwards, futures and options. The question now arises whether these hedging instruments provide different degrees of risk reduction and/or profit potential. There exist numerous studies which has discussed this issue by considering using currency forwards, especially from the viewpoint of U.S. investors. However, so far not much work has been done to examine the effectiveness of European options in an ex-post and ex-ante framework. In this study, we compare the effectiveness of several hedging strategies based on two major hedging instruments, currency forwards versus currency options, from the perspective of German investors.

*Jorion* (1985, 1986), *Eun/Resnick* (1988, 1994), *Levy/Lim* (1994), and *Bugar/Maurer* (2002) have shown that if the investors would not control the uncertainty parameter of foreign currency exposure, the potential gains from international portfolio diversification may not be enough to justify the expense of an international investment. Due to the high correlations among the exchange rate changes, much of the exchange risk may remain nondiversifiable in a multi-currency portfolio. Therefore it has been widely discussed that investors can conceivably eliminate much of the exchange rate risk by selling the expected foreign currency gains via derivatives on a currency-by-currency basis. Using the unitary forward hedge ratio strategy in order to hedge the exchange rate risk discussed by *Eun/Resnick* (1988, 1994)<sup>1</sup>, they showed that such a strategy compared with the unhedged one, would reduce the volatility of the portfolio returns without a substantial reduction in average returns. Therefore they called it a costless strategy in terms of portfolio returns, since it just reduces the portfolio risk<sup>2</sup>.

*Adler/Prasad* (1992) propose that investors can use the minimum variance hedge ratios (regression coefficients) that come from regressing the world market portfolio or any nation's stock market index on third currencies. Jensen's inequality guarantees that the hedge ratio will be the same for each national investor regardless of the numeraire currency. *Glen/Jorion* (1993) compared the risk adjusted performance of optimally hedged portfolios by using currency forwards with the unitary hedging strategy using Black's universal hedge ratio. They found that the optimally hedged portfolios performed best, but not statistically significantly better than the universal hedged strategy. *Larsen/Resnick* (2000) performed an ex-ante study comparing unhedged international equity investments, unitary hedging, an arbitrary estimate of 0.77 of Black's universal hedge ratio, and the universal regression hedge ratios of *Adler/Prasad* (1992). They found that a unitary hedging forward strategy works better than the others. In an ex-post study, *Jorion* (1994) compared unhedged international investment versus three methods, uniquely estimation of the optimal hedge ratios separate from the assets

---

<sup>1</sup> This is according to the theoretical work of *Eaker/Grant* (1990) and the empirical findings of *Adler/Simon* (1986).

<sup>2</sup> Through the same approach, *Black* (1989, 1990) proposed a universal hedge ratio that is less than unity for equity portfolios and is the same for all currencies and all national investors. His specific assumptions leading to universal hedge ratio have been criticized on various grounds.

optimization, the partial optimization in which the hedge ratios are optimized after a predetermined position in the assets portfolio, and a joint optimization over the currencies and assets. Using the Sharpe ratio for portfolio performance as the evaluation criterion shows that the potential benefit of hedging via the joint optimization dominates the partial (separate) ones. *Larsen/Resnick* (2000) in an ex-ante study examined the different construction of internationally diversified equity portfolios hedged against exchange rate uncertainty by the same methodology used in *Jorion* (1994) and their results show that the performance of a unitary hedging strategy is the best among all the other strategies.

Although there exist many empirical studies on forward contracts to hedge the currency risk, the evidence for other types of derivatives like options are not much. *Hsin/Kuo/Lee* (1994) and *Conover/Dubofsky* (1995) worked on the use of American options where they found that protective puts dominate fiduciary calls. Following this line of research, this study investigates the potential benefit of international portfolio diversification by comparing the hedging effectiveness of currency forwards versus currency options. In contrast to other studies we use an portfolio optimization framework and do not use the classical mean/variance approach, as the research framework of rational financial decision-making under risk. The basic limitation of such an approach is the lack of a satisfactory choice-theoretic foundation: The mean/variance framework requires either quadratic utility functions or symmetric return distributions. Neither assumption is in empirical situations necessarily correct. A quadratic utility function could be inappropriate, because it implies decreasing marginal utility of wealth and increasing absolute and relative risk-aversion. Both is criticized from a descriptive, as well as from a normative, perspective (see among others, *Hanoch/Levy* 1970; *Fishburn* 1977, 1984; *Weber* 1990 and *Sarin/Weber* 1993). The non-linear pay-off characteristic of options lead to complex, distinctly asymmetrical return distributions with significant moments beyond mean and variance using the classical mean/variance framework would lead to biased results<sup>3</sup>. In addition, the empirical observation on the stock indices approves the existence of asymmetric distributions for equity markets with higher moments which are statistically significant from the bell-shaped measures.

In order to avoid these critical assumptions a mean/shortfall-risk framework for rational financial decision-making in the asset allocation context is adopted in this study. Shortfall-risk measures formulate the (downside-) risk as a probability-weighted function of negative deviations from a predetermined target. These risk measures, which explicitly reflect the asymmetry of the probability distribution of asset returns, have attracted considerable interest in the more recent literature on portfolio diversification (e.g. *Harlow* 1991). The mean-LPM analysis has reasonable computational possibilities along with a fair degree of compatibility with the primary concerns expressed by investment managers. Additionally, the mean-LPM shows a satisfactory choice-theoretic foundation since it is consistent with utility functions reflecting the preferences of decision maker towards risk for below-target returns and it satisfies the stochastic dominance measurement which is a well-known criterion for the policy makers in uncertainty situations.

The next section explains the data. Following that, the methodology is briefly described in section three, where the optimal hedging schemes for currency futures and currency options are also outlined. Then the results of the ex-post analysis will be introduced in section four. In section five the existence of improvements is checked in an ex-ante framework and different strategies are compared. The final section summarizes the article.

---

<sup>3</sup> See *Bookstaber/Clarke* (1984, 1985) for that point.

## 2 Data

Equity and government bond markets in five countries have been considered, United Kingdom, Switzerland, Japan, Germany, and the United States which are also the most important financial markets in an international setting. Portfolio performance is examined at monthly intervals, based on portfolio values, spot exchange rates, and one-month forward rates as well as one month currency put options. The full period runs from first month 1985 to December 2002. The equity returns under consideration are computed from total return stock indices compiled by Datastream global index and adjusted for capital gains as well as dividend payments paid during the holding period. The indices for each country represent portfolios of all listed firms, included in the industry proportions that reflect industry composition in the local market. Each of the indices are value weighted, formed from major companies based on market capitalization. The bond indices are the Datastream government bond indices which represent the total return of the bond markets in local currency, and are value-weighted indices of bonds with at least one year to maturity. The forward contracts are contracts for the British Pound, Swiss Franc, Japanese Yen and US Dollar with respect to the German Mark with a maturity of one month.<sup>4</sup> For options, due to the lack of data the theoretically currency option time series following the *Garman/Kohlhagen* (1983) approach have been computed.

The first four moments of local returns in stock and bond markets have been presented in table 1 which not only gives the information on the average rate of returns in the both markets but also helps to discover the type of the probability distribution of the market's return (the returns are monthly percentage log returns). The average rate of return and the volatility of stock indices as it is already expected, indicates the substantially higher mean return than in the bond markets. Government bonds yield at most 0.84 percent (in United Kingdom), where the lowest average returns of stock markets would reach the level of 1.18 percent (in United Kingdom).

---

<sup>4</sup> All these data are available from Datastream.

**Table 1: Descriptive Statistics of Individual Stock and Bond Markets**

	UK	Switzerland	Japan	Germany	USA
<i>Stock Index Excess Returns</i>					
Average Returns	1.03	1.10	0.25	0.80	1.13
Standard Deviation	4.83	5.13	5.88	5.93	4.65
Skewness	-0.89	-1.08	0.07	-0.76	-0.80
Kurtosis	3.68	3.11	0.77	1.65	2.05
J/B	151.02	128.82	5.56	45.21	61.11
<i>P</i>	0.00	0.00	0.06	0.00	0.00
<i>Bond Index Excess Returns</i>					
Average Returns	0.83	0.44	0.48	0.57	0.74
Standard Deviation	1.81	0.96	1.31	0.96	1.41
Skewness	-0.04	-0.06	-0.56	-0.48	0.02
Kurtosis	1.39	0.54	1.73	-0.12	0.03
J/B	17.64	2.71	38.29	8.58	0.02
<i>P</i>	0.00	0.26	0.00	0.014	0.98

Notes: The table contains summary statistics for monthly returns on the stock and bond indices in our sample. Mean returns and standard deviations are in percentages. Skewness and excess of kurtosis respectively represents the third and fourth central moments of the rates of return. These moments can sometimes be examined to provide an informal check of normality; the excess kurtosis of a normal distribution is zero. Jarque-Bera associated with the *P*-value gives the test for normality of the returns. Returns are calculated from 216 observations for the time period of January 1985 until December 2002.

The degree of skewness and the excess-kurtosis indicates that all the stock markets except for Japan, are left skewed and have a significantly positive excess-kurtosis which means the fatter tails than normal distribution. In the bond market except for Germany and Japan the negative skewness is not much and the excess-kurtosis is slightly different from zero.

According to the statistics, the stock markets have the probability distribution which is known technically as leptokurtic distribution. In the case of the bond markets the normality distribution also would not be fit. These results are statistically confirmed by computing the statistical test of *Jarque/Bera* (1987) for the null-hypothesis of normality. The existence of a normal distribution for all the stock markets can be rejected at the significance level of 5%. In the case of bond markets, the empirical results show that the normal distribution also would not be accepted for the USA bond market at the significance level of 1% and for all the others at the significance level of 5%. Therefore the existence of a symmetric international portfolio return distribution, which is one of the base assumptions for using the mean-variance optimization, in all the cases would not be satisfied<sup>5</sup>.

Additionally as it shows in table 2, in an international portfolio framework when we look at the foreign exchange rate returns, the normality assumption for currency markets would be rejected for Switzerland and USA at the significance level of 1% and for the others at the significance level of 5%. The statistics of foreign exchange return shows that these markets are also skewed with a kurtosis of less than 3 for Swiss Franc and greater than 3 for the others,

<sup>5</sup> To use the mean-variance framework requires either the symmetric return distribution or the quadratic utility function, which none of them here is consistent with the reality.

which means the return distribution of these markets also contains a deviation from the normal distribution.

**Table 2: Descriptive Statistics of Currency Exchange Markets**

	UK	Switzerland	Japan	USA	Germany
<i>Exchange Rate Returns</i>					
Mean	-0.06	0.05	0.15	-0.18	0.00
Standard Deviation	2.34	1.16	3.22	3.28	0.00
Skewness	-0.41	0.29	0.81	0.24	---
Kurtosis	1.12	-0.07	2.29	0.31	---
J/B	17.35	3.01	71.07	2.96	---
<i>P</i>	0.00	0.22	0.00	0.23	---

Notes: The table contains summary statistics for monthly returns on the currency exchange rate in our sample. Mean returns and standard deviations are in percentages. Skewness and excess of kurtosis respectively represents the third and fourth central moments of the rates of return. These moments can sometimes be examined to provide an informal check of normality; the excess kurtosis of a normal distribution is zero. Jarque-Bera associated with the P-value gives the test for normality of the returns. Returns are calculated from 216 observations for the time period of January 1985 until December 2002.

### 3 Methodology: International Asset Allocation in a Downside Risk Framework

#### 3.1 Portfolio Optimization Process in a LPM - Framework

The aim in an international portfolio optimization is determining the most favorable combination of assets such that the portfolio is dominant on the others with a minimum risk at all levels of expected return. The concept of downside risk is goes back to Roy (1952) in the form of "safety first" rule. Markowitz (1952) formalized his seminal portfolio theory based on the semi-variance, defined as the squared deviation of return below a target return. Bawa (1975) generalized the semi-variance measure of risk to reflect a less restrictive class of decreasing absolute risk-averse utility function which called Lower Partial Moment or LPM. The common classes of LPM are the probability of loss ( $n = 0$ ), the target shortfall ( $n = 1$ ), the target semi-variance ( $n = 2$ ) and the target skewness ( $n = 3$ )<sup>6</sup>. The variable  $n$  can also be viewed as a measure of risk aversion where the degree of risk aversion increases with  $n^7$ . Therefore this definition can be generalized into n-order LPMs to cover a range of risk measures as:

$$LPM_n(\tau, R_i) = \int_{-\infty}^{\tau} (\tau - R_i)^n dF(R_i) \quad (1)$$

where  $\tau$  is "target return",  $R_i$  is the random return of asset  $i$  and  $dF(R_i)$  is the probability density function of return on asset  $i$  and  $n$  is the order of moment that characterizes the investor preferences of return dispersion below the target rate of return. Risk, as measured by the  $n$ -

<sup>6</sup> For more details see Bawa (1975, 1977).

<sup>7</sup> In other words, a more risk averse investor ( $n = 3$ ) prefers less risk than a less risk-averse investor ( $n = 1$ ) for the same level of return.



*LPM* reflects explicitly the asymmetry of the probability distribution of asset returns. As *Fishburn* (1977) shows this concept accurately reflects the decision maker's preferences between the combination of risk and return of a portfolio. Additionally the induced efficient set of this model strongly satisfies the stochastic dominance criteria<sup>8</sup> which is a well-known tool for investment decision evaluation and fits with several types of utility functions.

The algorithm of optimal investment for downside risk-averse investor in the downside risk asset allocation framework, based on the assumption of no short-selling was proposed by *Harlow/Rao* (1989) and *Harlow* (1991). Formally, the problem is to select an optimal mixes of assets such that the probability of the achieved portfolio return ( $R_p$ ) falling below the target rate of return ( $\tau$ ) would be minimized. This algorithm is defined as:

$$\min_{x_i} LPM_n(\tau, x_i) = \frac{1}{T} \sum_{t=1}^T \max \left\{ 0, \left( \tau - \sum_{i=1}^N x_{it} R_{it} \right)^n \right\} \quad (2)$$

subject to

$$C_1(x_i): \sum_{i=1}^N x_i \bar{R}_i = R_p$$

$$C_2(x_i): \sum_{i=1}^N x_i = 1$$

$$x_i \geq 0, \quad i = 1, 2, \dots, N$$

where  $T$  is the number of observed periods,  $\bar{R}_i$  is the mean return on the asset  $i$  over all periods,  $R_p$  is the predetermined portfolio return and  $x_i$  is the optimal weight of portfolio allocated to asset  $i$ . In addition, short sales were excluded because many institutional investors like insurance companies, mutual and pension funds are restricted in this regard. In this study the risk measure is the first order lower partial moment of downside risk which accords to  $n = 1$  (mean-LPM<sub>1</sub>). This would give a higher risk preference threshold in the optimization process to the international investor which gives a more general feature to our study and it is more concrete with the choice between the combination of the shortfall risk and the portfolio expected returns.

The target  $\tau$  is considered as the risk-free interest rate in the home country which has a good economic intuition for the international investor. Assume that the international investor uses the Deutsche Mark as his/her numeraire currency. Yet the  $R_i$  is the converted national return to the numeraire currency (German DM), for each financial market, from time  $t$  to time  $t+1$ :

$$R_i = R_{i,f} + e_f + R_{i,f} \cdot e_f \quad (3)$$

where  $R_{i,f}$  is the local currency rate of return on the  $i^{\text{th}}$  asset during one time interval in the foreign country,  $e_f = (SX_{t+1} - SX_t) / SX_t$  is the rate of appreciation (depreciation) of the related foreign currency market against the DM, and  $SX_t$  is the spot exchange rate of foreign financial market against German DM. Based on this equation it can be easily seen that the total portfolio performance is exposed to the changes in risk and returns of both, the local security market

<sup>8</sup> The efficient set of this model for  $n=0$  is a subset of the First Stochastic Dominance efficient set, for  $n=1$  is a subset of the Second Stochastic Dominance efficient set and for  $n=2$  is a subset of the Third Stochastic Dominance efficient set, *Fishburn* (1977, 1984).

and the currency exchange rate market. Therefore an appropriate currency hedging strategy becomes highly important for the international investors.

### 3.1 Currency Hedging with Forwards

First we use a currency forward contract to hedge the exchange rate risk. A currency forward contract is an agreement between two parties to buy (long position) or sell (short position) foreign currency with current spot price  $SX$ , at a future date and at an exchange rate  $F$  (the forward price), determined at the time of the transaction<sup>9</sup>. The forward premium<sup>10</sup> can be determined as  $f = F/S - 1$ <sup>11</sup>.

As with many other kinds of financial derivatives, currency forward contracts are offered by commercial banks and/or traded on organized financial markets, and typically have short maturities of one to nine months. Neglecting margin requirements, currency forward contracts produce a random payoff, but do not absorb capital upon closing of the position. The financial success from a forward short position offsets possible gains and losses from currency fluctuations on the investment in the foreign stock market. Now if the German investor wants to hedge through forwards, he has to determine simultaneously the optimal portfolio weights and the hedge ratios for each asset. For this purpose equation (3) has to be replaced by:

$$R_i^h = R_{i,f} + e_f + R_{i,f} \cdot e_f + h_i(f - e_f) \quad (4)$$

where  $f$  represents the forward premium and  $h_i$  represents the hedge ratio,<sup>12</sup> which determines the amount of the initial value of investment, should be sold forward. Through solving the optimization for the given target, the weights of investment in different markets ( $N$  investment weights) and the optimal hedge ratios ( $N-1$ ) will be determined<sup>13</sup>. The optimal investment weight normally depends on the hedge ratio which by itself depends on the currency market.

For the purpose of having no speculation position on the forward contracts - many regulated institutional investors like insurance companies, mutual and pension funds are restricted in this regard - one should consider that:

$$0 \leq h_i \leq 1 \quad (5)$$

To compare the optimal hedge ratios with an unhedged strategy, we would also optimize the above equation for  $h_i = 0$ .

### 3.2 Currency Hedging with Put Options

In order to use the currency option as a hedging instrument - which gives the investor (holder) the right (an optional guarantee), but not the obligation, to buy or sell a specific amount of currency at a specific exchange rate (the strike), on or before a specific future date - a premium would be required. Therefore the currency option compare to forwards is a costly hedge

<sup>9</sup> Cf. Abken/Shrikhande (1997), p. 37.

<sup>10</sup> If the interest rate parity (IRP)  $1 + f = (1 + r)/(1 + r_f)$  holds, then the forward premium (domestic currency units per foreign currency unit)  $f = F/S - 1$ , represents the difference between the nominal zero-coupon default free interest rates (i.e. the risk-less interest rate) with the same maturity as the forward contract of the domestic ( $r$ ) and the foreign ( $r_f$ ) country.

<sup>11</sup> When the forward premium is negative, it is referred to as a forward discount.

<sup>12</sup> Alternatively investors can hedge the exchange risk via borrowing in the international money market, for more detail refer to Eun/Resnick (1988).

<sup>13</sup> Since there is no need to hedge in the local market.

instrument which also gives more flexibility than traditional forwards. Besides, the holder of the option would achieve four alternatives as; when, whether and how much to exercise plus the right to choose the strike price of the contract. The two important key features of the currency option are first, its insurance protection and second, its profit potential. Through paying a premium by the holder to the writer (seller) of the option, a fixed exchange rate, required by the option holder would be guaranteed. On the other hand, hedging with an option will eliminate any chance of currency loss where the only outflow of funds would be the premium payment. Therefore, if the currency market movement is in the holders favor and upside potential is available, the option will be abandoned and the holder have the chance to enter into a spot deal when, if the movement is against the holder, the option will be "exercised" at the previously agreed rate. Thus an option profile exposes an "asymmetric risk". The most that a holder can lose is the option premium and the most that he can profit is limited only by how far the market moves.

To compare the two hedging products it can be pointed out that; first, currency option will give "the right" to sell (or to buy) the underline asset. Second, there would be "no obligation" to deliver or receive the currency at the strike rate. Third, it "eliminates downside risk whilst retaining unlimited profit potential" and finally it is a "perfect hedge tool for variable exposures", but can be expensive. While in forwards there exist "the obligation" to sell (or to buy) the underlying. Therefore, on one hand the unlimited amount of loss can be possible (as the forward ties the client into a fixed rate), and on the other hand it "eliminates all downside risk but allows no up-side potential" at all. So one can say that forwards compared to options are rigid hedge tools for the variable exposures.

In this study, we look at the European currency put option<sup>14</sup> in order to determine the optimal hedge ratio which gives the investor the right to sell the foreign currency at the predetermined exchange rate and will eliminate the downside risk of the currency movements.

There is no sample data for currency puts, therefore in order to calculate the returns of put options, first by using the *Garman/Kohlhagen* (1983) formula, the theoretically put premiums have been computed. Then the pay-off for at the money, in the money and out of the money put options would be first subtracted and then divided by the corresponding premiums<sup>15</sup> and then the returns would be achieved. Pricing models for European currency options have been derived by *Biger/Hull* (1983), *Garman/Kohlhagen* (1983) under the assumption of a geometric Brownian motion for the underlying foreign currency exchange rates, in which puts of the European type would be computed by:

$$P_t = -SX_t \exp(-r_f(T-t))\Phi(-d1) + K \exp(-r(T-t))\Phi(-d2) \quad (6)$$

where

$$d1 = \frac{\ln(SX_t / K) + r - r_f(T-t)}{\sigma\sqrt{T-t}} + (1/2)\sigma\sqrt{T-t}$$

and

---

<sup>14</sup> Going short in currency calls also can be considered, but here in order to consistency with "no short-selling" constraint, we just discuss on going long in currency puts which of course in each case the constraints in optimization procedure have to be normalized.

<sup>15</sup> Here we have European options where in the *Conover/Dubofsky* (1995) the American option returns has been used.

$$d2 = \frac{\ln(SX_t / K) + r - r_f(T - t)}{\sigma\sqrt{T - t}} - (1/2)\sigma\sqrt{T - t}$$

where  $SX_t$ , is the spot exchange rate at time  $t$ ,  $r$  and  $r_f$  are respectively risk free rate in the local (Germany) and foreign country,  $K$  is the strike price,  $T - t$  is the time to maturity and  $\sigma$  is the volatility of the log of spot rates. Therefore,  $P_t$  is the price of a European put option in the local currency (German DM) to sell one unit of the foreign currency exchange rate for a predetermined strike price that matures at time  $T$ .

To be concrete in our study in order to compare the effects of two different hedge tools - futures and put options - we compute the put premiums base on having one month as the time to maturity. Strike price which has also a direct effect on the total pattern of puts return, has been considered in three different amounts. So a general overlook on the effects of different types of European puts would be given by considering, put at the money option, in and, out of the money option. For the at the money put option, the strike price equals to spot rate of currency exchange at the beginning of each month. This for in the money puts equals to five percent higher than the related spot exchange rate at the beginning of each month and finally for out of the money put option, the strike been considered as one percent lower than the respected currency spot exchange rate. Of course these strikes are arbitrary and the same analyses can be built on the other amounts of strike price or time to maturity<sup>16</sup>.

The pay-off for currency put options at maturity is given by  $\max(K - SX, 0)$ . This would be first subtracted and then divided by the corresponding put premiums to get the return of such a position:

$$R_o^p = (\max [(K - SX), 0] - P) / P \quad (7)$$

As it is already expected in table 3, one can see that the returns distribution of different types of put options, at the money, in the money, and out of the money put options are asymmetrically distributed. The positively skewness of these returns are indicating that the losses due to using put options as a risk insurance would be smaller and the gains magnitude would be larger<sup>17</sup>.

Hence, adding this type of assets to the international portfolio would definitely induce into an asymmetric total expected return and therefore the optimization under the lower partial moments methodology would satisfy both the theoretical and the empirical features of our study. The converted national return  $R_i$  for each financial market in one time interval will be still equal to:

$$R_i = R_{i,f} + e_f + R_{i,f} \cdot e_f \quad (8)$$

where here  $R_i$  contains not only the local currency rate of returns of assets but also contains the local currency rate of returns of the related put options. Therefore now, for international portfolio manager each time there will be  $N+4$  assets which have to be decided to be opti-

<sup>16</sup> Notice that we did not considered the five percent out of the money European put options due to the very small put premiums for this type of options which results mostly in zero return and therefore would not have any additional role in our analysis due to the zero weights.

<sup>17</sup> When the skewness of an asset return distribution is negative (left skewed), the downside returns will occur in larger magnitudes than the upside returns; i.e., losses when they occur will tend to be large losses; And when the skewness of the distribution is positive (right skewed), the upside returns will occur in larger magnitudes than the downside returns (when losses occur, they will be smaller and when gains occur, they will be greater).

mally invested in<sup>18</sup>. To normalize the algorithm of the international asset diversification in order to be no-speculation in trading the currency puts, we have to customize our restrictions. Thus the optimal weights of puts for each currency should be less or equal to the amount of stocks and bonds invested in the respective market.

$$\tilde{x}_S + \tilde{x}_B \geq \tilde{x}_O * (SX / \tilde{P}_O) \quad (9)$$

where  $\tilde{x}_S$ ,  $\tilde{x}_B$  and  $\tilde{x}_O$  are the optimal weights of investment in each foreign stock, bond and currency option markets,  $\tilde{P}_O$  represents the puts premia in the local currency (German DM) and  $SX$  is the currency spot exchange rate<sup>19</sup>.

In the optimization, different types of puts will be analyzed separately in order to see which kind of put options would be more beneficial for the investor as a controlling tool for his/her currency exposure risk.

---

<sup>18</sup> This, in the case of using some combination of puts will be different, e.g. if the investor want to use both put at the money option and in the money option then has to decide on  $N+8$  assets to optimally been invested in.

<sup>19</sup> For more detail refer to Appendix A.

**Table 3: Currency Put Options Returns**

	<b>UK</b>	<b>Switzerland</b>	<b>Japan</b>	<b>USA</b>	<b>Germany</b>
<i>At the Money Puts</i>					
Average Returns	0.01	-0.07	0.001	0.11	---
Standard Deviation	1.60	1.28	1.46	1.54	---
Skewness	2.43	1.56	2.00	1.46	---
Excess of Kurtosis	8.67	2.01	4.93	1.48	---
J/B	890.15	124.79	363.43	96.87	---
<i>P</i>	0.00	0.00	0.00	0.00	---
<i>In the Money Puts</i>					
Average Returns	0.01	-0.004	0.005	0.05	---
Standard Deviation	0.49	0.24	0.58	0.62	---
Skewness	0.68	-0.24	0.17	0.26	---
Excess of Kurtosis	1.81	-0.06	0.19	-0.34	---
J/B	46.71	2.12	1.40	3.51	---
<i>P</i>	0.00	0.34	0.49	0.17	---
<i>Out of the Money Puts</i>					
Average Returns	0.01	-0.31	-0.05	0.10	---
Standard Deviation	2.26	2.14	1.96	1.94	---
Skewness	3.52	3.81	3.12	2.01	---
Excess of Kurtosis	16.97	15.34	12.06	3.81	---
J/B	3039.63	2643.16	1660.63	276.69	---
<i>P</i>	0.00	0.00	0.00	0.00	---

Notes: The statistics are derived by using the monthly data of spot currency exchange rates time series for English Pond, Swiss Franc, Japanese Yen and US dollar against the German Deutsche Mark during the time period of January 1985 till December 2002. Notice that computed premiums have the adjusted historical volatility in each three years time interval. For having the percentage of average returns and the percentage of the volatility these results should be multiplied by 100. Skewness and excess of kurtosis respectively represents the third and fourth central moments of the European put option returns. Jarque-Bera associated with the *P*-value gives the test for normality of the returns.

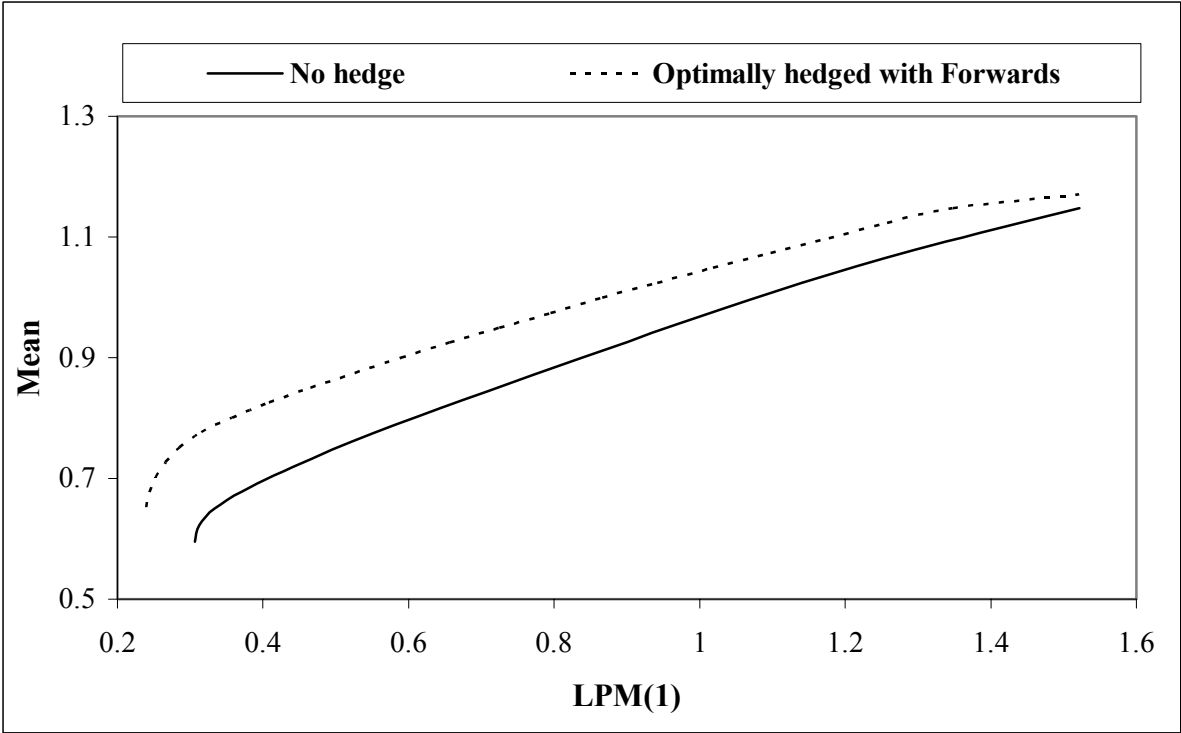
Here as we can see currency option - as an alternative hedge tool for the currency exposure risk - also shows a significant level of skewness and excess-kurtosis, which leads us to the rejection of the existence of a bell-shaped, symmetric distribution of the currency put option returns. So this also confirms that using the Markowitz mean-variance framework would lead us to the biased estimations and to avoid that we have to customize the mean/LPM framework where risk has been measured by going shortfall.

# 4 Ex-Post Analysis of the Potential Gains of International Portfolio Diversification and Hedging the Currency Risk

## 4.1 Hedging Policies and Mean/LPM-Efficient Frontiers

In this part we examine the impact of the two different hedging instruments, forwards and options, by comparing the risk/return characteristics of using these two instruments with the unhedged portfolio selection. Therefore the optimization problem in equation 4 is solved by using the input data, presented in tables 1, 2, and 3. For the case of using forwards, the unhedged and optimally hedged mean/LPM<sub>1</sub>-efficient frontiers are plotted in figure 1. The same has been done for the currency options<sup>20</sup> and the respective frontiers are shown in figure 2 for put at the money, in the money, and out of the money options. Finally, figure 3 exhibits the relations between hedging by forwards and in the money put options.

**Figure 1: Shortfall Risk and Return for International Efficient Portfolios – Unhedged and Optimally Hedged with Currency Forwards**

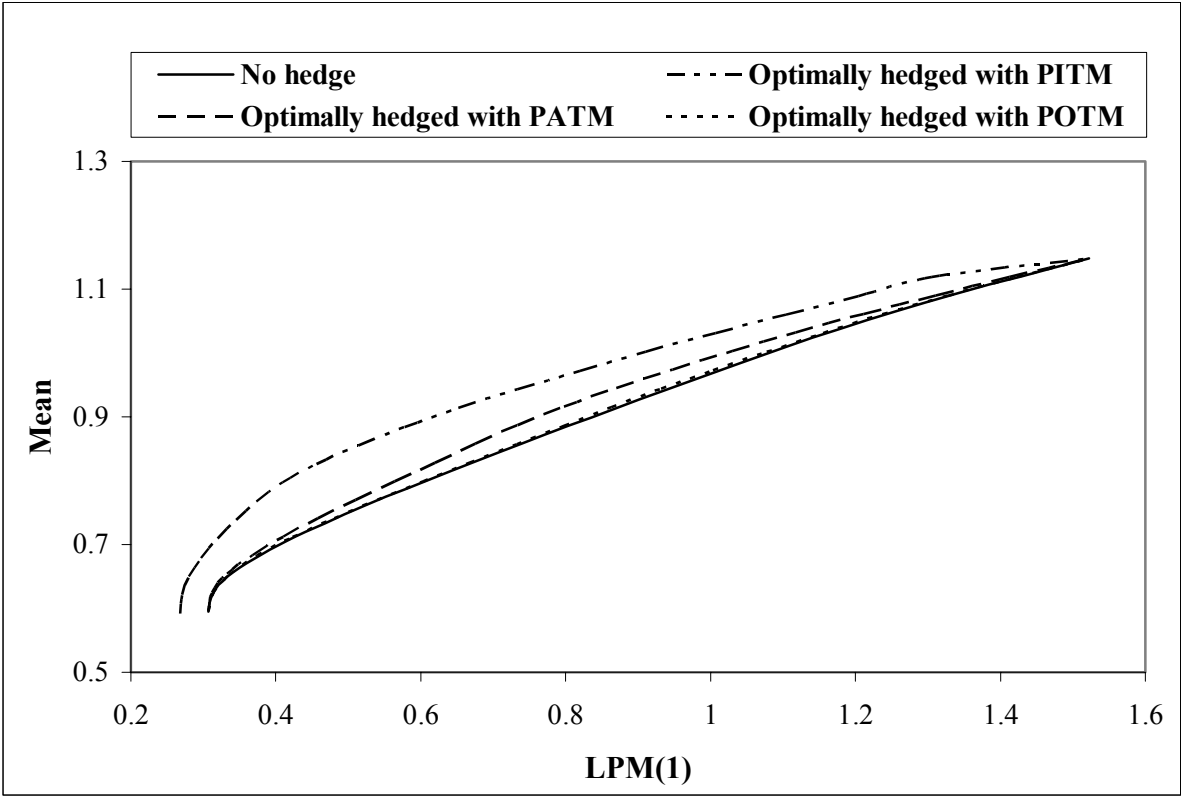


From figure 1 it can be seen that for using forwards as hedging instrument, the optimally hedged efficient frontier clearly dominates the unhedged one. The lowest amount of shortfall expectation in the unhedged case is 0.31, while it is 0.24 for the optimally hedged case with forwards. For all levels of risk, the international frontier represents higher levels of mean return whenever the investor hedges his/her currency exposure by using forwards. It is also obvious that hedging with forwards provides higher benefits, in terms of higher mean returns relative to the unhedged case for the low and medium risk portfolios, rather than for the high risk portfolios.

<sup>20</sup> Noticed that by construction of the model, there cannot be any full hedge for currency puts since they are treated as assets, where the optimization procedure would give the approximate optimal weights.

Regarding the different hedging strategies with put options, figure 2 shows that, while all (in/at/out of the money) put option strategies result in dominant efficient frontiers compared to the unhedged case, the in the money put options indicate the largest vertical shift of the frontier relative to the unhedged one. I.e., from the ex-post point of view, in the money put options provide the best hedging instrument among all the other types. The lowest amount of shortfall expectation for in the money put options as hedging instrument is 0.27. Considering frontiers, also show that there is not much difference between the results of optimal hedging with at the money and especially with out of the money put options compared to unhedged frontier. This is due to the low average observed return of at and out of the money put options which itself is dependent on the spot currency trends of our sample. Therefore, it arises the question on the degree of currency time trend effects on using options as hedge tools which later on will be discussed.

**Figure 2: Shortfall Risk and Return for International Efficient Portfolios – Unhedged and Optimally Hedged with Currency Put Options**

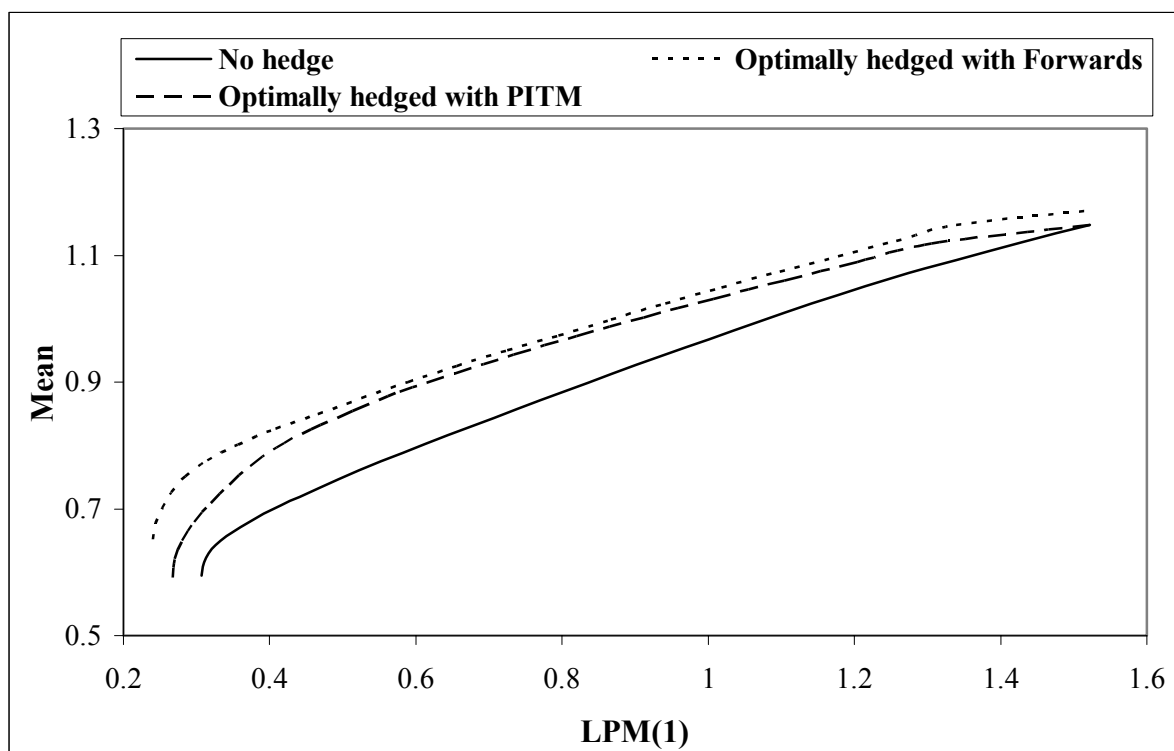


Comparing the hedging effectiveness of forwards and in the money put options, as has been done in table 3, shows that the forwards bring a better hedge performance for all possible portfolios than the in the money put options. However, while the additional benefits in terms of additional mean returns from the forwards hedging relative to the in the money put option hedging is relatively high for low risk portfolios, there are no big differences for the two hedging instruments regarding medium and high risk portfolios

To check the stability of these results in order to implement them in portfolio management, in the following we will have to look at these strategies in an ex-ante framework. Additionally in order to check for the effects of currency trends in using options we will make sub-sample analysis and see how the different types of options can better off the international investor during different financial cycles.



**Figure 3: Shortfall Risk and Return for International Efficient Portfolios – Unhedged and Optimally Hedged with Currency Forwards and Optimally Hedged with Currency Put In the Money Options**



## 4.2 Portfolio Compositions and Performance of the Different Strategies

In order to gain a more precise view of the extent of the diversification potential of the two types of hedging instruments, this section analyzes two selected portfolios in more detail: the minimum risk portfolio (MRP) and tangency portfolio (TP). MRP stands for the portfolio which gives the minimum level of risk, in terms of shortfall expectation. TP represents the portfolio for which the Sortino-ratio<sup>21</sup> has been maximized, i.e. the portfolio with the highest risk adjusted return. In this sense, the percentage of the monthly mean returns and shortfall expectations of the MRP and TP are provided in the following tables 4 and 5. Finally all strategies were evaluated by LPM measure and the related Sortino-ratios, respectively.

The results tabulated in tables 4 and 5, confirm those findings from the efficient frontier analyses in the previous section. Considering first the MRP, it is obvious, that the optimal hedge with currency forwards provides the best MRP, i.e. the MRP with the lowest risk (LPM). Also, the optimal hedge with in the money currency put option provides a considerable risk reduction relative to the unhedged MRP. However, the risk reduction of the LPM through currency forwards is of more extend. While the currency forward provides a decrease in risk relative to the unhedged MRP of about 21% the risk reduction through the in the money put option is only about 13%. Also interesting, while the risk reduction through the optimal hedge with currency forwards is accompanied by an increase in mean return, the op-

<sup>21</sup> The Sortino-ratio,  $SR = (E(R_p) - r_f) / LPM_1$ , for mean/LPM optimization is similar to the Sharp-ratio in the mean/variance framework and was introduced by *Sortino/Price* (1994). *Sortino/van der Meer* (1991) described the downside deviation (below target semi-deviation) and the reward to semi-variability ratio ( $R/SI$ ) as criteria for capturing the essence of downside risk. Sortino continued contributing in the area of performance measurement, e. g. *Sortino/Price* (1994), which are all following to the *Roy* (1952) safety-first technique and computed by maximizing a reward to variability ratio.

timal hedge with in the money put options has no effect on the mean return of the MRP. This also explains the considerable increase in the Sortino-ratio when one optimally hedges with currency forwards. Finally, using at the money and out of the money currency put options has no effect on the MRP, i.e. here the option weights are zero.

**Table 4: Ex-post Risk/Return Profiles of the MRP and TP – Unhedged and Optimally Hedged with Currency Forwards**

	Unhedged			Optimally Hedged with Forwards		
	<i>Mean</i>	<i>LPM</i>	SR	<i>Mean</i>	<i>LPM</i>	SR
MRP	0.596	0.306	0.520	0.650	0.241	0.898
TP	0.687	0.386	0.650	0.742	0.273	1.099

*Notes:* The table provides the mean return (in % p.m.), the first order lower partial moments (in % p.m.) to the risk free interest rate as target, and the Sortino-ratio of the different strategies in the ex-post framework. MRP represents the international minimum risk portfolio and TP is the international tangency portfolio. Results are computed by using the whole sample of observation from January 1985 until December 2002.

**Table 5: Ex-post Risk/Return Profiles of the MRP and TP – Optimally Hedged with Currency Put Options**

	Optimally Hedged with PATM			Optimally Hedged with PITM			Optimally Hedged with POTM		
	<i>Mean</i>	<i>LPM</i>	SR	<i>Mean</i>	<i>LPM</i>	SR	<i>Mean</i>	<i>LPM</i>	SR
MRP	0.596	0.306	0.520	0.596	0.267	0.579	0.596	0.306	0.520
TP	0.687	0.386	0.650	0.686	0.325	0.769	0.688	0.386	0.651

*Notes:* The table provides the mean return (in % p.m.), the first order lower partial moments (in % p.m.) to the risk free interest rate as target, and the Sortino-ratio of the different strategies in the ex-post framework. MRP represents the international minimum risk portfolio and TP is the international tangency portfolio. Results are computed by using the whole sample of observation from January 1985 until December 2002.

Considering the TP, again the optimal hedge with at the money and out of the money put options has nearly no effect on TP performance compared to the unhedged case. On the other hand the use of currency forwards as hedging instrument, results in a substantial increase in TP performance compared to the unhedged case. This increase is induced by an increase in mean return and a decrease in risk. The same, however to lower extend, can be observed for the optimal hedged TP using in the money currency put options. The TP performance, when hedged with in the money options, is also clearly higher than the unhedged TP. However, also in the case of the TP, the forwards provide a better hedge than the put options.

All in all, from the ex-post point of view, there exist clear risk reduction and performance improvement potentials for a German investor, through optimally hedging with currency forwards or (in the money) currency put options.

In table 6, asset weights and hedge-ratios for the respective hedged and unhedged MRPs and TPs are tabulated. Starting with the MRP, the unhedged strategy consists mainly of German Bonds (87.05% of the total wealth). Although there are also investments in the other bond and stock markets, the investment weights for these markets are relatively low.

**Table 6: Optimal Portfolio Weights and Hedge Ratios for Several Hedged and Unhedged MRPs and TPs**

	Stock Markets					Bond Markets					Derivative Markets				
	UK	CH	JP	USA	GER	UK	CH	JP	USA	GER	UK	CH	JP	USA	GER
<b>Unhedged Portfolio Strategies</b>															
<b>MRP</b>	0.00	2.99	0.00	1.67	0.78	0.40	5.14	1.01	0.96	87.05	-	-	-	-	-
<b>TP</b>	0.00	15.27	0.00	0.18	0.00	12.89	0.00	0.00	0.00	71.66	-	-	-	-	-
<b>Optimally Hedged Portfolio Strategies with Forwards</b>															
<b>MRP</b>	0.00	4.69	0.00	0.42	2.10	0.00	25.50	27.39	13.05	26.85	-	-	-	-	-
	(0.00)	(89.90)	(0.00)	(33.40)	(-)	(0.00)	(98.57)	(100.00)	(100.00)	(-)	-	-	-	-	-
<b>TP</b>	0.00	10.04	0.00	0.91	0.00	4.93	4.62	44.24	27.22	8.04	-	-	-	-	-
	(0.00)	(100.00)	(0.00)	(100.00)	(-)	(0.00)	(100.00)	(100.00)	(100.00)	(-)	-	-	-	-	-
<b>Optimally Hedged Portfolio Strategies with PATM</b>											<b>(Optimal Weights of PATM)</b>				
<b>MRP</b>	0.00	2.99	0.00	1.66	0.78	0.40	5.14	1.02	0.96	87.05	0.00	0.00	0.00	0.00	-
<b>TP</b>	0.00	15.27	0.00	0.18	0.00	12.89	0.00	0.00	0.00	71.66	0.00	0.00	0.00	0.00	-
<b>Optimally Hedged Portfolio Strategies with PITM</b>											<b>(Optimal Weights of PITM)</b>				
<b>MRP</b>	0.41	3.73	0.00	1.03	0.93	0.05	23.16	18.22	19.85	29.57	0.00	1.10	0.91	1.04	-
<b>TP</b>	0.00	8.21	0.00	5.33	0.00	17.20	0.00	0.00	4.81	63.08	0.86	0.00	0.00	0.51	-
<b>Optimally Hedged Portfolio Strategies with POTM</b>											<b>(Optimal Weights of POTM)</b>				
<b>MRP</b>	0.00	3.32	0.00	1.42	0.76	0.42	5.86	1.45	1.18	85.56	0.00	0.03	0.00	0.00	-
<b>TP</b>	0.00	15.26	0.00	0.19	0.00	12.87	0.00	0.01	0.00	71.66	0.00	0.00	0.00	0.01	-

**Notes:** The table contains the optimal weights for the different stock and bond markets for the several optimal hedged and unhedged MRPs and TPs from the viewpoint of a German investor that initially invests in the U.K., Switzerland, Japan, U.S. and his/her home country. Weights are reported in percentage and the values in parenthesis are the percentage optimal forward hedge ratios. MRP represents the minimum risk portfolio and TP is the tangency portfolio. Results are computed by using the whole sample of observation from January 1985 until December 2002.

Applying an optimal hedge with forwards results in a much more diversified portfolio. This optimal hedged MRP portfolio, exhibits substantial weights for the Swiss, Japanese, US, and German Bond Markets (together 92.79% of total wealth). Not surprisingly, the investment weights for the respective stock markets are still low. A similar diversification can be observed for the MRP that is optimally hedged with in the money put options. Also this portfolio has substantial weights on four of the five bond markets, while the amount of investment in the stock markets is still low. The other two put option hedging strategies result in nearly or exactly the same investment weights like the unhedged MRP, again indicating, that hedging via at and, out of the money options cannot improve the MRP of the German investors.

Considering the TP, it is interesting that the unhedged TP is relatively undiversified. Like for the unhedged MRP, the highest investment weight is given to German Bonds (71.66%). UK Bonds and Swiss Stocks also exhibit substantial weights (12.89% and 15.27% of total wealth), while the weights for all other markets are neglectable. Again this poor diversification is not changed by using at and out of the money put options for optimal hedging the TP. On the other hand, the in the money put options lead to a more diversified portfolio, while the diversification is still not broad. The TP hedge with currency forwards leads to a good diversification for the bond markets with a substantial weight for Swiss stocks (10.04% of total wealth).

Along with the optimal stock and bond market weights, table 6 shows the optimal option weights for the different hedging strategies. However the optimal option weights do not directly show how much of the respective foreign currency exposure is actually hedged. For this purpose table 7 provides the aggregated investment weights, i.e. the investment weights for stocks plus bonds of each country, as well as the aggregated hedge ratios for the case of forwards and in the money put options, i.e. the relative amount of the respective foreign currency exposure which is hedged.

**Table 7: Optimal (Aggregated) Investment Weights and Hedge Ratios for MRP and TP – Optimal Hedged with Forwards or In the Money Put Options**

		UK	CH	JP	USA
MRP	hedged with forwards	0.00	30.19	27.39	13.47
		(0)	(97)	(100)	(98)
	hedged with in the money puts	0.46	26.89	18.22	20.88
		(0)	(82)	(99)	(99)
TP	hedged with forwards	4.93	14.66	44.24	28.13
		(0)	(100)	(100)	(100)
	hedged with in the money puts	17.20	8.21	0.00	10.14
		(100)	(0)	(0)	(100)

*Notes:* All numbers are in percent. The numbers in the brackets are the aggregated hedge ratios in the case of currency forwards and currency in the money put options, and above of them are the related aggregated investment weights.

From table 7, it is obvious that the relatively low weights of in the money put options for the MRP and TP (see table 6) indicate very high hedge ratios, ranging between 82% till 100% of the respective initial foreign currency exposure. Comparing the optimally hedged MRP with forwards and in the money put options, clarifies that the aggregated investment weights for the different countries and especially the respective hedge ratios are relatively similar. In both cases the foreign currency exposure for each country is nearly fully hedged.

For the TP the optimal hedge via forwards and in the money put options clearly provide different aggregated investment weights for the different countries. However, also here the currency exposures for the both cases are mostly fully hedged.

To check these results and to compare the degree of advantage or disadvantage of using the two different types of hedging strategies (options vs. forwards), a back-test procedure is applied in the next section. This will help us to see how an investor would imply these opportunities when he is faced with these two possibilities and specially which of the hedging instruments statistically would improve his/her portfolio performance and dominates the others.

## **5 Ex-Ante Analysis and the Potential Diversification Benefits of Currency Risk Hedging**

### **5.1 Design, Structure, and Performance Measurement of Different Types of Portfolio Strategies under Different Scenarios**

The ex-ante evaluation investigates the consistency of the results of the proposed strategies in the ex-post outlook and checks the related impact within the time horizon. This evaluation is a fundamental tool for a portfolio manager as it provides practical advice for decision makers by checking the results in a out of sample framework. Therefore the back-ward testing procedure introduced by *Eun/Resnick* (1994) and *Levy/Lim* (1994) for both strategies, MRP and TP is applied.

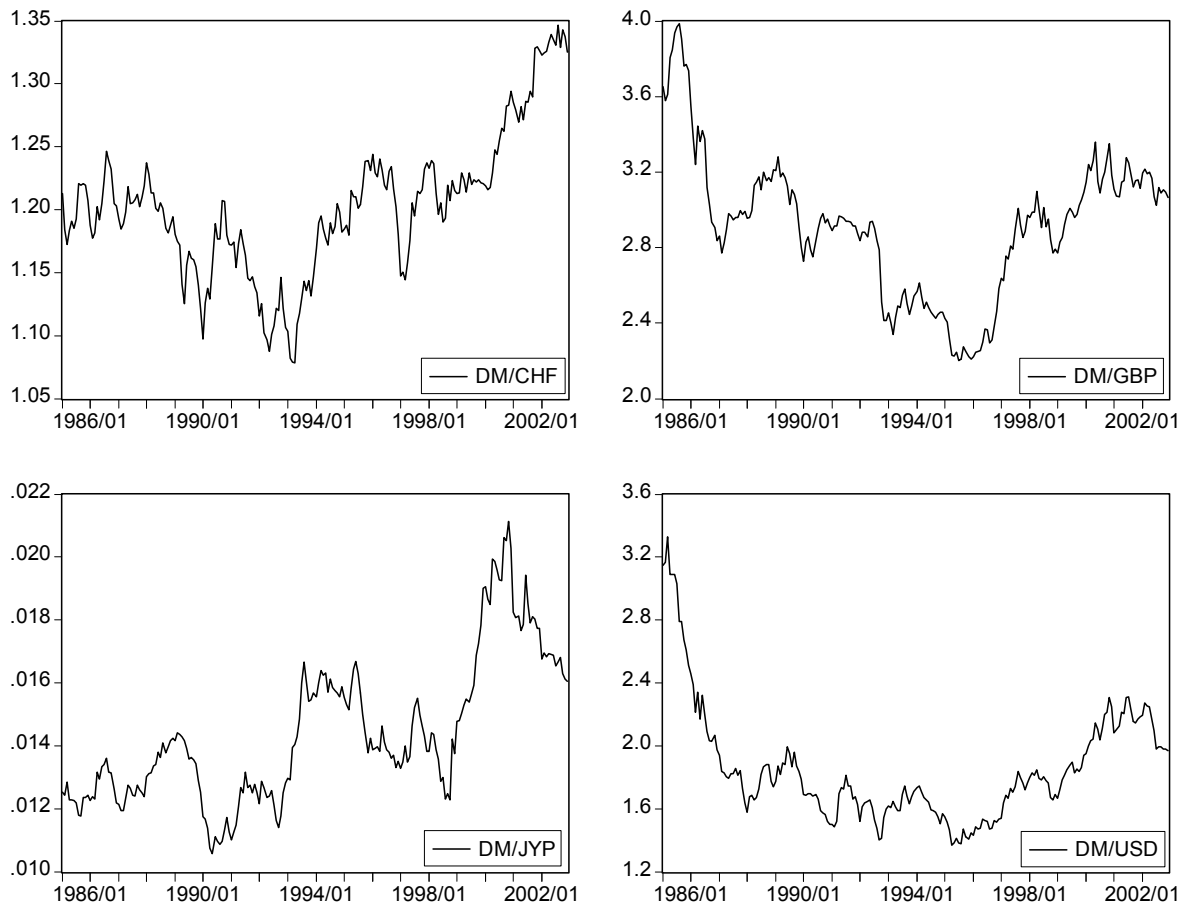
This is done by, first defining an appropriate estimation period length. In the estimation period the optimal weights for the different strategies are estimated by ordinary mean/LPM optimization. Then, the optimal weights are applied to the first period (out of sample period, in our case is one month) which follows the estimation period and the returns of the related portfolios are determined. This computation will be repeated by following the sliding window method, till the last observation will be included in the estimation procedure. This means, the estimation period is shifted one month forward, the respective portfolio weights are recalculated for the new estimation period and then applied for the next out of sample period, and so on. The resulting out of sample returns and shortfalls, which can be regarded as independent investment decisions, can be applied to evaluate independently all these different types of strategies.

Since by construction the return of the put options are currency trend dependence and in our sample horizon the currency time trend shows two different distinguishable types of time trend, we will also check the results for these specific sub-periods. In this way the stability of our results due to currency movements during different financial cycles and global trends can be analyzed and even we will have a bridge to these effects on the forward basis. Therefore the ex-ante evaluation also will be done for the two sub-periods where different scenarios of currency trend will be discussed and then the computed out of sample information will be applied for statistically testing for the existence of any improvement through hedging against the currency exposure.

As it is shown in Figure 4, till September 1995 the German Deutsche Mark had appreciation against the foreign currencies. These trends afterwards have opposite fluctuations and the depreciation of local currency - German Deutsche Mark - started. So we take this month as the breaking point for our sub-periods and divide the total 168 out of sample observation to first,

January 1989 to September 1995 and second, October 1995 till December 2002. Analyzing these results will give the answer to the degree of time dependence of the currency trend and its effect on the appropriate choice among risk controlling strategies.

**Figure 4: Spot Exchange Rate**



In tables 8 and 9 the average return, expected short-fall and the Sortino-ratio for the both strategies in three different scenarios tabulated. For the MRP, results show that optimally forward hedged portfolio brings a significant decrease in the amount of shortfall risk compare to the unhedged portfolio. In the money and out of the money put options also have a lower amount of risk compare to the unhedged portfolio but to a lower extend than forwards. Forward hedged portfolio brings 23% risk reduction when in the money and out of the money puts have only 1.9% and 1.7% decreasing power. This indicates that hedging would make a better off for the investor who searches for the minimum risk portfolio compare to doing nothing. For forwards the risk reduction is accompanied by a significant increase in the portfolio mean return which is not the case for the currency puts. Therefore we can see the higher Sortino-ratio for forward hedged portfolio than the unhedged one. In the case of tangency portfolio (TP), one can see that forward hedged has approximately four times higher Sortino-ratio compare to the unhedged one which is due to the higher amount of portfolio mean return, strengthened by lower degree of short-fall expectation. The Sortino-ratio difference for the put in the money option compared with the unhedged one is very low. Here we have a higher mean return but also higher shortfall risk which induced in a lower performance improvement for the in the money put options. At the money and out of the money puts have no word in this regard.

Simple comparison of two types of strategies show that in general minimum risk portfolio strategy gives a better choice than tangency portfolio, since besides of lower amount of short-fall risk, it also gives higher performance according to the higher Sortino-ratio, which contradicts the ex-post results.

**Table 8: Expectation of the Portfolio Returns and the Shortfall Risk in an Ex-Ante Framework**

→ → First Scenario (January 1989 – December 2002)						
	Unhedged			Optimally Hedged with Forwards		
	<i>Mean</i>	<i>LPM</i>	<i>SR</i>	<i>Mean</i>	<i>LPM</i>	<i>SR</i>
<i>MRP</i>	0.580	0.365	0.347	0.700	0.296	0.834
<i>TP</i>	0.581	1.054	0.121	0.819	0.536	0.682
→ → Second Scenario (January 1989 – September 1995)						
	Unhedged			Optimally Hedged with Forwards		
	<i>Mean</i>	<i>LPM</i>	<i>SR</i>	<i>Mean</i>	<i>LPM</i>	<i>SR</i>
<i>MRP</i>	0.614	0.458	-0.010	0.808	0.394	0.482
<i>TP</i>	0.374	1.487	-0.164	0.798	0.674	0.267
→ → Third Scenario (October 1995 – December 2002)						
	Unhedged			Optimally Hedged with Forwards		
	<i>Mean</i>	<i>LPM</i>	<i>SR</i>	<i>Mean</i>	<i>LPM</i>	<i>SR</i>
<i>MRP</i>	0.548	0.276	0.912	0.597	0.200	1.504
<i>TP</i>	0.771	0.641	0.752	0.839	0.400	1.355

Notes: The table provides the mean return, first order of lower partial moments with having the risk free interest rate as the target of having shortfall risk and the sortino ratio of different strategies in an ex-post framework. MRP represents the minimum risk international portfolio, regarding that risk is introduced by first order of lower partial moments and TP is the international tangency portfolio. For the calculation, in the First Scenario the 168 monthly out-of-sample observations of the individual return time series from January 1989 until December 2002 have been used, in the Second Scenario the sub-sample - 82 - monthly out-of-sample observations of the individual return time series from January 1989 until September 1995 have been implemented and for the Third Scenario the sub-sample - 86 - monthly out-of-sample observations of the individual return time series from October 1995 until December 2002 have been applied.

Considering the results of two sub-samples show that the amount of the portfolio mean return, shortfall risk and Sortino-ratio in the first sub-sample is considerably poorer than the second one. When we look at the global trend of currency exchange rate, this indicates that in the appreciation period of local currency, composing an international portfolio selection will bring much lower level of benefit than in the depreciation cycles. This can be interpreted as during the blooming period, the international investors would gain lower benefit compare to the depreciation currency period which actually accords with the economical interpretations.

More interesting is that, hedging by forwards during the blooming cycle of local currency would be much more beneficial than in the depreciation period. By comparing the percentage of improvement with the no hedged portfolio in the two sub-sample periods, one can see that in the first sub-sample this improvement on average equals to 200% where in the second sub-period this amount is around 45%.

**Table 9: Expectation of the Portfolio Returns and the Shortfall Risk in an Ex-Ante Framework**

→ → First Scenario (January 1989 – December 2002)									
	Optimally Hedged with PATM			Optimally Hedged with PITM			Optimally Hedged with POTM		
	<i>Mean</i>	<i>LPM</i>	SR	<i>Mean</i>	<i>LPM</i>	SR	<i>Mean</i>	<i>LPM</i>	SR
<i>MRP</i>	0.572	0.372	0.319	0.547	0.358	0.262	0.571	0.359	0.329
<i>TP</i>	0.508	1.172	0.046	0.585	1.078	0.122	0.228	1.275	-0.176

→ → Second Scenario (January 1989 – September 1995)									
	Optimally Hedged with PATM			Optimally Hedged with PITM			Optimally Hedged with POTM		
	<i>Mean</i>	<i>LPM</i>	SR	<i>Mean</i>	<i>LPM</i>	SR	<i>Mean</i>	<i>LPM</i>	SR
<i>MRP</i>	0.596	0.470	-0.049	0.560	0.481	-0.122	0.612	0.457	-0.015
<i>TP</i>	0.228	1.777	-0.220	0.394	1.548	-0.145	-0.334	1.949	-0.489

→ → Third Scenario (October 1995 – December 2002)									
	Optimally Hedged with PATM			Optimally Hedged with PITM			Optimally Hedged with POTM		
	<i>Mean</i>	<i>LPM</i>	SR	<i>Mean</i>	<i>LPM</i>	SR	<i>Mean</i>	<i>LPM</i>	SR
<i>MRP</i>	0.550	0.281	0.908	0.536	0.240	0.997	0.534	0.265	0.896
<i>TP</i>	0.774	0.595	0.803	0.767	0.630	0.748	0.765	0.633	0.741

Notes: The table provides the mean return, first order of lower partial moments with having the risk free interest rate as the target of having shortfall risk and the sortino ratio of different strategies in an ex-post framework. MRP represents the minimum risk international portfolio, regarding that risk is introduced by first order of lower partial moments and TP is the international tangency portfolio. For the calculation, in the First Scenario the 168 monthly out-of-sample observations of the individual return time series from January 1989 until December 2002 have been used, in the Second Scenario the sub-sample - 82 - monthly out-of-sample observations of the individual return time series from January 1989 until September 1995 have been implemented and for the Third Scenario the sub-sample - 86 - monthly out-of-sample observations of the individual return time series from October 1995 until December 2002 have been applied.

In the case of options, one can see that the total performance, average portfolio return and the shortfall risk in the first sub-sample is far below than the second one, which brings the same economical-financial interpretation. In the local currency depreciation period building an international diversified portfolio brings more benefit than in the blooms of the local currency. But in general in the ex-ante perspective, using options compare with forwards is not favorable.



**Table 10: Average Optimal Portfolio Weights in an Ex-Ante Analysis Framework**

	Stock Markets					Bond Markets					Derivative Markets				
	UK	CH	JP	USA	GER	UK	CH	JP	USA	GER	UK	CH	JP	USA	GER
<b>Unhedged Portfolio Strategies</b>															
<b>MRP</b>	0.28	1.35	0.59	0.66	2.38	3.56	14.37	2.28	2.67	71.87	-	-	-	-	-
<b>TP</b>	3.54	17.19	4.92	8.18	5.52	12.16	12.23	12.59	6.23	17.44	-	-	-	-	-
<b>Optimally Hedged Portfolio Strategies with Forwards</b>															
<b>MRP</b>	0.84	1.80	1.52	2.65	1.47	3.45	20.90	30.96	22.32	14.11	-	-	-	-	-
	(24.35)	(34.15)	(35.14)	(43.01)	(-)	(38.58)	(41.98)	(48.66)	(48.45)	(-)					
<b>TP</b>	0.86	6.99	3.59	9.85	1.75	10.37	15.69	13.48	27.03	10.39	-	-	-	-	-
	(14.36)	(34.41)	(35.84)	(49.13)	(-)	(27.01)	(36.34)	(46.11)	(47.56)	(-)					
<b>Optimally Hedged Portfolio Strategies with PATM</b>										<b>Optimal Weights of PATM</b>					
<b>MRP</b>	0.28	1.68	0.60	0.68	2.40	3.72	14.30	2.58	2.73	70.96	0.002	0.013	0.019	0.029	-
<b>TP</b>	3.47	16.87	4.94	7.92	5.43	12.11	12.21	12.53	6.21	17.40	0.073	0.081	0.488	0.272	-
<b>Optimally Hedged Portfolio Strategies with PITM</b>										<b>Optimal Weights of PITM</b>					
<b>MRP</b>	0.18	1.73	0.63	0.98	2.16	2.76	12.77	2.90	3.36	72.18	0.047	0.072	0.058	0.148	-
<b>TP</b>	3.31	16.15	4.98	8.01	5.12	11.87	12.25	12.28	6.29	17.23	0.845	0.261	0.401	0.985	-
<b>Optimally Hedged Portfolio Strategies with POTM</b>										<b>Optimal Weights of POTM</b>					
<b>MRP</b>	0.15	1.34	0.58	0.63	2.23	2.70	13.06	2.09	2.68	74.52	0.0004	0.013	0.0008	0.004	-
<b>TP</b>	3.43	16.96	4.89	8.00	5.47	12.10	12.29	12.61	6.21	17.33	0.018	0.471	0.048	0.174	-

Notes: The table contains the average optimal weights of stock indices in an ex-ante framework, for German investor that initially invests in United Kingdom, Switzerland, Japan U.S. and home country. Weights are reported in percentage and the values in parenthesis are the percentage optimal forward hedge ratios. MRP represents the minimum risk international portfolio, regarding that risk is introduced by first order of lower partial moments and TP is the international tangency portfolio. Results are computed by using the 168 monthly out-of-sample observations from January 1989 until December 2002.

The average optimal weights for the stock and bond markets as well as the hedge ratios of the both MRP and TP are presented in table 10. For the MRP, the unhedged portfolio is poorly diversified and mainly contains the German (72%) and partly the Swiss bonds (14%). Using currency put options does not change this feature which fits with our previous results. Still the main weights belong to the German and then Swiss bonds and the rest of the markets have neglectable proportion of the total investment. But using the optimally forward hedged strategy gives a much more diversified portfolio where four of the five bond markets have clear weights. Obviously still stocks have lower weights due to their higher amount of risk.

For the TP the unhedged portfolio gives a more diversified portfolio in terms of stock and bond markets. The Swiss stocks have now 17% and in general 40% of total amount of investment dedicated to the stock markets. Also all the bond markets now have more diversified portions of total wealth. Hedging by forwards changes this pattern, as Swiss stocks weight reduces from 17% to 7% and for the UK from 3.54% to 0.86%. Bonds compose 77% of the whole tangency portfolio where it is 30 to 50% hedged against the currency exposure. Hedging by puts does not change the prototype of tangency portfolio from the unhedged one which satisfies our previous results.

## **5.2 Stochastic Dominance and Strategy Performance in an Ex-Ante Framework**

The concept of stochastic dominance is quiet old. Hence it is just after 1969, with four independent papers by *Hadar/Russell* (1969), *Hanoch/Levy* (1969), *Rothschild/Stiglitz* (1970) and *Whitmore* (1970), became widely popular in various area of finance and economics. Because of its correspondence with several types of utility functions and its ability to avoid certain criticisms which are normally exist in the mean-target/risk dominance models, it has been enormously used for the decision making process and investment analysis under uncertainty. As *Porter* (1974) showed, if F dominates G by second degree of dominance then F dominates G by the mean-target semi-variance model<sup>22</sup>. *Levy/Kroll* (1978), *Bawa* (1978, 1982) and *Levy* (1992, 1998) discuss this when the portfolio also includes a risk less asset since without considering a risk less asset, this measure in general ends up to a relatively large number of efficient sets. Here in order to evaluate the performance improvement of the ex-ante strategies for the purpose of decision making, we do the SSD test for both with and without the risk-free asset by using the classification algorithm of *Levy/Kroll* (1979) with the extension by *Levy* (1992, 1998).

Results show that for the German investor the second degree of stochastic dominance without considering a risk-less asset contains, in the first scenario 7, in the second scenario 3 and in the third scenario 9 portfolios. To be more critical by considering a risk less asset, one can see that the only non-dominated portfolio is the minimum risk portfolio which has been optimized by using forwards in first and second scenarios. In the third scenario the optimally forward hedged tangency portfolio and minimum risk portfolio are the non-dominated strategies which can be offered to the decision maker.

---

<sup>22</sup>The  $\alpha$ -t efficient set for  $\alpha=2$  is a subset of the second degree stochastic dominance efficient set. Fishburn (1977) extends these results to the general class of  $\alpha$ -t models using first, second and third degree stochastic dominance relationships. When the appropriate derivatives of an investor's utility function exist, the first, second and third degree stochastic dominance correspond respectively to  $u' \geq 0$ ,  $u'' \geq 0$  and  $u''' \leq 0$ , and  $u' \geq 0$ ,  $u'' \leq 0$ ,  $u''' \leq 0$ .

These results are comparable to our previous discussion on the average amount of international performance improvement due to hedging the currency risk in different global trends. As we see in the local currency depreciation period the optimal forwards in both types of portfolio selections dominate other types of portfolio selections.

**Table 11: Second Degree Stochastic Dominance**

→ → First Scenario (January 1989 – December 2002)				
	No Hedging		Optimally Hedged with Forwards	
	<i>MRP</i>	<i>TP</i>	<i>MRP</i>	<i>TP</i>
<i>SSD</i>	✓	✓	✓	✓
<i>SSDR</i>			✓	

→ → Second Scenario (January 1989 – September 1995)				
	No Hedging		Optimally Hedged with Forwards	
	<i>MRP</i>	<i>TP</i>	<i>MRP</i>	<i>TP</i>
<i>SSD</i>	✓		✓	
<i>SSDR</i>			✓	

→ → Third Scenario (October 1995 – December 2002)				
	No Hedging		Optimally Hedged with Forwards	
	<i>MRP</i>	<i>TP</i>	<i>MRP</i>	<i>TP</i>
<i>SSD</i>	✓	✓	✓	✓
<i>SSDR</i>			✓	✓

Notes: The table gives the dominance strategies which provide the statistically performance improvement for the international portfolio manager. *MRP* represents the minimum risk international portfolio, regarding that risk is introduced by first order of lower partial moments and *TP* is the international tangency portfolio. For the calculation, in the First Scenario the 168 monthly out-of-sample observations of the individual return time series from January 1989 until December 2002 have been used, in the Second Scenario the sub-sample - 82 - monthly out-of-sample observations of the individual return time series from January 1989 until September 1995 have been implemented and for the Third Scenario the sub-sample - 86 - monthly out-of-sample observations of the individual return time series from October 1995 until December 2002 have been applied.

**Table 12: Second Degree Stochastic Dominance**

→ → First Scenario (January 1989 – December 2002)						
	Optimally Hedged with PATM		Optimally Hedged with PITM		Optimally Hedged with POTM	
	<i>MRP</i>	<i>TP</i>	<i>MRP</i>	<i>TP</i>	<i>MRP</i>	<i>TP</i>
<i>SSD</i>			✓	✓	✓	
<i>SSDR</i>						
→ → Second Scenario (January 1989 – September 1995)						
	Optimally Hedged with PATM		Optimally Hedged with PITM		Optimally Hedged with POTM	
	<i>MRP</i>	<i>TP</i>	<i>MRP</i>	<i>TP</i>	<i>MRP</i>	<i>TP</i>
<i>SSD</i>					✓	
<i>SSDR</i>						
→ → Third Scenario (October 1995 – December 2002)						
	Optimally Hedged with PATM		Optimally Hedged with PITM		Optimally Hedged with POTM	
	<i>MRP</i>	<i>TP</i>	<i>MRP</i>	<i>TP</i>	<i>MRP</i>	<i>TP</i>
<i>SSD</i>	✓	✓	✓	✓		✓
<i>SSDR</i>						

Notes: The table gives the dominance strategies which provide the statistically performance improvement for the international portfolio manager. MRP represents the minimum risk international portfolio, regarding that risk is introduced by first order of lower partial moments and TP is the international tangency portfolio. For the calculation, in the First Scenario the 168 monthly out-of-sample observations of the individual return time series from January 1989 until December 2002 have been used, in the Second Scenario the sub-sample - 82 - monthly out-of-sample observations of the individual return time series from January 1989 until September 1995 have been implemented and for the Third Scenario the sub-sample - 86 - monthly out-of-sample observations of the individual return time series from October 1995 until December 2002 have been applied.

## 6 Conclusion

Our experimental study explored the notion of currency hedging by using European put options and tried to compare two different risk controlling strategies in the various portfolio selections with using the lower partial moment methodology as the conception of measuring currency exposure risk. There has been a lot of intuitive reasoning in favor of the existence of asymmetrical return in our international diversified stock and bond portfolio, required the application of our methodology. The study contains five major financial markets of as United Kingdom, Switzerland, Japan, Germany and United States for a time period of January 1985 until December 2002.

The performance evaluation consists of two different perspectives, ex-post and ex-ante while the composition of some specific portfolio strategies in detail has been discussed. Gains in the ex-post analysis shows that only put in the money options present a comparable result with optimally forward hedged portfolios. The other puts have basically no noticeable effect. Considering the composition of portfolio in case of using in the money options and forwards show that using any of these hedge tools brings a much more diversified selection of stock and bond markets than no hedging strategy. The optimal option weights imply that put in the money option strategy is more active than at the money or out of the money put options which implies the dependency of put strategy on the level of strike price. Very interesting notation is that just through dedicating a very small part of investment in the options, the same amount of currency exposure risk can be hedged, as one uses the optimally forward hedging. Of course, options then have the advantage of giving an insurance position rather than a simple hedge.

In the out-of-sample study, the optimally forwards hedge in general presents a much better performance than any types of puts. Most of the times the gains of the higher level of portfolio mean returns due to using, in and out of the money put options substituted by higher level of shortfall risk which causes a lower improvement than the case of using forwards. The global trend and its quantitative effect on the degree of performance improvement for the both types of hedge instruments - forwards and options - have been discussed. The analysis shows that the potential diversification benefit through controlling currency exposure risk in the appreciation period of local currency significantly improves, mostly because of higher level of portfolio returns. Whilst during the depreciation cycle, this improvement becomes less than half compare to the blooming period mainly through the risk-reduction potential.

Overall, through considering our findings in the ex-ante perspective, the optimally forward hedged minimum risk portfolio dominates all other strategies while in the depreciation of local currency, this together with the forward hedged tangency portfolio selection would characterize the dominant portfolio strategies.

## References

- Adler, M. and B. Prasad (1992): On Universal Currency Hedges. *Journal of Financial and Quantitative Analysis*, 27, pp. 19-37.
- Adler, M. and D. Simon (1986): Exchange Rate Surprises in International Portfolios. *Journal of Portfolio Management*, 12, pp. 44-53.
- Bawa, V. S. (1975): Optimal Rules for Ordering Uncertain Prospects. *Journal of Financial Economics*, 2, pp. 95-121.
- Bawa, V. S. (1978): Safety First, Stochastic Dominance and Optimal Portfolio Choice. *Journal of Financial and Quantitative Analysis*, 13, pp. 255-271.
- Biger, N. and J. Hull (1983): The Valuation of Currency Option Hedges. *Journal of Financial Economics*, 10, pp. 178-201.
- Black, F. (1989): Universal Hedging: Optimizing Currency Risk and Reward in International Equity Portfolios. *Financial Analysts Journal*, 8, pp. 16-22.
- Black, F. (1990): Equilibrium Exchange Rate Hedging. *The Journal of Finance*, 45, pp. 899-907.
- Bookstaber, R. and R. Clarke (1984): Option Portfolio Strategies: Measurement and Evaluation. *Journal of Business* 57, pp. 469-492.
- Bookstaber, R. and R. Clarke (1985): Problems in Evaluating the Performance of Portfolios with Options. *Financial Analysts Journal*, January/February, pp. 48-62.
- Bugar, G. and R. Maurer (2002): International Equity Portfolios and Currency Hedging, The View Point of German and Hungarian Investors. *Astin Bulletin*, 32, No.1. pp. 171-197.
- Conover, J. A. and D. A. Dubofsky (1995): Efficient Selection of Insured Currency Positions, Protective Puts versus Fiduciary Calls. *Journal of Financial and Quantitative Analysis*, 30, pp. 295-312.
- Eaker, M. R. and D. M. Grant (1990): Currency Hedging Strategies for Internationally Diversified Equity Portfolios. *Journal of Portfolio Management*, 31, 30-32.
- Eun, C. S. and B. G. Resnick (1988): Exchange Rate Uncertainty, Forward Contracts and International Portfolio Selection. *Journal of Finance*, 43, pp. 197-215.
- Eun, C. S. and B. G. Resnick (1994): International Diversification of Investment Portfolios, Us and Japanese Perspective. *Management Science*, 40, pp. 140-160.
- Fishburn, P. C. (1977): Mean Risk Analysis with Risk Associated with below Target Returns. *The American Economic Review*, 67, No. 2, pp. 116-126.

- Fishburn, P. C. (1984): Foundation of Risk Measurement: Risk as a Probable Loss. *Management Science*, 30, pp. 116-126.
- Garman, G. and C. Kohlhagen (1983): Foreign Currency Option Values. *Journal of International Money and Finance*, 2, pp. 231-237.
- Glen, J. and P. Jorion (1993): Currency Hedging for International Portfolios. *Journal of Finance*, 48(5), pp. 1865-1886.
- Hanoch, G and Levy, H (1969): The Efficiency Analysis of Choices Involving Risk. *The Review of Economic Studies*, 36, No. 3, pp. 335-346.
- Harlow, W. V. (1991): Asset Allocation in Down-side Risk Framework. *Financial Analysts Journal*, 28, pp. 28-40.
- Harlow, W. V. and R. K. Rao (1989): Asset Pricing in a Generalized Mean Lower Partial Moment Framework, Theory and Evidence. *Journal of Financial and Quantitative Analysis*, 25, pp. 285-309.
- Hsin, C. W., J. Kuo, and C. F. Lee (1994): A New Measure to Compare the Hedging Effectiveness of Foreign Currency Futures versus Options. *The Journal of Futures Markets*, 14, pp. 685-707.
- Jarque, C. M. and A. K. Bera (1987): A Test for Normality of Observations and Regression Residuals. *International Statistical Review*, 55, pp. 163-172.
- Jorion, P. (1985): Bayes-Stein Estimation for Portfolio Analysis, *The Journal of Financial and Quantitative Analysis*, 21, No. 3, pp. 279-292.
- Jorion, P. (1985): International Portfolio Diversification with Estimation Risk. *Journal of Business*, 58, pp. 259-278.
- Larsen, G. A. and B. G. Resnick (2000): The Optimal Construction of Internationally Diversified Equity Portfolio Hedged Against Exchange Rate Uncertainty. *European Financial Management*, 6, pp. 479-519.
- Levy, H. and K. C. Lim (1994): Forward Exchange Bias, Hedging and the Gains from International Diversification of Investment Portfolios. *Journal of International Money and Finance*, 13, pp. 159-170.
- Levy, H. and Markowitz, H. M. and Yoram, K. (1984): Mean-Variance versus Direct Utility Maximization. *The Journal of Finance*, 39, No. 1. pp. 47-61.
- Markowitz, H. M. (1952): Portfolio Selection. *Journal of Finance*, 7, pp. 77-91.
- Roy, A. D. (1952): Safety First and the Holding of Assets. *Econometrica*, 20, pp. 431-439.

- Sarin, R.K. and M. Weber (1993): Risk-value models. *European Journal of Operational Research* 72, pp. 135-149.
- Sortino, F. A. and L. N. Price (1994): Performance Measurement in a Downside Risk Framework. *The Journal of Investing*, 3, pp. 59-64.
- Sortino, F. A. and R. van der Meer (1991): Downside Risk. *Journal of Portfolio Management*, 17, pp. 27-31.
- Weber, M. (1990): Risikoentscheidungskalküle in der Finanzierungstheorie, Stuttgart: Poeschel, 1990.



## Appendix A: Normalizing the Restrictions of the Lower Partial Moment Optimization in Case of Using Options as a Hedge Tool

Using put options as a hedge tool in order to control the currency risk in an international portfolio framework by construction is different from using futures. In order to use the currency option as a hedging tool which gives the investor an insurance against the risk and a type of optional guarantee rather an obligation to sell on a predetermined amount of currency rate, a premium would be required. Therefore the currency option compare to forwards is a costly hedge instrument which gives more flexibility than hedging by forwards. Due to the needed fee, in the optimization procedure our investor considered it as an individual asset which has its own return and costs. So the converted national return  $R_i$  for each financial market during one time interval will be equal to:

$$R_i = R_{i,f} + e_f + R_{i,f} \cdot e_f$$

where  $R_i$  contains not only the observed local currency returns of assets but also contains the local currency returns of the related put options in each specific financial market. Therefore for international portfolio manager each time there will be four more assets - due to having four different markets - which have to be decided to be optimally invested in. Of course this in the case of using some combination of puts will be different, e.g. if the investor want to use both puts, at the money and in the money options, then he has to decide on  $N+8$  assets. Now to normalize the algorithm of optimal investment for having no speculation in currency puts, we have to customize our restrictions in the way that these assets would be bought just in order to make a guarantee for having no downside risk. Hence, the optimal put option weights should be less or equal to the proportion of our wealth invested in each one of financial markets.

Consider as follows; the total wealth converted to foreign currencies would be equal to  $W / SX_t$  for the time interval  $t$ , where  $W$  stands for the total amount of investment. In each foreign market,  $(x_s + x_b) * (W / SX_t)$  is the optimal amount of foreign currency invested in the respective stock and bond markets. Put premiums computed for giving the right to the German investor to put one foreign currency at the end of the month for the pre-specified amount of Deutsche Mark. Therefore the optimal number of puts without having the possibility of speculation due to trading options can be implemented, when the amount of investment in options is less or equal to the amount of investment in the related foreign market. This amount for different types of puts is:

$$(\#_{PATM}) * (W / SX_t), (\#_{PITM}) * (W / SX_t), \text{ or } (\#_{POTM}) * (W / SX_t)$$

The number of puts in one time interval for each case is:

$$x_{PATM} / PATM, x_{PITM} / PITM ; x_{POTM} / POTM$$

So the restriction for having no speculation will be applied as in the following equation:

$$x_s + x_b \geq x_o * (SX / P_o)$$

where  $x_S$ ,  $x_B$  and  $x_O$  are the optimal weights of investing in the each foreign stock, bond and currency option,  $P_O$  is the respective puts premia in the local currency (DM) and  $SX$  is the respective foreign currency spot exchange rate.

In the optimization, different types of puts has been analyzed separately to see that which type of put options would be more beneficial for the German investor as a controlling hedge tool for his currency exposure and results in more favorable insurance position.

## Working Paper Series: Finance & Accounting

- No.108: **Raimond Maurer/Frank Reiner/Steffen Sebastian**, Financial Characteristics of International Real Estate Returns: Evidence from the UK, US, and Germany, May 2003
- No.107: **Anne d’Arcy/Michiyo Mori/Christine Rossbach**, The impact of valuation rules for intangible assets in Japanese and German accounts of listed companies, April 2003
- No.106: **Andreas Hackethal**, German banks – a declining industry?, March 2003
- No.105: **Ingo E. Tschach**, The long term impact of microfinance on income, wages and the sectoral distribution of economic activity, April 2003
- No.104: **Reinhard H. Schmidt/Marco Weiß**, Shareholder vs. Stakeholder: Ökonomische Fragestellungen, January 2003
- No.103: **Ingo E. Tschach**, The Theoretical Derivation of Credit Market Segmentation as the Result of a Free Market Process, March 2003
- No.102: **Samuel Lee/Nina Moisa/Marco Weiss**, Open Source as a Signalling Device – An Economic Analysis, March 2003
- No.101: **Christian Gaber**, Bewertung von Fertigerzeugnissen zu Voll- oder Teilkosten? Ansatz von Forderungen zum Nennwert oder Barwert? Eine agencytheoretische Analyse zur zielkongruenten Performancemessung, December 2002
- No.100: **Oliver Ruß/Günther Gebhardt**, Erklärungsfaktoren für den Einsatz von Währungsderivaten bei deutschen Unternehmen – eine empirische Logit-Analyse, August 2002
- No.99: **Christian Gaber**, Gewinnglättung und Steuerung dezentraler Investitionsentscheidungen bei sich gegenseitig ausschließenden Investitionsprojekten, September 2002
- No.98: **Volker Laux**, On the Value of Influence Activities for Capital Budgeting, September 2002
- No.97: **Gunter Löffler**, Avoiding the rating bounce: Why rating agencies are slow to react to new information, June 2002
- No.96: **Andreas A. Jobst**, Collateralized Loan Obligations (CLOs) – A Primer, December 2002
- No.95: **Günther Gebhardt/Rolf Reichardt/Carsten Wittenbrink**, Accounting for Financial Instruments in the Banking Industry, November 2002
- No.94: **Ulf Herold/Raimond Maurer**, Portfolio choice and estimation risk – A comparison of Bayesian approaches to resampled efficiency, June 2002
- No.93: **Olivia S. Mitchell/David McCarthy**, Annuities for an Ageing World, June 2002
- No.92: **Ulf Herold/Raimond Maurer**, How much foreign stocks? Classical versus Bayesian approaches to asset allocation, June 2002

- No.91: **Gunter Löffler/Patrick F. Panther/Erik Theissen**, Who Knows What When? – The Information Content of Pre-IPO Market Prices, June 2002
- No.90: **Reinhard Hujer/Sandra Vuletic/Stefan Kokot**, The Markov switching ACD model, April 2002
- No.89: **Markus C. Arnold/Robert M. Gillenkirch**, Stock Options as Incentive Contracts and Dividend Policy, April 2002
- No.88: **Anne d'Arcy /Sonja Grabensberger**, The Quality of Neuer Markt Quarterly Reports - an Empirical Investigation, January 2002
- No.87A: **Reinhard H. Schmidt/Ingo Tschach**, Microfinance as a Nexus of Incentives, May 2001
- No.87: **Reinhard H. Schmidt/Ingo Tschach**, Microfinance als ein Geflecht von Anreizproblemen, Dezember 2001 (erscheint in den Schriften des Vereins für Socialpolitik, 2002)
- No.86: **Ralf Elsas/Yvonne Löffler**, Equity Carve-Outs and Corporate Control in Germany, December 2001
- No.85: **Günther Gebhardt/Stefan Heiden/Holger Daske**, Determinants of Capital Market Reactions to Seasoned Equity Offers by German Corporations, December 2001
- No.84: **Hergen Frerichs/Gunter Löffler**, Evaluating credit risk models: A critique and a proposal, October, 2001
- No. 83: **Ivica Dus/Raimond Maurer**, Integrated Asset Liability Modelling for Property Casualty Insurance: A Portfolio Theoretical Approach, October 2001 (erscheint in Handbuch Asset-Liability Management, hrsg. von M. Rudolph u.a.)
- No.82: **Raimond Maurer/Frank Reiner**, International Asset Allocation with Real Estate Securities in a Shortfall-Risk Framework: The Viewpoint of German and US Investors, September 2001
- No.81: **Helmut Laux**, Das Unterinvestitionsproblem beim EVA-Bonussystem, August 2001
- No.80: **Helmut Laux**, Bedingungen der Anreizkompatibilität, Fundierung von Unternehmenszielen und Anreize für deren Umsetzung, July 2001
- No. 79: **Franklin Allen/Douglas Gale**, Banking and Markets, July 2001
- No.78: **Joachim Grammig/Michael Melvin/Christian Schlag**, Price Discovery in International Equity Trading, July 2001
- No.77: **Joachim Grammig/Reinhard Hujer/Stefan Kokot**, Tackling Boundary Effects in Nonparametric Estimation of Intra-Day Liquidity Measures, July 2001
- No.76: **Angelika Esser / Christian Schlag**, A Note on Forward and Backward Partial Differential Equations for Derivative Contracts with Forwards as Underlyings, June 2001
- No.75: **Reinhard H. Schmidt/Marcel Tyrell/Andreas Hackethal**, The Convergence of Financial Systems in Europe, May 2001 (erscheint in: Schmalenbach Business Review, 2002)

- No.74: **Ulf Herold**, Structural positions and risk budgeting - Quantifying the impact of structural positions and deriving implications for active portfolio management, May 2001
- No.73: **Jens Wüstemann**, Mängel bei der Abschlußprüfung: Tatsachenberichte und Analyse aus betriebswirtschaftlicher Sicht, April 2001 (erschieden in: „Der Wirtschaftsprüfer als Element der Corporate Governance“, Zentrum für Europäisches Wirtschaftsrecht, Bonn 2001, S. 25-60)
- No.72: **Reinhard H. Schmidt**, The Future of Banking in Europe, March 2001(erscheint in Kapitalmarkt und Portfolio Management, 2002)
- No.71: **Michael H. Grote/Britta Klagge**, Wie global sind Japans Banken? Die Veränderung institutioneller Bedingungen und ihre Auswirkungen auf die internationale Präsenz japanischer Kreditinstitute, April 2001
- No.70: **Stefan Feinendegen/Eric Nowak**, Publizitätspflichten börsennotierter Aktiengesellschaften im Spannungsfeld zwischen Regelberichterstattung und Ad-hoc-Publizität - Überlegungen zu einer gesetzeskonformen und kapitalmarktorientierten Umsetzung, März 2001 (erscheint in: Die Betriebswirtschaft)
- No.69: **Martin F. Grace/Robert W. Klein/Paul R. Kleindorfer**, The Demand for Homeowners Insurance with Bundled Catastrophe Coverages, March 2001
- No.68: **Raimond Maurer/Martin Pitzer/Steffen Sebastian**, Konstruktion transaktions-basierter Immobilienindizes: Theoretische Grundlagen und empirische Umsetzung für den Wohnungsmarkt in Paris, Februar 2001
- No.67: **Gyöngyi Bugár/Raimond Maurer**, International Equity Portfolios and Currency Hedging: The Viewpoint of German and Hungarian Investors, February 2001 (erscheint in. ASTIN-Bulletin)
- No.66: **Rainer Brosch**, Portfolio-aspects in real options management, February 2001
- No.65a: **Marcel Tyrell/Reinhard H. Schmidt**, Pension Systems and Financial Systems in Europe:A Comparison from the Point of View of Complementarity, July 2001
- No.65: **Marcel Tyrell/Reinhard H. Schmidt**, Pensions- und Finanzsysteme in Europa: Ein Vergleich unter dem Gesichtspunkt der Komplementarität, Februar 2001 (erschieden in gekürzter Fassung in: „Private Versicherung und Soziale Sicherung“, Festschrift zum 60. Geburtstag von Prof. Dr. Dr. h.c. Roland Eisen, hrsg. von H.-C. Mager, H. Schäfer, K. Schröder, Metropolis: Marburg),
- No.64: **Jutta Dönges/Frank Heinemann**, Competition for Order Flow as a Coordination Game, January 2001
- No.63: **Eric Nowak/Alexandra Gropp**, Ist der Ablauf der Lock-up-Frist bei Neuemissionen ein kursrelevantes Ereignis, Dezember 2000 (erschieden in Zeitschrift für betriebswirtschaftliche Forschung, Februar 2002)
- No.62: **Ulrich Kaiser/Andrea Szczesny**, Einfache ökonometrische Verfahren für die Kreditrisikomessung: Verweildauermodelle, Dezember 2000
- No.61: **Ulrich Kaiser/Andrea Szczesny**, Einfache ökonometrische Verfahren für die Kreditrisikomessung: Logit- und Probit-Modelle, Dezember 2000

- No.60: **Andreas Hackethal**, How Unique Are US Banks? - The Role of Banks in Five Major Financial Systems, , December 2000 (erschienen in: Zeitschrift für Nationalökonomie und Statistik, Vol. 221, S. 592-619)
- No.59: **Rolf Elgeti/Raimond Maurer**, Zur Quantifizierung der Risikoprämien deutscher Versicherungsaktien im Kontext eines Multifaktorenmodells, Oktober 2000 (erschienen in: Zeitschrift für die gesamte Versicherungswissenschaft 4/2000, S. 577- 603.)
- No.58: **Harald A. Benink/Reinhard H. Schmidt**, Towards a Regulatory Agenda for Banking in Europe, September 2000 (erschienen in: Research in Financial Services-Bank Crises: Causes, Analysis and Prevention, Vol.12, JAI Press-Elsevier Science, hrsg. von George G. Kaufman, 2000)
- No.57: **Thomas G. Stephan/Raimond Maurer/Martin Dürr**, A Multiple Factor Model for European Stocks, September 2000
- No.56: **Martin Nell/Andreas Richter**, Catastrophe Index-Linked Securities and Reinsurance as Substitutes, August 2000
- No.55: Four short papers on Development Finance, August 2000  
**Reinhard H. Schmidt**, Entwicklungsfinanzierung; (erschienen in: Handwörterbuch des Bank- und Finanzwesens, 3. Aufl., hrsg. von Wolfgang Gerke und Manfred Steiner, Stuttgart: Schäffer-Poeschel, 2001)  
**Reinhard H. Schmidt**, Banking Regulation contra Microfinance; (erschienen in: Savings and Development, Vol. 24 (2000) , S.111-121.)  
**Ingo Tschach**, The Impact of Inflation on Long-Term Housing Loans;  
**Eva Terberger-Stoy/Marcel Tyrell, Joseph E. Stiglitz** (erschienen in: Entwicklung und Zusammenarbeit, 41. Jahrgang (2000), S. 46-49)
- No.54: **Raimond Maurer/Thomas G. Stephan**, Vermögensanlagevorschriften für deutsche Versicherungsunternehmen: Status Quo und finanzwirtschaftliche Bewertungen, Juli 2000 (erschienen in: Handbuch Spezialfonds (hrsg. von J.M. Kleeberg und C. Schlenger), Bad Soden 2000, S. 143-176.),
- No.53: **Joachim Grammig/Reinhard Hujer/Stefan Kokot**, Bias-free Nonparametric Estimation of Intra-Day Trade Activity Measures, June 2000
- No.52: **Raimond Maurer / Steffen Sebastian / Thomas G. Stephan**, Immobilienindizes im Portfolio-Management, Mai 2000 (erscheint in Deutscher Aktuarverein (Hrsg.): Investmentmodelle für das Asset-Liability-Modelling von Versicherungsunternehmen, 2002)
- No.51: **Raimond Maurer / Steffen Sebastian**, Inflation Risk Analysis of European Real Estate Securities, Mai 2000 (erscheint in: Journal of Real Estate Research, 2002)
- No.50: **Andreas Hackethal / Reinhard H. Schmidt**, Finanzsysteme und Komplementarität, April 2000 (erschienen in: Kredit und Kapital, Beiheft 15 "Neue finanzielle Arrangements: Märkte im Umbruch", 2000, S. 53-102)
- No.49: **Mark Wahrenburg/ Susanne Niethen**, Vergleichende Analyse alternativer Kreditrisikomodelle, April 2000 (erschienen in: Kredit und Kapital, Heft 2, 2000)

- No.48: **Christian Leuz**, IAS versus US GAAP: A "New Market" Based Comparison, January 2000
- No.47: **Ralf Elsas/ Mahmoud El-Shaer/ Erik Theissen**, Beta and Returns Revisited – Evidence from the German Stock Market, December 1999
- No.46: **Michael H. Grote/Sofia Harrschar-Ehrnborg/Vivien Lo**, Technologies and Proximities: Frankfurt´s New Role in the European Financial Centre System, December 1999
- No.45: **Reinhard H. Schmidt/Adalbert Winkler**, Building Financial Institutions Developing Countries, November 1999 ( erschienen in: "Journal für Entwicklungspolitik", XVI/3, 2000, S. 329-346)
- No.44: **Konstantin Korolev/Kai D. Leifert/ Heinrich Rommelfanger**, Arbitrage theorie bei vagen Erwartungen der Marktteilnehmer, November 1999
- No.43: **Reinhard H. Schmidt/Stefanie Grohs**, Angleichung der Unternehmensverfassung in Europa –Ein Forschungsprogramm, November 1999 (erschieden in: Systembildung und Systemlücken in Kerngebieten des Europäischen Privatrechts, hrsg. von Stefan Grundmann, Tübingen: Mohr Siebeck, 2000, S. 146-188)
- No.42: **Konstantin Kovolev/Kai D. Leifert/ Heinrich Rommelfanger**, Optionspreistheorie bei vagen Daten, Oktober 1999
- No.41: **Christian Leuz/Robert E. Verrecchia**, The Economic Consequences of Increased Disclosure (erscheint in: Journal of Accounting Research, Supplement 2000), June 2000
- No.40: **Christian Leuz**, The Development of Voluntary Cash Flow Statements in Germany and the Influence of International Reporting Standards, July 1999 (erschieden in: Schmalenbach Business Review, Vol. 52 (2), April, 2000, S. 182-207.)
- No.39: **Ulrike Stefani**, Quasirenten, Prüferwechsel und rationale Adressaten, Juni 1999
- No.38: **Michael Belledin/Christian Schlag**, An Empirical Comparison of Alternative Stochastic Volatility Models, June 1999
- No.37: **Jens Wüstemann**, Internationale Rechnungslegungsnormen und neue Institutionenökonomik, Mai 1999
- No.36: **Robert Gillenkirch/Matthias M. Schabel**, Die Bedeutung der Periodenerfolgsrechnung für die Investitionssteuerung – Der Fall ungleicher Zeitpräferenzen, April 1999 (die überarbeitete Fassung "Investitionssteuerung, Motivation und Periodenerfolgsrechnung bei ungleichen Zeitpräferenzen" erscheint voraussichtlich 2001 in der ZfbF)
- No.35: **Reinhard H. Schmidt**, Differences between Financial Systems in Europe: Consequences for EMU, April 1999 (erschieden in "The Monetary Transmission Mechanism: Recent Developments and Lessous for Europe", hrsg. v. Deutsche Bundesbank, Houndsmill (UK), 2001, S. 208-240)
- No.34: **Theodor Baums/Erik Theissen**, Banken, bankeigene Kapitalanlagegesellschaften und Aktienemissionen, März 1999 (erschieden in: Zeitschrift für Bankrecht und Bankwirtschaft, 11 (1999), Heft 3, S. 125-134)

- No.33: **Andreas Hackethal/Reinhard H. Schmidt**, Financing Patterns: Measurement Concepts and Empirical Results, May 2000
- No.32: **Michael H. Haid/Eric Nowak**, Executive compensation and the susceptibility of firms to hostile takeovers – An empirical investigation of the U.S. oil industry, March 1999
- No.31: **Reinhard H. Schmidt/Jens Maßmann**, Drei Mißverständnisse zum Thema "Shareholder Value", Februar 1999 (erschieden in Kumar/ Osterloh/ Schreyögg (Hrsg.): Unternehmensethik und die Transformation des Wettbewerbs, Festschrift für Professor Dr. Dr. h. c. Horst Steinmann zum 65. Geburtstag, 1999, Schäffer-Poeschel Verlag Stuttgart, S.125-157 )
- No.30: **Eberhard Feess/Michael Schieble**, Credit Scoring and Incentives for Loan Officers in a Principal Agent Model, January 1999
- No.29: **Joachim Grammig/Dirk Schiereck/Erik Theissen**, Informationsbasierter Aktienhandel über IBIS, Januar 1999 (erscheint in überarbeiteter Fassung in: Zeitschrift für betriebswirtschaftlicher Forschung)
- No.28: **Ralf Ewert/Eberhard Feess/Martin Nell**, Auditor Liability Rules under Imperfect Information and Costly Litigation – The Welfare Increasing Effect of Liability Insurance, January 1999 (erschieden in European Accounting Review – genauer!))
- No.27: **Reinhard H. Schmidt/Gerald Spindler**, Path Dependence, Corporate Governance and Complementarity, March 2000 (erscheint in: Jeffrey Gordon & Mark Roe, eds.: Convergence and Persistence of Corporate Governance Systems, University of Chicago Press, 2001)
- No.26: **Thorsten Freihube/Carl-Heinrich Kehr/Jan P. Krahnert/Erik Theissen**, Was leisten Kursmakler? Eine empirische Untersuchung am Beispiel der Frankfurter Wertpapierbörse, Dezember 1998 (erschieden in: Kredit und Kapital, 32(1999), Heft3, S. 426-460.
- No. 25: **Jens Maßmann/Reinhard H. Schmidt**, Recht, internationale Unternehmensstrategien und Standortwettbewerb, December 1998 (erschieden in: Jahrbuch für Neue Politische Ökonomie, Band 18, hrsg. von K.-E. Schenk u.a., Tübingen 2000, S. 169-204)
- No. 24: **Eberhard Feess/Martin Nell**, The Manager and the Auditor in a Double Moral Hazard Setting: Efficiency through Contingent Fees and Insurance Contracts, December 1998
- No. 23: **Carl-Heinrich Kehr/Jan P. Krahnert/Erik Theissen**, The Anatomy of a Call Market: Evidence from Germany, December 1998
- No. 22: **Christian K. Muus**, Non-voting shares in France: An empirical analysis of the voting premium, December 1998
- No. 21: **Christian Leuz**, Voluntary Disclosure of Cash Flow Statements and Segment Data in Germany, September 1998
- No. 20: **Anne D`Arcy**, The Degree of Determination of National Accounting Systems – An Empirical Investigation, September 1998



- No. 19: **Helmut Laux**, Marktwertmaximierung und CAPM im Ein- und Mehrperioden-Fall, September 1998 (erschienen in Unternehmensführung, Ethik und Umwelt, Festschrift zum 65. Geburtstag von Hartmut Kreikebaum, hrsg. von Gerd-Rainer Wagner, Wiesbaden 1999, S. 226-251)
- No. 18: **Joachim Grammig/Reinhard Hujer/Stefan Kokot/Kai-Oliver Maurer**, Ökonometrische Modellierung von Transaktionsintensitäten auf Finanzmärkten; Eine Anwendung von Autoregressive Conditional Duration Modellen auf die IPO der Deutschen Telekom, August 1998
- No. 17: **Hanne Böckem**, An Investigation into the Capital Market Reaction on Accounting Standards Enforcement, July 1998
- No. 16: **Erik Theissen**, Der Neue Markt: Eine Bestandsaufnahme, April 1998 (erschienen in: Zeitschrift für Wirtschafts- und Sozialwissenschaften, Heft 4/98, S. 623-652)
- No. 15: **Jan Pieter Krahen**, Finanzierungstheorie: Ein selektiver Überblick, April 1998 (englische Fassung erschienen in "Gutenberg Centennial", hrsg. von Horst Albach, Berlin, 2000)
- No. 14: **Erik Theissen**, Liquiditätsmessung auf experimentellen Aktienmärkten, April 1998 (erschienen in: Kredit und Kapital, 32(1999), Heft 2, S. 225-264)
- No. 13: **Reinhard H. Schmidt**, Erich Gutenberg und die Theorie der Unternehmung, February 1998 (englische Fassung erschienen in "Theory of the Firm", hrsg. von Horst Albach u.a., Berlin 2000, S. 3-39)
- No. 12: **Adalbert Winkler**, Financial Development, Economic Growth and Corporate Governance, February 1998 (erschienen in: Asian Financial Markets, hrsg. von Lukas Menkhoff/Beate Reszat, Baden-Baden 1998, S. 15-44)
- No. 11: **Andreas R. Hackethal/Marcel Tyrell**, Complementarity and Financial Systems – A Theoretical Approach, December 1998
- No. 10: **Reinhard H. Schmidt/Andreas Hackethal/Marcel Tyrell**, Disintermediation and the Role of Banks in Europe: An International Comparison, January 1998 (erschienen in: Journal of Financial Intermediation, Vol. 8, 1999, S.37-67)
- No. 9: **Stefan Heiden/Günther Gebhardt/Irmelin Burkhardt**, Einflußfaktoren für Kursreaktionen auf die Ankündigung von Kapitalerhöhungen deutscher Aktiengesellschaften, December 1997
- No. 8: **Martin Nell**, Garantien als Signale für die Produktqualität?, November 1997 (erscheint in: Zeitschrift für betriebswirtschaftliche Forschung)
- No. 7: **Robert M. Gillenkirch**, Anreizwirkungen und Bewertung von Erfolgsbeteiligungen im Portefeuillemanagement, November 1997 (erschienen in: ZfB, Sonderheft Finanzmanagement 1999)
- No. 6: **Reinhard H. Schmidt/C.-P. Zeitinger**, Critical Issues in Microbusiness Finance and the Role of Donors, October 1997 (erschienen in: Strategic Issues in Microfinance, ed. by Kimenyi/Wieland/Von Pischke, Averbury, UK, 1998, S. 27-51)
- No. 5: **Erik Theissen/Mario Greifzu**, Performance deutscher Rentenfonds, September 1997 (erschienen in: Zeitschrift für betriebswirtschaftliche Forschung, 50. Jg., 1998, S. 436-461)

- No. 4: **Jan Pieter Krahn**~~en~~/**Martin Weber**, Marketmaking in the Laboratory: Does Competition Matter?, September 1997
- No. 3: **Reinhard H. Schmidt**, Corporate Governance: The Role of Other Constituencies, July 1997 (erschienen in: Pezard, Alice;Thiveaud, Jean-Marie (Hrsg.): Corporate Governance: Cross Border Experience, Paris, 1997, S. 61-74)
- No. 2: **Ralf Ewert/Christian Ernst**, Strategic Management Accounting, Coordination and Long-term Cost Structure, July 1997 (erschienen unter dem Titel "Target Costing, Coordination and Strategic Cost Management" in European Accounting Review, Vol.8, No.1 (1999), S. 23-49)
- No. 1: **Jan P. Krahn**~~en~~/**Christian Rieck/Erik Theissen**, Insider Trading and Portfolio Structure in Experimental Asset Markets with a Long Lived Asset, July 1997 (erschienen in European Journal of Finance, Vol. 5, Nr. 1, March 1999, S. 29-50)

**Kontaktadresse für Bestellungen:**

Professor Dr. Reinhard H. Schmidt  
Wilhelm Merton Professur für  
Internationales Bank- und Finanzwesen  
Mertonstr. 17  
Postfach 11 19 32 / HPF66  
D-60054 Frankfurt/Main

Tel.: +49-69-798-28269

Fax: +49-69-798-28272

e-mail: [rschmidt@wiwi.uni-frankfurt.de](mailto:rschmidt@wiwi.uni-frankfurt.de)

<http://www.finance.uni-frankfurt.de/schmidt/WPs/wp/wpliste.html>

Mit freundlicher Unterstützung der Unternehmen der  
Sparkassen-Finanzgruppe Hessen-Thüringen.